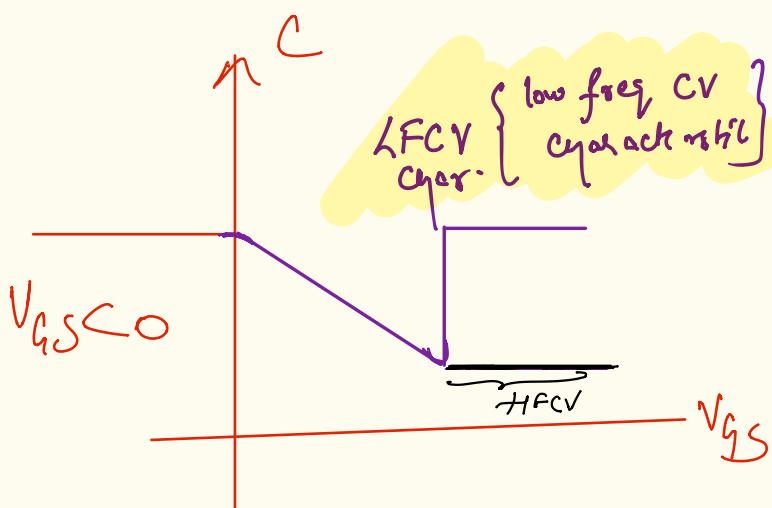


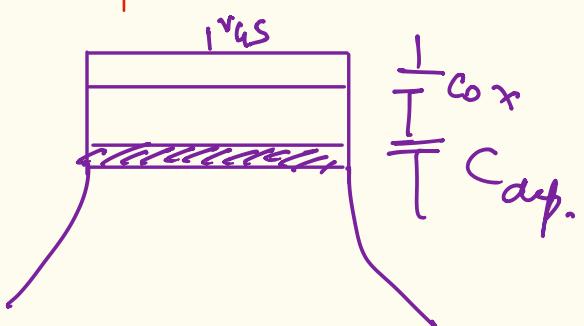
in n-MOS { p- + P Sub }

$$C_{ox} = \frac{\epsilon_0 \epsilon_{ox}}{t_{ox}}$$



when  $V_{GS} \geq 0$ ; inversion starts

$\therefore$  2 capacitor in working



# # Flat Band, Accumulation & Inversion

→ Inversion

$V_{GS}$  at which  $c^-$  Conc at Oxide-Substrate interface is equal to Conc of  $p$  is threshold voltage

$$p = N_v \exp\left(\frac{E_v - E_f}{kT}\right)$$

$$p_i = N_v \cdot \exp\left(\frac{E_v - E_{if}}{kT}\right)$$

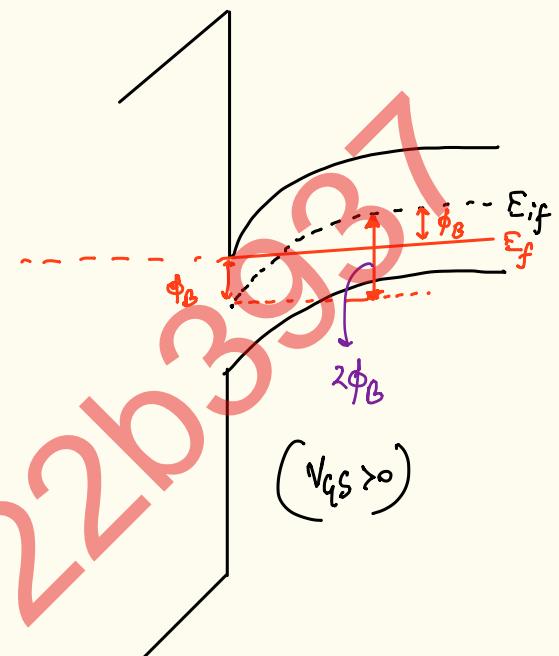
$$p = p_i \exp\left(\frac{E_{if} - E_f}{kT}\right)$$

$$p = n_i \cdot \exp\left(\frac{\phi_B}{kT}\right)$$

now; @ Si /  $\text{SiO}_2$  interface;

$$\eta = n_i \exp\left(+\frac{\phi_B}{kT}\right)$$

$$\phi_s = 2\phi_B$$



$$(V_{GS})_T \sim V_T = V_{ox} + 2\phi_B = 2\phi_B + t_{ox} \frac{\epsilon_s \epsilon_8}{\epsilon_{ox}}$$

Electric field

$$W_d = \sqrt{\frac{2\epsilon_s}{q} \left( \frac{1}{N_A} \cdot 2\phi_B \right)}$$

$$= 2\phi_B + \frac{\epsilon_s}{C_{ox}} \left( \frac{q \cdot N_A \cdot W_d}{\epsilon_8} \right)$$

depletion width

$$= 2\phi_B + \frac{q \cdot N_A}{C_{ox}} \left( \frac{2\epsilon_s \cdot 2\phi_B}{q \cdot N_A} \right)^{1/2}$$

$$\frac{\epsilon_{ox} \epsilon_{ox}}{\epsilon_8 \epsilon_8} = \frac{\epsilon_s \epsilon_8}{\epsilon_{ox}}$$

Electric field

Gauss law

$$\epsilon_{ox} \propto \epsilon_s$$

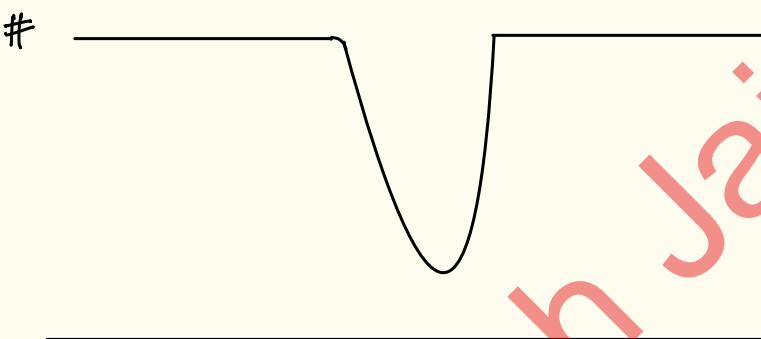
$$= 2\phi_B + \frac{1}{C_{ox}} \sqrt{4 \epsilon_s \cdot q \cdot N_A \cdot \phi_B}$$

Charge:  
Φ depletion

if  $\phi_m = \phi_s$

then; initially  
if  $\phi_m \neq \phi_s$

$$V_T = 2\phi_B + \phi_{mS} + \frac{\sqrt{4 \epsilon_s q N_A \phi_B}}{C_{ox}}$$



$$\phi_s (V_{GS} = V_T) = 2\phi_B = \frac{2kT \ln(\frac{N_A}{n_i})}{q}$$

$$N_A = 10^{18}$$

$$n_i = 10^{10}$$

$$\phi_B = 0.026 \cdot \ln \left( \frac{10^{18}}{10^{10}} \right) = 0.47$$

$$2\phi_B = 0.94$$

if  $V_{GS} > V_T$

$$\phi_B = 0.47 + 0.20 = 0.67$$

$$n = n_i \cdot \exp \left( \frac{\phi_B}{kT} \right)$$

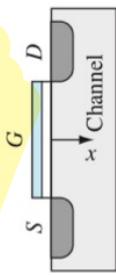
$$n = 10^{10} \cdot \exp \left( \frac{0.67}{0.026} \right) \\ = 10^{21} \text{ cm}^{-3}$$

