

### MTH 372: Quiz III

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#### Instructions

- Show all your work to score full marks.
  - Show results in their simplest forms.
1. (5 points) Let  $X_1, \dots, X_n$  be i.i.d. from  $N(\mu, \sigma^2)$  where  $\mu$  is unknown and  $\sigma$  is known. Find a pivot quantity based on the random sample, and then use the pivot quantity to set up a two-sided  $(1 - \alpha)$  confidence interval for  $\mu$ . The hypothesis  $H_0 : \mu = \mu_0$  versus  $H_1 : \mu \neq \mu_0$  could be considered.
  2. (2 points) Let  $X_i$  be independent  $\text{Binomial}(n_i, p)$ ,  $i = 1, \dots, k$ . Let  $U = \sum_{i=1}^k X_i$ , find the distribution of  $U$ .