

Q. 1 Find the current in the $10\ \Omega$ resistance in the circuit shown in Fig. 1.

[5 Marks]

Q.1

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Doing $\Delta \rightarrow Y$ transformation, we get following circuits:

$$I = \frac{180}{4 + 4 + 34 + 10 + 10} = \frac{180}{62} \text{ Amp.}$$

$$V_{AB} = \frac{180}{62} \times (4 + 34 + 10) = \frac{180 \times 48}{62}$$

R_{AB}

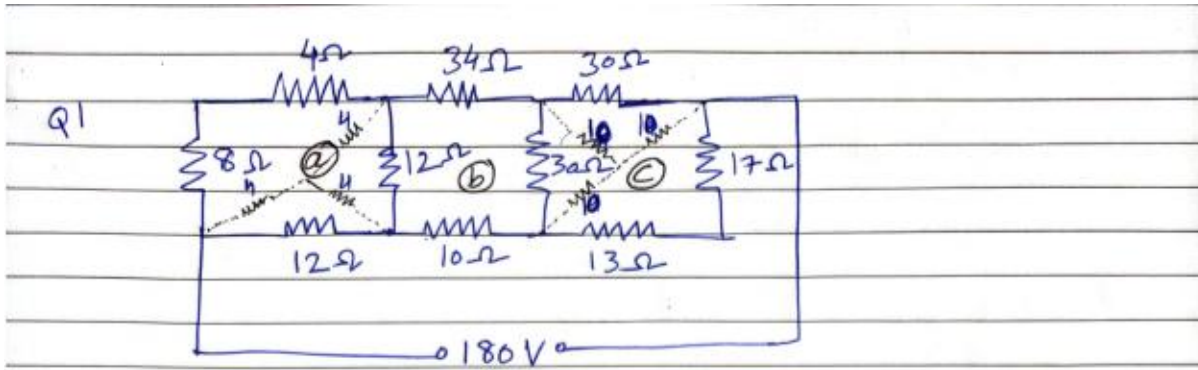
$$R_{AB} = 4 + 10 + \frac{48 \times 14}{62} = 14 + \frac{672}{62}$$

$$= \frac{868 + 672}{62} = \frac{1540}{62} \Omega$$

$$I_{10} = \frac{180 \times 48}{62} \times \frac{1}{10 + \frac{1540}{62}} = \frac{180 \times 48}{62} \times \frac{62}{620 + 154}$$

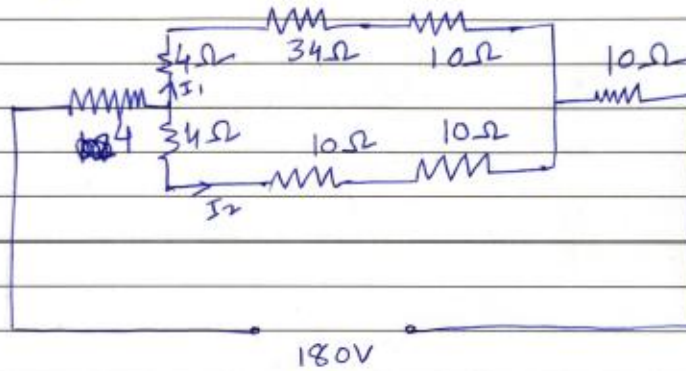
$$\frac{180 \times 48}{2160} = 4A$$

OR



Sohn

Applying Delta to star conversion in a & b, we get



$$I = \frac{180}{30} = 6 \text{ A}$$

$$I_2 = \frac{48}{48+24} \times 6 = \frac{48}{72} \times 6 = 4 \text{ A}$$

\therefore I in 10Ω is 4A

Q. 2 Use the Principles of Superposition to find the current in $2\ \Omega$ resistance connected between A and B in circuit shown in Fig. 2.

