University of Auckland Department of Accounting & Finance

Finance 788: Research Essay

A research essay presented in part fulfilment of the requirements for the degree of Bachelor of Commerce (Honours) in the Department of Accounting and Finance at The University of Auckland

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1 Acknowledgements

Paul Geertsema

2 Abstract

Introduction (3 Pages) 3

4 Research Question(s)

Can neural networks, optimized to maximise financial metrics (e.g., Hedge Portfolio Excess Return, Sharpe Ratio etc.,) outperform conventional loss minimisation optimisation strategies, when predicting excess returns in individual equities and equity hedge portfolios?

5 Motivation(s)

6 Literature Review (3 pages)

Overview of literature in asset pricing (761/751), ML application, factor pricing - very brief, 12pt, double spaced,

6.1 Asset Pricing

6.2 Machine Learning

Convexity is an important concept in optimisation Monotonic ranking

6.3 Machine Learning

A couple of recent publications highlight the increased application of machine learning algorithms in financial contexts. Li et al., 2020 Gu et al (2020) explore the comparative use of machine learning in empirical asset pricing.

6.4 Hypothesis

Include examples on the minimisation of sum of the square errors does not contribute to maximising returns

7 Methodology

The required methodology to construct the methods to build, develop, and deploy neural networks with custom objective functions.

7.1 Data

Hou et al., (2020) use an extensive data library to assess 452 anomalies across anomalies literature. Their analysis informs which abnormalities drive the cross section of expected returns. Most abnormalities fail under current standards of empirical finance when using a single hurdle test of absolute t-stat greater or equal to 1.96. Firstly, the paper finds economic fundamentals take precedence over trading frictions in explanatory power, statistical and economic significance. Secondly, micro-caps account for anomalies disproportionately, leading to NYSE breakpoints, value-weighted returns in both portfolio sorts and cross-sectional regressions with weighted least squares. Lastly, arguments in improving anomalies literature credibility follow a closer alignment to economic theory as the field persists to be statistical in nature. Overall, capital market efficiency is higher than expected. Jensen et al., 2021 use the above dataset to explore hierarchical bayesian models of alphas emphasising the joint behaviours of factors, and provide an alternative multiple testing adjustment, more powerful than common methods. Jensen et al., adapt the global dataset to focus only on one-month holding periods for all factors, only include most recent accounting data (quarterly or annually) and add 15 new factors. The authors provide documentation and web-based resources on GitHub to reconstruct an updated dataset from Wharton Research Data Services (WRDS) using SAS Studio. The dataset is exhaustive as illustrated by the both the summary statistics in 15.3 and Global Factor Data Documentation in the author's GitHub repository ¹ Identifier variables (e.g., size group), Accounting variables (e.g., COGS), accounting characteristics (e.g., change in net working capital, solvency ratios etc.), market variables (e.g., share price, excess return), market characteristics (e.g., market equity, 60 month CAPM β), and detailed characteristics (e.g., equity duration, Altman Z-Score) and Foreign Exchange Conversion Rates feature in the dataset's composition. The complete global dataset has 406 characteristics, a superset of the original 153 in Jensen et al., with 2,739,928 firm-year observations, across 524 features, from January 1st 1961 to December 31st 2020. Subsequently, the complete dataset has 1.435 billion data points. One month lead excess returns is the designated target variables for prediction as will inform the construction of hedge portfolio to assess relative performance between different optimisation functionalities. The exhaustive nature and accessibility of the global dataset makes it well-suited for exploring optimisation functions, maximising renown financial metrics, in deep neural-networks.

 $^{^{1}\}mathrm{View}$ summary statistics and in tandem for comprehension

7.2Infrastructure

The essay necessitates substantial software development, infrastructure, and technological configuration to undertake analysis. Google Cloud Platform Cloud Storage buckets manage large datasets. The deployment of Google Cloud Engine Compute Engine Virtual Machine (VM) Instances, optimised for machine learning, build, train, and evaluate deep neural networks. Cryptographic network protocols, mostly secure shells, establish remote connectivity between local and remote infrastructure to communicate and execute commands. Version control technologies, primarily Git and GitHub, manage and develop methods for analysis with the programming of approximately 40 methods, classes, and functions.

7.3 **Data Processing**

Analysis requires data preprocessing to form training, validation, and testing subsets fro the neural network. The initial training, testing, and validation sets comprise of 1031516, 706908, and 1001504 global equity firm-year observations across 524 features, respectively. The division of subsets is chronological with firm-year observations [1961-1990), [1990-2000), [2000-2020] for training, validation, and testing, respectively. However, the computational complexity exceeds resources available at the time of analysis. Subsequently, training sets require further preprocessing in addition to reconfiguring infrastructure. Further preprocessing includes: Reducing the number of factors from Jensen et al., (2021) to approximately the same number of features (160) Hou et al., (2020) use to explore portfolio replication. The replacement of NaN values in a feature columns with the median value of the respective column to retain observations. The removal of firm-year observations with Micro or Nano size grouping designations, non-overlapping, value weighted by market capitalisation on the New York Stock Exchange (NYSE)). Mega, Large, and Small remain, reflecting equities with market capitalisations greater than the 80th, 50th, and 20th percentile of all NYSE stocks, respectively. Micro equities reside between the 1st and 20th percentiles, with Nano between below the 1st percentile. The rational for their exclusion is Mega, Large, and Small equities account for the majority of stock market returns (80%). Hypothetically, their omission will not materially influence results. Furthermore, the reduction in numerical feature precision from float64 to float32 effectively halves memory usage. The training, testing, and validation sets comprise of 532218, 294581, and 531461 global equity firm-year observations across 160 features after above revisions, respectively. Subsequently, the revised dataset has 217.321,600 data points, suitable to use in analysis. Memory monitoring methods accompany the aforementioned preprocessing adjustments, monitoring CPU and GPU utilisation, reconfiguring GPU's, and configuring application programming interfaces for monitoring modelling performance.

7.4 Feature Encoding

Deep neural networks require tensors as inputs for fitting, training, and evaluating data to make predictions. A tensor is a mathematical object describing the physical properties of an object. In other words, multilinear relationships between sets of algebraic objects related in vector set. Transformation laws govern tensors. Therefore, a tensor is considered an n dimensional arrays in conjunction with associated transformation laws. The dataset must take the form of a tensor for analysis. Essentially, every value for every feature must be encoded to take a numerical form. A feature matrix is correct term for the dataset in this application. Firstly, the labelling of target variable is necessary for training, validating, and testing the model. Secondly, a shuffling of columns and instances in feature matrix promotes better training as accommodates randomness. This analysis sacrifices shuffling the training set due to memory issues. Lastly, an encoding process encodes both categorical and numerical feature columns. The revised dataset includes eight categorical variables:

- 1. **size_group**: The aforementioned size grouping in 7.1
- 2. **permno**: Permanent unique firm identifier from CRSP
- 3. **permco**: Permanent unique issue identifier from CRSP
- 4. crsp_shrcd: CRSP share code
- 5. **crsp_exchcd**: Compustat stock exchange code
- 6. sic: Firm SIC industry
- 7. **ff49**: Classification of stocks in 49 industry groups based on SIC codes and the methodology in F.Fama & K.French 1997 with the addition of the software industry.
- 8. adjfct: Share Adjustment Factor

Categorical encoding transforms the set of instances for a features into a series of binary variables. These may be one-hot encoded, and/or stored in sparse tensors, depending on input and desired application. The remaining variables are numerical where a normalization normalizes each feature to zero mean and unit variance.

7.5 Neural Network Configuration

7.5.1 Multi Layer Perceptron (MLP)

Artificial Neural Nets (ANN) are versatile, powerful, and scalable. They frequently outperform other machine learning algorithms on large and complex problems. Linear threshold units (LTU) compose

neural networks. A linear threshold unit (LTU) feeds the weighted sum of input values (??) into a step function (2). A perceptron is a single layer of LTUs connected to every input. Perceptrons are suitable for both regression and classification tasks. Perceptrons utilize a training algorithm assessing the strength of connections between perceptrons while considering errors. A perceptron is fed one training instance at a time, making predictions for each instance. For every output LTU that produced a wrong prediction, it re-enforces the connection weights using the perception learning rule (6) from the inputs that would have contributed to the right prediction. One LTU input layer, multiple LTU hidden layers, and an output LTU layer create an Multi Layer Perceptron (MLP). The step functions in each LTU are replaced by a logistic (??) or ReLU function (4) to enable gradient descent for optimisation. A shared activation function replaces the individual activation functions in the output layer to enable exclusive classification or regression. The linear activation function (5) is most suitable output layer activation function for regression task as predict values between $(-\infty, \infty)$ directly, suitable for evaluating excess returns.

$$z = \mathbf{w}^T \cdot \mathbf{x} \tag{1}$$

$$h_w(\mathbf{x}) = step(z) \tag{2}$$

$$\sigma(z) = \frac{1}{1 + exp(-z)} \tag{3}$$

$$ReLU(z) = max(0, z)$$
 (4)

$$Linear(z) = z \tag{5}$$

$$w_{i,j}^{\text{next step}} = w_{i,j} + \eta(\hat{y}_j - y_j)x_i \tag{6}$$

Where

- $w_{i,j}$ is the connection weights between the ith input neuron and the jth output neuron.
- x_i is the ith input value of the current training instance.
- \hat{y}_j is the output of the jth output neuron for the current training instance.
- \bullet y_j is the output of the jth output neuron for the current training instance.
- η is the rate.

The architecture for analysis is a large MLP.

7.5.2 Model Configuration

Figure 1 visualises the topography of a standard neural network.

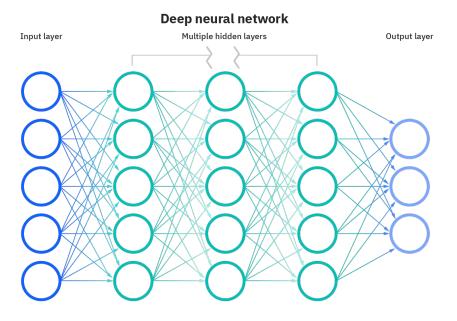


Figure 1: Standard Neural Network Topography (Source: IBM)

The dots and lines represent nodes and connections between nodes, respectively. The architecture of the network is derivative of the model's intended use. The set of

Figure 2 illustrates the configuration for this project (work in prgoress).

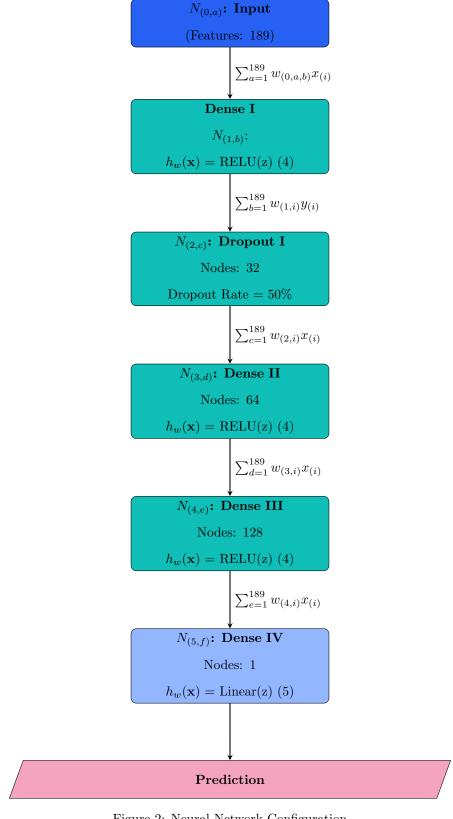


Figure 2: Neural Network Configuration

10 epochs, 207 runs per epochs.

