

# Optical Design of PICO, a Concept for a Space Mission to Probe Inflation and Cosmic Origins

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## ABSTRACT

The Probe of Inflation and Cosmic Origins (PICO) is a probe-class mission concept currently under study by NASA. PICO will probe the physics of the Big Bang and the energy scale of inflation, constrain the sum of neutrino masses, measure the growth of structure in the universe, and constrain its reionization history by making full sky maps of the cosmic microwave background with sensitivity 70 times higher than the Planck space mission. With bands at 21-799 GHz and arcmin resolution at the highest frequencies, PICO will make polarization maps of galactic synchrotron and dust emission to observe the role of Galactic magnetic fields in galactic evolution and star formation. We describe the current state of the PICO instrument design. We discuss the choice of optical system, which is based on an open-Dragone telescope that, to our knowledge, has not been used for mm-wave astrophysical observations. We also present the focal plane design, a white noise model of the instrument, and the expected noise level.

did you review the abstract? does it accurately represent the contents of the paper? Is it highlighting the unique and new things you are reporting? Is it quantitative? In order; yes, yes, I think so, and somewhat.

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**Keywords:** Cosmic microwave background, cosmology, mm-wave optics, polarimetry, instrument design, satellite, mission concept

## 1. INTRODUCTION

Over the last decade NASA’s astrophysics division has funded design and construction of space missions that are either Explorer-class, with cost cap of  $\leq \$250\text{M}$  or Flagship-class that cost above  $\$1\text{B}$ . To study the science opportunities available at intermediate costs, NASA initiated studies of Probe-class missions with cost window between  $\$400\text{M}$  and  $\$1\text{B}$ . We are conducting one these studies for a mission called the Probe of Inflation and Cosmic Origins (PICO). A paper by Sutin et al.<sup>1</sup> in these proceedings gives an overall review of PICO and the scientific motivation. This paper describes the design of the telescope and focal plane and gives our current best estimates for the sensitivity of the instrument. The mission study is not complete; the final report is due in December 2018. Therefore, the quantitative assessments we provide are temporary in nature and subject to revision. Even so, the design is fairly mature and we do not expect significant changes. Values in this paper, such as component temperatures and detector noise levels, are current best estimates. They are not finalized mission requirements.

## 2. MISSION AND SPACECRAFT

PICO will conduct scientific observations for five years from an orbit around the Earth-Sun L2 Lagrange point. The design had 21 bands centered at 21–799 GHz. The spacecraft design impacted the optical design and sensitivity in two primary ways; volume constraints limited the physical size of the telescope and optical component temperatures impacted noise levels.

The maximum diameter of the spacecraft was limited by the SpaceX’s Falcon 9 launch vehicle, which carried payloads up to 4.6 m in diameter. This diameter limited the V-groove shields’ size, which, along with the scan strategy, defined the ‘shadow cone’ in Figure 1. The shadow cone was the volume protected from solar illumination, and all optical components were contained within it. The shadow cone and inner V-grooves defined an available volume for the telescope. We opted not to use deployable shields as they presented added cost and risk which outweighed the benefits. The thermal model indicated the temperatures of the optical elements as given in Figure 1. The primary reflector was passively cooled, while the optics box, secondary reflector, and focal plane were actively cooled; Sutin et al.<sup>1</sup> gives more details of the thermal system.

## 3. OPTICAL SYSTEM

The choice of telescope design was driven by a combination of science requirements and the physical limits discussed in Section 2. The science requirements were: a large diffraction limited field of view (DLFOV)\* sufficient to support  $\mathcal{O}(10^4)$  detectors, arcminute resolution at 800 GHz, low instrumental polarization, and low sidelobe response. Additionally, the transition edge sensor bolometers baselined for PICO require a telecentric focal plane which is sufficiently flat that it can be tiled by 10 cm detector wafers without reduction in optical quality.

To increase aperture efficiency and reduce sidelobes we concentrated on off-axis optical designs. More than 30 years ago Dragone analyzed the performance of several off-axis systems and found solutions with low cross-polarization at the center of the field of view and with astigmatism, or astigmatism and coma, canceled to first order.<sup>2–4</sup> These systems also had no cross-polarization at the center of the field of view. A number of recent CMB instruments used off-axis systems, and several began the design optimization with systems based on designs by Dragone.<sup>5–10</sup> For PICO we began the optimization with a two-reflector Dragone system that, to our knowledge, has not been implemented in CMB instruments before. We call it an ‘open-Dragone’ because of its overall geometry and in contrast to the widely used ‘cross-Dragone’, see Figure 3. We used a 1.4 m entrance aperture as this aperture diameter satisfied the science requirements.

We considered two additional Dragone systems, a Gregorian Dragone and a cross-Dragone, and compared the relative performance of all three systems in terms of DLFOV, compactness, and rejection of sidelobes. Compared

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\* We consider an area in the FOV diffraction limited when the Strehl ratio is larger than 0.8.