Beyond inversion; Small Change in  $V_{GS}$  results  
in large Change in "η"

$$\phi_s = 2\phi_f$$

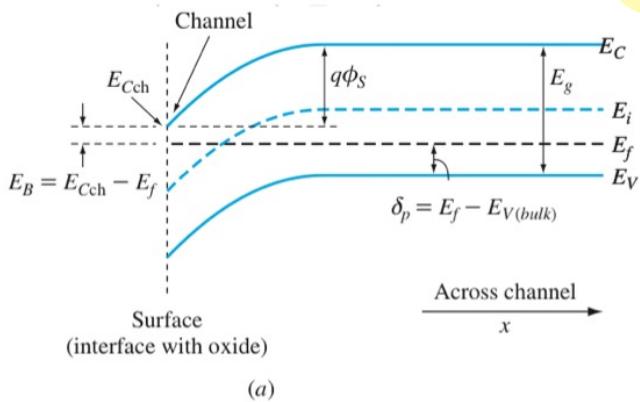
$$\phi_f = \frac{E_i - E_f}{q}$$

$$E_i - E_f = KT \ln \left( \frac{N_A}{n_i} \right)$$



$$n_s = N_C e^{-E_B/kT} \quad (7.5)$$

$$\phi_s = \frac{1}{q} [E_g - E_B - \delta_p]$$



$$V_{GS} - V_T = \phi_{ox} - \phi_{ox}^{th}$$

$\{ V_{GS} > V_T \}$

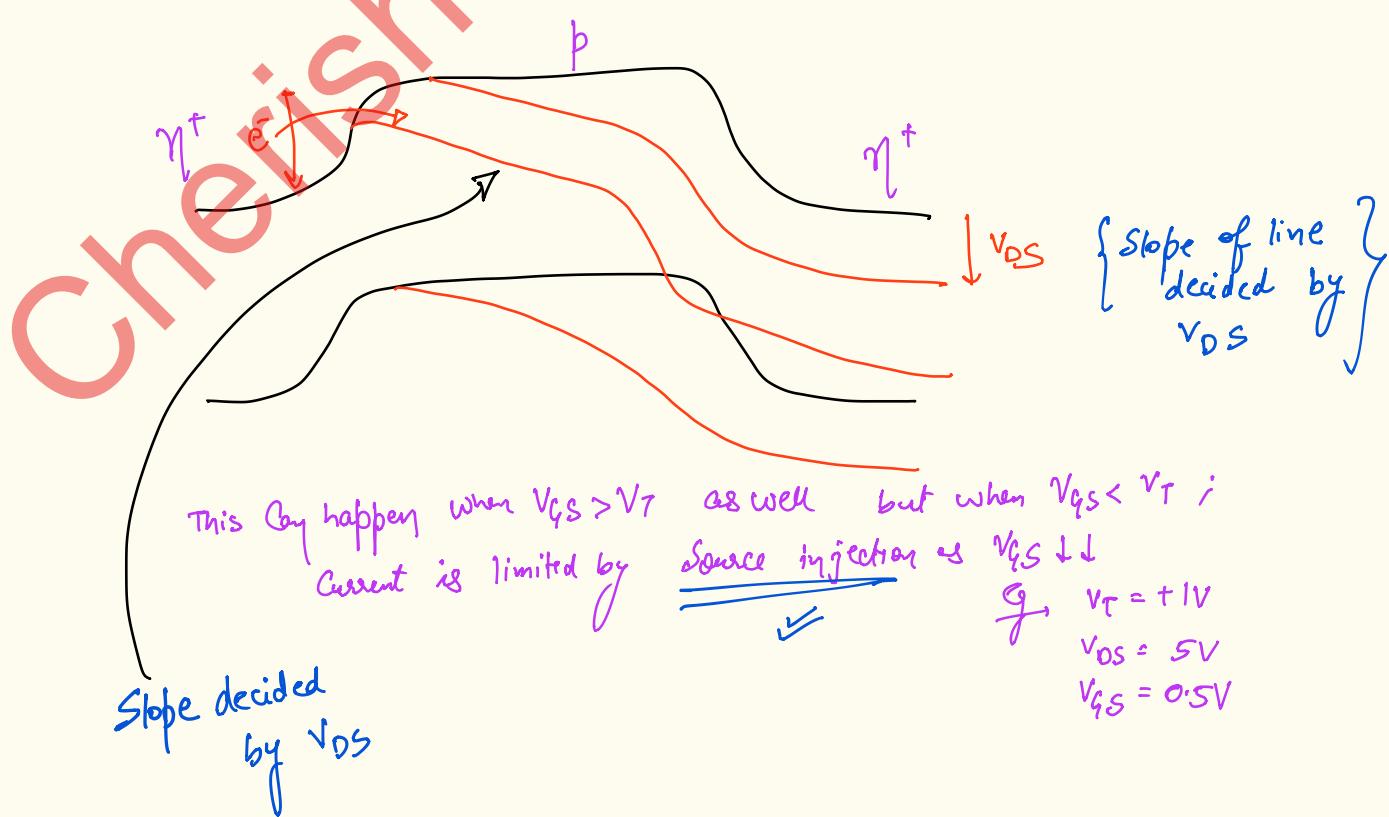
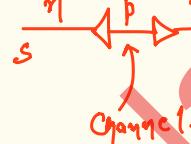
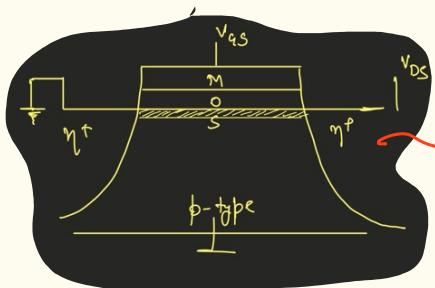
Oxide voltage @ threshold

$$I_{DS} = 0, \quad V_{GS} < V_T$$

$$= I_0 e^{\left( \frac{V_{GS} - V_T}{KT} \right)}, \quad V_{GS} < V_T \quad \{ \text{Sub-threshold} \}$$

Similar to Diode eqn:  $I = I_0 \left( e^{\frac{V}{KT}} - 1 \right)$

{ Sub-threshold }

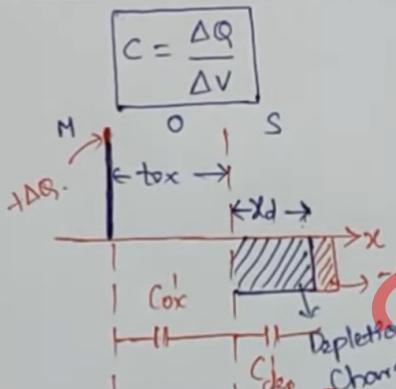
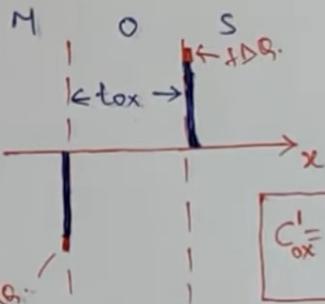


## C-V Characteristics

Techgurukula

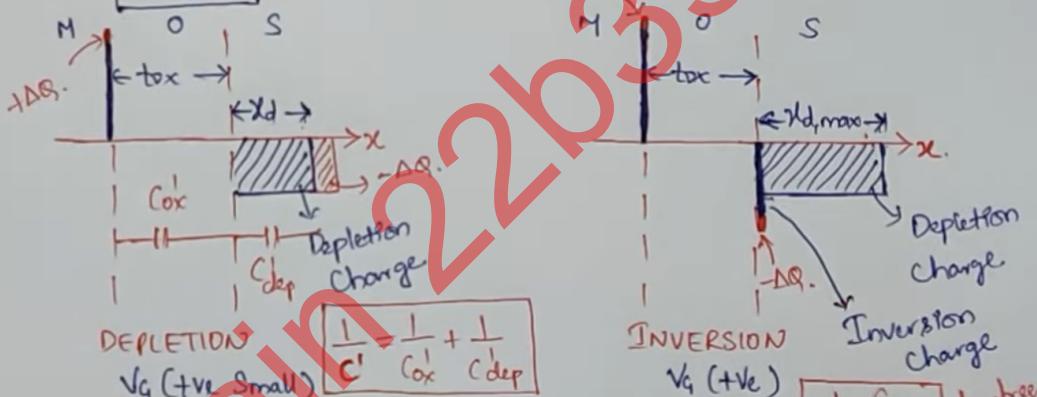
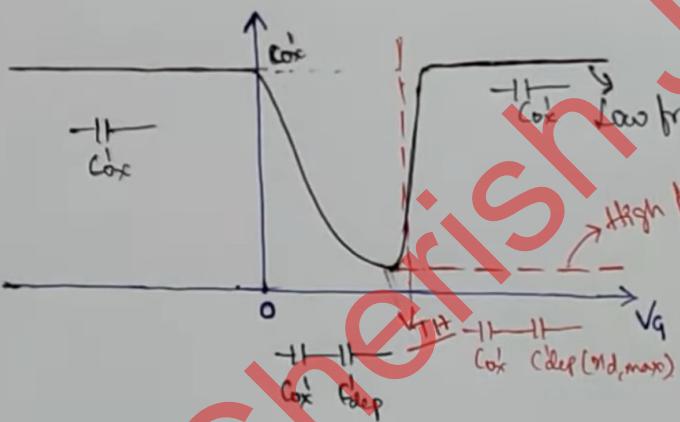
$$V + \Delta V$$

