Grade of Membership (GoM) models for counts data

Kushal K Dey

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samp ₂	c ₁₂	c ₂₂		c _{2G}
samp _N	c _{N1}	c _{N2}		C _{NG}

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Model

We assume for sample n,

$$(c_{n1}, c_{n2}, \cdots, c_{nG}) \sim Mult(c_{n+}, p_{n1}, p_{n2}, \cdots, p_{nG})$$

where $c_{n+} = \sum_{g=1}^{G} c_{ng}$.

Assuming number of clusters to be K, write p_{ng} as

$$p_{ng} = \sum_{k=1}^{K} \omega_{nk} \theta_{kg}$$
 $\sum_{k=1}^{K} \omega_{nk} = 1$ $\sum_{g=1}^{G} \theta_{kg} = 1$

Assume the priors

$$(\omega_{n1}, \omega_{n2}, \cdots, \omega_{nK}) \sim Dir\left(\frac{1}{K}, \frac{1}{K}, \cdots, \frac{1}{K}\right)$$
 $(\theta_{k1}, \theta_{k2}, \cdots, \theta_{kG}) \sim Dir\left(\frac{1}{KG}, \frac{1}{KG}, \cdots, \frac{1}{KG}\right)$

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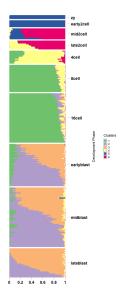
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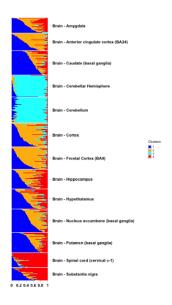
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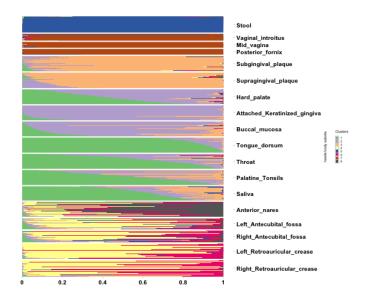
Example: Single cell development



GTEx v6 Brain clustering



Metagenomics HMP data



Possible routes

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We may want to build networks over the OTUs and compare these network method results with the GoM output.

The End