

Casey Levy

CS 225: Discrete Structures in CS

Homework 9 – Part 1

Set 10.1

**#9 (i).**

$e_1, e_2, e_7$

**(ii).**

$v_1, v_2$

**(iii).**

$e_2, e_7$

**(iv).**

$e_1, e_3$

**(v).**

$e_4, e_5$

**(vi).**

$v_4$

**(vii).**

2

**(viii).**

14

**#22.**

This kind of graph does not exist because the most degrees a graph of 5 vertices can have is 4.

**#37f.**

The graph is not bipartite since  $v_1 \in V_1$ ,  $v_2 \in V_2$ ,  $v_3 \in V_1$  and  $v_4 \in V_2$ .  $v_5$  isn't an element of either set.

**#44a.**

Yes because there are at most  $n-1$  edges between a vertex and another vertex.

**b.**

Based off what we know from above, a graph with 4 vertices ( $n$ ), means each degree is  $n-1$  giving us degrees of 0,1,2 and 3.  $v_3$  must be connected to all other vertices but  $v_0$  cannot be connected since it has no edges. Therefore the answer is no.

**c.**

Similar to above, there cannot be a graph with all different degrees if there exists a vertex degree of 0.