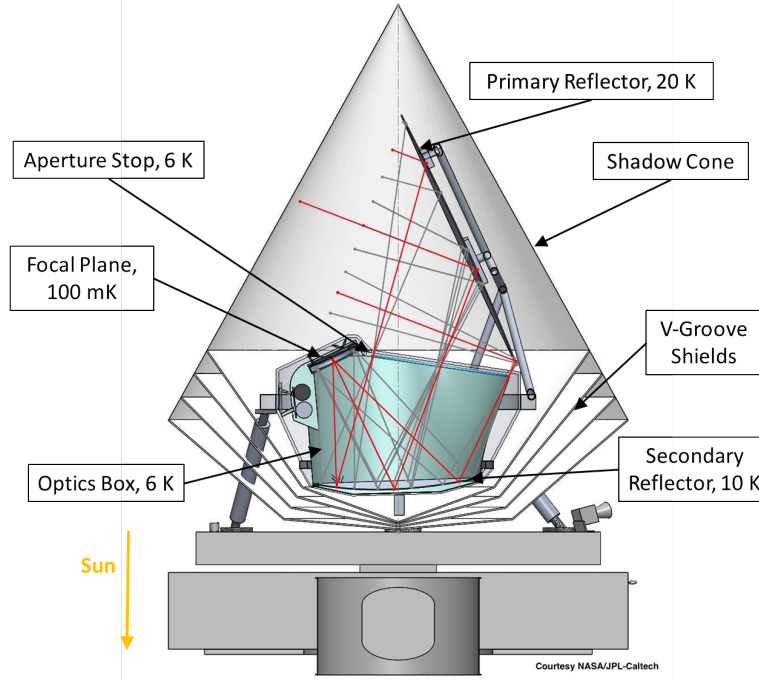


Figure 1. Mechanical design of the PICO satellite. Components relevant to this paper are labeled, for other details see Sutin et al.<sup>1</sup> The symmetry axis of the satellite precesses around the satellite-sun axis (orange arrow) with an angle of 26 deg figure is confusing; show the spin axis; show the sun along the shadow cone; show the boresight explicitly; show the 26 and 69 degrees. This precession defines the shadow cone which is shown in light gray.

to the open-Dragone, the Gregorian had half the DLFOV for the same  $F$ -number and could not support  $\mathcal{O}(10^4)$  detectors. It was therefore rejected. The cross-Dragone had roughly  $4\times$  the DLFOV of the open-Dragone, but was more difficult to pack inside the spacecraft volume while avoiding the known sidelobes shown in Figure 2. We found that the largest cross-Dragone which meets the PICO volume constraints had a 1.2 m aperture and an  $F$ -number of 2.5, while the largest open-Dragone aperture was 1.4 m with an  $F$ -number of 1.42. The larger  $F$ -number of the cross-Dragone system implied a larger physical focal plane, and therefore higher mass and cost, for the same number of pixels. For the PICO case, we concluded that the advantages of a low  $F$ -number and easily baffled sidelobes made the open-Dragone a good starting point for further optimization.

We designed the initial open Dragone following Granet’s method.<sup>11</sup> We began with a solution with  $F = 1.42$ , a 1.4 m aperture (that was verified to satisfy the volume constraints), and a large DLFOV. We forced a circular aperture stop between the primary and secondary reflectors and numerically optimized its angle and position to obtain the the largest DLFOV. The stop diameter was chosen such that, for the center feed, it projected a 1.4 m effective aperture onto the primary. Adding a stop in this way increased the size of the primary reflector, because different field angles illuminated different areas on the reflector. Actively cooling the aperture stop, however, reduced detector noise, and the stop shielded the focal plane from stray radiation. At this stage the system still met the Dragone condition and is defined by the ‘Initial Open-Dragone’ parameters in Table 1.

In his publications Dragone provides a prescription to eliminate coma in addition to the cancellation of astigmatism provided by the baseline designs.<sup>3</sup> The corrections involve adding distortions to the primary and secondary reflectors which are proportional to  $r^4$  where  $r = 0$  is at the chief ray impact point on each reflector. We thus attempted to increase the DLFOV using two methods.

In ‘Method1’, one of the coauthors (RH) used Zemax to add Zernike polynomials to the base conics which described the reflectors. These Zernike polynomials were offset from the symmetry axis of the conic by 624.2 cm for the primary and 76.1 cm for the secondary. This placed the origin of polynomials at the chief ray impact point for each reflector. Inspired by the Dragone corrections, all Zernike terms up to fourth order and the first

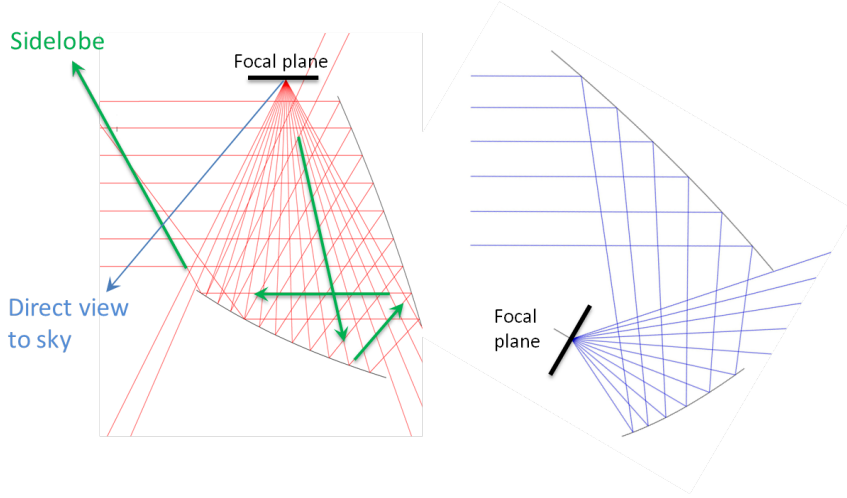


Figure 2. Comparison of sidelobes for a cross-Dragone (left) and an open-Dragone (right) please add labels to Figure as well. Rays are traced from the center of the focal plane toward the sky same angular opening of rays?. For both systems spillover around the secondary is straightforward to mitigate with absorptive baffles show sketch of such baffles?. However, the rays labeled ‘sidelobe’ and ‘direct view to sky’ in the cross-Dragone system present added challenges. The challenges can be mitigated—with a long forebaffle or larger  $F$ -number (see for example Matsumrua et al.<sup>9</sup>—but doing so increases the overall physical size of the system, which is problematic in the PICO case.