[5 Marks]

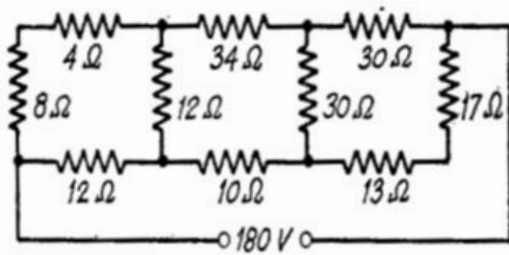


Figure 1

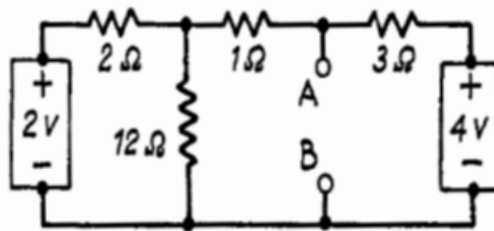


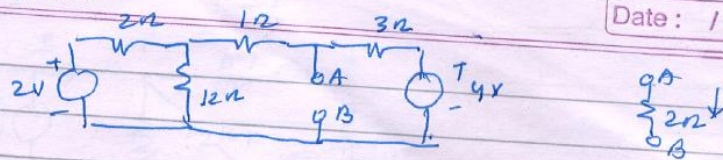
Figure 2

Q2

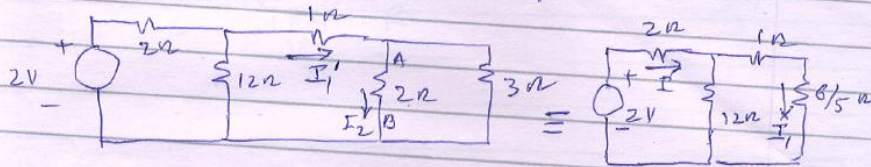
Superposition

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Taking left source into account only, the circuit reduces to



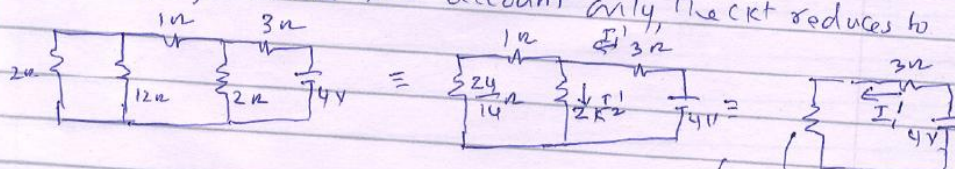
$$I_1 = \frac{2}{2 + \frac{12 \times 2}{12 + 2}} = \frac{2}{2 + \frac{24}{5}} = \frac{2}{\frac{14}{5}} = \frac{10}{7} \text{ A}$$

$$I_1' = \frac{12 \times I_1}{12 + 2} = \frac{12}{14} \times \frac{10}{7} = \frac{10}{4.9} \text{ A}$$

$$I_2' = \frac{3}{3 + 2} \times I_1 = \frac{3}{5} \times \frac{10}{7} = \frac{6}{7} \text{ A}$$

$$I_2 = \frac{36}{71} \text{ A} = 0.507 \text{ A} = 0.2535 \text{ A}$$

Taking right source into account only, the circuit reduces to



$$I_2' = \frac{4}{3 + \frac{76}{66}} = \frac{4 \times 66}{198 + 76} = \frac{264}{274}$$

$$I_2' = \frac{I_2' \times 38/14}{38/14 + 2} = \frac{I_2' \times 38}{66} = \frac{4 \times 66}{274} \times \frac{38}{66} = \frac{76}{274} \text{ A}$$

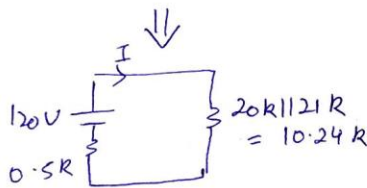
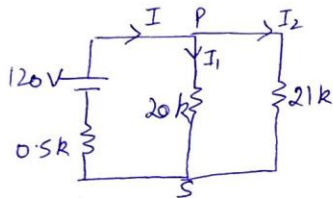
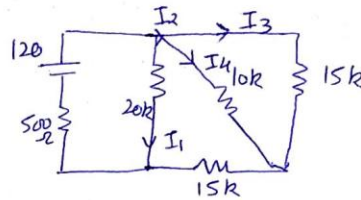
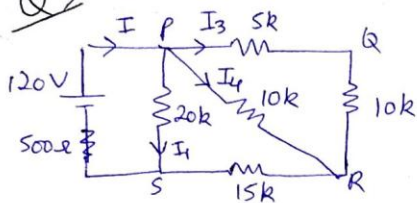
$$\left(\frac{2 \times \frac{38}{14}}{38 \times 2/14} \right) \times \frac{264}{274} = \frac{76}{274} \text{ A}$$

Q. 3 Determine the (a) current given by 120 V battery (b) potential difference across RS and (c) magnitude and direction of current in PR for the circuit shown in Fig. 3.

[5 Marks]

ANS:

Q3.



