

# **Principles of Compiler Construction**

```
Step:
1文法预处理
2自底向上,增广文法 S'->S
自自顶向下
3parsing table
```

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# Lecture 7. LR Parsing

- 1. Introduction to LR Parsing
- 2. Motivation of LR Parsing
- 3. Simple LR Parsing
  - LR(0) and SLR(1)
- 4. More Powerful LR Parsing
  - LR(1) and LALR(1)
- 5. Ambiguity in LR Parsing
- 6. Error Recovery in LR Parsing

# 1. Introduction to LR Parsing



### Proposed by

- D. Knuth (Stanford U.). **On the Translation of Languages from Left to Right**. Information and Control, 8(6), 1965, pp.607-639
  - Prof. 高德纳: The Art of Computer Programming(TAOCP), T<sub>E</sub>X, Literate Programming, LR Parsing, Attribute Grammar, etc.

### Pros

- Recognize almost all practical CFGs (more powerful than LL parsing).
- High efficiency.
- Detect errors as soon as possible.

#### Cons

- A large size of parsing table.
- Hard to construct the parsing table manually.

# 2. Motivation of LR Parsing

- Critical: shift-reduce decision making
  - Maintain states to keep track of where we are in the parsing procedure.
- States are represented by items
  - A  $\rightarrow$  X Y Z yields four items (LR(0) items)

```
stacko A \rightarrow • X Y Z Tookstack

\circ A \rightarrow X • Y Z

\circ A \rightarrow X Y • Z

\circ A \rightarrow X Y Z •
```

• A  $\rightarrow \epsilon$  yields only one item: A  $\rightarrow$  •

### Items

- Different forms of items
  - $A \rightarrow X \bullet a Z$   $S \rightarrow bBB \longrightarrow$  移进状态
    - A "shift" item 移进项目
    - Indicates the shift of symbol a.
  - $\bullet \ \mathsf{A} \ \to \ \mathsf{X} \bullet \mathsf{B} \mathsf{Z}$ 
    - A "reduce-expected" item. 待约项目
    - Indicates the expectation of reducing a B from the remaining input string.
  - $\bullet A \rightarrow X Y Z \bullet$ 
    - A "reduce" item 归约项目
    - Indicates a handle has appeared on top of stack.
  - $\bullet S \rightarrow XYZ \bullet$ 
    - An "accept" item (special form of reduce items)
    - Indicates the state of accepting the input.

# Augmented Grammar 拓展文法

- o How and why of augmented grammars?
  - Add a new start symbol S'

$$\begin{array}{ccc} \circ \ \mathsf{S}' \ \to \ \mathsf{S} \\ \circ \ \mathsf{S} \ \to \ \ldots \end{array}$$

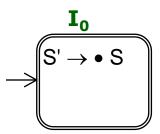
- Intent of augmenting a grammar
  - The start symbol will never appear in the body of any productions.
  - Then the accepting state (items) is unique:

$$S' \rightarrow S \bullet$$

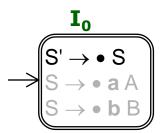
# A Motivating Example

Consider the following grammar

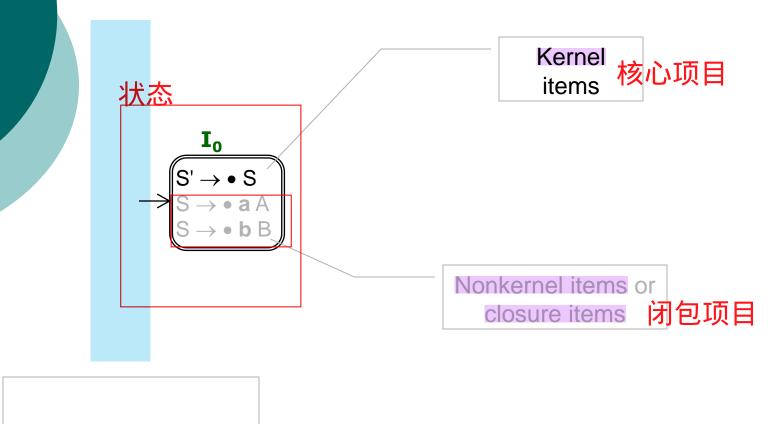
```
S' \rightarrow S
S \rightarrow aA \mid bB
A \rightarrow cA \mid d
B \rightarrow cB \mid d
```



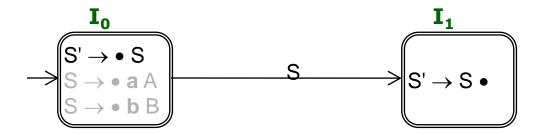
Initial state



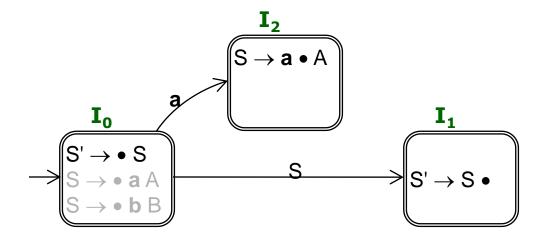
Equivalent closure



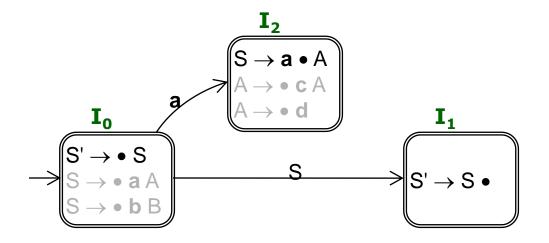
Equivalent closure



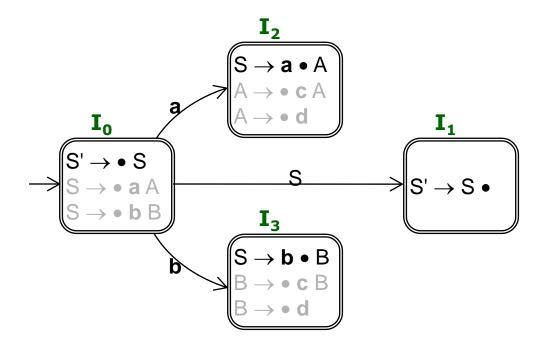
If the remaining string can be reduced to S (expected!)



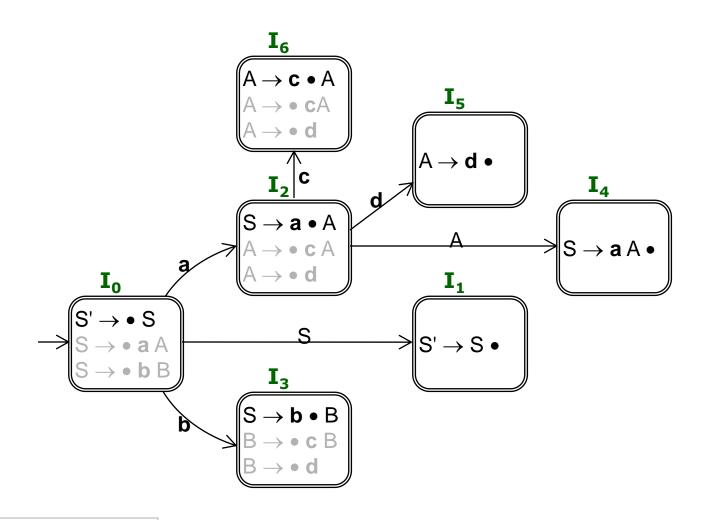
If the first symbol of remaining string is **a** (shift!)



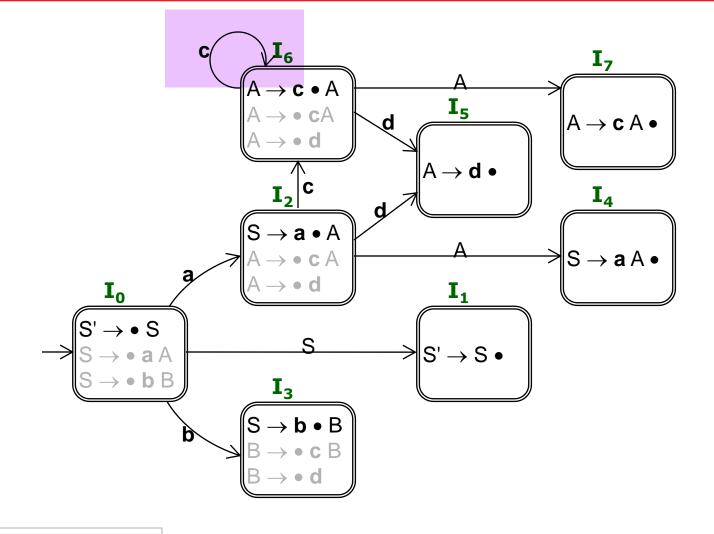
Equivalent closure in state  ${\rm I_2}$ 