fifth order term were allowed to vary. The optimization metric was minimization of the rms spot diameter at the following locations: the center of the FOV,  $\pm 2$  deg in  $Y$ , and  $\pm 4$  deg in  $X$ . The center of the FOV was given a weight of 100 while each outer point was given a weight of 1. To constrain the optimization, the  $X$  and  $Y$  effective focal lengths were held fixed as was the impact point of the chief ray on the focal plane. This optimization step increased the DLFOV by factors of 1.15, 2.4 and 10.5 at 21, 155 and 799 GHz, respectively. We further increased the DLFOV by approximately 50% at all frequencies by including a curved focal surface and rerunning the optimization. A small ( $\sim 4\%$ ) additional gain in DLFOV was achieved by adding Zernike terms up to sixth order, allowing the secondary to focal surface distance to vary, adding a weighted constraint on the effective focal length, and adding fields with weight of 0.01 to the rms spot diameter metric at  $\pm 7.5$  deg in  $Y$  and  $+15$  deg in  $X$ . These additional fields were necessary to constrain the corrections at the reflector edges.

In ‘Method2’ another coauthor (JM) used CodeV and allowed additional geometric parameters of the system to vary. To adjust the reflector shapes, we added Zernike polynomial corrections to the conic surfaces which defined the two reflectors. The Zernike polynomials were defined in the same coordinate systems as the base conics. We varied the 4th and 9th-13th Zernike coefficients. We allowed the focal surface curvature and focal surface to secondary distance  $L_s$  to vary. The primary-secondary distance  $L_m$ , primary offset  $h$ , and the primary and secondary rotation angles,  $\alpha$  and  $\beta$ , were varied as well. The optimization metric was the rms spot diameter across the field of view, with weighted constraints requiring telecentricity and maintaining the  $X$ - and  $Y$ -focal lengths. We added Lagrange constraints to enforce beam clearances and place an upper limit on overall system size. Once the optimization converged to an acceptable optical system, we added higher order Zernike terms, 19th-25th, and refined the reflector shapes using the same metric and constraints. The current PICO optical design is from the Method2 optimization procedure.

Figure 4 shows that Method2 greatly increased the DLFOV relative to the initial open-Dragone design. The DLFOV increased by factors of 1.9, 3.8, 4.3, and 4.6 at 21, 129, 155, and 799 GHz, respectively. The most important gain was at frequencies of 129 and 155 GHz. We used this extra area to add more C and D pixels, see Figure 5 and Section 4. The C and D pixels contained the bands most sensitive to the CMB, and adding hundreds of these pixels into the focal plane gave PICO unprecedented levels of CMB sensitivity. Method2 gave somewhat better performance at lower frequencies with a DLFOV 1.11 and 1.15 times larger than Method1 at 21 and 155 GHz, respectively. At 799 GHz Method2 gave DLFOV only 0.3 times that of Method1’s area, but the

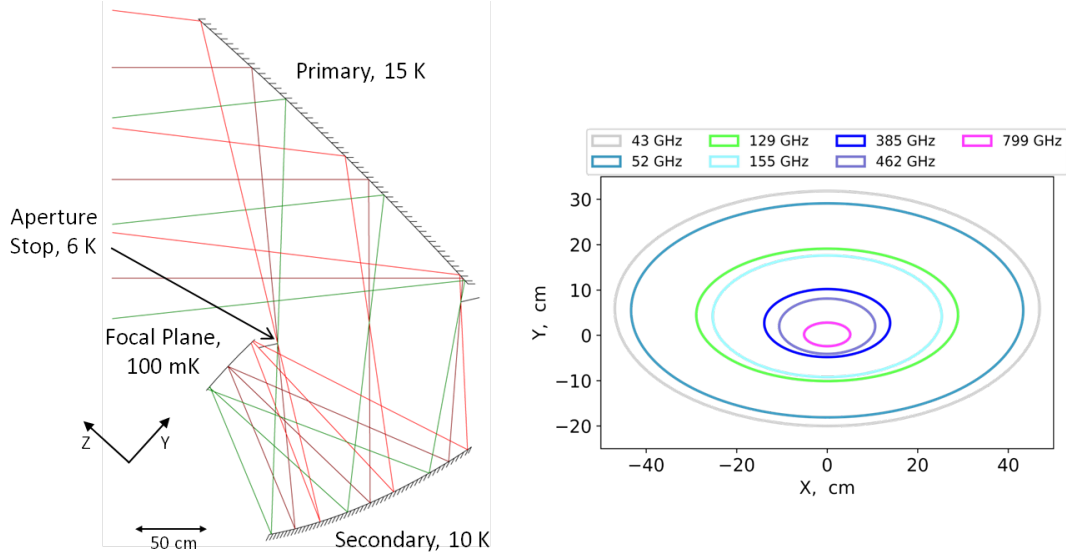


Figure 3. Raytrace (left) and Strehl = 0.8 contours (right) for the PICO optical design.