8 Brief Description of Remaining Methods

- Use stochastic gradient descent, train model with 10 epochs (2709 runs per epoch) for each of the six loss functions (tensorflow mse, custom mse, sharpe ratio, sharpe ratio mse, hedge portfolio mse, information ratio). Validate with validation set and evaluate with testign set.
- Make predictions using entire testing set for each model. Merge predictions with fama french factors on month
- Perform newy west regressing hedge portfolio returns on fama factors. Predictions grouped by month, hedge formed by mean of top decile mean of bottom decile creating hedge return for the month.
- Second set of regressions does a panel regression accounting Heteroskedasticity Robust Covariance as Fama MacBeth did not execute due to rank deficiencies.

9 Work in Progress

9.1 Loss Functions & Performance Metrics

9.1.1 Modelling, Loss, and Optimisation

We summarize the theory surrounding predictive modelling, loss functions, and optimisation algorithms. These functions train models by comparing predictions to realized observations using optimisation algorithms to minimize the loss function. We examine a linear model as our predictive model (7). Mean square error (8) and Gradient Descent (GD) are basic examples of a loss function and optimisation algorithm, respectively.

$$\hat{y} = mx_i + b \tag{7}$$

$$f(y, (mx_i + b)) = \frac{1}{n} \sum_{i=1}^{n} (y_i - (mx_i + b))^2$$
(8)

Firstly, gradient descent takes the partial derivatives of the loss function, with the respect to the parameters in our predictive model. In our example, equations 9 and 10 are the partial derivatives for the

mean square error loss function.

$$\frac{\partial f(y, (mx_i + b))}{\partial m} = \frac{1}{n} \sum_{i=1}^{n} -2x_i (y_i - (mx_i + b))^2$$
(9)

$$\frac{\partial f(y, (mx_i + b))}{\partial b} = \frac{1}{n} \sum_{i=1}^{n} -2(y_i - (mx_i + b))^2$$
(10)

Secondly, the algorithm explores epochs, using a learning rate to update parameters to move in the opposite directions of the partial derivatives until settling in a local minima. This extrema is the optimisation of the loss function, quantifying the accuracy of the predicative model. Ordinary Least Squares (OLS) regressions is an extension of the linear model prevalent in asset pricing. The mathematical rigor and suitability of the OLS estimator section 15.1. The theory underlying OLS informs the common practice in minimising of the sum of least squares when evaluating prediction performance. The mathematical tractability, in accordance with the aforementioned assumption, frame our thinking surrounding the derivation of custom loss functions.

9.1.2 Automatic Differentiation

9.1.3 Loss & Metric Definition

9.2 Hedge Portfolio Construction

9.3 Regression Analysis

10 Limitations

Further research will rely on addressing several limitation.

10.1 Lack of Computational Resources

The lack of resources to explore the entire dataset within reasonable timeframes, and at reasonable costs. The most material inhibitions are the inability to explore all 524 factors for all size groupings, the reducing in level of precision for numerical features, the ability to shuffle training sets at lengths greater than or equal to the input sets

10.2 Loss Functions & Performance Metrics

Table 1 emphasises the separation between training and validation datasets.

Variable	Description	$MSE(y, \hat{y})$	$HP(y,\hat{y})$
θ	Estimation Training	$\hat{ heta}_{MSE}$	$\hat{ heta}_{HP}$
λ	Validation	$\hat{\lambda}_{MSE}$	$\hat{\lambda}_{HP}$

Table 1: Objective (MSE: Mean Square Error, HP: Hedge Portfolio)

10.2.1 Mean Square Error (MSE)

Section 9.1.1 outlines advantages to Ordinary Least Squares. Subsequently, MSE serves as a baseline for loss function and performance metric comparisons. The following function (11) and partial derivative (12) describe Tensorflows's Mean Square Error implementation, both from in-built and custom contexts. Python classes describe equation 11 to enable Tensorflow's automatic differentiation capabilities, approximating the partial derivatives of the loss function (12) with numerical methods. Please note the use of Hadamard exponentiation $(x^{\circ n})$ as an element-wise operation.

$$f(y, X^T \hat{\theta}) = \frac{\vec{1}}{\vec{1}^T \vec{1}} (y - X^T \hat{\theta})^{\circ 2}$$

$$\tag{11}$$

$$\frac{\partial f(y, X^T \hat{\theta})}{\partial \hat{\theta}} = \frac{\vec{1}}{\vec{1}^T \vec{1}} (-2(y - XT \hat{\theta})^{\circ 1})$$
(12)

10.2.2 Hedge Portfolio

Hedge portfolios rely on monotonic ranking functions for optimisation as their monotonic nature preserves or reverses a given ordered set. The analysis cross-section of one-month lead portfolio excess returns using monotonic functions

$$R(y_{i,t}) \tag{13}$$

The ranking function $(R(y_{i,t}))$ and thresholds (u,v) form subsets of long and short portfolios. Long (L) or Short (S) sets include excess returns conditioned on the associated monotonic ranking given a threshold, bound by the cardinality of the excess return vector (|y|). The subsequent truth sets mathematically express aforementioned time-series hedge portfolios.

$$L = \{y_{i,t} | R(y_{i,t}) \le u\}$$

$$S = \{y_{i,t} | R(y_{i,t}) \ge v\}$$

$$0 < u \le |y|$$

$$0 < v \le |y|$$

$$u < v$$

Equation 14 describes hedge portfolio lead excess returns (H_t) at a given time (t).

$$H_t = \frac{1}{|L|} \sum_{i \in L} y_{i,t} - \frac{1}{|S|} \sum_{i \in S} y_{i,t}$$
(14)

Figure 3) illustrates an approximate linear monotonic ranking function with a sample of 100 uniformly distributed excess returns between -10% and 10%. Boundary conditions u and v are set to 20 and 80, respectively. Subsequently, excess returns above (below) the green (blue) dotted line belong to the long (L) (short (S)) set.

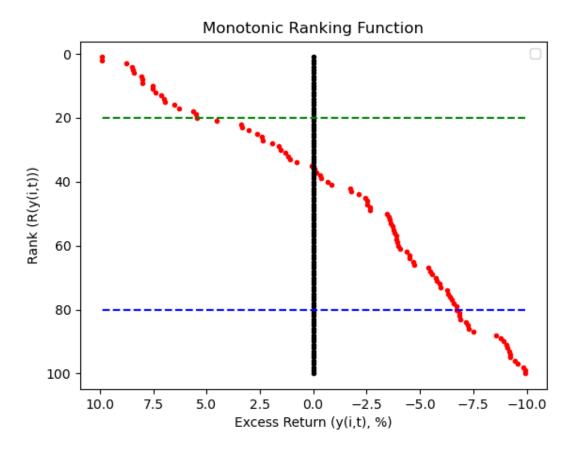


Figure 3: Approximate Linear Monotonic Ranking Function

The permutations in monotonic ranking functions, and subsequent hedge portfolios, are endless. This research essay develops a monotonic ranking function proportionally weighting one month lead excess returns (15). Therefore, equation 16 defines the loss function.

$$R(\hat{y}) = W$$

$$W := \frac{\hat{y}}{\hat{\mathbf{I}}\hat{y}}$$

$$\hat{y} = X^T \hat{\theta}$$
(15)

$$f_{\hat{\theta}}(X) = \left(\frac{X^T \hat{\theta}}{\mathbf{1} X^T \hat{\theta}}\right)^\top X^T \hat{\theta} \tag{16}$$

The above loss function is differentiable using symbolic mathematic as shown in equation 17.

$$\frac{\partial f_{\hat{\theta}}(X)}{\partial \hat{\theta}} = \frac{\partial ((\frac{X^T \hat{\theta}}{\vec{1} X^T \hat{\theta}})^\top X^T \hat{\theta})}{\partial \hat{\theta}}
\frac{\partial (f_{\hat{\theta}}(X))}{\partial \hat{\theta}} = \frac{1}{(\hat{\theta}^\top X \vec{1})} X X^\top \hat{\theta} + \frac{1}{\vec{1} X^\top \hat{\theta}} X X^\top \hat{\theta} - \frac{1}{(\hat{\theta}^\top X \vec{1})^2} \hat{\theta}^\top X X^\top \hat{\theta} X \vec{1}$$
(17)

Our research Subsection 9.1.1 explains the theory supporting loss minimisation. Applying gradient

descent methods to the product of the loss function and scaler of -1 transforms the minimisation to maximisation. This transformation leads to finding the argmax of maximisation function with respect to $\hat{\theta}$ (18). The aforementioned transformation is simply and suitable for exploration in the context of the research intent. More sophisticated methods exist for maximisation such as reinforcement learning (10.4).

$$\underset{\hat{\theta}}{\operatorname{argmax}} : (\frac{X^T \hat{\theta}}{\vec{\mathbf{1}} X^T \hat{\theta}})^\top X^T \hat{\theta} \tag{18}$$

10.3 Conventional Asset Pricing Models

Conventional asset pricing methodologies persist in academic literature. The use of the Capital Asset Pricing Model (CAPM) persists, regardless of the identifiable shortcomings in market proxies and empirical failings invalidating use (Fama and French, 2004). Nonetheless, this research essay uses the model as a performance metric for comparative purposes.

$$R_{i,t} - R_{f,t} = \alpha_{i,t} + \beta_{i,t}^1 (R_{M,t} - R_{f,t})$$
(19)

E. Fama and K. French (1992) validate the explanatory power of size and value (book-to-market) factors in their ability to capture the cross-sectional variation in average stock returns, in association with market risk, size, leverage, book-to-market, and earnings-price ratios. E. Fama and K. French further their analysis on the common characteristics between stocks and bonds (Fama and French, 2021)¹, and add two additional factors to consider profitability and investment. The main combinations are the Fama French Three (FF3) (20) and Five (FF5) (21) models. E. Fama and K. French consider a momentum factor on international stock returns in subsequent years (Fama and French, 2012). The omission of momentum from the models stand.

$$R_{i,t} - R_{f,t} = \alpha_{i,t} + \beta_{i,t} (R_{M,t} - R_{f,t})$$
(20)

$$R_{i,t} - R_{f,t} = \alpha_{i,t} + \beta_{i,t} (R_{M,t} - R_{f,t})$$
(21)

where

- $R_{i,t} R_{f,t}$: Portfolio Excess Return on the market for a given portfolio and time, value-weighted using all incorporated US CRSP firms incorporated in the US, listed on the NYSE, AMEX, or NASDAQ.
- $\alpha_{i,t}$: Jensen's alpha indicating mispricing in the asset.

