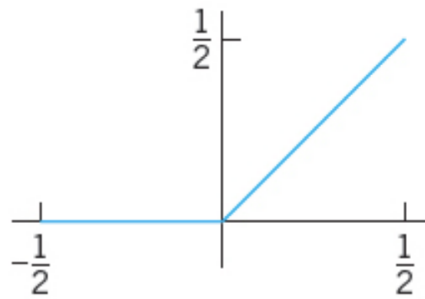


**Problem 1.** Find the Fourier series of the function  $x^2$  which is assumed to be periodic outside with period  $2\pi$  when  $-\pi < x < \pi$ .

**Problem 2.** Find the Fourier series of the periodic function  $f(x)$ , such that

$$f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ x, & 0 < x < \pi \end{cases}$$

**Problem 3.** Calculate the Fourier series of period  $p = 1$  of the function below



**Problem 4.** Find a general solution of the ODE

$$y'' + \omega^2 y = \sin(\alpha t) + \sin(\beta t)$$

with  $\omega^2 \neq \alpha^2, \beta^2$ .

**Problem 5.** Find the eigenvalues and eigenfunctions of

$$\left(\frac{y'}{x}\right)' + (\lambda + 1)\frac{y}{x^3} = 0 \quad y(1) = 0, \quad y(e^\pi) = 0$$

The following strategy is suggested:

- Do the change of variable  $x = e^t$ .
- Find the general solution without considering boundary constraints.
- Apply the boundary conditions to find the eigenvalues and eigenfunctions of the ODE.