Table 1. Telescope geometric parameters **ADD F# to Table**

PICO optical system				Initial Open-Dragone <sup>b</sup>	
	Primary	Secondary	Telescope parameters <sup>b</sup>		Fundamental design parameters
Reflector size <sup>a</sup> (cm)	270 × 205	160 × 158	Aperture (cm)	140	Aperture (cm) 140
Radius of curvature (cm)	∞	136.6	<i>F</i> -number	1.42	$\theta_0$ (deg) 90
Conic constant, <i>k</i>	0	-0.926	<i>h</i> (cm)	624.2	$\theta_e$ (deg) 20
Normalization radius (cm)	524.8	194.1	$\alpha$ (deg)	74.2	$\theta_p$ (deg) 140
4th Zernike Coefficient (cm)	2018.4	-61.1	$\beta$ (deg)	62.3	$L_m$ (cm) 240
9th Zernike Coefficient (cm)	-37.0	16.7	$L_m$ (cm)	229.3	
10th Zernike Coefficient (cm)	-2919.8	-15.1	$L_s$ (cm)	140.5	
11th Zernike Coefficient (cm)	-1292.7	22.3			Derived parameters
12th Zernike Coefficient (cm)	120.6	-3.8	Focal Surface		<i>F</i> -number 1.42
13th Zernike Coefficient (cm)	-74.5	4.9	Ellipse major axes (cm)	69 × 45	<i>h</i> (cm) 624.2
19th Zernike Coefficient (cm)	-75.8	3.4	Ellipse major axes (deg)	19 × 13	$\alpha$ (deg) 38.6
20th Zernike Coefficient (cm)	-398.9	6.3	Radius of curvature (cm)	455	$\beta$ (deg) 101.4
21st Zernike Coefficient (cm)	-319.5	23.3			$L_s$ (cm) 122.2
22nd Zernike Coefficient (cm)	-276.6	-8.5			Primary, <i>f</i> (cm) 312.1
23rd Zernike Coefficient (cm)	-201.6	-3.2			Secondary, <i>a</i> (cm) 131
24th Zernike Coefficient (cm)	-127.4	-1.9			Secondary, <i>e</i> 1.802
25th Zernike Coefficient (cm)	-55.0	0.1			

<sup>a</sup> The maximum physical size of the reflectors.

<sup>b</sup> Telescope parameters follow the definitions in Granet 2001.<sup>11</sup>

DLFOV still satisfied our science requirements. Figure 4 also shows that Method2 reduced the overall telescope volume and gave more physical margin relative to the shadow cone.

The geometric parameters of the PICO optical system are given in Table 1. The system was diffraction limited for 799 GHz at the center of the field of view. At 155 GHz the DLFOV was 82.4 deg<sup>2</sup> and the total throughput at 20 GHz was 910 cm<sup>2</sup>sr. Figure 3 shows Strehl of 0.8 contours for all pixel types. The slightly concave focal surface, which had a radius of curvature of 4.55 m, was telecentric to within 0.12 deg across the entire FOV.

An additional benefit of the optimization was the concave focal surface. The open-Dragone's focal surface is naturally curved. Matching this curvature reduced defocus, increased the DLFOV, and increased telecentricity. The unoptimized system was telecentric to within 2.5 deg while the optimized version was telecentric to within

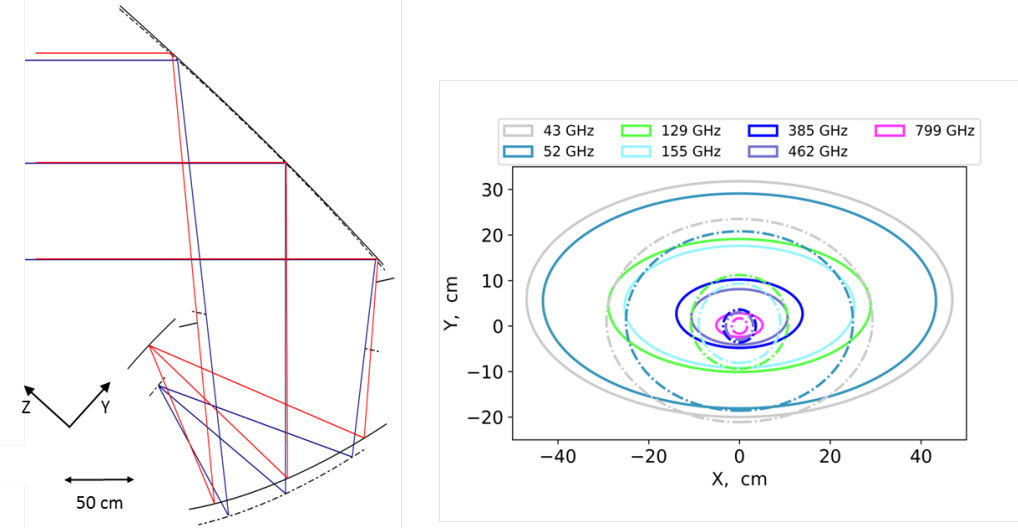


Figure 4. Comparison between the open-Dragone optimized using method two and the initial open-Dragone. The ray traces (left) are aligned at the chief ray impact point on the primary. The **final optical system, optimized with Method2 (red rays, solid reflectors)**, is smaller in the vertical direction than the unoptimized version **original dragone or Method1?** (blue rays, dash-dot reflectors). The overlaid Strehl = 0.8 contours (right) show the improvement at all frequencies in the optimized (solid lines) system over the unoptimized (dash-dot lines) system. **same question? Perhaps show all three options?**

0.12 deg. If the focal surface was too strongly curved tiling it with flat detector wafers would result in large defocus at the edges of these wafers. This was not the case for PICO. The focal surface radius of curvature, 4.55 m, resulted in a defocus of 0.1 mm at the edge of a 10 cm wafer.