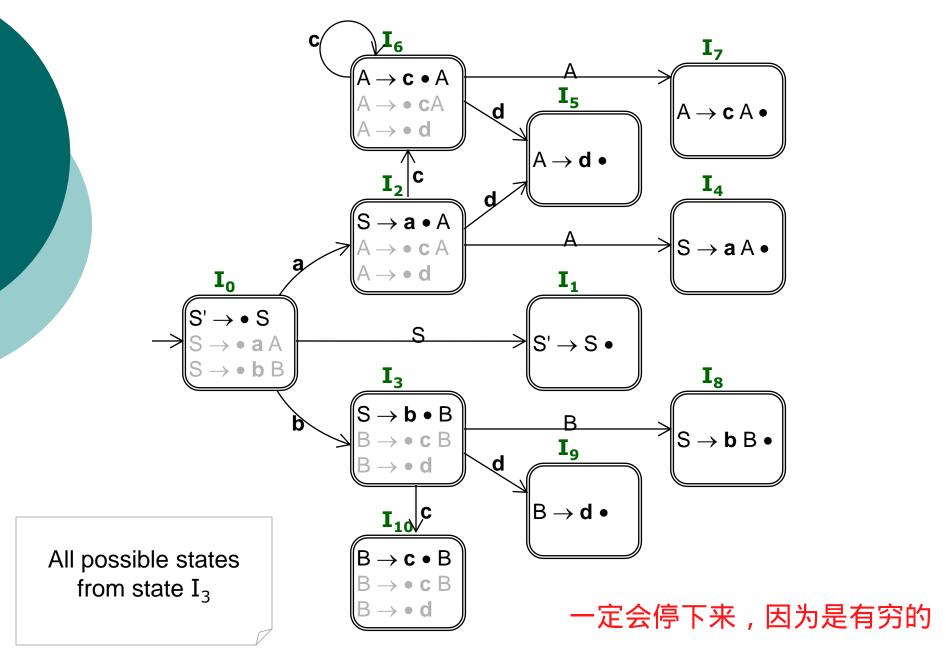
If the first symbol of remaining string is **b** (shift!)

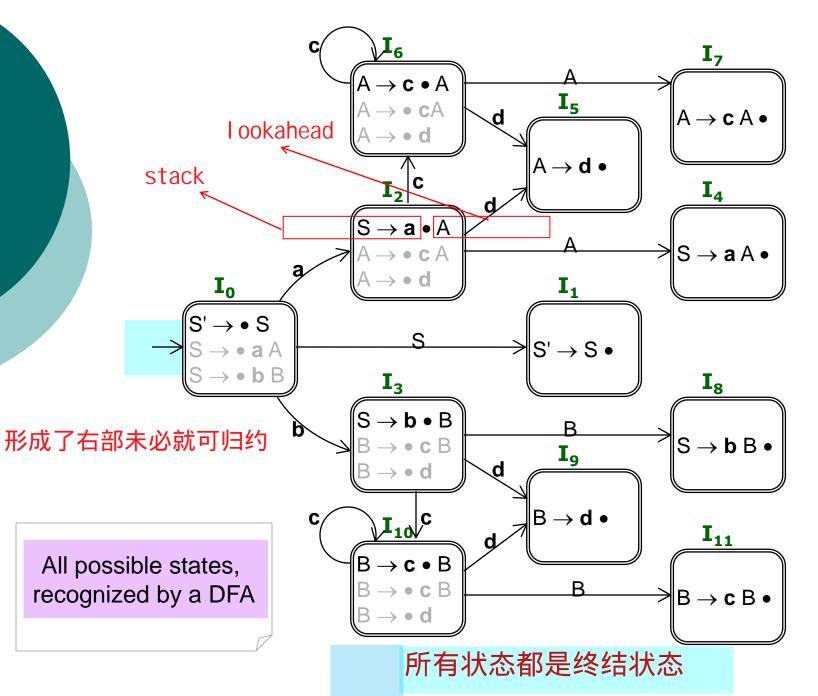


All possible states from state  $I_2$ 



All possible states from state  ${\rm I}_6$ 





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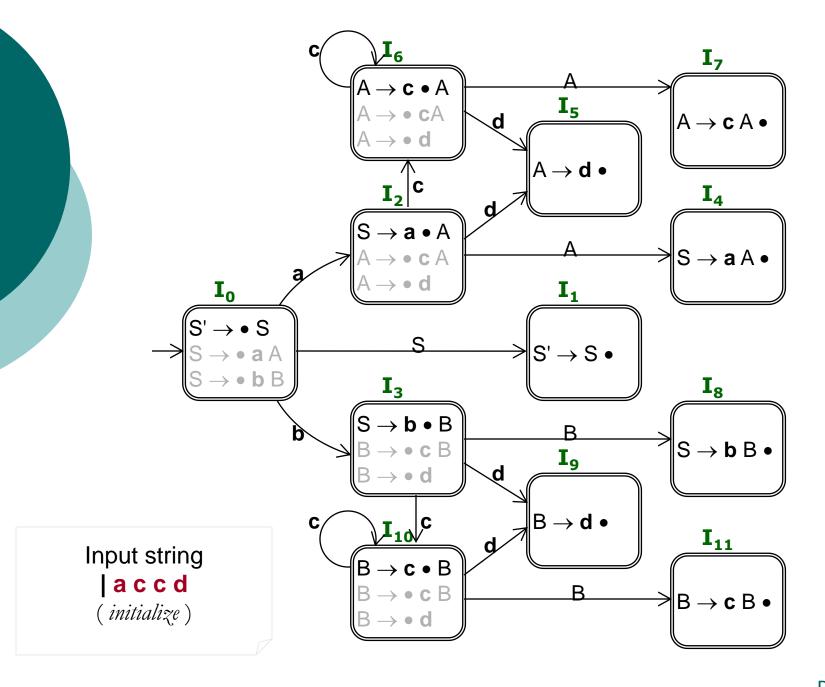
# Working with the DFA

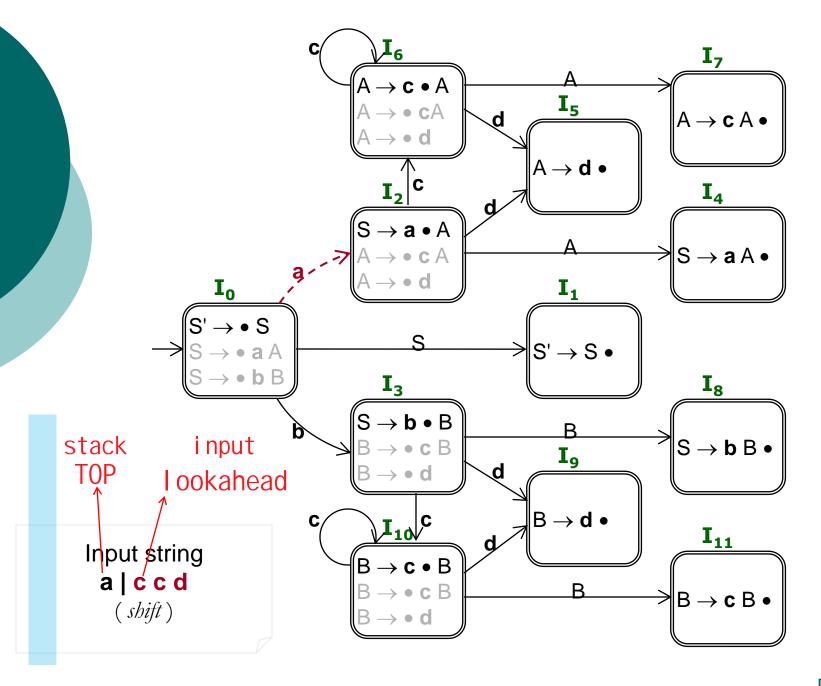
Consider the following sentence:

