程与解. 12132387

$$f(-2) = 0$$
 $f(-2) = f(-2)$

according to Roll's law 0 = 3 c G[-2, 1], f(t) = 0 $f(x) = 4x^3 - 8x = 4x(x^2 - 2)$ for f(x) = 0

so c can take value of 0, I, - 52.

②
$$f(0) = 0 = f(2\pi)$$

according to Roll's law $\frac{1}{2} c \in [0, \pi]$ let $f(0) = 0$
 $f'(x) = \cos x + 2 \cos 2x = \cos x + 2 [2\cos^2 x - 1]$

for $f'(x) = 0$, we get:

 $x = \begin{cases} 53.625^\circ = 0.92359 \\ 147.4657^\circ = 2.5738 \end{cases}$

Problem 2:

Because $P_N(x)$ is the Lagrange polynomial of N-degree f(x) so we have: $P_N(x_i) = f(x_i)$ ($T_i = 0, i$, 2,... M)

And $F_N(x) = P_N(x_i) - P_N(x)$ so $F_N(x_i) = 0$ ($T_i = 0, 1, ... N$)

Now let's consider the special function $f(x_i)$ and $f(x_i) = f(x_i) - f_N(x_i) = 0$ and $f(x_i) = f(x_i) - f_N(x_i) - f_N(x_i) - f_N(x_i) = 0$

So,
$$g(t)$$
 has $N+2$ root: $[X_0, X_1, \dots X_N, X]$

According to the generalized Rolle's theorem, he have. $\exists . \S$ Let $g^{(n+1)}(\S) = 0$

and $g^{(n+1)}(\S) = \int_{\mathbb{R}^N} f^{(n+1)}(\S) = \int_{\mathbb{R}^N} f^{($

50
$$0 = f^{(m+1)}(3) - \frac{E_{N}(x)(M+1)!}{(x-x_0)...(x-x_N)}$$

50 $E_{N}(x) = \frac{f^{(m+1)}(4)}{(M+1)!}(x-x_0)...(x-x_N)$

Problem 3

$$X_{1} = \frac{-b+\sqrt{b^{2}-4ac}}{2a} = \frac{1}{2a} \frac{b^{2}-4ac-b^{2}}{\sqrt{b^{2}-4ac+b}} = -\frac{2e}{\sqrt{b^{2}-4ac+b}}$$

$$X_{2} = \frac{-be-\sqrt{b^{2}-4ac}}{2a} = -\frac{1}{2a} \frac{b^{2}-4ac-b^{2}}{\sqrt{b^{2}-4ac-b}} = \frac{2c}{\sqrt{b^{2}-4ac-b}} = -\frac{2c}{b-\sqrt{b^{2}-4ac}}$$

Problem 4

Shown in hwl- problem 4. ipynb.

Problem 5

As the problem shown:
$$f(x) = x^2 - A$$
, we get: $f(x) = 3x^2$.

if we use newtoon-Raphson method: we have
$$g(x) = x - \frac{f(x)}{f(x)} = x - \frac{x^3 - A}{3x^2} = \frac{2x^3 - A}{3x^2} = \frac{2x - A/x^2}{3}$$

so we have iterative formula
$$P_{K} = \frac{2P_{K-1} - \frac{A}{P_{K-1}^{2}}}{3} \quad \text{for } K = 1, 2, \dots$$

Shown in hwl- problem 6. ipynb.

Problem 7:

$$0 = f(P_k) + f(P_k) (P - P_k) + \frac{1}{2} f'(C_k) (P - P_k)^2$$

if we assume $f'(x) \neq 0 \Rightarrow f(P_k) \neq 0$

$$\Rightarrow 0 = \frac{f(Pk)}{f(Pk)} + (P-Pk) + \frac{1}{2} \frac{f'(ck)}{f(Pk)} (P-Pk)^{2}$$

$$= \int (P - P_{1k}) + \frac{f(P_{1k})}{f(P_{1k})} = -\frac{1}{2} \frac{f''(c_{1k})}{f'(P_{1k})} (P - P_{1k})^{2}.$$

$$= \left(P - P + \frac{f(Pk)}{f(Pk)}\right)$$
$$= -\frac{2f'(Ck)}{2f(Pk)} (P-Pk)^{2}$$

$$= -\frac{of'(C_K)}{2f(P_K)} \stackrel{?}{=} E_K^2$$
And we assume $f'(P_K) \approx f'(P)$ $f''(C_K) \approx f''(P)$