

Quiz-5
Solution

From the figure, we get-

$$y(t) = 10t$$

$$-1 < t \leq 1$$

(ie in one time period)

Also, since $T=2$ ——— ① mark
 $\omega_0 = \pi$ ——— ① mark

Using the Fourier series expansion, we have

$$c_k = \frac{1}{2} \int_{-1}^1 10t e^{-jk\pi t} dt$$

$$= 5 \int_{-1}^1 t e^{-jk\pi t} dt$$

$$= 5 \left[\frac{t e^{-jk\pi t}}{-jk\pi} - \frac{e^{-jk\pi t}}{(jk\pi)^2} \right]_{-1}^1$$

$$= 5 \left[\left(\frac{e^{-jk\pi}}{-jk\pi} + \frac{e^{jk\pi}}{-jk\pi} \right) - \left(\frac{e^{-jk\pi}}{(jk\pi)^2} - \frac{e^{jk\pi}}{(jk\pi)^2} \right) \right]$$

$$\therefore e^{-jk\pi} = e^{jk\pi} = (-1)^k$$

$$= \frac{10(-1)^k}{-jk\pi}$$

$$= \frac{10j(-1)^k}{k\pi}$$

$$k \neq 0$$

— 2 marks

2 marks

— ① mark