¹Reprinted. Originally published in 1993

- β_t^1 : Market Risk Factor (co-efficient)
- β_t^1 : Size Factor (co-efficient)
- β_t^2 : Value Factor (co-efficient)
- β_t^2 : Value Factor (co-efficient)
- β_t^3 : Profitability Factor (co-efficient)
- β_t^4 : Investment Factor (co-efficient)
- $(R_{M,t} R_{f,t})$: Market Risk Premium
- SMB_t : Size Premium (small minus big) is the difference in average return between nine small stock and nine large value-weighted portfolios.
- HML_t : Value Premium (high minus low) is the difference in average return between two value and two growth value-weighted portfolios.
- RMW_t : Profitability Premium (robust minus weak) is the difference in average return between two robust operating profitability and two weak operating profitability value-weighted portfolios.
- CMA_t : Investment Premium minus aggressive is the difference in average return on the two conservative and two aggressive investment portfolios

K. French continues to maintain FF3 and FF5 related datasets (French, 2021) E. Fama, with J. MacBeth, developed the Fama-MacBeth regression (Fama and MacBeth, 1973) to estimate factor loadings and prices. The methodology is a two-stage estimation process, similar for estimating factor loadings, and prices, for a given portfolio. The first step requires determining each asset's β exposures by regressing each of n asset returns against m proposed 22. The second step determines the risk premium (factor pricing) for each asset by regressing all asset returns for each of T periods against previously estimated β s (23).

$$R_{n,t} = \alpha_n + \sum_{f=1}^{F} \beta_{n,F_f} F_{f,t} + \epsilon_{n,t}$$
 (22)

$$\forall n \in \{1, ..., N\}$$

$$R_{i,t} = \gamma_{t,0} + \sum_{f=1}^{F} \gamma_{t,f} \hat{\beta_{i,F_f}} + \epsilon_{i,t}$$

$$(23)$$

$$t \in \{1, ..., N\}$$

Where

- $R_{n,t}$: Return for an asset (n) at a time (t).
- α_n : Jensen's alpha for an asset (n) implying mispricing.
- β_{n,F_f} : An asset's (n) exposure to a factor (f)
- $\hat{\beta_{i,F_f}}$: Estimated factor loading for a factor (f) from regression of asset (i)
- $\epsilon_{n,t}$: Residual for an asset at a time (t)
- $\gamma_{t,f}$: Factor pricing for a factor (f)

The residuals of risk-return regressions and co-efficient 'fair game' observations are consistent with the efficient market hypothesis ((Samuelson, 2016), (Fama, 1995), (Fama, 1963), (Fama, 1965) (Fama, 2021)). Subsequently, this research essay uses the excess one month lead returns of the hedge portfolio (??)), Capital Asset Pricing Model (19), Fama-French Three Factor Model (20), and Fama-French Five Factor Model (21) as performance metrics for each loss function. Table 2 outlines the proposed]performance metrics and loss functions.

Performance Metric	Loss Function
Hedge Portfolio Mean	Hedge Portfolio Excess Returns
Hedge Portfolio FF3	Sharpe Ratio
Hedge Portfolio FF5	Information Ratio
Sharpe Ratio	Validation
Information Ratio	Validation
Mean Square Error	Mean Square Error

Table 2: Proposed Loss Functions and Performance Metrics

Hou et al (2021) provide the required data to derive these performance metric and loss functions.

10.3.1 Sharpe Ratio

Nobel Laurette William F. Sharpe (1994) introduced the Sharpe Ratio (24) as a measure for risk-adjusted returns where $\mathbb{E}[R_a - R_f]$ is the expectation for excess returns and $\sigma(R_a)$ is the standard deviation of

excess returns.

$$SR = \mathbb{E} \frac{[R_a - R_f]}{\sigma(R_a)}$$

$$\sigma = \sqrt{\sum_{i=1}^n \frac{(R_a) - \bar{R_a}^2}{n}}$$
(24)

The matrix notation for the Sharpe Ratio loss function () follows:

$$SR = 1\partial SR \tag{25}$$

10.3.2 Information Ratio

The Information Ratio (IR) is another risk-return measure (26), evaluating the performance of a portfolio compared to a selected benchmark e.g., an exchange traded fund. $\mathbb{E}[R_a - R_b]$ is the excess return on the benchmark. $\sigma(R_a - R_b)$ is the standard deviation of the difference between the portfolio and benchmark known as the tracking error.

$$IR = \mathbb{E}\frac{[R_a - R_b]}{\sigma(R_a - R_b)} \tag{26}$$

Both Sharpe and Information ratios supplement hedge portfolio-related loss functions and performance metrics.

- 10.4 Reinforcement learning
- 10.4.1 Dynamic Programming
- 10.4.2 Bellman's Algorithm
- 10.4.3 Q-Learning

11 Results

11.1 Performance Matrix

Hlavac, 2018 enables the tables in the regression analysis.

11.2 Model Performance

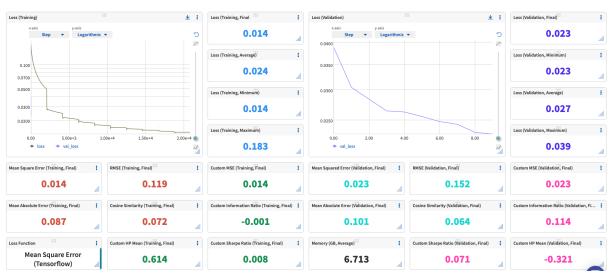


Figure 4: Mean Square Error Model (Tensorflow)

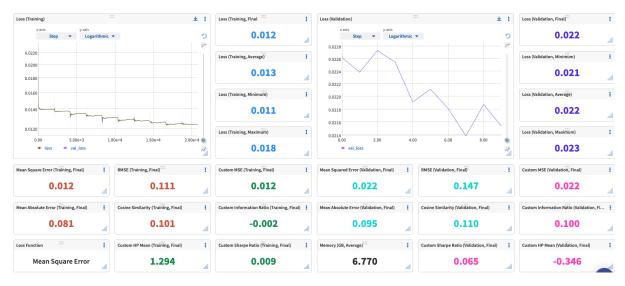


Figure 5: Mean Square Error Loss Function

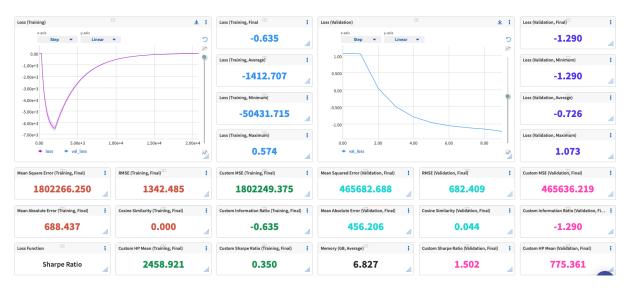


Figure 6: Sharpe Ratio Loss Function

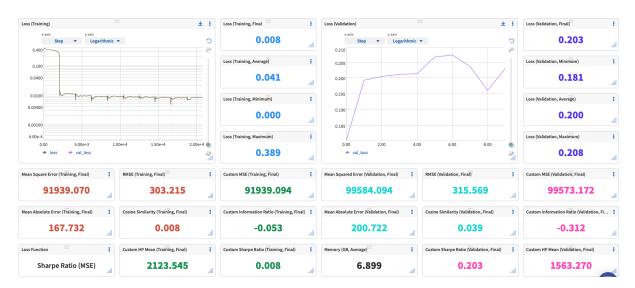


Figure 7: Sharpe Ratio (MSE) Loss Function

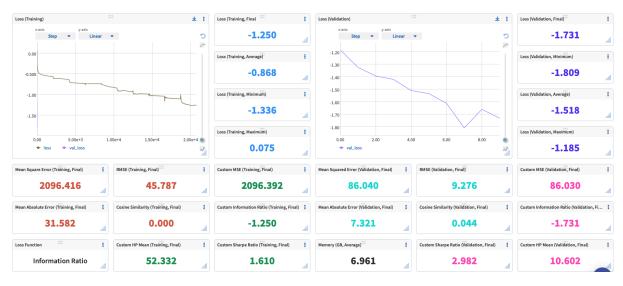


Figure 8: Information Ratio Loss Function

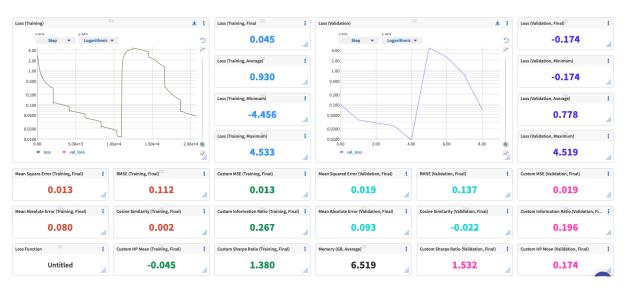


Figure 9: Hedge Portfolio Loss Function

11.3 Hedge Portfolio Performance

11.3.1 Realised Excess Returns

	One Mon	th Lead Excess Portfolio F	One Month Lead Excess Portfolio Return using realised excess returns:	returns:
	CAPM	FF3	FF4	FF5
CMA				0.000
HML		0.001*	0.000	0.000
		(0.001)	(0.001)	(0.001)
Mkt- RF	-0.001	-0.001	-0.001	-0.001
	(0.001)	(0.001)	(0.001)	(0.001)
$_{ m RMW}$			0.003**	0.003**
			(0.001)	(0.001)
$_{ m SMB}$		0.001	0.002	0.002
		(0.001)	(0.001)	(0.001)
const	0.004	0.004	0.003	0.003
	(0.003)	(0.003)	(0.002)	(0.002)
Observations	252	252	252	252
R^2	0.011	0.025	0.042	0.042
Adjusted R^2	0.007	0.013	0.026	0.022
Residual Std. Error	0.043(df = 250)	0.043(df = 248)	0.042(df = 247)	0.043(df = 246)
F Statistic	2.402 (df = 1.0; 250.0)	1.849 (df = 3.0; 248.0)	1.958 (df = 4.0; 247.0)	1.717 (df = 5.0 ; 246.0)
Note:)>d _*	*p<0.1; **p<0.05; ***p<0.01

11.3.2 Mean Square Error (Tensorflow)

CAPM FF3 CAPM CAPM -0.001** (0.001) -0.001* (0.001) -0.000* (0.000) -0.018*** (0.000) -0.018*** (0.004) 112 252 (0.004) 1252 (0.004) 13 252 (0.004) 14 Error (0.025) (0.026)		One	Month Lead Excess Portfolic	One Month Lead Excess Portfolio Return using mean squared error:	error:
RF -0.001^{**} (0.001) -0.001^{*} (0.000) I rvations 252 0.029 0.043 0.025(df = 250) 0.021^{**} 0.001^{*} 0.0001		CAPM	FF3	FF4	FF5
RF -0.001^{**} (0.001) -0.001^{*} (0.000) -0.000 -0.018^{***} (0.000) -0.018^{***} (0.004) rvations 252 0.029 0.025 0.025 0.043 ual Std. Error $0.025(df = 250)$ 0.025(df = 248)	CMA				0.001
RF (0.001) (0.000) (0.000) (0.000) (0.000) (0.000) (0.004) rations 252 0.029 0.029 0.043 ual Std. Error $0.025(df = 248)$	HML		-0.001**	-0.002***	(0.001)
RF -0.001^* -0.001^* (0.000) (0.000) -0.018^{***} (0.004) rations 252 252 0.029 $0.055anal Std. Error 0.025(\mathrm{df} = 250) 0.025(\mathrm{df} = 248)$			(0.001)	(0.001)	(0.001)
(0.000) (0.000) (0.000) (0.000) (0.000) (0.0018*** (0.004) (0.004) (0.004) (0.004) (0.004) (0.0055) (0.029 (0.029 (0.055 (0.029 (0.025 (0.043 (0.025 (0.025 (0.043 (0.025 (0.025 (0.043 (0.043	Mkt- RF	-0.001*	-0.001*	-0.001	-0.000
-0.000 (0.000) -0.018*** (0.004) (0.004) (0.004) (0.004) (0.004) (0.0055) (0.029 (0.025 0.025 0.026 0.043) (0.025 (df = 250) (0.025 (df = 248)		(0.000)	(0.000)	(0.000)	(0.000)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$_{ m RMW}$			0.002^{***}	0.002^{***}
-0.000 (0.000) (0.004) (0.004) (0.004) (0.004) (0.004) (0.004) (0.004) (0.005) (0.029 (0.055) (0.026 (0.025)				(0.001)	(0.001)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$_{ m SMB}$		-0.000	0.000	0.000
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			(0.000)	(0.000)	(0.000)
$\begin{array}{cccc} (0.004) & (0.004) \\ 252 & 252 \\ 0.029 & 0.055 \\ 0.026 & 0.043 \\ \text{Error} & 0.025(\mathrm{df}=250) & 0.025(\mathrm{df}=248) \end{array}$	const	-0.018***	-0.018***	-0.019^{***}	-0.019^{***}
252 252 0.029 0.055 0.055 0.026 0.025 (df = 250) 0.025(df = 248)		(0.004)	(0.004)	(0.004)	(0.004)
$\begin{array}{ccc} 0.029 & 0.055 \\ 0.026 & 0.043 \\ \text{Error} & 0.025(\text{df} = 250) & 0.025(\text{df} = 248) \end{array}$	Observations	252	252	252	252
Error 0.026 0.025 $(df = 250)$ 0.025 $(df = 248)$	R^2	0.029	0.055	0.082	0.088
Error $0.025(df = 250)$ $0.025(df = 248)$	Adjusted R^2	0.026	0.043	0.067	0.069
	Residual Std. Error	0.025(df = 250)	0.025(df = 248)	0.025(df = 247)	0.025(df = 246)
$3.816^* \text{ (df} = 1.0; 250.0)$ $3.080^{**} \text{ (df} = 3.0; 248.0)$	F Statistic	$3.816^* \text{ (df} = 1.0; 250.0)$	$3.080^{**} \text{ (df} = 3.0; 248.0)$	3.644^{***} (df = 4.0; 247.0)	$3.023^{**} \text{ (df} = 5.0; 246.0)$