#### 4. FOCAL PLANE

Modern mm/sub-mm bolometers are photon noise limited. An effective way to increase sensitivity is to increase the number of detectors in the focal surface. The PICO focal surface had 12,996 detectors, 175 times the number flown on *Planck*. PICO achieved this by having a large DLFOV and using multichroic pixels (MCPs).<sup>12,13</sup> The MCP architecture assumed for PICO had three bands per pixel with two single polarization transition edge sensor (TES) bolometers per band and therefore six bolometers per pixel. We assumed the MCPs were coupled to free space using lenslets and sinuous antennae,<sup>12</sup> but the pixel sizes, numbers, and spacing will not change significantly if horn or phased array coupling is used instead.

PICO had 21 overlapping bands with centers spanning the range 21–799 GHz. The bands were divided amongst nine pixel types labeled A to I; see Figure 5. The 25% fractional bandwidth was broader than the interband spacing causing neighboring bands to overlap and requiring them to be in separate pixels. The exceptions to the MCP architecture were the highest three bands, because they were above the superconducting band gap of the niobium used for transmission lines, antennae, and filters in MCPs. For bands G, H, and I, we assumed feedhorn-coupled polarization sensitive bolometers. The technology has high TRL as it has been used successfully with *Planck*<sup>14</sup> and Herschel SPIRE.<sup>15</sup>

Figure 6 shows the PICO focal plane. We optimized the diameter of each MCP by calculating the array sensitivity for that pixel type. The calculation included the increasing illumination of the aperture stop as the pixel diameter decreased, as described in Section 5.1. We chose a pixel diameter of  $2.1F\lambda_{\text{mid}}$ , where  $\lambda_{\text{mid}}$  referred to the center band of each pixel. This gave an edge taper,  $T_e$ , on the stop of 10 dB for the center band of each pixel.

Differencing detectors sensitive to orthogonal polarization states will enable each pixel to make a measurement of a particular Stokes parameter. Pixels sensitive to the  $U$  Stokes parameter were rotated by 45 deg relative to



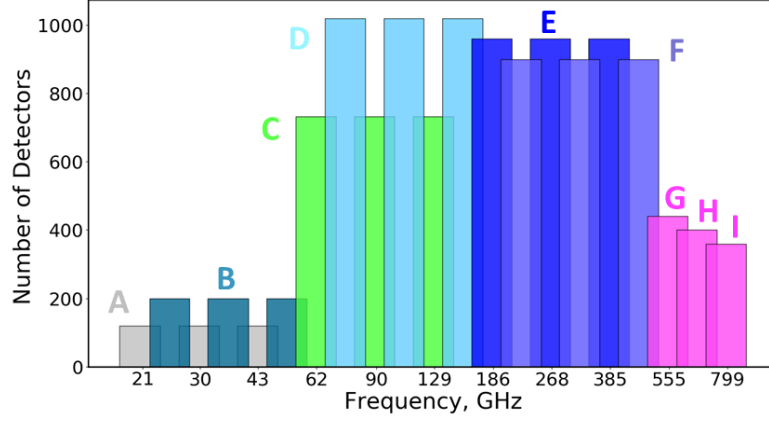


Figure 5. Frequency coverage of the PICO bands. Each color (excluding magenta) denotes a different MCP, labeled A-F. The bar height indicates the number of detectors per band. Bar width gives the bandwidth. All bands are top-hats with 25% fractional bandwidth; the  $x$ -axis is logarithmic. The three highest frequencies (magenta) are the single color pixels G, H, and I.

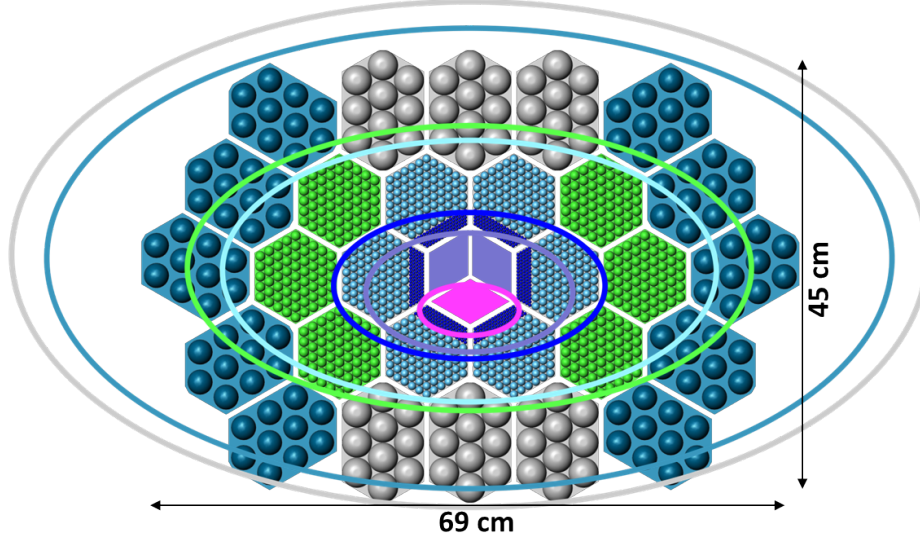


Figure 6. PICO focal plane layout with Strehl = 0.8 contours for each pixel type. The pixel and Strehl contour colors match the band colors, A-I, in Figure 5

those that were sensitive to  $Q$ . This Q/U measurement was in the instrument reference frame with the  $x$ -axis parallel to the scan direction; see Figure 7. **combine Figures 6 and 7 together?**

The PICO focal plane readout was designed around  $\times 128$  time domain multiplexing (TDM), but this choice was not a significant driver for the focal plane layout or overall noise budget.