$$Q + \Delta Q$$

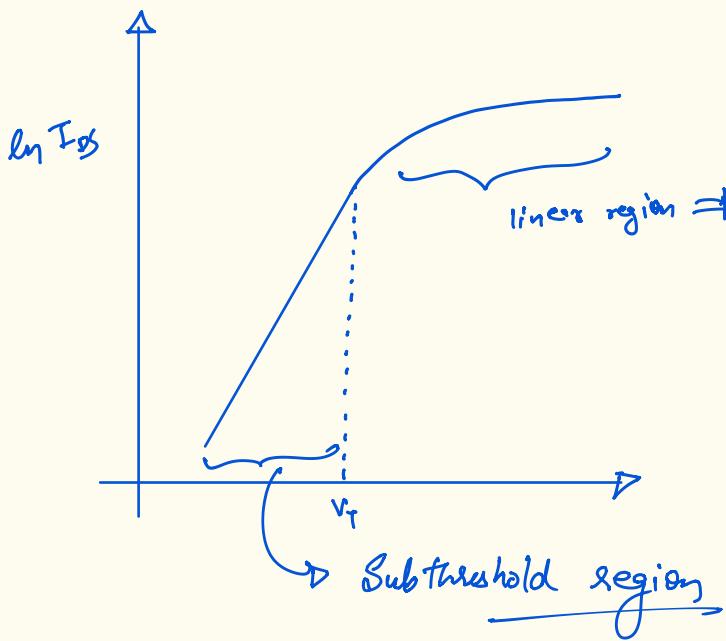


$$\frac{1}{C'} = \frac{1}{C_{ox}} + \frac{1}{C_{dep}}$$

$$C_{dep} = \frac{E_{si}}{x_d}$$



$$\frac{1}{C'} = \frac{1}{C_{ox}} + \frac{1}{C_{dep} (x_d, max)}$$



Mosfet Eq<sup>"</sup>'s

$$I_{DS} = I_{DSS} e^{\frac{V_{GS}-V_T}{\eta V_T}}$$

;  $V_{GS} < V_T$

$$= \frac{\mu_n C_{ox} W}{L} \left[ (V_{GS}-V_T)V_{DS} - \frac{V_{DS}^2}{2} \right]$$

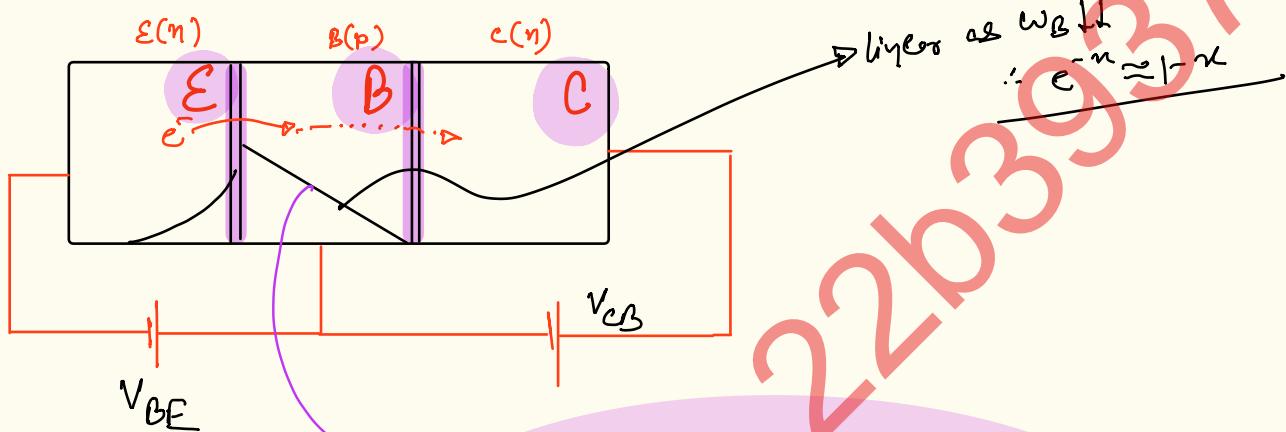
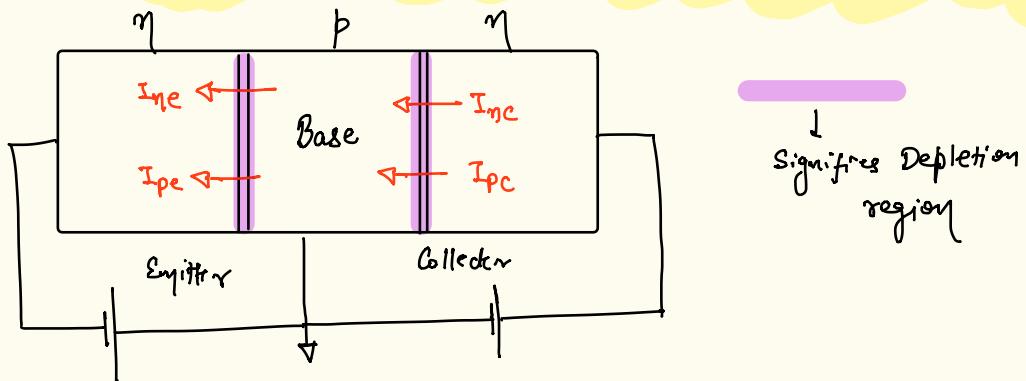
;  $V_{DS} < V_{GS} - V_T > 0$

$$= \frac{\mu_n C_{ox} W}{2L} (V_{GS}-V_T)^2 ;$$

$V_{DS} > V_{GS}-V_T > 0$

Cherish Jain 22b38  
→ These eq<sup>"</sup> are applicable to JFET as well.

# Bipolar Junction Transistor



Cherish Jain 22b3931

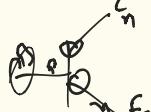
So i)  $W_B = \text{Small} \Rightarrow e^- \text{ won't dwell too much in Base.}$

ii) Base lightly doped  $\Rightarrow$  less recomb<sup>n</sup> in Base

Aim:-  $e^-$  that come to E-B junction should go to C-B junction

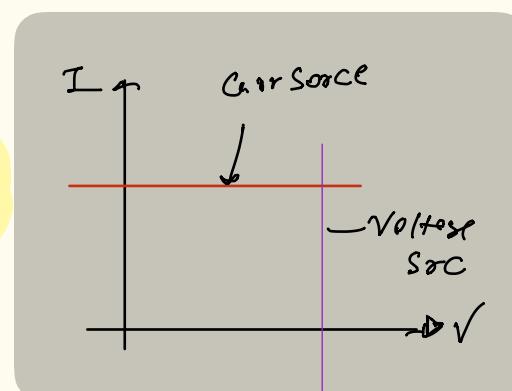
$$J_{nC} = J_{nE}$$

Current depends on  $V_{BE} \checkmark$   
 $V_{CB} \times$



# Base Current

Control Signal.