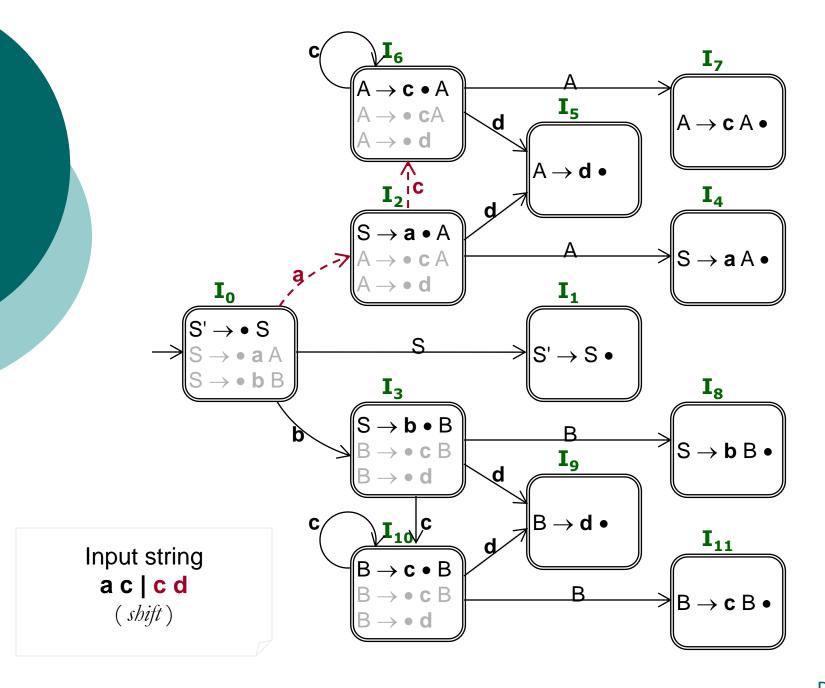
a c c d

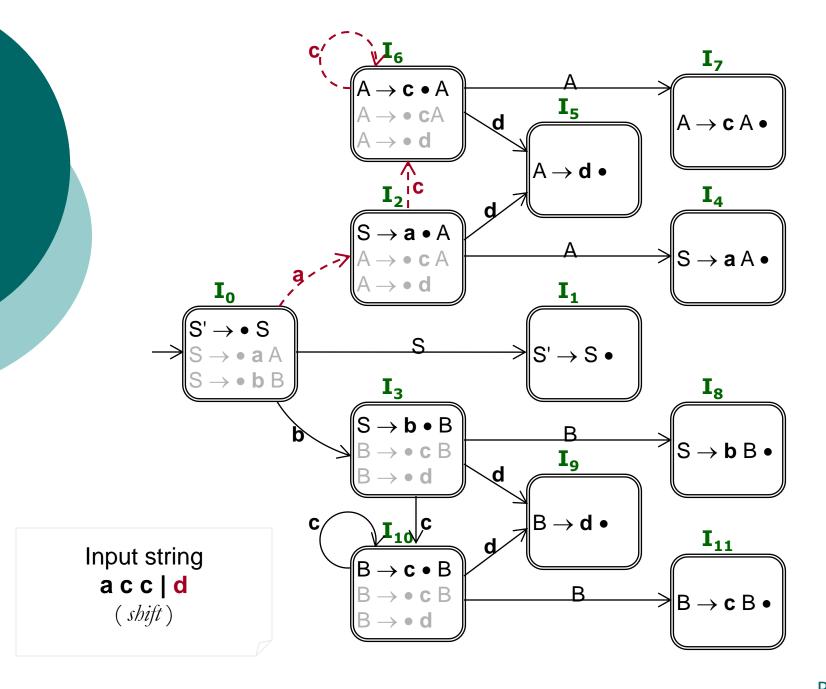
We have the right-most derivation:

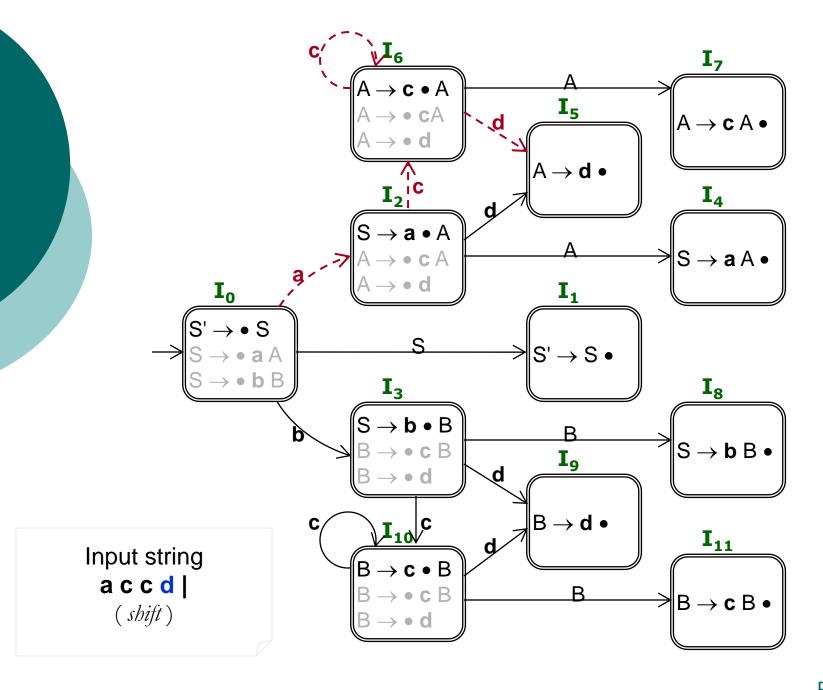
 $S' \Rightarrow S \Rightarrow a A \Rightarrow a c A \Rightarrow a c c A \Rightarrow a c c d$ 