All correct circuits

2 marks

$$I = \frac{120V}{0.5k + 10.24k} = \frac{120V}{10.74k} = 11.17 \text{ mA}$$

1 mark

$$I_1 = \frac{21}{20+21} \cdot I = \frac{21}{41} \times 11.17 = 5.72 \text{ mA}$$

$$I_2 = \frac{20}{20+21} \cdot I = \frac{20}{41} \times 11.17 = 5.44 \text{ mA}$$

$$I_3 = \frac{10}{10+15} \cdot I_2 = \frac{10}{25} \times 5.44 = 2.176 \text{ mA}$$

1 mark

$$I_4 = I_2 - I_3 = 5.44 - 2.176 = 3.264 \text{ mA}$$

$$V_{RS} = 15k \times 5.44 \text{ mA} = 81.6 \text{ V}$$

1 mark

Q. 4 What is the difference in potential between the points X and Y, in the circuit shown in Fig. 4.

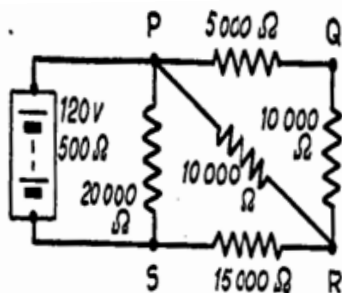


Figure 3

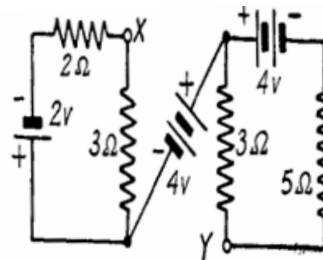


Figure 4

[5 Marks]

Q. 4

$V_{xy} = ?$

$$I_1 = \frac{2}{2+3} = \frac{2}{5} = 0.4 \text{ Amp} \quad (1)$$

$$I_2 = \frac{4}{3+5} = \frac{4}{8} = 0.5 \text{ Amp} \quad (1)$$

$$V_{xy} = V_{X1} + V_{12} + V_{2Y}$$

$$= -3I_1 - 4V + 3I_2 \quad (2)$$

$$= -3 \times 0.4 - 4 + 3 \times 0.5$$

$$= -3.7V$$

Point Y is 3.7V more positive than point X

Q. 5 State whether the following statements are TRUE or FALSE. Give appropriate justification for your answer in brief.

- I. In Fig. 3(a), the switch has been in position A for a long time. If the switch is moved suddenly from A to B at $t = 0$, the current flowing through the resistance 2 K ohm at time $t = 20 \text{ ms}$ will be equal to 10 mA.

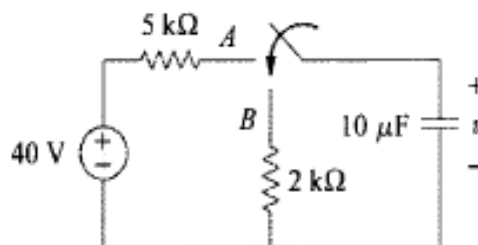


Figure 3(a)

ANS:

Since switch has been in position A for long time, the capacitor will be charged to source voltage i.e. $v = 40 \text{ V}$.

So $v(0^-) = 40 \text{ V}$.

After switch is moved to position B, the capacitor will discharge through 2 k resistance. And the capacitor voltage $v(t)$ is given as

$$v(t) = v(0) e^{-\frac{t}{2k810\mu}}$$

$$= 40 e^{-t/20\text{ mS}}$$

At $t = 20\text{ mS}$, $v(20\text{ mS}) = v_1 = 40 e^{-20\text{ mS}/20\text{ mS}} = 40 e^{-1}\text{ V}$

Current $= v_1/2K = 7.35\text{ mA}$

FALSE

- II. A DC voltage of 200 V is suddenly applied across a series circuit consisting of resistance 10 ohm in series with an inductance of 0.1 H. The voltage across the inductance just after the application of voltage is equal to 0 V and current at 0.01 s is also 0 A.

ANS:

At the instant of switching on $I = 0$, so $I R = 0$, hence all applied voltage drop across inductance only. **Voltage drop across inductance = 200 V not 0 V as given.**

At $t = 0.01\text{ s}$, current grows exponentially and the applied voltage is partly drops across resistance and partly across the coil.

The time period of the circuit $= L/R = 0.1/10 = 0.01\text{ s}$ and given time is equal to time constant. Thus current is not 0 A.