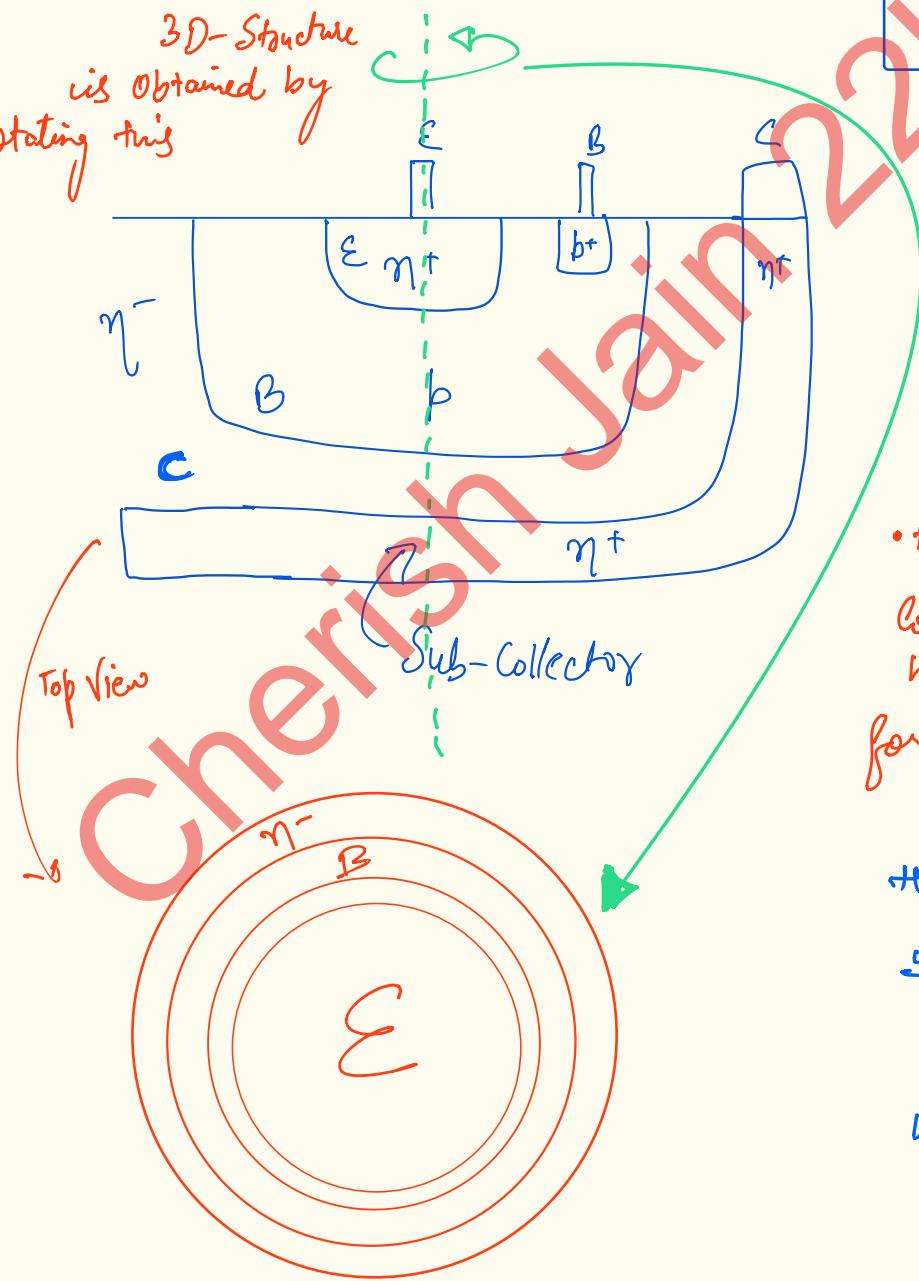
in mosfet ;  $g_m = \frac{\partial I_{DS}}{\partial V_{GS}}$  ; Voltage controlled Current Source

BJT ;  $\beta = \frac{I_C}{I_B}$  Current Contd Current Source

\* We want  $J_{PE} \gg J_{PE}$

p-moderate  
Achieved by n base Doping { if very light then the 2 depletion regions may conflict }  
Emitter very heavily Doped  
Collector lightly doped { we want Depletion region to be protruding on Right Side rather than left }

3D-Structure  
is obtained by  
rotating tri

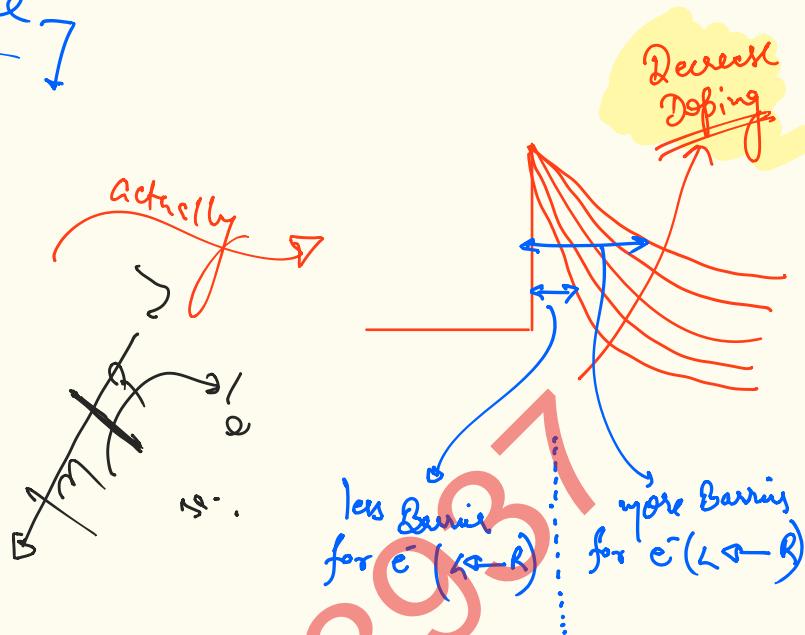
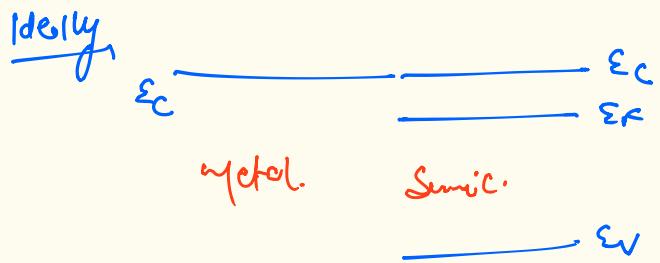


BJT  $\rightarrow$  Vertical device  
MOS  $\rightarrow$  Horizontal "

- Heavy doping is req. for contact; Hence for Base a heavy p+ pocket is made for making Contact.

Heavy doping ensures low resistance; Hence while making Contact; we deliberately dope more

# Low Doping = more Resistance



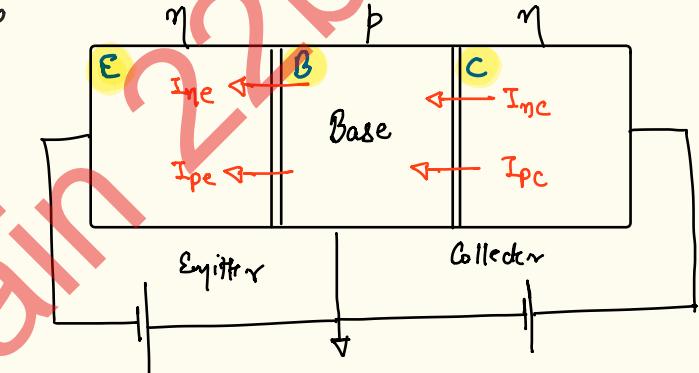
$$I_E = I_{nE} + I_{pE} + I_{recomb}$$

$$I_C = I_{nC} + I_{pC} + I_{gen}$$

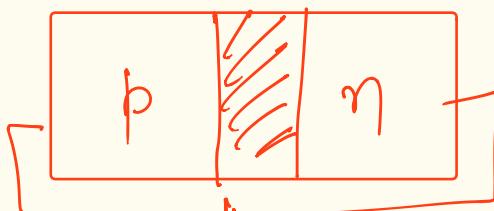
$$I_E = I_C + I_B$$

$$I_{nE} = \alpha_s I_{nE} + I_{RB, \eta}$$

$$I_{pC} = I_{RB, \eta}$$



• Recombination  $I$  in base region.