## 5. INSTRUMENT NOISE

We developed an end to end noise model of the PICO instrument to predict full mission sensitivity and provide a metric by which to evaluate mission design trade-offs. This model assumed white noise at all frequencies. The overall sensitivity did not include calibration uncertainties or estimates of other possible systematic effects. To construct the model we estimated the optical load, calculated noise equivalent power (NEP) by source, combined

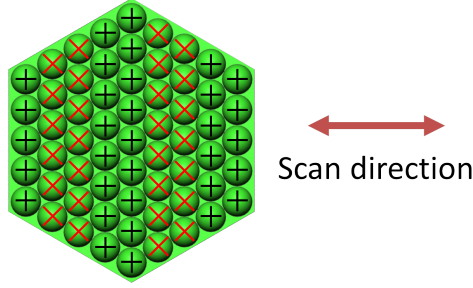


Figure 7. Layout of pixels sensitive to Stokes Q (black crosses) and Stokes U (red exes) for an example wafer.

all NEP terms to get detector noise, combined all detectors to get noise per frequency band, and then included total mission time to find overall mission sensitivity.<sup>16,17</sup> Each of these steps included various assumptions and design decisions, which are discussed in this section. The assumptions are summarized in Table 2. The values presented in this section are current best case estimates. Instrument noise *requirements*, which would have larger noise levels, were still being determined.

To validate our model we compared two independent calculations using codes that were used for several earlier CMB instruments. The calculations agreed within 1% for individual noise terms and for overall mission noise. We also used our model to calculate CORE and LiteBIRD noise from their published system parameters. The results were consistent with published values when similar assumptions were used. **move these to later; let's talk on the phone** From these test we concluded that our model was correct and our assumptions were reasonable.

Table 2. Noise model parameters, see text for details.

Throughput	single moded, $\lambda^2$
Fractional Bandwidth	25%
Reflector emissivity	$\epsilon = \epsilon_0 \sqrt{\nu/150 \text{ GHz}}$ , $\epsilon_0 = 0.07\%$
Aperture stop emissivity	1
Low pass filter reflection loss	8%
Low pass filter absorption loss <sup>a</sup>	frequency dependent, 0.2%–2.8%
Bolometer absorption efficiency	70%
$T_e$ of low, middle, and high bands (dB)	4.8, 10.0, 20.7
$\eta_{\text{stop}}$ of low, middle, and high bands	0.68, 0.90, 0.99
Bose noise fraction, $\xi$	1
Bolometer yield	90%
Bath temperature, $T_o$ (mK)	100
TES critical temperature, $T_c$ (mK)	187
Safety factor, $P_{\text{sat}}/P_{\text{abs}}$	2
Thermal power law index, $n$	2
Intrinsic SQUID noise (aW/ $\sqrt{\text{Hz}}$ )	3
TES operating resistance, $\Omega$	0.03
TES transition slope, $\alpha$	100
TES loop gain	14
Mission length (years)	5
Observing efficiency	95%

<sup>a</sup>Assumes different thickness per pixel type.

## 5.1 Single bolometer noise

### 5.1.1 Model

The sources of optical load were the CMB, the primary and secondary reflectors, the aperture stop, and low pass filters. These elements are shown schematically in Figure 8. The total load absorbed at the bolometer was the



sum of the power emitted by each element reduced by the transmission efficiency of the elements between the emitting surface and the bolometer. The absorbed power was

$$P_{\text{abs}} = (((P_{\text{CMB}}\eta_{\text{PRI}} + P_{\text{PRI}})\eta_{\text{stop}} + P_{\text{stop}}(1 - \eta_{\text{stop}}))\eta_{\text{SEC}} + P_{\text{SEC}})\eta_{\text{filter}} + P_{\text{filter}})\eta_{\text{bolo}}, \quad (1)$$

where  $P_{\text{elem}}$  is the in band power emitted by a given element for a single polarization and  $\eta_{\text{elem}}$  is the transmission efficiency of the element. Power emitted by the stop was a special case. We multiplied  $P_{\text{stop}}$  by  $(1 - \eta_{\text{stop}})$  because  $\eta_{\text{stop}}$  is the spillover efficiency, the fraction of the throughput passing through the stop. Therefore  $(1 - \eta_{\text{stop}})$  is the fraction of the throughput which views the stop. We determined  $\eta_{\text{stop}}$  in the following way. The MCP angular beam width depends on the wavelength and pixel diameter as<sup>16</sup>

$$\theta_{1/e^2} = \frac{2.95\lambda}{\pi D_{\text{px}}}. \quad (2)$$

We fixed  $D_{\text{px}}$  such that the edge taper,  $T_e$ , of the middle frequency band in each pixel was 10 dB and calculated  $T_e$  for the upper and lower bands using Equation 2. This changing illumination of the stop is shown schematically by the dashed rays in Figure 8. For each MCP in pixels A-H,  $T_e$  was 4.8, 10, and 20.7 dB for the lower, middle, and upper bands, respectively. These edge tapers corresponded to  $\eta_{\text{stop}}$  of 0.68, 0.90, and 0.99. The changing  $\eta_{\text{stop}}$  had two main effects; changing optical efficiency between bands, which affected optical load and the NEP to noise equivalent temperature (NET) conversion, and telescope beam size not scaling smoothly with  $\lambda$ . The left panel of Figure 9 gives the optical load as a function of frequency. The jumps in load between neighboring bands near 70 and 200 GHz, were due to  $\eta_{\text{stop}}$  changing with frequency, which was a consequence of using MCPs.