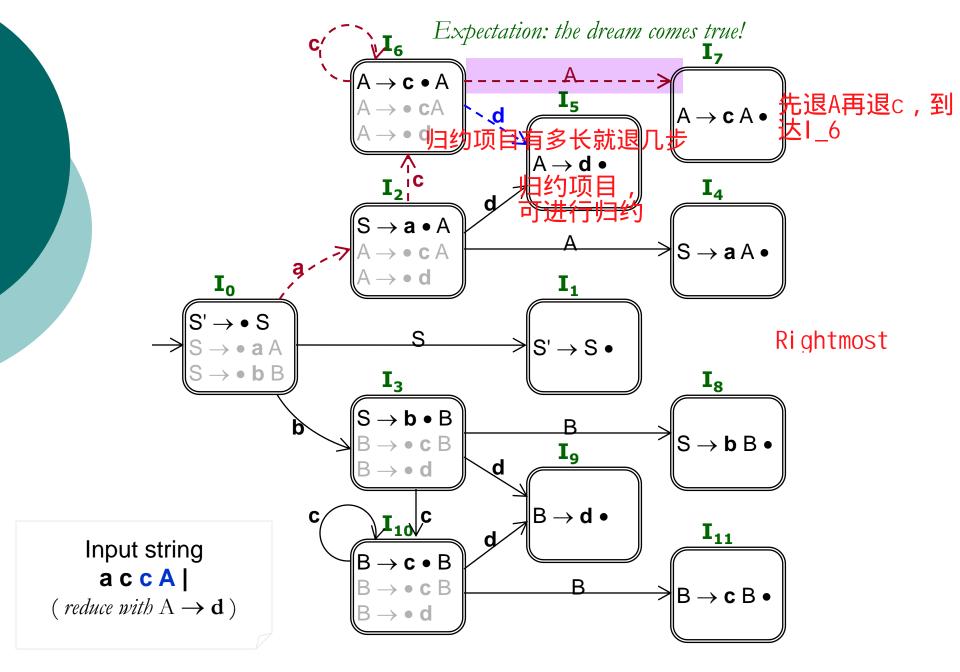


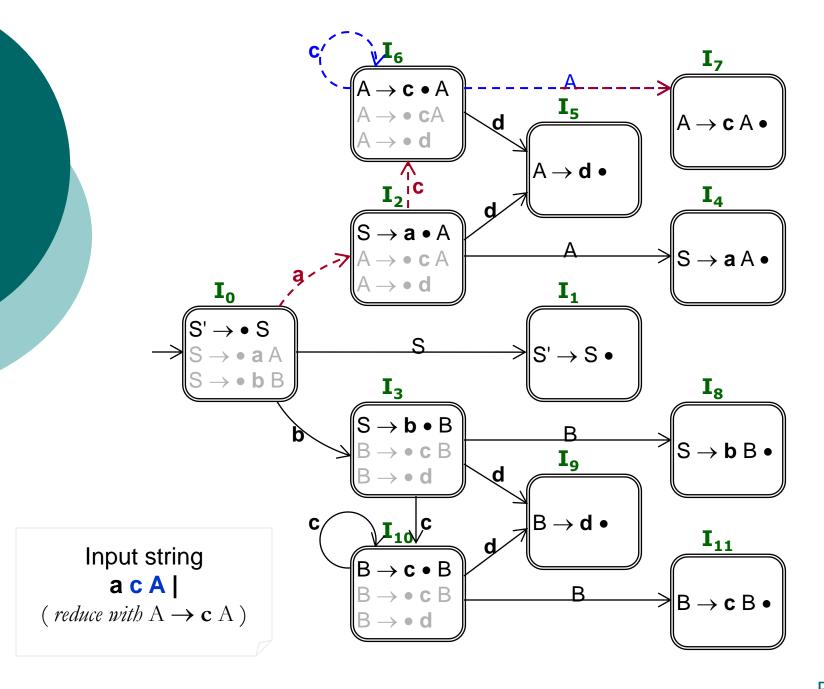


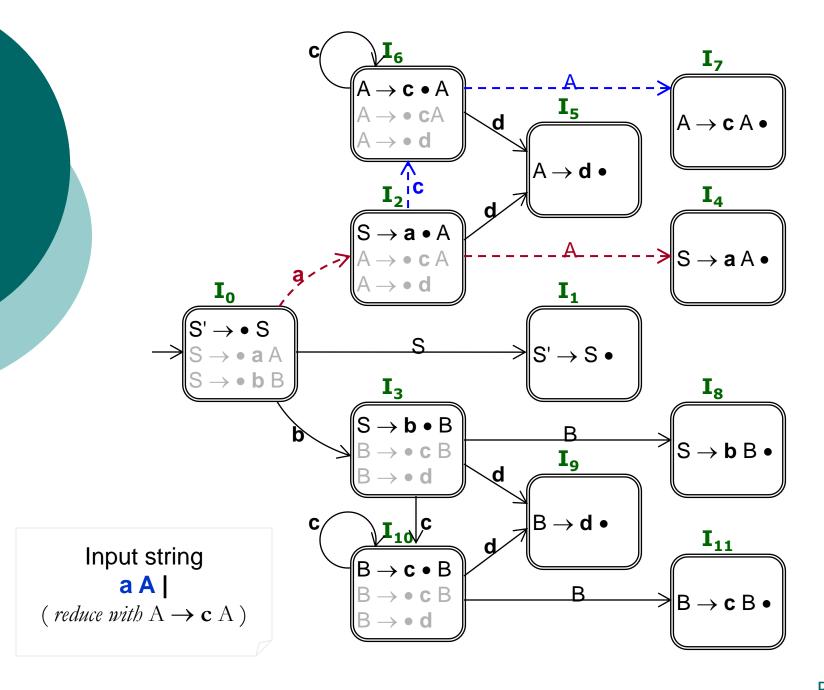


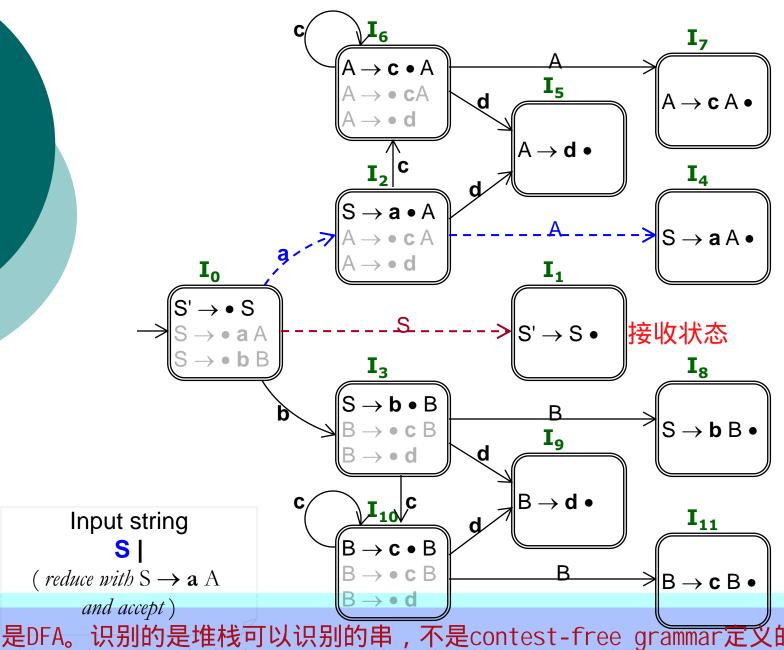












是DFA。识别的是堆栈可以识别的串,不是contest-free grammar定义的语言,之所以能够实现是因为借助了stack。栈是状态栈(里面是状态I\_0...),符号栈只是辅助理解。

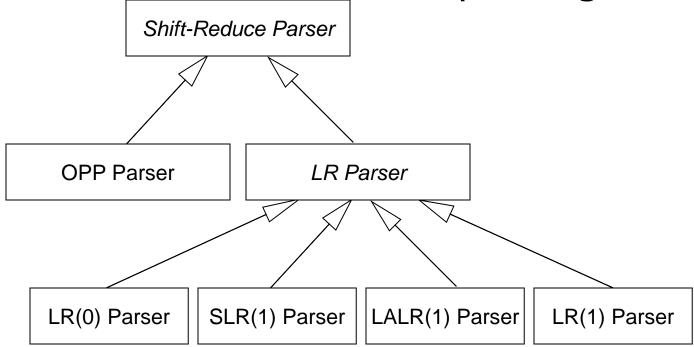
# **Parsing Decisions**

Step	Symbol	State	Input	Reference	Action	Output
1	\$	0	accd\$	S → • <b>a</b> A	shift	
2	\$ a	0 2	c c d \$	A → • <b>c</b> A	shift	
3	\$ac	0 2 6	c d \$	A → • <b>c</b> A	shift	
4	\$acc	0 2 6 6	d \$	A → • <b>d</b>	shift	
5	\$accd	02665	\$	A → <b>d</b> •	reduce	A → <b>d</b>
6	\$accA	02667	\$	A → <b>c</b> A •	reduce	A → <b>c</b> A
7	<b>\$</b> a c A	0 2 6 7	\$	A → <b>c</b> A •	reduce	A → <b>c</b> A
8	<b>\$ a</b> A	0 2 4	\$	S → <b>a</b> A •	reduce	$S \rightarrow \mathbf{a} A$
9	<b>\$</b> S	0 1	\$	$S' \rightarrow S \bullet$	accept	

栈底

### Review

 Implementations of the abstract model for shift-reduce parsing



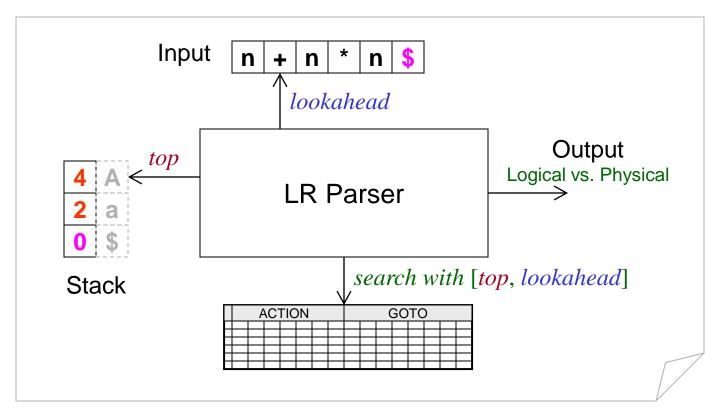
### LR Parsers

- Concrete implementations
  - Parsing table

- o ACTION 状态+Lookahead 状态\*(T+1)
- GOTO 大小: 状态\*(T+N)
- **Explicit stack** 
  - States
  - Grammar symbols (optional)
- Reducable substring
  - Handles

### A Concrete Model for LR Parser

### LR Parser



## What Language the DFA recognizes?

- Viable prefixes of the grammar
  - All strings of grammar symbols that can appear on the stack.
  - A viable prefix is a prefix of a right-sentential form, that does not continue past the right end of the right-most handle of that sentential form. (DBv2, pp.256, seg.4, line.2-4) 意思是:形成句柄就立刻geduce,不再shift

Learn how to build up a formulation!

### Properties of Viable Prefixes

- A viable prefix must be a prefix of a rightsentential form.
  - $S \Rightarrow_{rm}^* \alpha \omega$ , where  $\alpha$  is the content of the stack and  $\omega$  contains no nonterminals.
- Not all prefixes of a right-sentential form are viable prefixes.
  - $E \Rightarrow_{rm}^* F * \mathbf{n} \Rightarrow_{rm} (E) * \mathbf{n}$
  - where (, ( E, ( E ) are viable prefixes,
  - but (E) \* is not, since the parser will perform reduction once the handle appears.

### Definition: Valid Item

- The definition of a valid item
  - Item  $A \rightarrow \beta_1 \bullet \beta_2$  is valid for a viable prefix  $\alpha \beta_1$ , if there exists a derivation

$$S' \Rightarrow_{rm}^* \alpha \land \omega \Rightarrow_{rm} \alpha \beta_1 \beta_2 \omega$$

where  $\omega$  contains terminals only.

- Hints provided by valid items
  - o If  $\beta_2 \neq \epsilon$ , the parser should do shift() since a handle has not appear on top of parsing stack.
  - $\circ$  If  $β_2 = ε$ , the parser should do reduce().

### 合法项目,用于pp闭包项目生成

### Theorem 1 on Valid Items

 Foundation of closure(), which is used to construct the states of DFA.

```
If A \to \beta_1 \bullet B \beta_2 is a valid item for \alpha\beta_1, and B \to \gamma is a production, then B \to \bullet \gamma is also a valid item for \alpha\beta_1.
```

[Proof]

```
\circ S' \Rightarrow^*_{rm} \alpha A \omega \Rightarrow_{rm} \alpha \beta_1 B \beta_2 \omega \quad \text{(definition)}
\circ \Rightarrow^*_{rm} \alpha \beta_1 B \delta \omega \quad \text{(suppose } \beta_2 \omega \Rightarrow^*_{rm} \delta \omega \text{)}
\circ \Rightarrow_{rm} \alpha \beta_1 \gamma \delta \omega \quad \text{(we have } B \rightarrow \gamma \text{)}
\circ B \rightarrow \bullet \gamma \text{ is a valid item for } \alpha \beta_1 \quad \text{(definition)}
```

#### Theorem 2 on Valid Items

- Foundation of goto(), which is used to construct the transitions of DFA.
  - If  $A \to \beta_1 \bullet X \beta_2$  is a valid item for  $\alpha\beta_1$ , then  $A \to \beta_1 X \bullet \beta_2$  is a valid item for  $\alpha\beta_1 X$ .
  - [Proof]

```
\circ S' \Rightarrow^*_{rm} \alpha A \omega \Rightarrow_{rm} \alpha \beta_1 X \beta_2 \omega \quad \text{(definition)}
```

$$\circ S' \Rightarrow^*_{rm} \alpha A \omega \Rightarrow_{rm} \alpha \beta_1 X \beta_2 \omega \quad \text{(definition)}$$

$$\circ A \rightarrow \beta_1 X \bullet \beta_2$$
 is valid for  $\alpha \beta_1 X$  (definition)

#### 3. Simple LR Parsing

- Steps of parsing table construction
  - Augment the grammar. 开始符号不在右部 说明
    - To ensure a unique accepting state.
  - Draw the DFA recognizing all viable prefixes of the grammar.
  - Calculate FIRST() and FOLLOW() sets of all nonterminal symbols.
    - Or on-demand calculating while filling the table.
  - Fill the LR parsing table (ACTION and GOTO).
    - Using lookahead to decide reductions.