in depletion region

$$\eta_p > \eta_i^2$$

$$J_{rec} = B \cdot (n_p - n_i^2)$$

Bimolecular Recombination Weight

$$J_{\eta C} = \alpha' \cdot J_{\eta E}$$

$\alpha' < 1$  because of  $J_{\text{rec}}$

$$\begin{aligned} \alpha &= \frac{J_C}{J_E} = \frac{J_{\eta E}}{J_E} \cdot \frac{J_{\eta C}}{J_{\eta E}} \cdot \frac{J_C}{J_{\eta C}} \\ &= \gamma \alpha_T M \quad \left. \begin{array}{l} \text{we want} \\ \gamma \rightarrow 1 \\ \alpha_T \rightarrow 1 \\ M \rightarrow 1 \end{array} \right\} \end{aligned}$$

for all practical purposes;

$$\alpha = f \alpha_T \quad M \approx 1$$

$$\alpha_T = \frac{J_{\eta E} - J_{\text{rec}}}{J_{\text{rec}}}$$

Common

Current gain

Typical  $\alpha$  in BJT  $\approx 0.99$  (always  $< 1$  except when  $M > 1$ )

$\gamma = \text{Emitter injection efficiency}$

$$= \frac{J_{\eta E}}{J_{\eta E} + J_{pE}}$$

$\alpha_T = \text{Base transport factor}$

$M = \text{Collector efficiency}$

$$= \frac{J_{\eta C} + J_{pC}}{J_{\eta C}} \approx 1$$

$$E-B \rightarrow FB$$

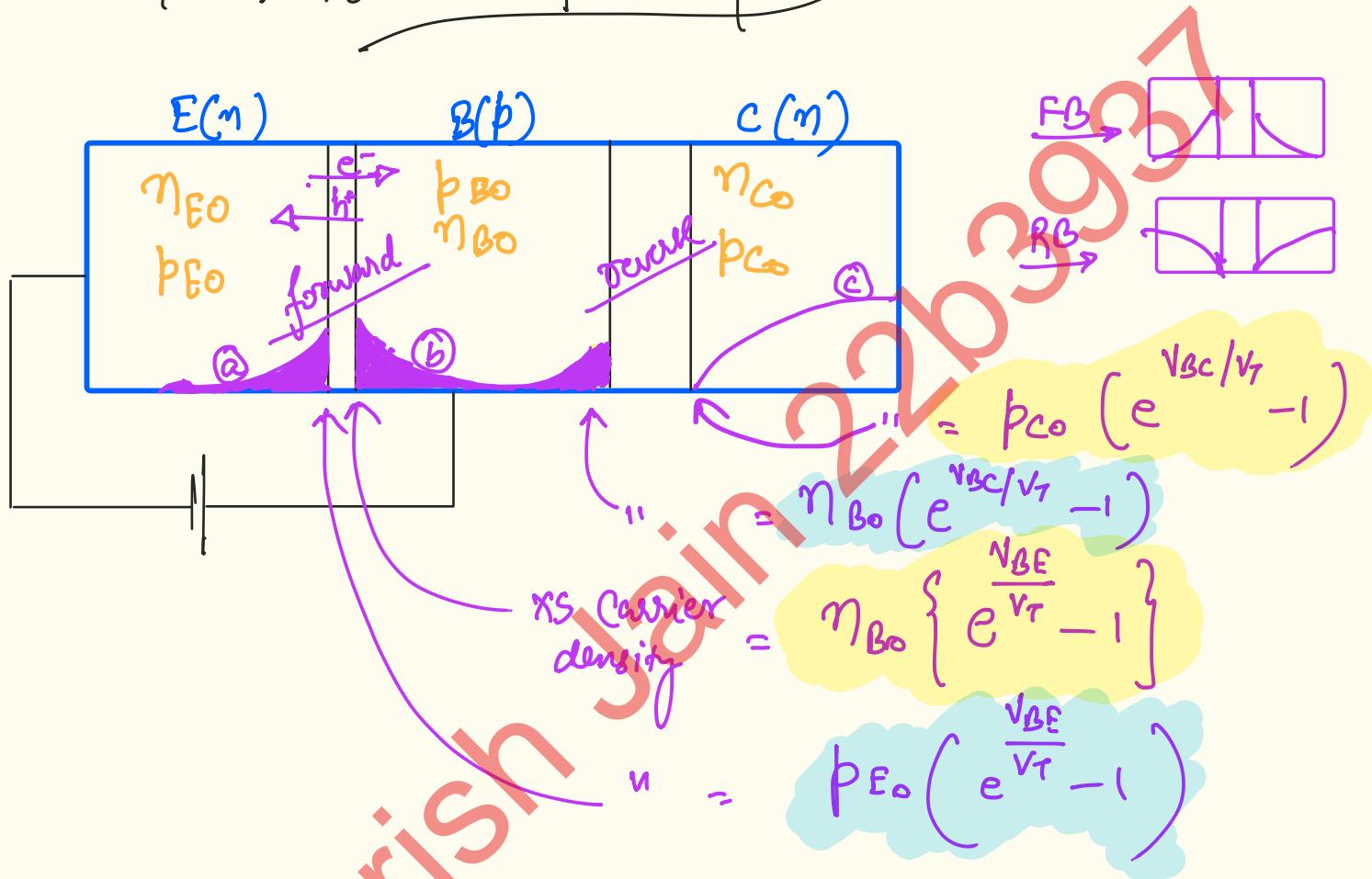
$$C-B \rightarrow RB$$

$$\alpha = \frac{I_C}{I_E}$$

$\approx eg \cdot 0.99 \rightarrow$  Typical Si Homojunction

$$\beta = \frac{I_C}{I_B} = \frac{I_C}{I_E - I_C} = \frac{\alpha}{1 - \alpha} \rightarrow eg \approx 100$$

Normal operating  
Cond<sup>n</sup> is Forward Active Mode



(a) hole density in emitter region

$$p_E(x) = p_{EO} \left( e^{\frac{V_{BE}}{V_T}} - 1 \right) \cdot \left( e^{-x/L_p} \right)$$

ignore offset!

(b) rise only when BC  $\rightarrow$  for. biased. ; generally there is  $\eta_0$

rise-

$$\eta_B(x) = A \cdot e^{-x/L_n} + B e^{x/L_m}$$

(offset ignored)

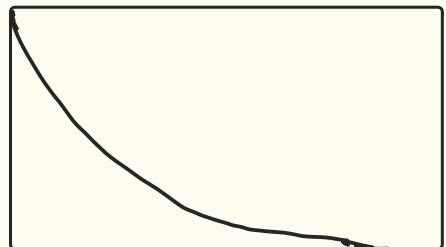
$$\gamma_B(x=0) = \eta_{B0} \left( e^{\frac{V_B \epsilon}{kT}} - 1 \right)$$

$$\eta_B(x=w_B) = \eta_{B0} \left( e^{-\frac{V_C B}{kT}} - 1 \right)$$

④ Revolving Biased region

$$p_C(x) = p_{C0} \left( e^{-\frac{V_C B}{kT}} - 1 \right) e^{-\frac{x}{L_n}}$$

↑ (offset ignored)