11.3.3 Mean Square Error

	0	One Month Lead Excess Portf	One Month Lead Excess Portfolio Return using custom mse:	
	CAPM	FF3	FF4	FF5
CMA				0.001
HML		-0.001**	-0.002***	-0.002***
		(0.000)	(0.001)	(0.001)
Mkt- RF	-0.001*	-0.000	-0.000	-0.000
	(0.000)	(0.000)	(0.000)	(0.000)
$_{ m EMW}$			0.001**	0.001**
			(0.001)	(0.001)
SMB		-0.001	-0.000	-0.000
		(0.000)	(0.000)	(0.000)
const	-0.023***	-0.023***	-0.024***	-0.024^{***}
	(0.003)	(0.003)	(0.003)	(0.003)
Observations	252	252	252	252
R^2	0.015	0.047	0.063	0.068
Adjusted R^2	0.011	0.035	0.048	0.049
Residual Std. Error	0.022(df = 250)	0.022(df = 248)	0.021(df = 247)	0.021(df = 246)
F Statistic	$2.857^* \text{ (df} = 1.0; 250.0)$	3.870^{***} (df = 3.0 ; 248.0)	3.411^{***} (df = 4.0 ; 247.0)	$2.990^{**} \text{ (df} = 5.0; 246.0)$

*p<0.1: **p<0.05: ***p<0.01

11.3.4 Hedge Portfolio

	O_1	One Month Lead Excess Portfolio Return using custom hp:	olio Return using custom h	<i>.</i> :
	CAPM	FF3	FF4	FF5
$_{ m CMA}$				-0.001
HML		-0.001**	-0.001***	-0.001**
		(0.000)	(0.000)	(0.000)
Mkt- RF	0.000	0.000	0.000	0.000
	(0.000)	(0.000)	(0.000)	(0.000)
$_{ m RMW}$			0.000	0.000
			(0.000)	(0.000)
SMB		-0.000	-0.000	-0.000
		(0.000)	(0.000)	(0.000)
const	0.012^{***}	0.012^{***}	0.012^{***}	0.012^{***}
	(0.001)	(0.001)	(0.001)	(0.001)
Observations	252	252	252	252
R^2	0.001	0.057	0.062	0.072
Adjusted R^2	-0.003	0.046	0.047	0.054
Residual Std. Error	0.009(df = 250)	0.009(df = 248)	0.009(df = 247)	0.009(df = 246)
F Statistic	0.115 (df = 1.0; 250.0)	2.132^* (df = 3.0 ; 248.0)	$1.990^* \text{ (df} = 4.0; 247.0)$	1.733 (df = 5.0; 246.0)

:0.0>0*

Note:

11.3.5 Sharpe Ratio

	One .	Month Lead Excess Portfol	One Month Lead Excess Portfolio Return using custom sharpe:	urpe:
	CAPM	FF3	FF4	FF5
CMA				-7.212*
				(3.768)
HML		-2.980	-3.227	-0.582
		(2.366)	(2.374)	(2.345)
Mkt-RF	-3.354	-3.153	-3.032	-3.944^{*}
	(2.203)	(2.325)	(2.188)	(2.234)
RMW			0.666	0.338
			(2.312)	(2.347)
SMB		-0.938	-0.681	-0.307
		(1.943)	(2.490)	(2.434)
const	23.034	23.419	23.042	25.094
	(16.190)	(15.903)	(15.527)	(15.747)
Observations	252	252	252	252
R^2	0.021	0.030	0.030	0.041
Adjusted R^2	0.017	0.019	0.015	0.022
Residual Std. Error	104.887(df = 250)	104.810(df = 248)	105.012(df = 247)	104.629(df = 246)
F Statistic	2.317 (df = 1.0; 250.0)	1.534 (df = 3.0; 248.0)	1.167 (df = 4.0; 247.0)	1.376 (df = 5.0; 246.0)
Note:)>d _*	*p<0.1; **p<0.05; ***p<0.01

11.3.6 Sharpe Ratio (MSE)

	One M_0	onth Lead Excess Portfolio	One Month Lead Excess Portfolio Return using custom sharpe mse:	ve mse:
	CAPM	FF3	FF4	FF5
CMA				**696.6
HMI,		4.486	4.014	$(4.457) \\ 0.358$
		(2.978)	(2.918)	(2.623)
Mkt-RF	-0.554	-0.513	-0.281	0.980
	(1.786)	(1.802)	(1.762)	(1.635)
RMW			1.271	1.724
			(3.101)	(2.945)
SMB		-0.295	0.195	-0.321
		(2.132)	(2.441)	(2.385)
const	-131.292***	-131.559^{***}	-132.280^{***}	-135.116***
	(16.512)	(15.873)	(16.058)	(15.706)
Observations	252	252	252	252
R^2	0.001	0.022	0.023	0.046
Adjusted R^2	-0.003	0.010	0.007	0.026
Residual Std. Error	100.581(df = 250)	99.906(df = 248)	100.072(df = 247)	99.075(df = 246)
F Statistic	0.096 (df = 1.0; 250.0)	0.903 (df = 3.0; 248.0)	0.698 (df = 4.0; 247.0)	1.422 (df = 5.0; 246.0)
Note:			>d*	*p<0.1; **p<0.05; ***p<0.01

11.3.7 Information Ratio

CAPM CMA HML Wkt-RF Wkt-RF (0.053) RMW SMB const const Const (0.479) Observations 252	onth Lead Excess Portfolio	One Month Lead Excess Portfolio Return using custom information:	nation:
F. ations	FF3	FF4	FF5
F. ations			-0.039
F. ations	-0.024	-0.076	(0.119) -0.062
F ations	(0.052)	(0.063)	(0.075)
ations	-0.061	-0.035	-0.040
ations	(0.055)	(0.053)	(0.060)
rvations		0.141**	0.139^{**}
rvations		(0.065)	(0.064)
rvations	-0.009	0.046	0.048
rvations	(0.060)	(0.072)	(0.072)
servations	5.288***	5.208***	5.219^{***}
servations	(0.479)	(0.477)	(0.483)
	252	252	252
R^{-}	0.010	0.020	0.021
Adjusted R^2 0.005	-0.002	0.004	0.001
Residual Std. Error $2.968(df = 250)$	2.979(df = 248)	2.970(df = 247)	2.975(df = 246)
F Statistic $1.581 \text{ (df} = 1.0; 250.0)$ 0	0.628 (df = 3.0; 248.0)	2.136^* (df = 4.0 ; 247.0)	1.750 (df = 5.0; 246.0)

*p<0.1; **p<0.05; ***p<0.01

Fama MacBeth Regressions using individual securities. PooledOLS replaces Fama MacBeth in this instance.

11.4 Individual Panel Regressions

11.4.1 Realised Excess Returns

Dep. Va	riable:	ret_exc_lead1	m	R-squared:		0.0015	
Estimate	or:	PooledOLS		R-squared (Between):		-0.0742	
No. Obs	ervations:	531461		R-squared (Within):		0.0011	
Date:	r -	Γue, Jan 11 20)22	R-s	squared (C	Overall):	0.0015
Time:		11:47:07		Log	g-likelihoo	d	3.019e+05
Cov. Est	imator:	Robust					
				F-s	tatistic:		813.86
Entities:		7282		P-value		0.0000	
Avg Obs:		72.983		Distribution:		F(1,531459)	
Min Obs:		1.0000					
Max Obs:		252.00		F-statistic (robust):		521.20	
				P-value		0.0000	
Time periods:		252		Distribution:		F(1,531459)	
Avg Obs:		2109.0					
Min Obs:		1869.0					
Max Obs:		3400.0					
	Parameter	Std. Err.	T-st	tat	P-value	Lower CI	Upper CI
const	0.0067	0.0002	34.2	27	0.0000	0.0063	0.0071
Mkt-RF	0.0012	5.072 e-05	22.8	30	0.0000	0.0011	0.0013

Dep. Variable:	ret_exc_lead1m	R-squared:	0.0022	
Estimator:	PooledOLS	R-squared (Between):	-0.0683	
No. Observations:	531461	R-squared (Within):	0.0013	
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0022	
Time:	11:47:08	Log-likelihood	3.02e+05	
Cov. Estimator:	Robust			
		F-statistic:	387.46	
Entities:	7282	P-value	0.0000	
Avg Obs:	72.983	Distribution:	F(3,53145	
Min Obs:	1.0000			
Max Obs:	252.00	F-statistic (robust):	238.06	
		P-value	0.0000	
Time periods:	252	Distribution:	F(3,53145	
Avg Obs:	2109.0			
Min Obs:	1869.0			
Max Obs:	3400.0			

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0070	0.0002	35.904	0.0000	0.0066	0.0073
Mkt-RF	0.0012	5.393e-05	23.130	0.0000	0.0011	0.0014
SMB	-0.0006	7.995e-05	-7.5937	0.0000	-0.0008	-0.0005
HML	-0.0009	7.383e-05	-11.770	0.0000	-0.0010	-0.0007

Dep. Variable:	ret_exc_lead1m	R-squared:	0.0057
Estimator:	PooledOLS	R-squared (Between):	-0.0922
No. Observations:	531461	R-squared (Within):	0.0053
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0057
Time:	11:47:09	Log-likelihood	3.03e + 05
Cov. Estimator:	Robust		
		F-statistic:	757.73
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(4,531456)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	526.03
		P-value	0.0000
Time periods:	252	Distribution:	F(4,531456)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
Paramete	r Std. Err. T-	stat P-value Lower C	I Upper CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0091	0.0002	44.309	0.0000	0.0087	0.0095
Mkt-RF	0.0006	5.855 e-05	9.9063	0.0000	0.0005	0.0007
SMB	-0.0022	8.173 e-05	-27.137	0.0000	-0.0024	-0.0021
HML	0.0007	7.583e-05	9.1125	0.0000	0.0005	0.0008
$\mathbf{R}\mathbf{M}\mathbf{W}$	-0.0037	0.0001	-36.210	0.0000	-0.0039	-0.0035