#### **Augmented Grammar**

 Given the previous example augmented and numbered:

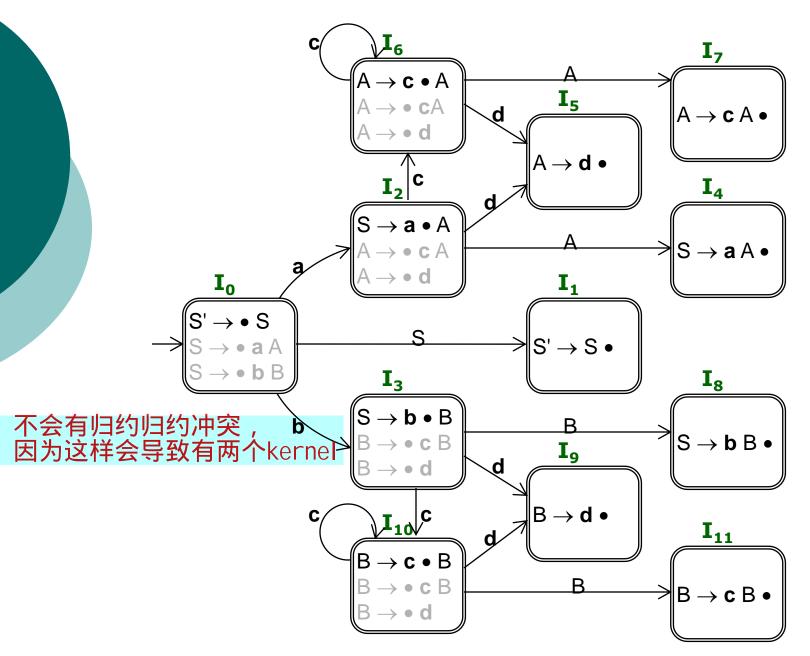
```
(0) S' \rightarrow S 引用序号进行reduce
```

- $(1) S \rightarrow aA$
- (2) S  $\rightarrow$  **b** B
- $(3) A \rightarrow cA$
- (4) A  $\rightarrow$  **d**
- $(5) B \rightarrow c B$
- (6)

#### FIRST() and FOLLOW() Sets

#### We have

- FIRST(S) = { **a**, **b** }
- FIRST(A) = { **c**, **d** }
- FIRST(B) = { **c**, **d** }
- FOLLOW(S) = { \$ }
- FOLLOW(A) = { \$ }
- FOLLOW(B) = { \$ }



Recall: DFA recognizing all viable prefixes

- o ACTION 状态+lookahead 状态\*(T+1)
- o GOTO 大小: 状态\*(T+N)

定义:用LR(0)没有冲突

#### LR(0) Parsing Table

	•	-			_				
					9	「际上是	两张表	画在一起	_
	Ctata			ACTION				GOTO	
	State	а	b	С	d	\$	S	А	В
	0	s2r	s3				1 ←	前往的	状态
	1	shi ft	后去状态	<b>£</b> 2		acc			
	2			s6	s5			4	
ton∓∏	3			s10	s9				8
top和 I ookahead	4	r1	r1	r1	r1	r1			
连在一起就	5	r4	r4	r4	r4	r4			
连在一起就 是右句型	6			s6	s5			7	
	7	r3	r3	r3	r3	r3			
SLR只是利用 I ookahead	8	r2	r2	r2	r2	r2			
TUUKAHEAU	9	r6	r6	r6	r6	r6			
	10			s10	s9				11
	11	r5	r5	r5	r5	r5			

LR(0) uses 0 lookahead to decide reducing

r:reduce r1:用产生式1来归约

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# Overlap of Two Tables

Ctata			ACTION				GOTO	
State	а	b	С	d	\$	S	А	В
0	<b>s</b> 2	<b>s</b> 3				1		
1					acc			
2			s6	s5			4	
3			<b>s</b> 10	s9				
4	r1	r1	r1	r1	r1			
5	r4	r4	r4	r4	r4			
6			s6	s5			7	
7	r3	r3	r3	r3	r3			
8	r2	r2	r2	r2	r2			
9	r6	r6	r6	r6	r6			
10			<b>s</b> 10	<b>s</b> 9				
11	r5	r5	r5	r5	r5			

#### Overlap of Two Tables (cont')

Ctata			ACTION				GOTO	
State	а	b	С	d	\$	S	А	В
0	s2	s3				1		
1					acc			
2			s <b>6</b>	s5			4	
3			s <b>10</b>	s <b>9</b>				8
4	r1	r1	r1	r1	r1			
5	r4	r4	r4	r4	r4			
6			s <b>6</b>	s <b>5</b>			7	
7	r3	r3	r3	r3	r3			
8	r2	r2	r2	r2	r2			
9	r6	r6	r6	r6	r6			
10			s <b>10</b>	s <b>9</b>				11
11	r5	r5	r5	r5	r5			

#### Decisions Based on Parsing Table

Step	Symbol	State	Input	Reference	Action	Output
1	15	0	accd\$	a[0, <b>a</b> ] = s2	shift	
2	<b>\$</b> a	0 2	ccd\$	a[2, <b>c</b> ] = s6	shift	
3	\$ a c	0 2 6	c d \$	a[6, <b>c</b> ] = s6	shift	
4	\$ a c c	0266	d \$	a[6, <b>d</b> ] = s5	shift	
5	\$accd	02665	<b>\$</b>	a[5, <b>\$</b> ] = r4 g[6, A] = 7	reduce	A  o d
6	\$accA	02667	<del>\$</del>	a[7, <b>\$</b> ] = r3 g[6, A] = 7	reduce	A → <b>c</b> A
7	<b>\$</b> a c A	0267	<del>\$</del>	a[7, \$] = r3 g[2, A] = 4	reduce	A → <b>c</b> A
8	<b>\$</b> a A	0243	\$	a[4, \$] = r1 1 g[0, S] = 1	reduce	$S \stackrel{2}{\rightarrow} a A$
9	<b>\$</b> S <b>4</b> \ \	0 1 5	\$	a[1, <b>\$</b> ] = acc	accept	

在parsing时辅助理解,无实际作用。实际上用于存储结果 Page 45/91

区别:一行有reduce就全行是reduce,依据:填的越精准,冲突越小;在 SLR只填follow的

#### Simple LR (SLR) Parsing Table

Ctata			ACTION				GOTO	
State	а	b	С	d	\$	S	А	В
0	s2	s3				1		
1					acc			
2			s6	s5			4	
3			s10	s9				8
4					r1			
5					r4			
6			s6	s5			7	
7					r3			
8					r2			
9					r6			
10			s10	s9				11
11					r5			

SLR(1) simply uses 1 lookahead to decide reducing (Lookaheads must be in the FOLLOW set of the reduced symbol)
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#### Difference between LR(0) and SLR(1)

#### Parsing with the LR(0) parsing table

Step	Symbol	State	Input	Reference	Action	Output
1	\$	0	add\$	a[0, <b>a</b> ] = s2	shift	
2	\$ a	0 2	d d \$	a[2, <b>d</b> ] = s5	shift	
3	\$ a d	0 2 5	d \$	$a[5, \mathbf{d}] = r4, g[2, A] = 4$	reduce	$A \rightarrow d$
4	<b>\$ a</b> A	0 2 4	d \$	a[4, d] = r1, g[0, S] = 1	reduce	$S \rightarrow a A$
5	<b>\$</b> S	0 1	d \$	a[1, <b>d</b> ] = empty	error	

#### Parsing with the SLR(1) parsing table

Step	Symbol	State	Input	Reference	Action	Output
1	\$	0	add\$	a[0, <b>a</b> ] = s2	shift	
2	\$ a	0 2	d d \$	a[2, <b>d</b> ] = s5	shift	
3	\$ a d	0 2 5	d \$	a[5, <b>d</b> ] = empty	error	

差别是报错速度的快慢,但一定会报错;

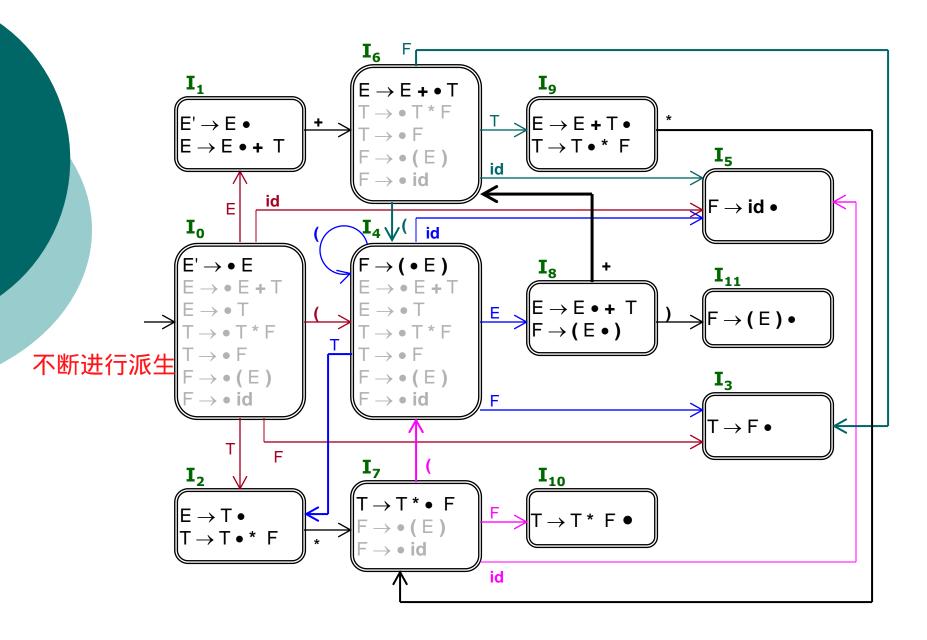
#### A More Complicated Example

 Consider the unambiguous grammar for expressions

$$E \rightarrow E + T \mid T$$
  
 $T \rightarrow T * F \mid F$   
 $F \rightarrow (E) \mid id$ 

Augmented grammar (numbered)

```
(0) \quad E' \quad \rightarrow \quad E
(1) \quad E \quad \rightarrow \quad E + T
(2) \quad E \quad \rightarrow \quad T
(3) \quad T \quad \rightarrow \quad T * F
(4) \quad T \quad \rightarrow \quad F
(5) \quad F \quad \rightarrow \quad (E)
(6) \quad F \quad \rightarrow \quad id
```