$x=0$

$x=w$

$$\checkmark W \gg L_n$$

$$\Delta n(x) = \Delta n(x=0) \cdot e^{-x/L_n}$$

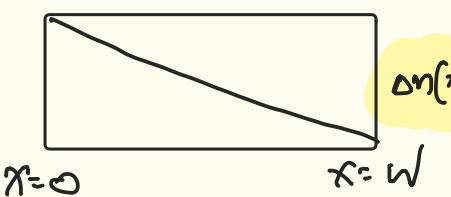
$$\checkmark W \ll L_n$$

$$\left. \begin{array}{l} \text{assume } x=w \text{ is sink} \\ \Delta n(x=w) = 0 \end{array} \right\}$$

$$\Delta n(x) = \Delta n(x=0) \cdot \left[ 1 - \frac{x}{L_n} + \dots \right]$$

High Order Terms  
↓

$$\Delta n(x) = \Delta n(x=0) \cdot \left[ 1 - \frac{x}{L_n} \right] \quad \dots$$



$x=0$

$x=w$

$(W \ll L_n)$

Hyper Profile

$$\Delta n(x) = \Delta n(x=0) \cdot \left[ 1 - \frac{x}{L_n} \right]$$

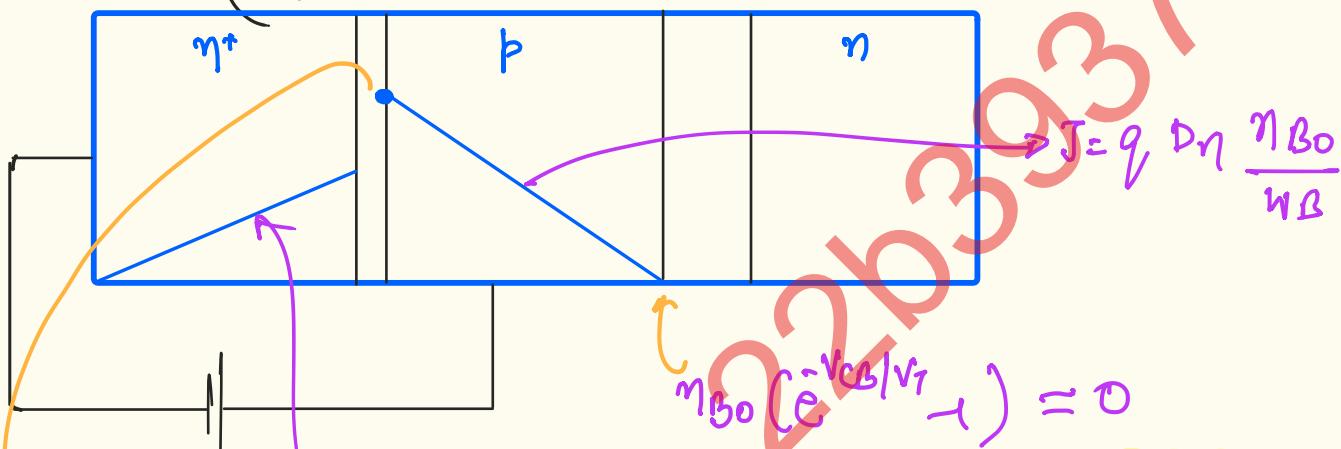
✓ for all practical purposes, we keep  $W_E \ll L_P$

$\therefore$  Linear profile

$$p_E = p_{EO} \left( e^{\frac{V_{BE}}{V_T}} - 1 \right) \left[ 1 - \frac{x}{W_P} \right]$$



✓ for all practical; CB is rev. biased; also  $W_B \ll L_N$   
 Large width gives recomb" which isn't desired



larger cuz more  
c- injection as  
compared to holes.

$$n_B = n_{B0} \left( e^{\frac{V_{CB}}{V_T}} - 1 \right) \left[ 1 - \frac{x}{W_B} \right]$$

$x: 0 \rightarrow \infty$

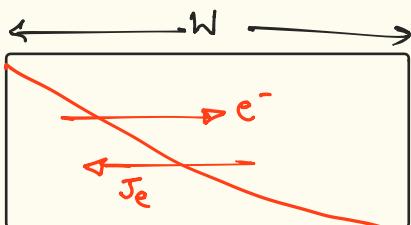
#



$$J = + q_D n \left( \frac{\partial n}{\partial x} \right)$$

$$J = - q_D n \left( \frac{\Delta n(x=0)}{W} \right)$$

$$J = q_D n \cdot \frac{p_{EO}}{W_E}$$



$$x=0 \\ \Delta n(x=0)$$

$$x=W \\ \Delta n(x=W)=0$$

$$\frac{W \ll L_n}{\downarrow} \\ 0.1 - 0.2 \mu_{ms}$$

$$D_n \frac{\partial^2 \Delta n}{\partial x^2} = -\frac{\Delta n}{L_n}$$

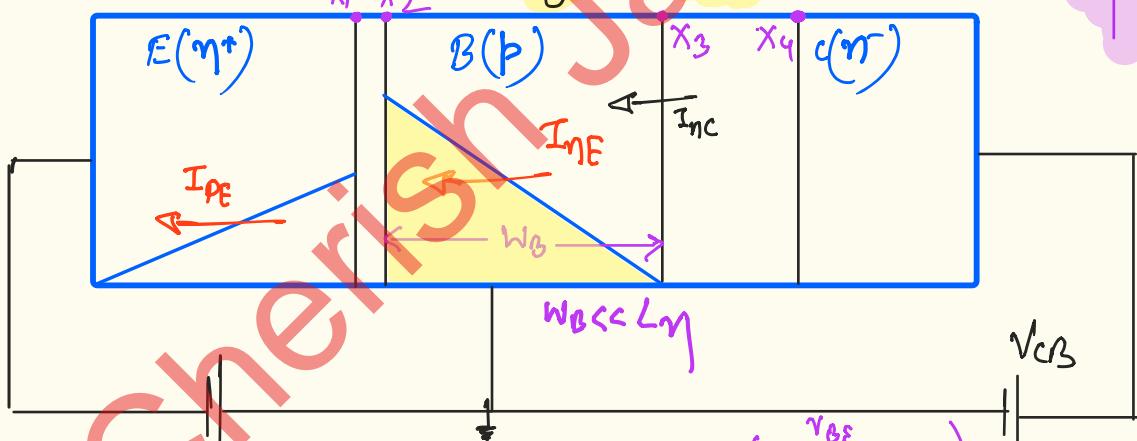
$$\frac{\gamma^2(\Delta n)}{\partial x^2} = -\frac{\Delta n}{L_n^2} ; L_n = \sqrt{D_n \tau_n}$$

$$\frac{\partial^2 \Delta n}{\partial x^2} = 0 \quad \text{if } L_n \ll x$$

Hence linear profile; now put Boundary Cond's {negligible recomb'}

$$\Delta n = \Delta n(x=0) \left[ 1 - \frac{x}{W} \right]$$

$$J = q \cdot D_n \cdot \frac{\partial \Delta n}{\partial x} \\ = q \cdot D_n \cdot \frac{\Delta n(x=0)}{W}$$



$$\Delta p(x_1) = p_{EO} \left( e^{\frac{V_{BE}}{V_T}} - 1 \right)$$

$$\Delta n(x_2) = n_{BO} \left( e^{\frac{V_{BE}}{V_T}} - 1 \right)$$

{ @ eq'n }

$$J_{pE} = \left| q \cdot D_p \left( \frac{\partial \Delta p}{\partial x} \right) \right| = \frac{q \cdot D_p \cdot \Delta p(x_1)}{W_E}$$