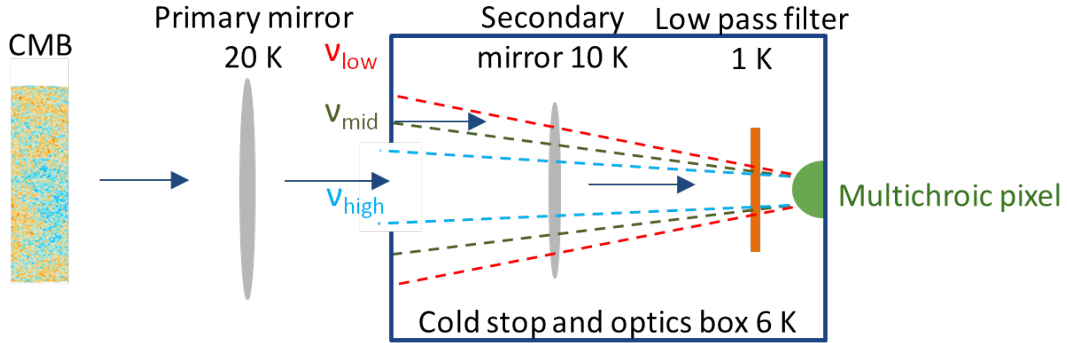


Figure 8. Schematic representation of the prediction of optical load. Power emitted by each element was modified by the efficiency of the following elements and added to the total expected load. The multichroic pixel illuminated the stop differently for each of the three bands.

We considered four noise sources per bolometer; photon, phonon, TES Johnson, and readout. Photon noise depends on the absorbed power,<sup>18</sup>

$$NEP_{\gamma}^2 = \int_{\text{band}} 2h\nu p_{\nu} d\nu + 2\xi \int_{\text{band}} p_{\nu}^2 d\nu, \quad (3)$$

where  $p_{\nu}$  is the power spectral density for a single polarization absorbed at the bolometer and  $\xi = 1$  is the fraction of correlated Bose photon noise. We included a factor of 2 in the Bose noise term because the bolometers received power from a single polarization. From  $P_{\text{abs}}$  we calculated the TES bolometer properties and phonon noise.<sup>19</sup> We calculated TES Johnson noise, which depended on bolometer bias parameters, for each frequency band. All noise sources in the cold and warm readout electronics were lumped under the readout term. The combined NEP and the NEP per noise source are shown in Figure 9 as a function of frequency; the combined values are given in Table 3.

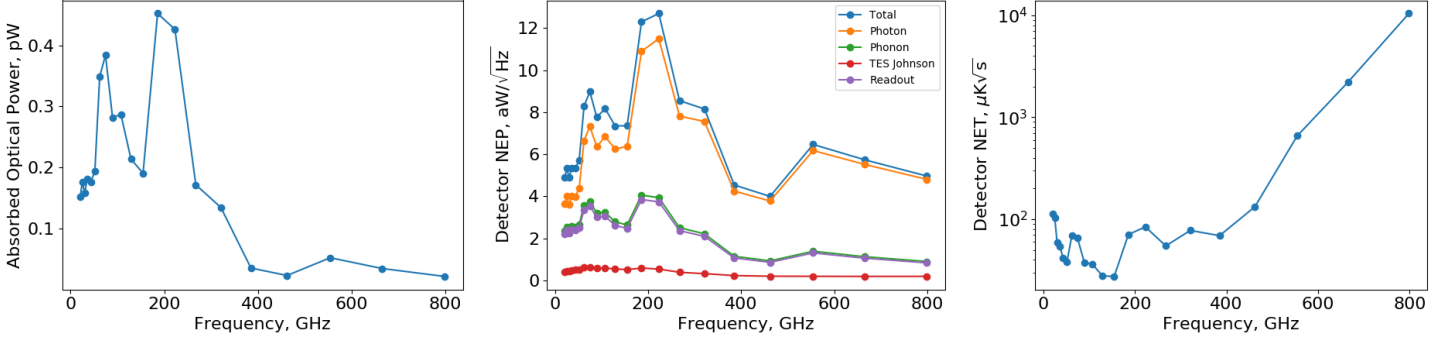


Figure 9. Left: Expected optical load as a function of frequency for single polarization PICO bolometers. Center: Breakdown of NEP sources across the PICO frequency range. Photon noise dominates even at the lowest frequencies. Right: Single detector NET for the PICO bands.

### 5.1.2 Results

The primary contributor to noise was the optical load. The CMB and stop accounted for the majority of the optical load at all frequencies. Even at 800 GHz the CMB and stop accounted for 12% more power than the reflectors; **show components in the Figure? This is not really feasible in the available time. We can just quote the numbers and remove ‘see the left . . .’ see the left panel of Figure 9. is the following consistent with the previous sentence? Yes. (fraction from CMB + stop) / (fraction from reflector) = 53/47 = 1.12** The load from the reflectors was greatest at 799 GHz where it was 47% of the total optical load. The CMB provided more than half the load in the middle and upper bands of the multichroic pixels, but the stop dominated the load in the lowest band of each pixel. Load from the stop in the lowest band of each pixel ranged from 1.2 times the CMB load at 21 GHz to a maximum of 4.7 times the CMB load at 223 GHz. **did we consider two bands per pixel? Did we consider dual-chroic pixels in the design phase? No, or at least not in any quantitative detail.**