DFA recognizing all viable prefixes

#### FIRST() and FOLLOW() Sets

 From the previous lectures, it is easy to calculate the following sets:

```
FIRST(E) = { (, id }
FIRST(T) = { (, id }
FIRST(F) = { (, id }
FOLLOW(E) = { +, }, $ }
FOLLOW(T) = { +, *, }, $ }
FOLLOW(F) = { +, *, }, $ }
```

考试: 增广文法、(求follow)、画出DFA、填写parsing table、问一个语句的工作过程或者只是简单问是不是SLR,还是要重复上述过程SLR(1) Parsing Table

Ctata			ACT	ION				GOTO	
State	id	+	*	(	)	\$	Е	Т	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2 📮	填E的f	ollow	
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1 只	填E的f	ollow	
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

# This Is Not an LR(0) Grammar!

Ctata			ACT	ION				GOTO	
State	id	+	*	(	)	\$	Е	Т	F
0	s5			s4			1	2	3
1		s6				acc			
2	r2	r2	s7/r2	r2	r2	r2 全	行填re	duce	
3	r4	r4	r4	r4	r4	r4			
4	s5			s4			8	2	3
5	r6	r6	r6	r6	r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9	r1	r1	s7/r1	r1	r1	r1			
10	r3	r3	r3	r3	r3	r3			
11	r5	r5	r5	r5	r5	r5			

#### 4. More Powerful LR Parsing

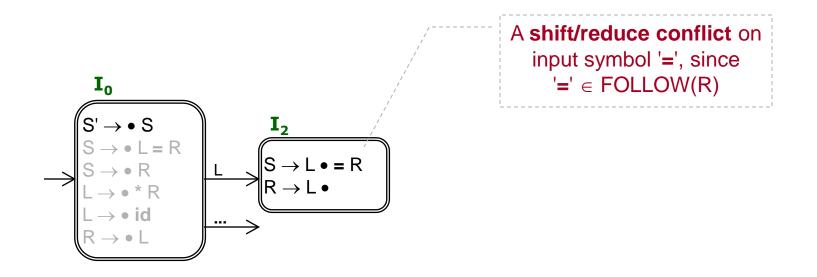
- A Grammar That Is Not SLR(1)
- LR(1) Parsing Table
- LALR(1) Parsing Table
- Conflicts in LALR(1) Parsing

# An Unambiguous But Not SLR(1) Grammar

 Consider the unambiguous grammar, which is not SLR(1):

```
S \rightarrow L = R \mid R
L \rightarrow R \mid id
R \rightarrow L
```

#### Conflicts in Items



Part of the DFA recognizing all viable prefixes

# Motivation of LR(1) Parsing

How to make use of the lookahead?

LR(0): does not use the lookahead.

All columns are filled with the same reduction.

SLR(1): simply make use of the lookahead.

Only columns in the FOLLOW set are filled.

More accurate than LR(0), thus less conflicts.

More powerful LR parsing - LR(1) 最精准,代价大

o Only columns (symbols) that can follow the viable prefixes are filled. follow所有活前缀

More accurate than SLR(1).

Trade-off – LALR(1)

More efficient but less powerful than LR(1).

More powerful than SLR(1).



# Definition: Valid LR(1) Item

- The definition of a valid item
  - Item  $[A \to \beta_1 \bullet \beta_2^{\nu}, a]$  is valid for a viable prefix  $\alpha\beta_1$ , if there exists a derivation  $S' \Rightarrow_{rm}^* \alpha A \otimes_{rm} \alpha \beta_1 \beta_2 \otimes_{rm} \alpha \beta_1 \otimes_{rm} \alpha \beta_1 \otimes_{rm} \alpha \beta_1 \otimes_{rm} \alpha \beta_1 \otimes_{rm} \alpha \beta_2 \otimes_{rm} \alpha \beta_1 \otimes_{rm} \alpha \beta_2 \otimes_{rm}$

区别

#### Theorem 1 on Valid LR(1) Items

- Foundation of closure(), which is used to construct the states of DFA.
  - If  $[A \to \beta_1 \bullet B \beta_2, a]$  is a valid item for  $\alpha\beta_1$ , and  $B \to \gamma$  is a production, then  $[B \to \bullet \gamma, b]$  is also a valid item for  $\alpha\beta_1$ , where  $b \in FIRST(\beta_2 a)$ .

#### 考试易出错的是a

[Proof]

```
o S' \Rightarrow^*_{rm} \alpha A a \omega \Rightarrow_{rm} \alpha \beta_1 B \beta_2 a \omega (definition)

o \Rightarrow^*_{rm} \alpha \beta_1 B b \delta (suppose \beta_2 a \omega \Rightarrow^*_{rm} b \delta)

o \Rightarrow_{rm} \alpha \beta_1 \gamma b \delta (we have B \rightarrow \gamma)

o [B \rightarrow \bullet \gamma, b] is valid for \alpha\beta_1 (definition)
```

#### Theorem 2 on Valid LR(1) Items

- Foundation of goto(), which is used to construct the transitions of DFA.
  - If  $[A \to \beta_1 \bullet X \beta_2, a]$  is a valid item for  $\alpha\beta_1$ , then  $[A \to \beta_1 X \bullet \beta_2, a]$  is a valid item for  $\alpha\beta_1X$ .
  - [Proof]

```
\circ S' \Rightarrow^*_{rm} \alpha \land a \otimes \Rightarrow_{rm} \alpha \beta_1 \lor \beta_2 \lor a \otimes (definition)
```

$$\circ S' \Rightarrow^*_{rm} \alpha A a \omega \Rightarrow_{rm} \alpha \beta_1 X \beta_2 a \omega \quad \text{(definition)}$$

 $\circ [A \to \beta_1 X \bullet \beta_2, a]$  is valid for  $\alpha \beta_1 X$  (definition)

#### An Example

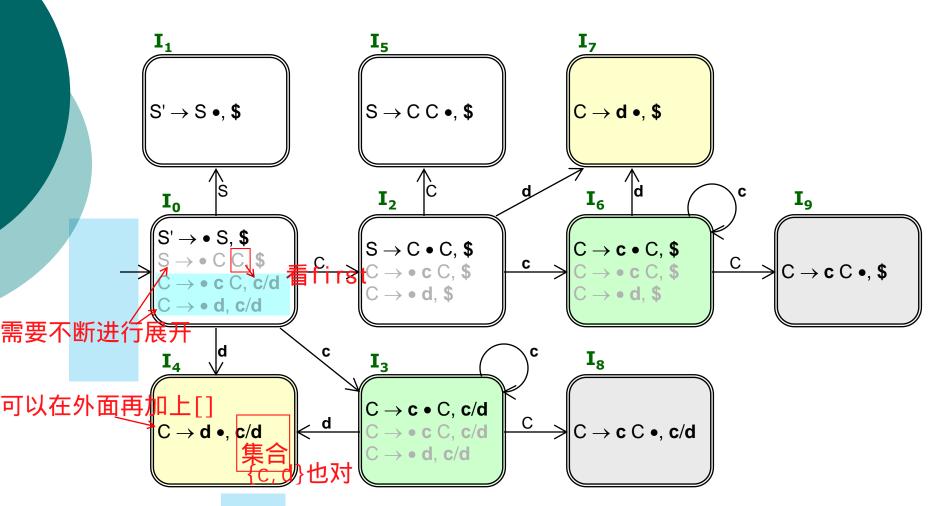
- Consider the following grammar
  - $(0) S' \rightarrow S$
  - $(1) S \rightarrow CC$
  - $(2) C \rightarrow cC$
  - $(3) C \rightarrow \mathbf{d}$

# FIRST() and FOLLOW() Sets

• It is easy to calculate the following sets:

```
    FIRST(S) = FIRST(C) = { c, d }
    FOLLOW(S) = { $ } 这些已经不care
    FOLLOW(C) = { c, d, $ }
    这时看的是first
    SLR看的是FOLLOW
```

 $FIRST(S) = FIRST(C) = \{ c, d \}$ parsing table实际两张,只是overloading



因为augmentation,所以有\$保证S不在其他的右部 D

DFA recognizing all viable prefixes

活前缀

DFA可以识别ifuxilou

#### 结构错误很严重,要注意

# LR(1) Parsing Table

Ctata		ACTION		GO	OTO
State	c -	<b>d</b>	<b>\$</b>	/S	) O
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

#### LALR(1) Parsing Table

- Lookahead-LR parsing in practice
  - Number of states, such as C or Pascal
    - o LR(0) = SLR(1): several hundreds.
    - LR(1): several thousands (10 times).
  - Strategy for LALR(1): merge the states with the same **core**. lookahead LR(1)
    - $\circ$  E.g.  $I_3$  and  $I_6$ ,  $I_4$  and  $I_7$ ,  $I_8$  and  $I_9$
    - Lookaheads of the same item are merged.
    - o GOTO() depends only on the core.
      只是因为Lookahead不同而分开,其他都一样,所以合并在一起

# LALR(1) vs. LR(1)

- The merge will never produce new shiftreduce conflicts
  - Suppose in the merged state
    - $\circ$  [A  $\to \alpha \bullet$ , a] calls for a reduction

- LR1还是可能有冲突 [B  $\rightarrow \beta \bullet$  a  $\gamma$ , b] calls for a shift
  - Since the original states have the same core, there must be some state have
    - $\circ$  [A  $\rightarrow \alpha \bullet$ , a] calls for a reduction
    - $\circ$  [B  $\rightarrow \beta \bullet$  a  $\gamma$ , c] calls for a shift (for some c)
  - Then the original state already has conflicts.