{ Current Constituted by holes in emitter }

$$\therefore I_{pE} = A \cdot q \cdot D_p \cdot \frac{\Delta p(x_1)}{W_B}$$

$$I_{nE} = A \cdot q \cdot D_n \cdot \frac{\Delta n(x_2)}{W_E}$$

$$\gamma = \frac{I_{nE}}{I_E} = \frac{I_{nE}}{I_{nE} + I_{pE}}$$

$$= \frac{1}{1 + \frac{I_{pE}}{I_{nE}}}$$

$$\gamma = \frac{1}{1 + \frac{D_p \cdot \rho_{EO}}{D_n \cdot \eta_{BO}} \left( \frac{W_B}{W_E} \right)}$$

$$\gamma \approx 1$$

$\frac{W_B}{W_E} \rightarrow$  as small as possible

\*  $\frac{\rho_{EO}}{\eta_{BO}}$  → as small as possible

$$\rho_{EO} \ll \eta_{BO}$$

$$\frac{\eta_i^2}{N_D, G} \ll \frac{\eta_i^2}{N_A, B}$$

## # Base Transport factor ( $\alpha_T$ )

$$\frac{I_{\eta c}}{I_{\eta E}} = \frac{I_{\eta E} - I_{rec.}}{I_{\eta E}}$$

$$= 1 - \frac{I_{rec.}}{I_{\eta E}} = 1 - \frac{q \frac{1}{2} \cdot \Delta n(x_2) \cdot w_B}{g \cdot D_\eta \cdot \frac{\Delta n(x_2)}{w_B}}$$

$$J_{rec} = \frac{A \cdot q \cdot \frac{1}{2} \Delta n(x_2) \cdot w_B}{\zeta_\eta}$$

$$I = \frac{d\phi}{dt}$$

Hence  $\alpha_T = 1 - \frac{w_B^2}{2 \zeta_\eta^2}$

for  $\alpha_T \rightarrow 1$   
 $w_B \leftrightarrow L_{nB}$

$\alpha \approx 0.89$

#  $B = \frac{I_C}{I_B} = \frac{I_C}{I_C - I_E} = \left( \frac{I_C/I_E}{I_C/I_E - 1} \right)$

$B = \left| \frac{d}{\alpha - 1} \right|$

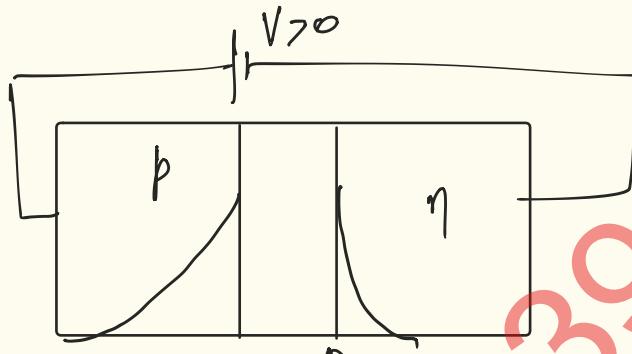
$B = 99$

$$I_C \approx I_E$$

$$I_C \gg I_B$$

# Rev. Bias profile

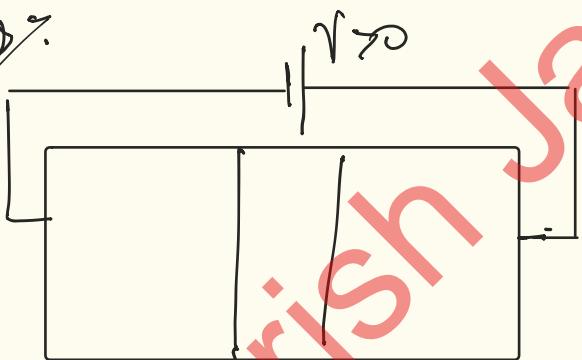
forward bias



$$\Delta p = \Delta p(x=0) \left[ 1 - e^{-x/L_p} \right]$$

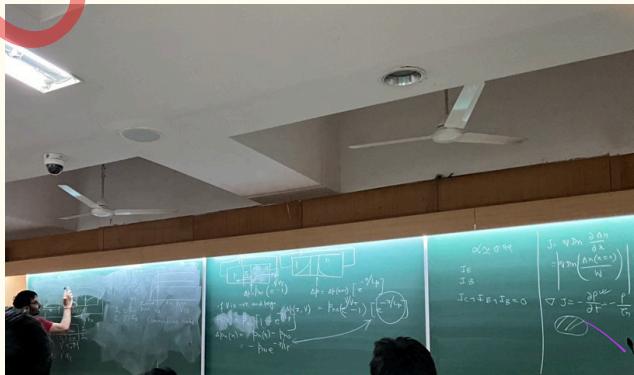
$$\Delta p(x=0) = p_{n_0} (e^{V/V_T}) (1 - e^{-x/L_p})$$

