

## Quiz 1

Time: 10:30AM - 11:50AM

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*Instruction: Uploading of your answer sheet needs to be completed before 12:00PM in your google classroom page. Any upload after 12:00PM but before 1:00PM will result in 2 points deducted from your final score. Any upload after 1:00PM will not be counted.*

*Your answers to question 3, 4 and 5 needs to be properly explained. All steps leading to your conclusion should be clearly demonstrated, to obtain full score for these three questions.*

*You may refer to the text book or class-notes.*

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1. Identify each of the following subsets of the Euclidean plane  $\mathbb{R}^2$  as open set or closed set or neither: *[0.5 point each]*

- (a)  $\{(x, y) : x^2 + y^2 < 2\}$ .
- (b)  $\{(x, y) : |x| + |y| < 1\}$ .
- (c)  $\{(x, y) : \max(|x|, |y|) \leq 1\}$ .
- (d)  $\{(0, y) : 0 < y < 1\}$ .

2. Find and sketch the domains for each of the following functions: *[1 point each]*

- (a)  $f(x, y) = \sqrt{(x^2 - 25)(y^2 - 16)}$ .
- (b)  $f(x, y) = \tan^{-1}\left(\frac{y}{x}\right)$ .

3. Find all the points for which the following function is continuous: *[2 points]*

$$f(x, y, z) = \frac{1}{z - \sqrt{x^2 + y^2}}$$

4. Does the following limit exist? *[2 points]*

$$\lim_{(x,y) \rightarrow (1,1)} \frac{xy^2 - 1}{y - 1}$$

5. Let

$$f(x, y) = \begin{cases} 0, & \text{if } x^2 < y < 2x^2 \\ 1, & \text{otherwise.} \end{cases}$$

Show that  $f_x(0, 0)$  and  $f_y(0, 0)$  exists, but  $f$  is not differentiable at  $(0, 0)$ . *[2 points]*