#### LALR(1) vs. LR(1) (cont')

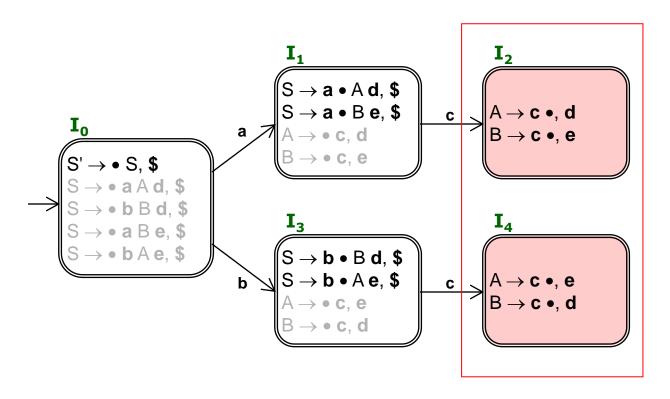
- But the merge will produce new reducereduce conflicts
  - For example

```
S' \rightarrow S
S \rightarrow a A d | b B d | a B e | b A e
A \rightarrow c
B \rightarrow c
```

{[A → c •, d], [B → c •, e]} is valid for viable prefix ac, {[A → c •, e], [B → c •, d]} is valid for viable prefix bc. But the merge has conflicts:

```
\circ \{[A \rightarrow c \bullet, d/e], [B \rightarrow c \bullet, d/e]\}
```

#### Example: New Conflicts in LALR(1)



Part of the DFA recognizing all viable prefixes

# More Efficient Algorithm to Construct LALR(1) Parsing Tables

Just feel free to ignore it.

LR0

LR1

SLR多个产生式

```
But why do you ignore it?

1.栈和输入合并后一直是右句式,规范句型
2.LR(0):全行为reduce - rr冲突、rs冲突-》那么就不是LR(0)
3.SLR:A ->aB·: follow(A)才进行归约(4)4.上面两个表和LALR的大小一样
5.自动产生-----yacc:LALR; lex

DFA:
```

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#### 简洁,但又二义性

# 5. Ambiguity in LR Parsing

- Trade-off and consequence for ambiguity in LR parsing
  - Resolving ambiguities at the grammar level
    - Pros and cons? 简单,但是文法臃肿
  - Resolving ambiguities at the parsing table level
    - o Pros and cons? 额外约束
  - Resolving ambiguities at the source code level
    - Pros and cons? 最灵活,最累

二义性有两种:

先天:语言的二义性

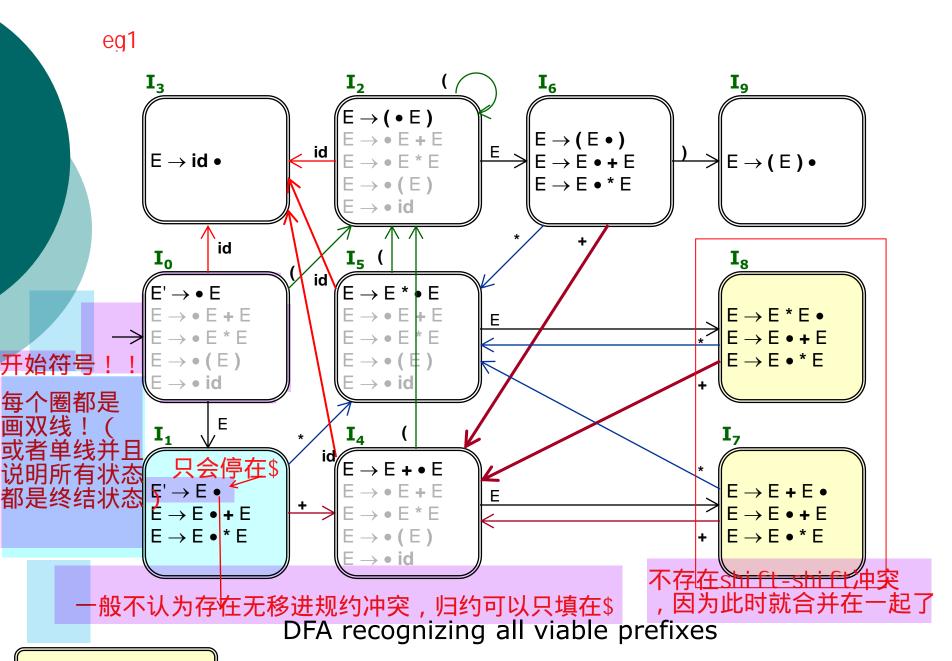
后天:表达式/文法的二义性

yacc:要求LALR,因此写DNF的时候需要改文法使之满足LALR文法。考试则不要求改造

#### **Ambiguous Expression Grammar**

Given the ambiguous grammar

- $(0) E' \rightarrow E$
- $(1) E \rightarrow E + E$
- $(2) E \rightarrow E * E$
- $(3) E \rightarrow (E)$
- $(4) E \rightarrow id$



# SLR(1) Parsing Table

State			ACT	ION			GOTO
State	id	+	*	(	)	\$	Е
0	s3			s2			1
1		s4	s5			acc	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		<b>r1</b> /s4	r1/s5		r1	r1	
8		<b>r2</b> /s4	<b>r2</b> /s5		r2	r2	
9		r3	r3		r3	r3	

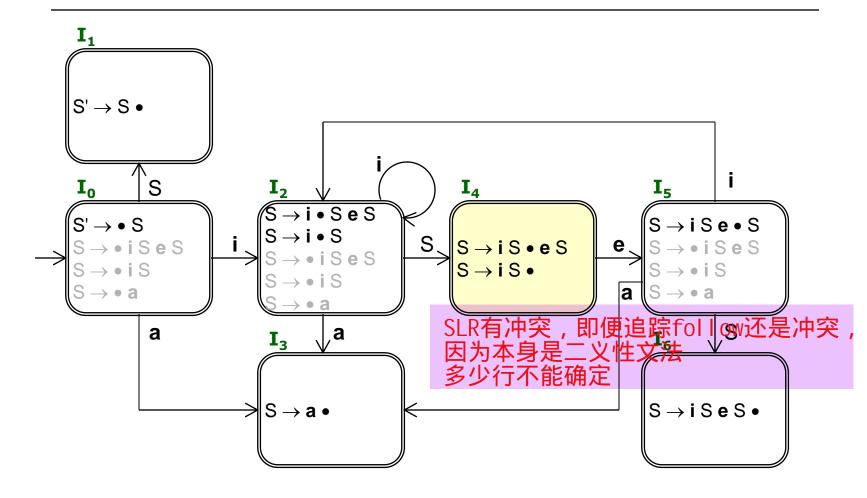
在分析表上消除二义性

Resolve ambiguities at the parsing table level

# Dangling-else Grammar

- Given the ambiguous grammar
  - $(0) S' \rightarrow S$
  - $(1) S \rightarrow i S e S$
  - $(2) S \rightarrow iS$
  - $(3) S \rightarrow a$

## DFA Recognizing All Viable Prefixes



# SLR(1) Parsing Table

State		GOTO			
	i	е	а	\$	S
0	s2		s3		1
1				acc	
2	s2		s3		4
3		r3		r3	
4		r2/s5		r2	
5	s2		s3		6
6		r1		r1	

Resolve ambiguities at the parsing table level

# Parsing a Sentence

Step	Symbol	State	Input	Reference	Action	Output
1	\$	0	iiaea\$	a[0, i] = s2	shift	
2	\$ i	0 2	iaea\$	a[2, <b>i</b> ] = s2	shift	
3	\$ii	0 2 2	aea\$	a[2, a] = s3	shift	
4	\$iia	0 2 2 3	e a \$	a[3, <b>e</b> ] = r3 g[2, S] = 4	reduce	$S \rightarrow a$
5	\$iiS	0224	ea\$	a[4, <b>e</b> ] = s5	shift	
6	\$iiSe	02245	a \$	a[5, a] = s3	shift	
7	\$iiSea	022453	<del>()</del>	a[3, <b>\$</b> ] = r3 g[5, S] = 6	reduce	$S  o \mathbf{a}$
8	<b>\$ii</b> S <b>e</b> S	022456	\$	a[6, <b>\$</b> ] = r1 g[2, S] = 4	reduce	$S \rightarrow i S e S$
9	<b>\$ i</b> S	0 2 4	\$	a[4, \$] = r2 g[0, S] = 1	reduce	$S \rightarrow i S$
10	<b>\$</b> S	0 1	\$	a[1, <b>\$</b> ] = acc	accept	

## 6. Error Recovery in LR Parsing

- For errors in an input sentence
  - All errors will be found by all LR parsers
    - If we can construct a parsing table without conflicts.
  - More reductions before reporting an error
    - $\circ$  LR(0)  $\geq$  SLR(1)  $\geq$  LALR(1)  $\geq$  LR(1)
    - But all of them will never shift an erroneous input symbol onto the stack.