Bose noise was most significant at lower frequencies with  $\text{NEP}_{\text{Bose}}/\text{NEP}_{\text{Poisson}} = 1.5$  in the lowest band. (All NEP ratios were calculated using units of  $\text{W}/\sqrt{\text{Hz}}$  for the dividend and divisor.) However, Poisson noise increased as  $\sqrt{P_{\text{abs}}\nu}$  while Bose was proportional to  $P_{\text{abs}}$ . Poisson noise equaled Bose noise at 30 GHz and dominated at higher bands;  $\text{NEP}_{\text{Bose}}/\text{NEP}_{\text{Poisson}} < 10\%$  at 321 GHz. Phonon noise was the second most significant source,  $\text{NEP}_{\text{phonon}}/\text{NEP}_{\text{photon}}$  ranged from 65% at 21 GHz to 19% at 799 GHz.

For TDM readout, phonon and readout noise were approximately equal with TES Johnson noise being insignificant. We also modeled noise for frequency domain multiplexing readout (FDM). For FDM the TES Johnson noise was higher, 2/3 of the readout NEP, but the readout noise was lower. Comparing the combined TES Johnson and readout NEPs for TDM and FDM we found essentially identical performance with total noise differing by less than 3% across all bands. For both systems we required a focal plane temperature,  $T_o$ , of 100 mK and a bolometer safety factor of 2 to remain photon noise dominated at the lowest bands. **what does this mean? that if the safety factor is higher we are not photon noise dominated? Yes. At safety factor 2.5 phonon noise is larger than photon at 21 GHz.**

## 5.2 Combined array noise

Using single detector NEPs from Section 5.1 and the detector counts from Section 4 we calculated the combined NEP of the detector array for each band. Combining detectors simply reduced noise by  $\sqrt{N}$  except for Bose photon noise. For the lowest band of each MCP the pixel spacing was  $0.4F\lambda$  and thus the pixels oversampled the point spread function leading to correlated photon noise between pixels. Accounting for this effect gave a 26% increase in the combined array NEP for the 21 GHz band and a 0.003% increase at 799 GHz.

From the array NEP we converted to noise equivalent temperature (NET) per band using

$$\frac{NEP}{NET} = \sqrt{2}\eta_{\text{opt}} \int_{\text{band}} \left. \frac{dp_{\nu}}{dT} \right|_{T_{\text{CMB}}} d\nu. \quad (4)$$

The  $\eta_{\text{opt}}$  term contributed to the ‘jumps’ in *NET* seen in Figure 9, because  $\eta_{\text{opt}}$  varied band to band. Numerical values for the NET are given in the second to last column in Table 3.

Assuming evenly weighted observations of the full sky, 5 years of mission duration, and 95% efficiency, we calculated full mission map sensitivities in polarization; see the final column in Table 3. Combining all bands gave a total CMB map depth for the entire PICO mission of  $0.62 \mu\text{K}_{\text{CMB-arcmin}}$ .

Table 3. PICO frequency channels and noise.

Pixel Type	Band GHz	FWHM arcmin	Bolometer NEP $\text{aW}/\sqrt{Hz}$	Bolometer NET $\mu\text{K}_{\text{CMB}}\sqrt{s}$	$N_{\text{bolo}}$	Array NET $\mu\text{K}_{\text{CMB}}\sqrt{s}$	Polarization map depth $\mu\text{K}_{\text{CMB-arcmin}}$ Jy/sr	
A	21	38.4	4.89	112.2	120	13.6	19.2	6.69
B	25	32.0	5.33	103.0	200	9.56	13.5	7.98
A	30	28.3	4.92	59.4	120	5.90	8.31	7.93
B	36	23.6	5.36	54.4	200	4.17	5.88	9.59
A	43	22.2	5.33	41.7	120	4.01	5.65	13.9
B	52	18.4	5.73	38.4	200	2.86	4.03	16.8
C	62	12.8	8.29	69.2	732	3.13	4.42	37.0
D	75	10.7	8.98	65.4	1020	2.47	3.47	48.1
C	90	9.5	7.76	37.7	732	1.49	2.10	44.5
D	108	7.9	8.18	36.2	1020	1.21	1.70	57.0
C	129	7.4	7.35	27.8	732	1.09	1.53	69.7
D	155	6.2	7.36	27.5	1020	0.91	1.28	84.6
E	186	4.3	12.30	70.8	960	2.52	3.54	383
F	223	3.6	12.70	84.2	900	3.05	4.29	579
E	268	3.2	8.55	54.8	960	1.87	2.62	369
F	321	2.6	8.16	77.6	900	2.73	3.84	518
E	385	2.5	4.54	69.1	960	2.35	3.31	318
F	462	2.1	4.00	132.6	900	4.66	6.56	403
G	555	1.5	6.47	657.8	440	33.1	46.5	1569
H	666	1.3	5.74	2212	400	117	164	1960
I	799	1.1	4.97	10430	360	560	816	2321
Total					12996	0.46	0.65	

[SH Here](#)

## 6. CONCLUSIONS/SUMMARY

The PICO optical system was a simple two reflector open-Dragone which we numerically optimized to maximize the DLFOV. The addition of a cold aperture stop and cold reflectors minimized optical load and reduced noise. The focal plane took advantage of the large DLFOV and MCP technology to implement 12996 polarization sensitive detectors in 21 bands from 21-799 GHz. When combining all bands our instrument noise model predicted a full mission polarization map depth of  $0.62 \mu\text{K}_{\text{CMB-arcmin}}$ .

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