FALSE

- III. Transient disturbance is produced in a circuit only when its applied voltage or applied current are suddenly changed.

ANS:

TRUE

When a switched is either made on or off, there is sudden change in applied voltage or current through the circuit containing energy storage elements i.e. L and C.

The other reasons are shorting of the circuit of sudden change in supply voltage or current..

Thus there will be transient disturbances.

- IV. There are no transients in a circuit consisting of only resistance because the circuit obeys Ohm's law

ANS:

FALSE

The circuit obeys ohms law, but there are no energy storage element in purely resistive circuits.

So for transient we must have L or C connected in purely resistive elements.

- V. The time constant associated with the circuit in Fig. 3(b) is 4 s.

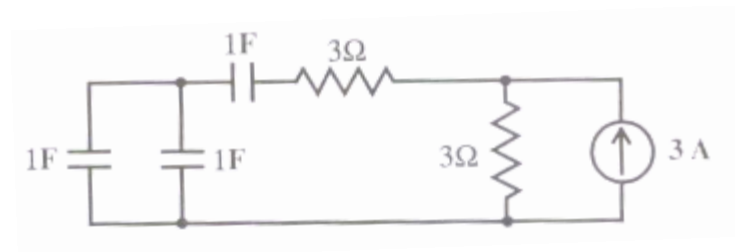


Figure 3(b)

Figure 3

ANS:

Total resistance will be 6 ohms.

Total capacitance is 1 F capacitance in series with two 1 F capacitance in parallel.

Total capacitance = $1 \times 2 / (1 + 2) = 2/3$ F

Time constant = 6 ohm \times $2/3$ F = 4 s

TRUE

[5 X (1+3) = 20 Marks]

Q. 6 A student is given an unknown resistive network as illustrated in Figure 4(a). She/he wishes to determine whether the network is linear, and if it is, what its Thévenin equivalent circuit is.

The only equipment available to the student is a voltmeter (assumed ideal), 100-k Ω and 1-M Ω test resistors that can be placed across the terminals during a measurement as in Figure 4(b).

The following data were recorded:

Test Resistor	Voltmeter Reading
Absent	1.5 V
100 k Ω	0.25 V
1 M Ω	1.0 V

What should the student conclude about the network from these results? Support your conclusion with plots of the network v i characteristics.

ANS:

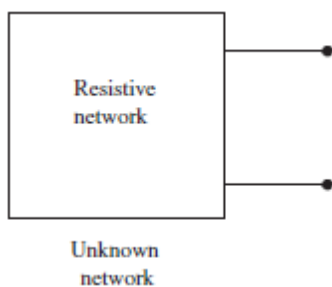


Figure 4(a)

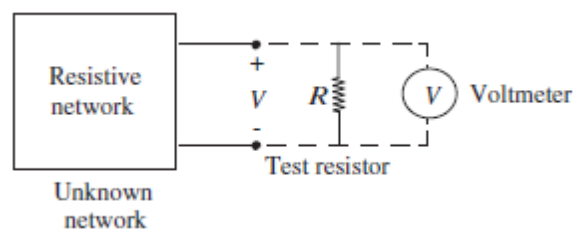
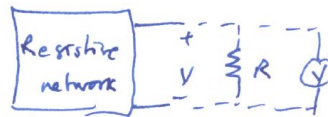


Figure 4(b)



Unknown network



Unknown network

(a) $R = \infty$

$$V_{DC} = 1.5 \text{ V}$$

$$R_1 = 100 \text{ k}$$

$$V_1 = 0.25 \text{ V}$$

$$R_2 = 1 \text{ M}$$

$$V_2 = 1 \text{ V}$$

Since open circuit voltage $= 1.5 \text{ V}$; $V_T = 1.5 \text{ V}$

$$V_1 = \frac{V_T}{R_T + R_1} \times R_1 = \frac{1.5 \times R}{R_T + R} = \frac{1.5 \times 100 \text{ k}}{R_T + 100 \text{ k}} = 0.25$$

$$150 = 0.25 R_T + 25$$

$$0.25 R_T = 125 \Rightarrow R_T = \frac{125}{0.25}$$

$$= 500 \text{ k}\Omega$$

$$V_2 = \frac{V_T}{R_T + R_2} \times R_2 = \frac{1.5 \times 1 \text{ M}}{R_T + 1} = 1 \text{ V}$$

$$R_T + 1 = 1.5$$

$$R_T = 1.5 - 1 = 0.5 \text{ M}$$

Network is linear