

Worksheet-2  
Course Name: Math-III (Section-A)  
Total marks = 20  
Date: 14/09/2022

1. Find the limits (if exists) of the following functions:. (2+2+2+2)
  - (a)  $\lim_{(x,y) \rightarrow (\pi/2,0)} \frac{\cos y + 1}{y - \sin x}$
  - (b)  $\lim_{(x,y) \rightarrow (0,0)} \frac{e^y \sin x}{x}$
  - (c)  $\lim_{(x,y,z) \rightarrow (1,-1,-1)} \frac{2xy+yz}{x^2+z^2}$
  - (d)  $\lim_{(x,y) \rightarrow (4,3)} \frac{\sqrt{x}-\sqrt{y+1}}{x-y-1}; x \neq y+1$
2. If  $f(x_0, y_0) = 3$ , what can you say about  $\lim_{(x,y) \rightarrow (x_0, y_0)} f(x, y)$  if  $f$  is continuous at  $(x_0, y_0)$ ?  
If  $f$  is not continuous at  $(x_0, y_0)$ ? Give reasons for your answer. (4)
3. At what point  $(x, y)$  in the plane is the function  $f(x, y) = \frac{x^2+y^2}{x^2-3x+2}$  continuous ? (4)
4. Show that the function  $f(x, y) = \frac{xy}{|xy|}$  have no limits as  $(x, y) \rightarrow (0, 0)$ . (4)