Dep. Variable:	ret_exc_lead1m	R-squared:	0.0063
Estimator:	PooledOLS	R-squared (Between):	-0.0995
No. Observations:	531461	R-squared (Within):	0.0063
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0063
Time:	11:47:10	Log-likelihood	3.031e+05
Cov. Estimator:	Robust		
		F-statistic:	675.07
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	478.68
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
Paramete	r Std. Err. T-	stat P-value Lower C	I Upper CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0084	0.0002	41.037	0.0000	0.0080	0.0088
Mkt-RF	0.0009	5.779 e-05	15.519	0.0000	0.0008	0.0010
SMB	-0.0024	8.158e-05	-28.972	0.0000	-0.0025	-0.0022
HML	-0.0001	9.671 e- 05	-1.4864	0.1372	-0.0003	4.58e-05
$\mathbf{R}\mathbf{M}\mathbf{W}$	-0.0036	0.0001	-35.222	0.0000	-0.0038	-0.0034
CMA	0.0022	0.0002	14.439	0.0000	0.0019	0.0025

11.4.2 Mean Square Error (Tensorflow)

University of Auckland

Dep. Var	riable:	predict		R-s	squared:		4.125e-05
Estimato	or:	PooledOLS		R-s	squared (H	Between):	-0.0132
No. Obse	ervations:	531461		R-s	squared (V	Vithin):	-0.0002
Date:	F.	Γue, Jan 11 20)22	R-s	squared (C	Overall):	4.125 e-05
Time:		08:58:34		Log	g-likelihoo	d	1.669e + 05
Cov. Est	imator:	Robust					
				F-s	tatistic:		21.921
Entities:		7282		P-v	alue		0.0000
Avg Obs	:	72.983		Distribution:		F(1,531459)	
Min Obs	:	1.0000					
Max Obs	s :	252.00		F-s	tatistic (r	obust):	17.988
				P-v	alue		0.0000
Time per	riods:	252		Distribution:			F(1,531459)
Avg Obs	:	2109.0					
Min Obs	:	1869.0					
Max Obs	s :	3400.0					
	Parameter	Std. Err.	T-st	tat	P-value	Lower CI	Upper CI
const	0.0297	0.0002	121.	.47	0.0000	0.0292	0.0302
Mkt-RF	0.0002	5.776e-05	4.24	112	0.0000	0.0001	0.0004

Dep. Variable:	$\operatorname{predict}$	R-squared:	0.0025
Estimator:	PooledOLS	R-squared (Between):	-0.0054
No. Observations:	531461	R-squared (Within):	0.0012
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0025
Time:	08:58:35	Log-likelihood	1.676e + 05
Cov. Estimator:	Robust		
		F-statistic:	446.89
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(3,531457
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	415.95
		P-value	0.0000
Time periods:	252	Distribution:	F(3,531457
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0304	0.0002	123.07	0.0000	0.0299	0.0309
Mkt-RF	0.0004	5.859e-05	7.1392	0.0000	0.0003	0.0005
SMB	-0.0013	6.84 e- 05	-18.769	0.0000	-0.0014	-0.0011
HML	-0.0023	7.143e-05	-32.227	0.0000	-0.0024	-0.0022

Dep. Variable:	$\operatorname{predict}$	R-squared:	0.0026
Estimator:	PooledOLS	R-squared (Between):	-0.0049
No. Observations:	531461	R-squared (Within):	0.0014
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0026
Time:	08:58:36	Log-likelihood	1.676e + 05
Cov. Estimator:	Robust		
		F-statistic:	342.47
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(4,531456
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	312.26
		P-value	0.0000
Time periods:	252	Distribution:	F(4,531456
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0300	0.0003	119.12	0.0000	0.0295	0.0305
Mkt-RF	0.0005	6.484 e- 05	8.1115	0.0000	0.0004	0.0007
SMB	-0.0010	8.513e-05	-12.028	0.0000	-0.0012	-0.0009
HML	-0.0026	8.929 e-05	-28.599	0.0000	-0.0027	-0.0024
$\mathbf{R}\mathbf{M}\mathbf{W}$	0.0006	0.0001	5.4812	0.0000	0.0004	0.0008

Dep. Variable:	predict	R-squared:	0.0027
Estimator:	PooledOLS	R-squared (Between):	-0.0036
No. Observations:	531461	R-squared (Within):	0.0013
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0027
Time:	08:58:37	Log-likelihood	1.676e + 05
Cov. Estimator:	Robust		
		F-statistic:	285.26
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	284.89
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0304	0.0003	117.58	0.0000	0.0299	0.0309
Mkt-RF	0.0004	6.989 e-05	5.1521	0.0000	0.0002	0.0005
SMB	-0.0009	8.628 e - 05	-10.985	0.0000	-0.0011	-0.0008
\mathbf{HML}	-0.0021	0.0001	-18.879	0.0000	-0.0023	-0.0019
$\mathbf{R}\mathbf{M}\mathbf{W}$	0.0005	0.0001	4.8979	0.0000	0.0003	0.0008
CMA	-0.0012	0.0001	-7.7008	0.0000	-0.0014	-0.0009

11.4.3 Mean Square Error

Dep. Var	riable:	predict	F	R-squared:		6.43 e-05
Estimato	r:	PooledOLS	F	R-squared (I	Between):	-0.0089
No. Obse	ervations:	531461	F	R-squared (V	Within):	-0.0001
Date:		Γue, Jan 11 20)22 F	R-squared (Overall):	6.43 e-05
Time:		08:58:40	I	og-likelihoo	\mathbf{d}	2.055e + 05
Cov. Est	imator:	Robust				
			F	'-statistic:		34.175
Entities:		7282	F	-value		0.0000
Avg Obs	:	72.983	Ι	Distribution:		F(1,531459)
Min Obs	:	1.0000				
Max Obs	3 :	252.00	F	F-statistic (robust):		28.730
			F	-value		0.0000
Time per	riods:	252	Ι	Distribution	:	F(1,531459)
Avg Obs	:	2109.0				
Min Obs	:	1869.0				
Max Obs	s :	3400.0				
	Parameter	Std. Err.	T-sta	t P-value	Lower CI	Upper CI
const	0.0214	0.0002	93.984	0.0000	0.0210	0.0219
Mkt-RF	0.0003	5.307e-05	5.3600	0.0000	0.0002	0.0004

Dep. Variable:	predict	R-squared:	0.0017
Estimator:	PooledOLS	R-squared (Between):	-0.0045
No. Observations:	531461	R-squared (Within):	0.0011
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0017
Time:	08:58:41	Log-likelihood	2.06e + 05
Cov. Estimator:	Robust		
		F-statistic:	308.29
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(3,531457)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	297.07
		P-value	0.0000
Time periods:	252	Distribution:	F(3,531457)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0219	0.0002	95.496	0.0000	0.0215	0.0224
Mkt-RF	0.0004	5.4e-05	7.7053	0.0000	0.0003	0.0005
SMB	-0.0010	6.218 e-05	-15.717	0.0000	-0.0011	-0.0009
\mathbf{HML}	-0.0018	6.507e-05	-27.074	0.0000	-0.0019	-0.0016

Dep. Variable:	predict	R-squared:	0.0018
Estimator:	PooledOLS	R-squared (Between):	-0.0043
No. Observations:	531461	R-squared (Within):	0.0012
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0018
Time:	08:58:42	$\operatorname{Log-likelihood}$	2.06e + 05
Cov. Estimator:	Robust		
		F-statistic:	234.78
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(4,531456)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	222.75
		P-value	0.0000
Time periods:	252	Distribution:	F(4,531456)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
\mathbf{const}	0.0217	0.0002	92.559	0.0000	0.0212	0.0222
Mkt-RF	0.0005	5.902 e-05	8.2365	0.0000	0.0004	0.0006
SMB	-0.0008	7.861e-05	-10.281	0.0000	-0.0010	-0.0007
HML	-0.0019	8.234 e - 05	-23.385	0.0000	-0.0021	-0.0018
$\mathbf{R}\mathbf{M}\mathbf{W}$	0.0004	0.0001	3.8405	0.0001	0.0002	0.0006

Dep. Variable:	predict	R-squared:	0.0018
Estimator:	PooledOLS	R-squared (Between):	-0.0037
No. Observations:	531461	R-squared (Within):	0.0011
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0018
Time:	08:58:43	$\operatorname{Log-likelihood}$	2.06e + 05
Cov. Estimator:	Robust		
		F-statistic:	192.28
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	195.66
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	0.0219	0.0002	90.855	0.0000	0.0214	0.0224
Mkt-RF	0.0004	6.376 e - 05	6.1033	0.0000	0.0003	0.0005
SMB	-0.0008	7.971e-05	-9.5798	0.0000	-0.0009	-0.0006
\mathbf{HML}	-0.0017	0.0001	-16.147	0.0000	-0.0019	-0.0015
$\mathbf{R}\mathbf{M}\mathbf{W}$	0.0004	0.0001	3.4742	0.0005	0.0002	0.0006
CMA	-0.0007	0.0001	-4.8160	0.0000	-0.0009	-0.0004

11.4.4 Hedge Portfolio

Dep. Var	iable:	predict	R-8	squared:		0.0001
Estimato	r :	PooledOLS	R-s	squared (H	Between):	-0.0012
No. Obse	ervations:	531461	R-9	squared (V	Vithin):	-8.467e-05
Date:	,	Γue, Jan 11 20)22 R -s	squared (C	Overall):	0.0001
Time:		08:59:03	Log	g-likelihoo	\mathbf{d}	8.196e + 05
Cov. Esti	imator:	Robust				
			F-s	tatistic:		58.421
Entities:		7282	P-v	alue	0.0000	
Avg Obs:		72.983	Dis	stribution:	F(1,531459)	
Min Obs:		1.0000				
Max Obs	ax Obs: 252		F-s	tatistic (r	46.726	
			P-v	alue		0.0000
Time per	iods:	252	Dis	Distribution:		F(1,531459)
Avg Obs:		2109.0				
Min Obs:		1869.0				
Max Obs	:	3400.0				
	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	-0.0001	7.083e-05	-1.4700	0.1416	-0.0002	3.471e-05
Mkt-RF	0.0001	1.713e-05	6.8356	0.0000	8.354e-05	0.0002

Dep. Variable:	predict	R-squared:	0.0010
Estimator:	PooledOLS	R-squared (Between):	0.0004
No. Observations:	531461	R-squared (Within):	0.0001
Date:	Tue, Jan 11 2022	2 R-squared (Overall):	0.0010
Time:	08:59:04	Log-likelihood	8.198e + 05
Cov. Estimator:	Robust		
		F-statistic:	176.39
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(3,531457)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	167.12
		P-value	0.0000
Time periods:	252	Distribution:	F(3,531457)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
Paramete	r Std. Err.	Γ-stat P-value Lower C	I Upper CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	9.651e-06	7.199e-05	0.1341	0.8934	-0.0001	0.0002
Mkt-RF	0.0001	1.72 e-05	8.5634	0.0000	0.0001	0.0002
\mathbf{SMB}	-0.0002	2.031e-05	-11.030	0.0000	-0.0003	-0.0002
\mathbf{HML}	-0.0004	2.141e-05	-18.841	0.0000	-0.0004	-0.0004