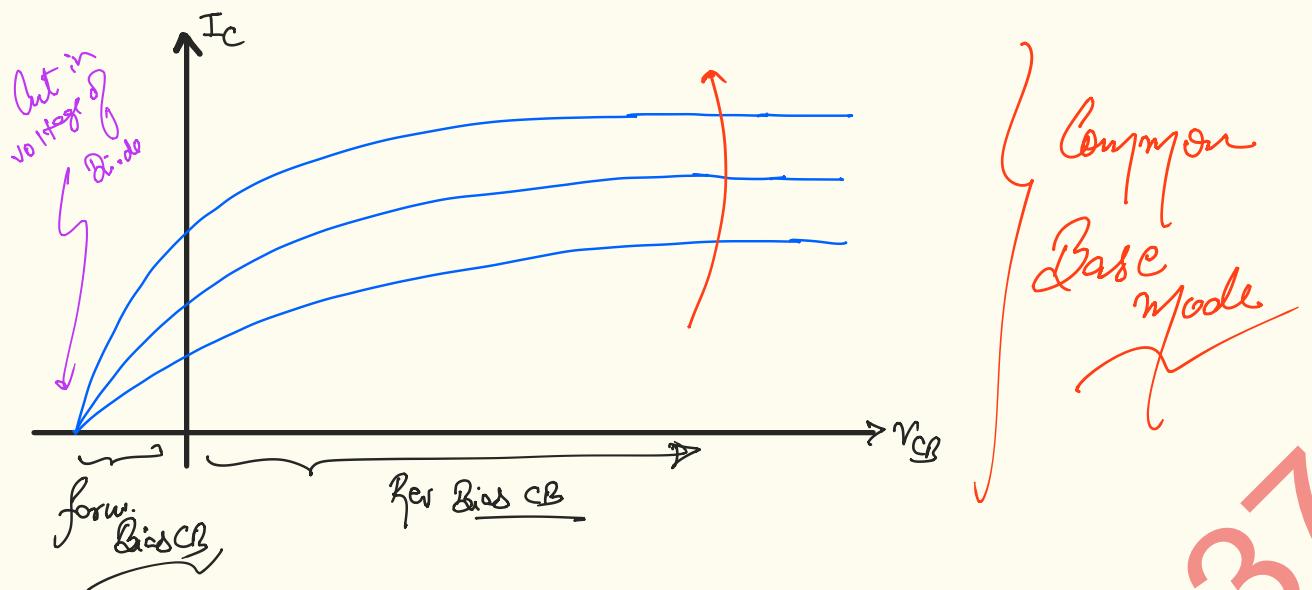
Rev. bias



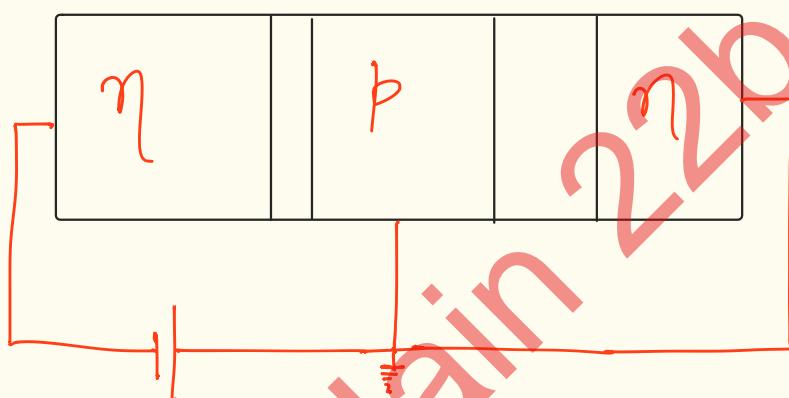
$$p_{n_0} (e^{V/V_T} - 1)$$

if  $V < 0$  & very

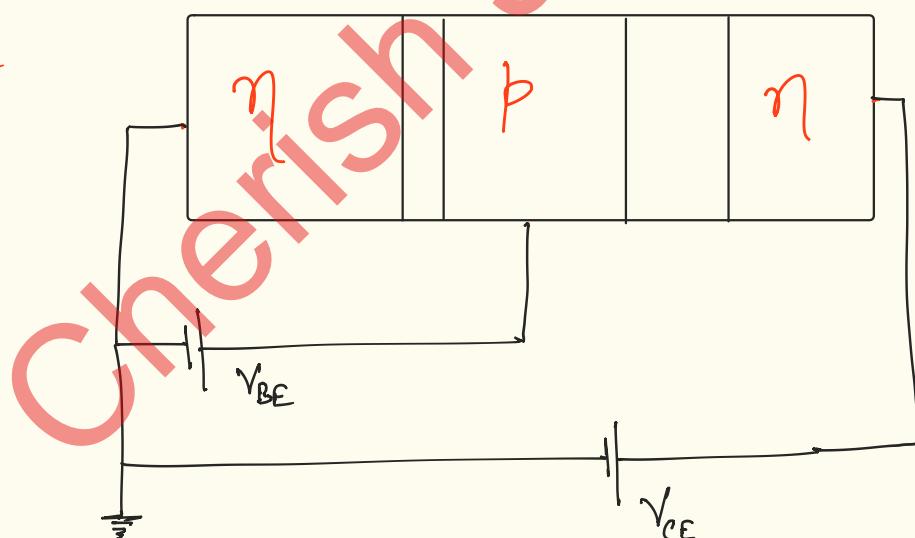




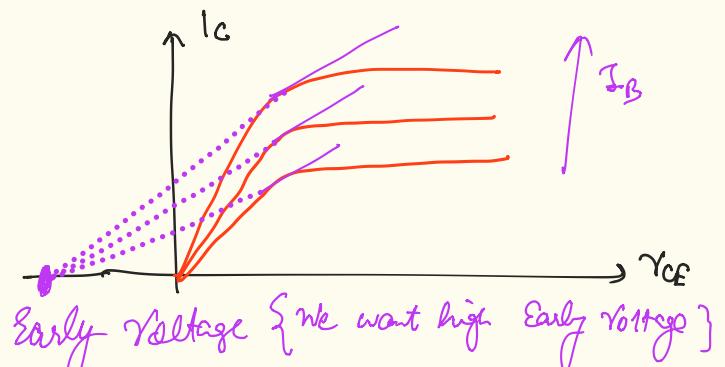
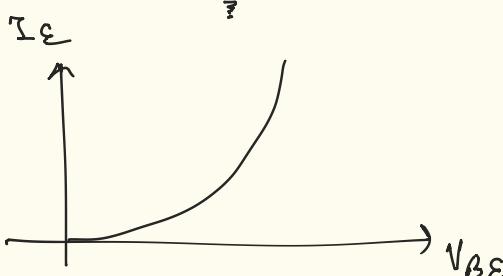
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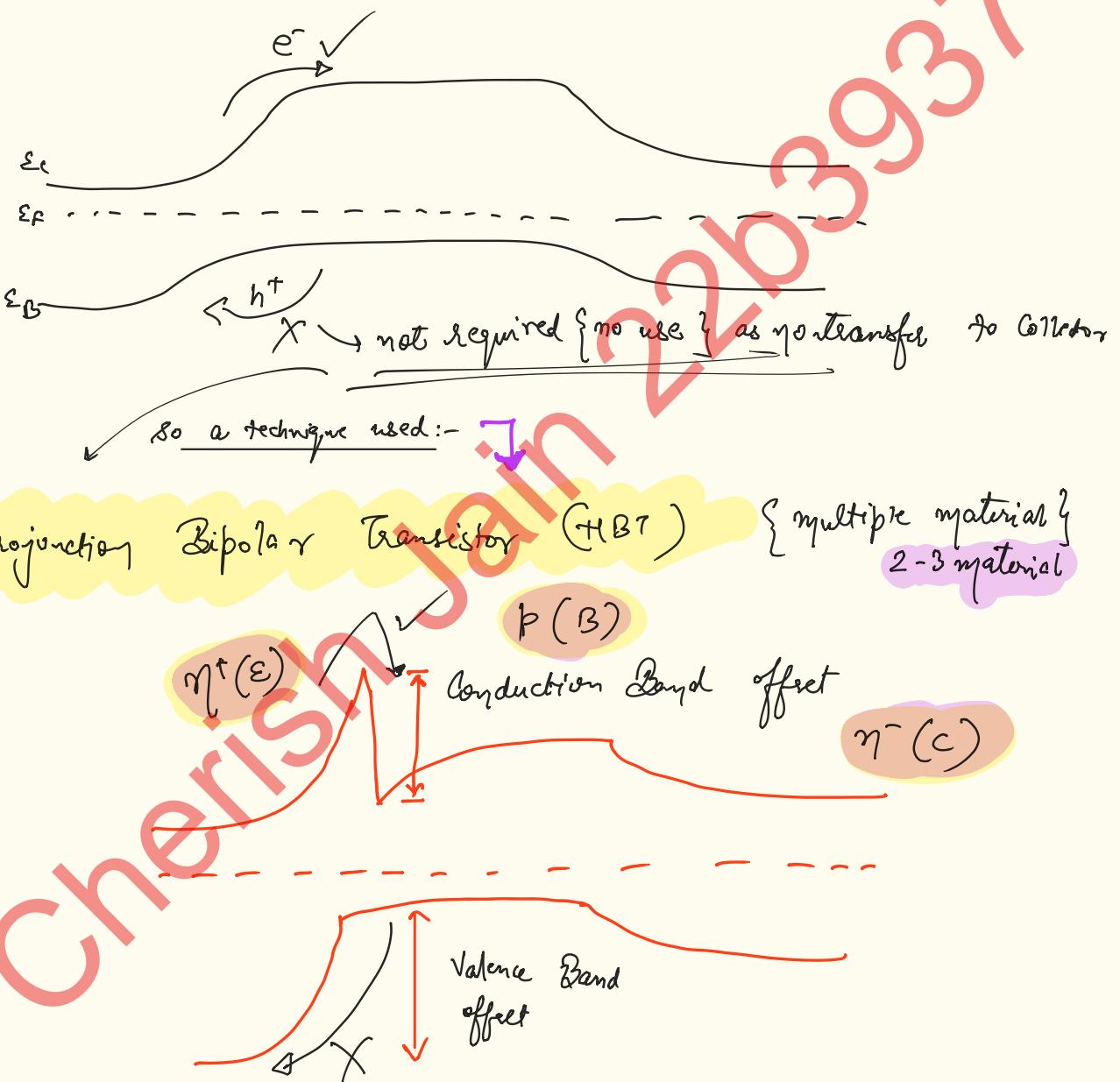
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$$V_{CE} = V_{CB} + V_{BE}$$

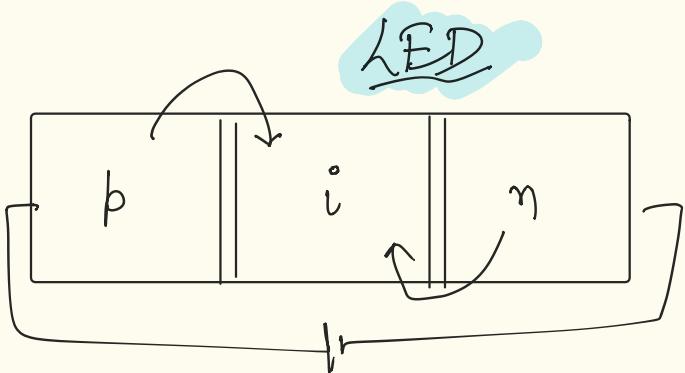


## # Technique to ↑ α, β



# p-i-n diode.

Laser Characteristics



- 1) Directional
- 2) Intensity
- 3) faster recombination
- 4) Spectral Purity

Cherish Jain 22b3931

cherish Jain 22b3937V