

MTH210 – SUBMISSION_202210139

For $n \in \mathbb{Z}^+$, $n \geq 2$, put $X_n = \{1, 2, \dots, n\}$ and put $V = \{0, 1\}$. How many functions are there from X_n to V , which :

- a) Are injective ? (1 mark)
- b) Assign 0 to both 1 and n ? (2 marks)
- c) Assign 1 to exactly one of the positive integers $< n$? (2 marks)

Note: Show your calculations if any, and give a brief explanation of your approach (one or two sentences).

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List of Common Errors and Marks Deductions:

1. Using an undefined symbol.
2. Writing an equation in which the LHS and RHS are not comparable. For example, the LHS is a set, and the RHS is an integer.
3. Writing a meaningless or completely illogical statement.

Deduct 0.5 marks for each occurrence of an error of the above type. **However, the total marks for the submission should remain non-negative.**

Marks to be awarded as follows:

Part a) \rightarrow 0.25 marks for each correct answer (2 cases, $n = 2$, $n \geq 3$);
0.25 marks for each explanation.

Part b) \rightarrow 1 mark for answer; 1 mark for explanation.

Part c) \rightarrow 1 mark for answer; 1 mark for explanation.

Remark: Very easy questions – no partial credit.