Mkt-RF

 \mathbf{SMB}

 \mathbf{HML}

 $\mathbf{R}\mathbf{M}\mathbf{W}$

0.0002

-0.0002

-0.0004

7.986e-05

Dep. Va	riable:	predict	R-9	squared:		0.0010
Estimate	or:	PooledOLS	R-s	R-squared (Between):		0.0006
No. Obs	ervations:	531461	R-5	squared (V	Vithin):	0.0001
Date:	- -	Γue, Jan 11 20)22 R- s	squared (C	Overall):	0.0010
Time:		08:59:05	\mathbf{Lo}_{2}	g-likelihoo	\mathbf{d}	8.198e + 05
Cov. Est	imator:	Robust				
			F-s	statistic:		133.80
Entities:		7282	P	value		0.0000
Avg Obs	:	72.983	Dis	stribution:		F(4,531456)
Min Obs	:	1.0000				
Max Ob	s:	252.00	F-s	statistic (r	obust):	129.24
			P-1	value		0.0000
Time pe	riods:	252	Dis	stribution:		F(4,531456)
Avg Obs	::	2109.0				
Min Obs	:	1869.0				
Max Ob	s :	3400.0				
	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	-3.686e-05	7.419e-05	-0.4968	0.6193	-0.0002	0.0001

8.0783

-7.5228

-16.363

2.4627

2.001e-05 2.518e-05

 $2.67\mathrm{e}\text{-}05$

 $3.243\mathrm{e}\text{-}05$

0.0000

0.0000

0.0000

0.0138

0.0001

-0.0002

-0.0005

 $1.63\mathrm{e}\text{-}05$

0.0002

-0.0001

-0.0004

0.0001

Dep. Variable:	predict	R-squared:	0.0011
Estimator:	PooledOLS	R-squared (Between):	0.0007
No. Observations:	531461	R-squared (Within):	0.0002
Date:	Tue, Jan 11 20	22 R-squared (Overall):	0.0011
Time:	08:59:06	Log-likelihood	8.199e + 05
Cov. Estimator:	Robust		
		F-statistic:	113.57
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	133.90
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
Paramete	r Std. Err.	T-stat P-value Lower Cl	Upper CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	4.601 e-05	7.61e-05	0.6046	0.5454	-0.0001	0.0002
Mkt-RF	0.0001	2.208 e - 05	5.6471	0.0000	8.14e-05	0.0002
SMB	-0.0002	2.569 e - 05	-6.7134	0.0000	-0.0002	-0.0001
HML	-0.0003	3.493 e - 05	-9.7189	0.0000	-0.0004	-0.0003
$\mathbf{R}\mathbf{M}\mathbf{W}$	6.67 e-05	3.287 e - 05	2.0290	0.0425	2.27e-06	0.0001
CMA	-0.0003	4.498e-05	-5.7222	0.0000	-0.0003	-0.0002

11.4.5 Sharpe Ratio

Dep. Va	riable:	predict		R-s	squared:		0.0005
Estimate	or:	PooledOLS		R-s	squared (H	Between):	-0.0182
No. Obs	ervations:	531461		R-s	squared (V	Vithin):	0.0022
Date:	ŗ	Tue, Jan 11 20)22	R-s	squared (C	Overall):	0.0005
Time:		08:58:46		Log	g-likelihoo	d	-4.309e+06
Cov. Est	imator:	Robust					
				F-s	tatistic:		251.19
Entities:		7282		P-v	alue		0.0000
Avg Obs	: :	72.983		Distribution:			F(1,531459)
Min Obs	:	1.0000					
Max Ob	s:	252.00		F-statistic (robust):			224.05
				P-value			0.0000
Time pe	riods:	252		Distribution:			F(1,531459)
Avg Obs	: :	2109.0					
Min Obs	::	1869.0					
Max Ob	s:	3400.0					
	Parameter	Std. Err.	T-st	tat	P-value	Lower CI	Upper CI
const	515.46	1.1181	461.	.03	0.0000	513.26	517.65
Mkt-RF	3.7710	0.2519	14.9	068	0.0000	3.2773	4.2648

Dep. Variable:	predict	R-squared:	0.0009
Estimator:	PooledOLS	R-squared (Between):	-0.0157
No. Observations:	531461	R-squared (Within):	0.0026
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0009
Time:	08:58:47	Log-likelihood	-4.309e+06
Cov. Estimator:	Robust		
		F-statistic:	165.26
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(3,531457)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	153.89
		P-value	0.0000
Time periods:	252	Distribution:	F(3,531457)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	513.97	1.1160	460.56	0.0000	511.78	516.15
Mkt-RF	2.9933	0.2597	11.528	0.0000	2.4844	3.5023
SMB	4.4845	0.3187	14.072	0.0000	3.8599	5.1090
\mathbf{HML}	2.8799	0.3230	8.9149	0.0000	2.2467	3.5131

Dep. Variable:	predict	R-squared:	0.0011
Estimator:	PooledOLS	R-squared (Between):	-0.0164
No. Observations:	531461	R-squared (Within):	0.0030
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0011
Time:	08:58:48	Log-likelihood	-4.309e+06
Cov. Estimator:	Robust		
		F-statistic:	140.23
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(4,531456)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	131.53
		P-value	0.0000
Time periods:	252	Distribution:	F(4,531456)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	511.59	1.1429	447.61	0.0000	509.35	513.83
Mkt-RF	3.7253	0.2698	13.809	0.0000	3.1966	4.2541
SMB	6.2516	0.4032	15.505	0.0000	5.4614	7.0418
HML	1.1687	0.3995	2.9256	0.0034	0.3857	1.9517
$\mathbf{R}\mathbf{M}\mathbf{W}$	4.0757	0.5158	7.9025	0.0000	3.0649	5.0866

Dep. Variable:	predict	R-squared:	0.0014
Estimator:	PooledOLS	R-squared (Between):	-0.0147
No. Observations:	531461	R-squared (Within):	0.0036
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0014
Time:	08:58:49	Log-likelihood	-4.309e+06
Cov. Estimator:	Robust		
		F-statistic:	151.56
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	147.55
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
D	C4-1 Ti TI.	-t-t Dl I C	I II CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	508.43	1.1759	432.38	0.0000	506.13	510.74
Mkt-RF	5.1358	0.2896	17.731	0.0000	4.5681	5.7035
SMB	5.6035	0.4077	13.744	0.0000	4.8044	6.4026
\mathbf{HML}	-2.5464	0.4888	-5.2093	0.0000	-3.5045	-1.5884
$\mathbf{R}\mathbf{M}\mathbf{W}$	4.5776	0.5163	8.8654	0.0000	3.5656	5.5896
CMA	9.8143	0.7153	13.721	0.0000	8.4124	11.216

11.4.6 Sharpe Ratio (MSE)

Dep. Va	riable:	predict		R-squared:		0.0012
Estimato	or:	PooledOLS]	R-squared (Between):		-3.227e-05
No. Obs	ervations:	531461]	R-squared (Within):	0.0036
Date:		Γue, Jan 11 20	022	R-squared (Overall):	0.0012
Time:		08:58:51]	Log-likelihoo	od	-4.012e+06
Cov. Est	imator:	Robust				
]	F-statistic:		615.62
Entities:		7282]	P-value		0.0000
Avg Obs	:	72.983]	Distribution:		F(1,531459)
Min Obs	:	1.0000				
Max Obs	5:	252.00]	F-statistic (1	robust):	546.40
]	P-value		0.0000
Time per	riods:	252]	Distribution	:	F(1,531459)
Avg Obs	:	2109.0				
Min Obs	:	1869.0				
Max Obs	5:	3400.0				
	Parameter	Std. Err.	T-sta	at P-value	Lower CI	Upper CI
const	-2.0195	0.6382	-3.164	16 0.0016	-3.2703	-0.7687
Mkt-RF	3.3761	0.1444	23.37	5 0.0000	3.0930	3.6592

Dep. Variable:	predict	R-squared:	0.0021
Estimator:	PooledOLS	R-squared (Between):	-0.0008
No. Observations:	531461	R-squared (Within):	0.0062
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0021
Time:	08:58:52	Log-likelihood	-4.012e+06
Cov. Estimator:	Robust		
		F-statistic:	371.06
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(3,531457)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	347.27
		P-value	0.0000
Time periods:	252	Distribution:	F(3,531457)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	-3.2212	0.6373	-5.0544	0.0000	-4.4702	-1.9721
Mkt-RF	2.6580	0.1490	17.844	0.0000	2.3660	2.9499
SMB	3.9864	0.1869	21.333	0.0000	3.6201	4.3526
HML	1.7573	0.1883	9.3333	0.0000	1.3883	2.1264

Dep. Variable:	predict	R-squared:	0.0021
Estimator:	PooledOLS	R-squared (Between):	-0.0009
No. Observations:	531461	R-squared (Within):	0.0063
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0021
Time:	08:58:54	Log-likelihood	-4.012e+06
Cov. Estimator:	Robust		
		F-statistic:	281.52
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(4,531456)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	263.88
		P-value	0.0000
Time periods:	252	Distribution:	F(4,531456)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	-2.6172	0.6523	-4.0123	0.0001	-3.8957	-1.3387
Mkt-RF	2.4717	0.1559	15.856	0.0000	2.1662	2.7772
SMB	3.5368	0.2331	15.169	0.0000	3.0798	3.9937
HML	2.1927	0.2301	9.5277	0.0000	1.7416	2.6438
$\mathbf{R}\mathbf{M}\mathbf{W}$	-1.0370	0.2967	-3.4951	0.0005	-1.6185	-0.4555

Dep. Variable:	predict	R-squared:	0.0024
Estimator:	PooledOLS	R-squared (Between):	-0.0015
No. Observations:	531461	R-squared (Within):	0.0070
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0024
Time:	08:58:55	Log-likelihood	-4.012e+06
Cov. Estimator:	Robust		
		F-statistic:	251.06
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	240.31
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
Paramete	or Std Err T-	stat P-value Lower C	I Upper CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	-4.0803	0.6692	-6.0970	0.0000	-5.3920	-2.7686
Mkt-RF	3.1248	0.1671	18.699	0.0000	2.7972	3.4523
SMB	3.2367	0.2354	13.750	0.0000	2.7753	3.6980
HML	0.4725	0.2805	1.6844	0.0921	-0.0773	1.0224
$\mathbf{R}\mathbf{M}\mathbf{W}$	-0.8046	0.2974	-2.7058	0.0068	-1.3874	-0.2218
CMA	4.5442	0.4090	11.109	0.0000	3.7425	5.3459

 ${\bf Connor\ McDowall}$

11.4.7 Information Ratio

Mkt-RF

0.0537

0.0051

Dep. Variable:	predict	R-squared:		0.0003
Estimator:	PooledOLS	R-squared	(Between):	-0.0262
No. Observations:	531461	R-squared	(Within):	0.0003
Date:	Tue, Jan 11 202	2 R-squared	(Overall):	0.0003
Time:	08:58:57	Log-likelih	boo	-2.199e+06
Cov. Estimator:	Robust			
		F-statistic:		143.01
Entities:	7282	P-value		0.0000
Avg Obs:	72.983	Distributio	n:	F(1,531459)
Min Obs:	1.0000			
Max Obs:	252.00	F-statistic	(robust):	112.22
		P-value		0.0000
Time periods:	252	Distributio	n:	F(1,531459)
Avg Obs:	2109.0			
Min Obs:	1869.0			
Max Obs:	3400.0			
Paramet	er Std. Err.	T-stat P-valu	e Lower CI	Upper CI
const 12.010	0.0208	578.36 0.0000	11.969	12.050