错误都会被找出来, 只是时间不同 是LRO就必定是后三者 是SLR就必定是后两者 是LALR就必定是LR1

## Review: Error Recovery Techniques

- Panic-Mode Error Recovery
  - Skip inputs until synchronizing token found.
- Phrase-Level Error Recovery
  - Assign each empty entry a specific error routine. 内部节点就是phrase
- Error-Productions 精准报错与恢复,需要事先直到出错模式 耗时较大且性价比不高
   Suitable for common errors but not all errors.
- Global-Correction
  - Globally analyze the input to find the error.
  - Expensive and not in practice.

#### 考试不好考

## Panic-Mode Error Recovery

#### 一路退到有接受A出去的状态为止

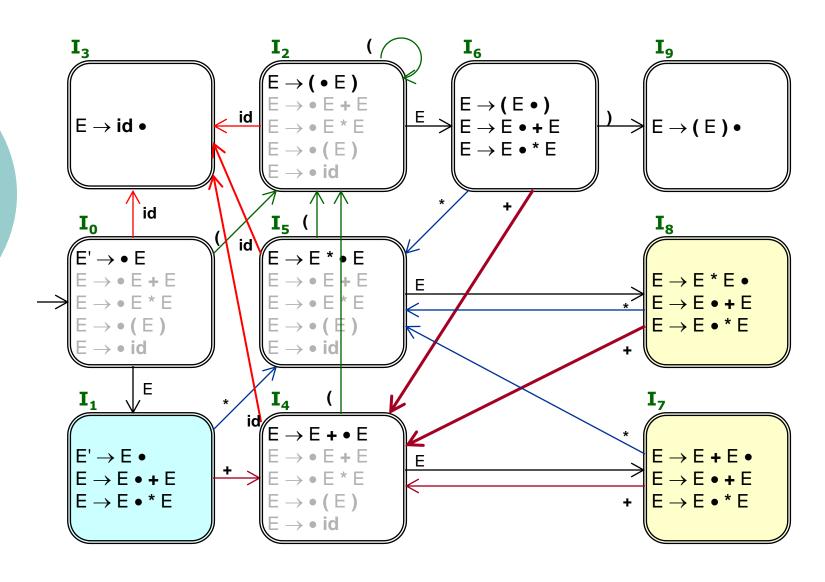
- Pop until a state s with a GOTO() on a particular nonterminal A is found.
  - Usually A represents major constructs, e.g. stmt, expr, or block.
  - It indicates that the construct A has errors.
- Push GOTO(s, A).
- 0 or more lookaheads are then discarded, until a symbol that can follow A.

It is easier to understand if we look from the viewpoint of DFA

## Phrase-Level Error Recovery

- Examine each empty entry, and assign it a pointer to a specific error-handling routine.

   ¬<sub>凡后面的表格</sub>
- Ad hoc: depending on the usage of the language.



The Previous DFA recognizing all viable prefixes

# The Previous Parsing Table

n+m <u>除\$外的共同</u> 构成GOTO表

Ctata	ACTION n+1						→ GOTO
State	id	+	*	(	)	\$	/ E
0	s3	e1	e1	s2	e2	e1	1
1	e3	s4	s5	e3	e2	acc	
2	s3	e1	e1	s2	e2	e1	6
3	r4	r4	r4	r4	r4	r4	
4	s3	e1	e1	s2	e2	e1	7
5	s3	e1	e1	s2	e2	e1	8
6	e3	s4	s5	e3	s9	e4	
7	r1	r1	s5	r1	r1	r1	
8	r2	r2	r2	r2	r2	r2	
9	r3 、	r3	r3	r3	r3	r3	

#### 全部填满去reduce还是会报错

Postpone error detection until one or more reductions are made

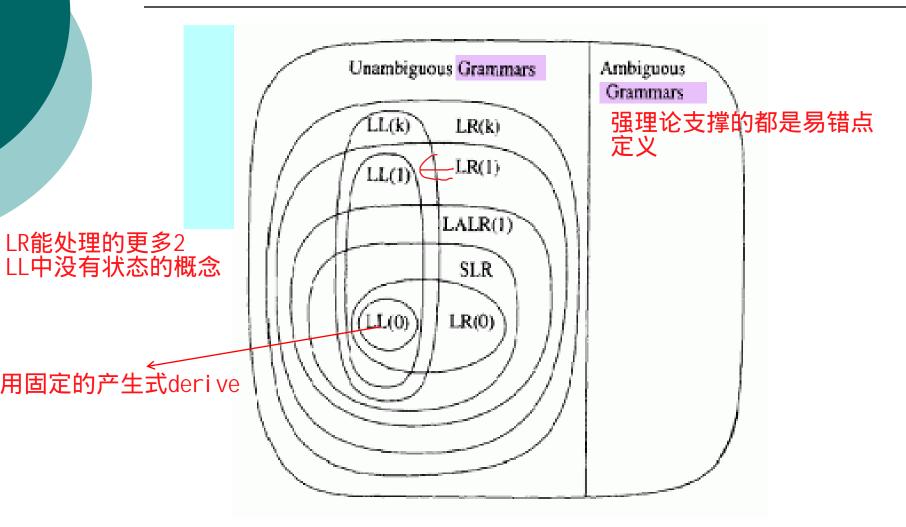
## **Error-Handling Routines**

- e1: an operand ('id' or '(') is expected.
  - push state 3; // add a symbol 'id'
- e2: unbalanced right parenthesis.
  - drop one lookahead; // remove ')'
- e3: an operator is expected.
  - push state 4; // add a symbol '+'
- e4: a right parenthesis is expected.
  - push state 9; // add a symbol ')'

# Parsing an Erroneous Input

Step	Symbol	State	Input	Reference	Action	Output
1	\$	0	id + ) \$	a[0, <b>id</b> ] = s3	shift	
2	\$ id	0 3	+)\$	a[3, +] = r4 g[0, E] = 1	reduce	E  o id
3	<b>\$</b> E	0 1	+)\$	a[1, <b>+</b> ] = s4	shift	
4	\$ E +	0 1 4	) \$	a[4, <b>)</b> ] = e2	drop	Unbalanced ')'
5	\$ E +	0 1 4	<b>\$</b>	a[4, <b>\$</b> ] = e1	push 3	Operand expected
6	\$ E + id	0 1 4 3	<del>\$</del>	a[3, <b>\$</b> ] = r4 g[4, E] = 7	reduce	E  o id
7	\$ E + E	0147	<del>\$</del>	a[7, <b>\$</b> ] = r1 g[0, E] = 1	reduce	$E \rightarrow E + E$
8	<b>\$</b> E	0 1	\$	a[1, <b>\$</b> ] = acc	end	

# Conclusions: Context-Free Grammar Classification



## **Exercise 7.1**

Consider the grammar

```
S \rightarrow (SR \mid \mathbf{a})
R \rightarrow ,SR \mid )
```

 Try to construct an SLR(1) parsing table for the grammar, and see if there are conflicts in the parsing table.

要求画才画

## Exercise 7.2

Consider the grammar

$$S \rightarrow S a b \mid a R$$

$$R \rightarrow S \mid a$$

Is the grammar an SLR(1) grammar? and why?

DFA画出说哪里有就行画局部 ->... 哪里有冲突

### Exercise 7.3

Consider the grammar

```
S \rightarrow A
A \rightarrow BA \mid \epsilon
B \rightarrow aB \mid b
```

- Prove that the grammar is an LR(1) grammar.
- Construct an LR(1) parsing table for the grammar.
- Show the detailed parsing procedure for the sentence abab, following the style in slides of this lecture.

## Exercise 7.4\*

 (DBv2, pp.278, ex.4.7.4) Show that the grammar

$$S \rightarrow Aa \mid bAc \mid dc \mid bda$$

$$A \rightarrow d$$

is LALR(1) but not SLR(1).

不用画表,局部DFA给出结论就好

最核心的内容结束

11-12 test全部内容,题目会难的,出个难的

## **Further Reading**

- Dragon Book, 2<sup>nd</sup> Edition (DBv2)
  - Comprehensive Reading:
    - Section 4.6 on SLR(1) parsing.
    - Section 4.7 on LR(1) and LALR(1) parsing.
    - Section 4.8.1-4.8.2 on ambiguities in LR parsing.
  - Skip Reading:
    - Section 4.8.3 on error recovery in LR parsing.

# Enjoy the Course!