10.593

0.0000

0.0438

0.0636

Dep. Variable:	predict	R-squared:	0.0029
Estimator:	PooledOLS	R-squared (Between):	-0.0261
No. Observations:	531461	R-squared (Within):	0.0065
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0029
Time:	08:58:58	Log-likelihood	-2.199e+06
Cov. Estimator:	Robust		
		F-statistic:	520.75
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(3,531457)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	506.96
		P-value	0.0000
Time periods:	252	Distribution:	F(3,531457)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	12.069	0.0211	572.27	0.0000	12.028	12.111
Mkt-RF	0.0714	0.0051	14.048	0.0000	0.0615	0.0814
SMB	-0.1252	0.0061	-20.526	0.0000	-0.1371	-0.1132
HML	-0.1996	0.0063	-31.919	0.0000	-0.2119	-0.1873

Dep. Variable:	predict	R-squared:	0.0030
Estimator:	PooledOLS	R-squared (Between):	-0.0257
No. Observations:	531461	R-squared (Within):	0.0068
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0030
Time:	08:58:59	Log-likelihood	-2.199e+06
Cov. Estimator:	Robust		
		F-statistic:	400.77
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(4,531456)
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	381.25
		P-value	0.0000
Time periods:	252	Distribution:	F(4,531456)
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		
Danamata	on Std Enn T	stat Duralus Lawar C	I Upper CI

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	12.034	0.0218	553.25	0.0000	11.991	12.077
Mkt-RF	0.0824	0.0058	14.096	0.0000	0.0709	0.0938
SMB	-0.0988	0.0074	-13.351	0.0000	-0.1134	-0.0843
HML	-0.2251	0.0077	-29.230	0.0000	-0.2402	-0.2100
$\mathbf{R}\mathbf{M}\mathbf{W}$	0.0608	0.0095	6.3937	0.0000	0.0421	0.0794

Dep. Variable:	predict	R-squared:	0.0031
Estimator:	PooledOLS	R-squared (Between):	-0.0253
No. Observations:	531461	R-squared (Within):	0.0069
Date:	Tue, Jan 11 2022	R-squared (Overall):	0.0031
Time:	08:59:01	Log-likelihood	-2.199e+06
Cov. Estimator:	Robust		
		F-statistic:	327.62
Entities:	7282	P-value	0.0000
Avg Obs:	72.983	Distribution:	F(5,531455
Min Obs:	1.0000		
Max Obs:	252.00	F-statistic (robust):	354.15
		P-value	0.0000
Time periods:	252	Distribution:	F(5,531455
Avg Obs:	2109.0		
Min Obs:	1869.0		
Max Obs:	3400.0		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
const	12.059	0.0221	544.73	0.0000	12.016	12.103
Mkt-RF	0.0711	0.0063	11.378	0.0000	0.0589	0.0834
SMB	-0.0937	0.0075	-12.426	0.0000	-0.1085	-0.0789
HML	-0.1956	0.0099	-19.690	0.0000	-0.2151	-0.1761
$\mathbf{R}\mathbf{M}\mathbf{W}$	0.0568	0.0096	5.9294	0.0000	0.0380	0.0756
CMA	-0.0780	0.0130	-6.0181	0.0000	-0.1034	-0.0526

12 Discussion

13 Contributions

14 Conclusion

15 Appendix

15.1 Ordinary Least Squares (OLS)

The OLS regression is the most prominent statistical model in asset pricing theory. Rosenfeld (2021) summarises OLS. The composition of the true OLS (27) model includes four components. Firstly, \mathbf{X} , an n x k matrix of k independent variables for n observations. Secondly, \mathbf{y} , an n x 1 vector of observation on the dependent variable. Thirdly, ϵ , an n x 1 vector of unexplained error. Lastly, θ , a k x 1 vector of parameters to be estimated.

$$y = X\theta + \epsilon \tag{27}$$

15.1.1 Estimation Criteria

The criteria to obtain the parameter estimate $(\hat{\theta})$ relies on the minimisation of the sum of squared residuals (28). We highlight the observed residuals (e) are distinct from unexplained disturbances (ϵ) . Equation 29 derives residuals by taking the difference between observations based on parameter estimates.

$$\sum e_i^2 \tag{28}$$

$$e = y - X\hat{\theta} \tag{29}$$

Expanding the quadratic $e^T e$ after substituting in equation 29 leads to the alternative expression of the sum of squared residuals in equation 30. Minimizing the sum of square residuals requires taking the partial derivative of equation 30 with respect to the estimated parameters (equation) using matrix differentiation (31). It is imperative X has full rank where all vectors in the matrix are linearly independent, validating both the presence of a positive definite matrix and minimum.

$$e^T e = y^T y - 2\hat{\theta}^T X^T y + \hat{\theta}^T X^T \hat{\theta} X \tag{30}$$

$$\frac{\partial e^T e}{\partial \hat{\theta}} = -2X^T y + 2X^T X \hat{\theta} = 0 \tag{31}$$

We find the expression for the Ordinary Least Squares (OLS) estimator (32) after rearranging equation 31 to normal form, utilizing inverse matrices to form identity matrices, and simplifying.

$$2X^{T}X\hat{\theta} = 2X^{T}y$$

$$(X^{T}X)^{-1}(X^{T}X)\hat{\theta} = (X^{T}X)^{-1}X^{T}y$$

$$I\hat{\theta} = (X^{T}X)^{-1}X^{T}y$$

$$\hat{\theta} = (X^{T}X)^{-1}(X^{T}y)$$
(32)

Therefore, we can use the OLS estimator to make predictions with OLS (33).

$$\hat{y} = X^T \hat{\theta} \tag{33}$$

15.1.2 Properties of OLS Estimators

There are six key properties in addition to the satisfaction in minimizing the summation of squared residuals.

- 1. The residuals are uncorrelated with the observed values of X i.e., $X^T e = 0$.
- 2. The sum of the residuals is zero i.e., $\sum e_i = 0$.
- 3. The sample mean of the residuals is zero i.e., $\bar{e} = \frac{\sum e_i}{n} = 0$.
- 4. The regression hyperplane passes through the means of observed values i.e., $\frac{e}{=} \frac{y X\theta}{n} = 0$. Since $\bar{e} = 0$ assumed, it is implied $\bar{y} = \bar{x}\bar{\theta}$.
- 5. The residuals are uncorrelated with the predicted y i.e., $\hat{y} = X\hat{\theta}$, $\hat{y}^T e = (X\hat{\beta})^T e = b^T X^T e = 0$
- 6. The mean of \hat{y} for the sample will equal the mean of the y.

15.1.3 The Gauss-Markov Theorem

However, OLS makes Gauss-Markov assumptions about the true model to make inferences regarding β from $\hat{\beta}$. The intention of the Gauss-Markov Theorem, conditional on the below assumptions, states the

OLS estimator is the best linear, unbiased, and efficient estimator:

$$y = x\beta + \epsilon$$

$$E[\epsilon|X] = 0 \tag{34}$$

$$E(\epsilon \epsilon^T | X) = \Omega = \sigma^2 I \tag{35}$$

 $\epsilon |X| N[0, \sigma^T I]$ (hypothesis testing)

- X is an n x k matrix of full rank
- X must be generated randomly, or fixed, by a mechanism uncorrelated to disturbances.

Equation 34 implies $E(y) = X\beta$ as no observations of the independent variables convey any information about the expected values of the disturbances. Equation 35 captures homoskedasticity and no autocorrelation assumptions.

15.2 Technical Details

15.2.1 Organisation

This research essay uses data science best practise (Wilson et al., 2016). Data and results saved regularly and reproducible. Data retention in all forms receives high levels of attention. Project files synchonises continuously to Google Drive (Google LLC, 2020). Git (Linus Torvalds, 2020) manages version control protocols for source code, data, documents, and results. Git stores a complete history of versions using Git hashes. These hashes are strings unique to each state of the publicly available finance-honours repository¹. Git hashes enable discretisation of finance-honours development, enabling the accessibility and recollection of all previous states given a unique git hash. This functionality enables reproducibility, error correction, and the ability to revert to previous models.

15.2.2 Version Control

Git, hosted by GitHub, provides a comprehensive set of version control technologies and range of benefits. Firstly, Git enables collaborative functionalities. The master version of a project is accessible for all who have access to the repository. Each contributor can create custom copies of branches through pull requests on the master branch. Contributors can commit changes to custom branches and push these changes to the master branch through push requests. Product managers can review push requests, approving valid requests for integrating changes to the master branch. Collaborative efforts are possible with commit messages describing contributions from each contributor. This research essay has only one contributor,

¹https://github.com/CMCD1996/finance-honours

rendering collaborative functionalities redundant in this instance. Git ensures the storage of code, work, and author histories. The descriptive nature of commit logs ensures journal accuracy.

15.2.3 Directories

This research essay follows directory structure recommendations from Wilson et al (2016). Organisation is crucial as the modelling of artificial neural networks involves integrating a range of optimisation models, data files and documents. Directory management is most efficient and comprehensive. **finance-honours** is the root directory containing the following sub directories: bin, data, doc, src, and results. The **bin** sub directory contains external scripts and compiled programmes. The **data** sub directory contains all raw data associated with the project. The **doc** sub directory stores user guides, academic resources, research reports and project deliverables. The **results** sub directory contains the outputs from project analysis. The **src** sub directory stores the source code for preparing datasets, partitioning sets of geographies with varying granularities. All files were continuously backed up using Google Drive and Git.

15.2.4 Python

Python 3.9.7 is the primary programming language for this research essay. The language is omnipresent, widespread in software development. Python's language design makes the language highly productive and simple to use. Python can hand off computationally straining tasks to C/C++ using supporting first-class integration capabilities. The language also has a very active and supportive community. Python is the most popular coding language on the planet defined by the PYPL PopularitY of Programming Language Index. As at December 2021, Python has 30.21% of all language tutorial search instances on Google (PYPL, 2021). Python's dynamic, low cost, and open source nature makes programming quick.

15.2.5 Package Management

The Anaconda package management platform for Python (Anaconda, Inc., 2020) is the chosen coding environment. Anaconda is a well defined, free platform, with known versions of python packages such as matplotlib, numpy, and pip. The use of this environment ensures reproducibility and consistency across infrastructure. Pip is the default package manager for Python, included in the Anaconda package. Pip manages package installation and updates.

15.2.6 Code Style

The PEP8 style for Python Code is formatting style for development code Guido Van Rossum and Coghlan, 2001. Yapf, a formatter maintained by Google, manages formatting. Standardised formatting is important as makes supports readability, optimisation, and consistency. Docstrings and rigourous

commenting are important in documentation. A docstring is a Python inline comment describing function use, inputs, and outputs. An unique docstring belongs to each Python class and function. The Google style docstring is most appropriate because of it's readability, writing ease, and consistency with Google's Style Guide. The parsing of yapf docstrings enables automated documentation generators to create docstring documents describing functions and classes.

15.2.7 Infrastructure

This research essay deploys variations in artificial neural networks of changing size and complexity. Analysis either took place locally, or remotely, depending on the computational requirements for the particular analysis. An Apple MacBook Pro 13 Inch 2019 with 8 GB 2133 MHz LPDDR3 memory and 1.4 GHz Quad-Core Intel Core i5 processor handles simple tasks locally. A Virtual Machine Instance on the Google Cloud Platform Insert specification before submission handles complex tasks remotely.

15.2.8 Documentation

The research essay documentation keeps an accurate record of key design decisions. Commit histories (15.2.2) is the most important form of documentation. Application of auxiliary documentation methods are supplementary.

15.3 Dataset Summary Statistics

	count	mean	$ \operatorname{std} $	mim_	25%	20%	15%	max
permno	2739928.0	5.405281e+04	5.405281e+04 2.782267e+04	10000.0000	2.651800e + 04	5.715400e+04	5.715400e + 04 8.018600e + 04 9.343600e + 04	9.343600e+04
permco	2739928.0	\dashv	843974e+04 1.402881e+04	3.0000	7.702000e+03	1.640850e+04	1.640850e + 04 2.321000e + 04 5.766700e + 04	5.766700e+04
crsp_shrcd	2739928.0	1.089520e+01	4.571000e-01	10.0000	1.100000e+01	1.100000e+01	1.100000e+01 $1.100000e+01$ $1.200000e+01$	1.200000e+01
crsp-exchcd	2739928.0	2.127400e+00	9.343000e-01	1.0000	1.000000e+00	3.000000e+00	3.000000e+00 $3.000000e+00$ $3.000000e+00$	3.0000000e+00
sic	2692217.0	4.605936e+03 $1.921398e+03$	1.921398e+03	100.0000	3.271000e+03	4.011000e+03	4.011000e + 03 6.036000e + 03 9.999000e + 03	9.999000e+03
ff49	2674304.0	$3.037380e+01 \left 1.341740e+01 \right $	1.341740e+01	1.0000	1.800000e+01	3.400000e+01	3.400000e+01 $4.300000e+01$ $4.900000e+01$	4.900000e+01
adjfct	2739928.0	2.838700e+00	1.267170e+01	0.0000	1.000000e+00	1.000000e+00	1.000000e+00	1.215000e+03
shares	2739928.0	6.078630e + 01	2.852566e + 02	0.0830	4.399000e+00	1.251900e+01	3.808200e+01 2.920640e+04	2.920640e+04
me	2739928.0	2.241254e+03	1.473073e+04	1.1708	4.367020e+01	1.565628e + 02	$1.565628e+02 \left 7.167608e+02 \right 2.255969e+06$	2.255969e + 06
me_company	2739928.0	2.283180e + 03 $1.527340e + 04$	1.527340e+04	1.1708	4.387450e+01	1.574086e+02	7.211363e+02	2.255969e + 06
prc	2739928.0	2.876220e+01	6.488772e+02	0.0078	7.875000e+00	1.612500e+01	2.912500e+01 1.416000e+05	1.416000e+05
prc_local	2739928.0	2.876220e+01	6.488772e + 02	0.0078	7.875000e+00	1.612500e+01	$1.612500e + 01 \boxed{2.912500e + 01} \boxed{1.416000e + 05}$	1.416000e+05
dolvol	2580622.0	3.282292e+08 $2.520900e+09$	2.520900e+09	0.0000	1.070786e + 06	7.165154e+06	$7.165154e+06 \left 7.076108e+07 \right 8.441730e+11$	8.441730e+11
ret	2719460.0	1.640000e-02	1.672000e-01	-1.0000	-5.880000e-02	4.100000e-03		7.410000e-02 2.400000e+01
ret_local	2719460.0	1.640000e-02	1.672000e-01	-1.0000	-5.880000e-02	4.100000e-03	7.410000e-02	7.410000e-02 2.400000e+01
ret_exc	2719460.0	1.270000e-02	1.673000e-01	-1.0068	-6.250000e-02	7.000000e-04		7.060000e-02 2.399690e+01
ret_lag_dif	2739928.0	1.000000e+00 0.000000e+00	0.0000000e+00	1.0000	1.000000e+00	1.000000e+00	1.000000e+00 $1.000000e+00$ $1.000000e+00$	1.0000000e+00
ret_exc_lead1m	2732542.0	6.400000e-03	1.559000e-01	-1.0113	-6.560000e-02	-1.800000e-03		6.710000e-02 1.988170e+01
market_equity_rank_x	2739928.0	5.982920e+01 2.380660e+01	2.380660e+01	1.0000	4.000000e+01	6.000000e+01	$6.000000e+01 \boxed{8.000000e+01} \boxed{9.950000e+01}$	9.950000e+01
enterprise_value_rank_x 2480615.0 5.	2480615.0	5.845440e+01	845440e+01 2.501660e+01	1.0000	1.0000 $3.800000e+01$		$5.900000e + 01 \left 8.0000000e + 01 \right 9.950000e + 01$	9.950000e+01

	count	mean	std	mim	25%	20%	25%	max
book_equity_rank_x	2452453.0	5.800700e+01	2.593820e+01	1.0000	3.800000e+01	5.900000e+01	5.900000e+01 8.000000e+01 $ 9.950000e+01$	9.950000e+01
assets_rank_x	2522907.0	$5.751850e + 01 \boxed{2.635510e + 01}$	2.635510e + 01	1.0000	3.700000e+01	5.900000e+01	$5.900000e+01 \boxed{8.000000e+01} \boxed{9.950000e+01}$	9.950000e+01
sales_rank_x	2509790.0	5.691950e+01	2.717080e+01	1.0000	3.600000e+01	5.900000e+01	5.900000e+01 8.000000e+01 9.950000e+01	9.950000e+01
net_income_rank_x	2517298.0	5.581200e+01	2.878360e+01	1.0000	3.300000e+01	6.000000e+01	$6.000000e+01 \boxed{8.000000e+01} \boxed{9.950000e+01}$	9.950000e+01
bidask_x	2739928.0	1.289000e-01	3.351000e-01	0.0000	0.000000e+00		0.000000e+00	1.000000e+00
prc_high_x	2355383.0	2.540480e+01	2.608370e + 01	0.1790	9.250000e+00	1.850000e+01	$1.850000e+01 \boxed{3.300000e+01} \boxed{4.617600e+02}$	4.617600e+02
prc_low_x	2365005.0	2.211970e+01 $2.325750e+01$	2.325750e+01	0.0818	7.640000e+00	1.600000e+01	$1.600000e+01 \boxed{2.880000e+01} \boxed{4.175300e+02}$	4.175300e+02
tvol_x	2580622.0	8.316484e+06 $2.941295e+07$	2.941295e+07	0.0000	9.875000e+04	5.510000e+05	$5.510000e + 05 \boxed{3.923700e + 06} \boxed{6.485186e + 08}$	6.485186e+08
div1m_me_x	2718102.0	1.30000e-03	3.700000e-03	0.0000	0.0000000e+00	0.000000e+00	0.000000e+00 0.000000e+00	9.010000e-02
div3m_me_x	2718121.0	4.000000e-03	6.000000e-03	0.0000	0.0000000e+00	0.0000000e+00	6.700000e-03	1.164000e-01
div6m_me_x	2660395.0	8.100000e-03	1.170000e-02	0.0000	0.0000000e+00	0.0000000e+00	1.360000e-02	1.472000e-01
div12m_me_x	2548844.0	1.670000e-02	2.350000e-02	0.0000	0.0000000e+00	3.800000e-03	2.780000e-02	4.015000e-01
chcsho_1m_x	2720001.0	3.200000e-03	2.550000e-02	-0.1168	0.0000000e+00		$0.0000000e+00 \boxed{0.0000000e+00} \boxed{1.096800e+00}$	1.096800e+00
chcsho_3m_x	2681179.0	1.240000e-02	6.180000e-02	-0.1424	0.0000000e+00	0.000000e+00		3.300000e-03 1.686700e+00
chcsho_6m_x	2624125.0	2.810000e-02	1.189000e-01	-0.1880	0.0000000e+00	9.000000e-04		1.070000e-02 3.832600e+00
chcsho_12m_x	2514147.0	6.190000e-02	2.297000e-01	-0.2696	0.0000000e+00	4.700000e-03		3.390000e-02 8.477000e+00
eqnpo_1m_x	2718435.0	-1.500000e-03	2.310000e-02	-0.6801	-0.6801 -0.000000e+00	0.0000000e+00	0.000000e+00 0.000000e+00	1.263000e-01
ednpo-3m-x	2677912.0	-6.200000e-03	5.200000e-02	-0.9973	-1.800000e-03	0.000000e+00	8.000000e-03	1.696000e-01
ednpo_6m_x	2618619.0	-1.350000e-02	8.900000e-02	-1.5754	-7.400000e-03	0.0000000e+00	1.640000e-02	2.788000e-01
$eqnpo_12m_x$	2504936.0	-2.670000e-02	1.474000e-01	-2.2489	-2.450000e-02	0.0000000e+00	3.340000e-02	4.743000e-01
ret_1_0_x	2541516.0	1.490000e-02	1.481000e-01	-0.7242	-6.120000e-02	7.900000e-03		7.690000e-02 2.176500e+00

	count	mean	std	mim	25%	20%	75%	max
ret_2_0_x	2521767.0	2.960000e-02	2.125000e-01	-0.8327	-8.110000e-02	1.480000e-02	1.176000e-01	$1.176000e{-}01 3.342500e{+}00 $
ret_3_0_x	2503682.0	4.400000e-02	2.649000e-01	-0.8864	-9.610000e-02	2.270000e-02	1.506000e-01	1.506000e-01 5.000000e+00
ret_3_1_x	2502019.0	2.870000e-02	2.108000e-01	-0.8310	-8.140000e-02	1.440000e-02	1.167000e-01	1.167000e-01 3.342500e+00
ret_6_0_x	2447794.0	8.830000e-02	3.970000e-01	-0.9396	-1.267000e-01	4.500000e-02	2.336000e-01	2.336000e-01 8.555600e+00
ret_6_1_x	2446030.0	7.230000e-02	3.553000e-01	-0.9171	-1.184000e-01	3.700000e-02	2.059000e-01	2.059000e-01 8.411800e+00
ret_9_0_x	2393988.0	1.336000e-01	5.093000e-01	-0.9721	-1.466000e-01	6.750000e-02	3.069000e-01	3.069000e-01 9.857100e+00
ret_9_1_x	2392087.0	1.168000e-01	4.700000e-01	-0.9555	-1.414000e-01	5.930000e-02	2.812000e-01	2.812000e-01 9.273700e+00
ret_12_0_x	2341375.0	1.813000e-01	6.179000e-01	-0.9783	-1.593000e-01	9.080000e-02	3.773000e-01	3.773000e-01 1.301590e+01
ret_12_1_x	2339380.0	1.635000e-01	5.789000e-01	-0.9728	-1.558000e-01	8.200000e-02	3.514000e-01	3.514000e-01 1.223080e+01
ret_12_7_x	2337747.0	7.050000e-02	3.478000e-01	-0.9055	-1.163000e-01	3.610000e-02	2.015000e-01	2.015000e-01 8.509400e+00
ret_18_1_x	2239551.0	2.625000e-01	7.812000e-01	-0.9850	-1.710000e-01	1.321000e-01	4.926000e-01	4.926000e-01 2.048480e+01
ret_24_1_x	2145964.0	3.596000e-01	9.260000e-01	-0.9890	-1.717000e-01	1.837000e-01	6.267000e-01	6.267000e-01 1.484620e+01
ret_24_12_x	2142652.0	1.821000e-01	6.037000e-01	-0.9678	-1.493000e-01	9.260000e-02	3.714000e-01	3.714000e-01 1.345160e+01
ret_36_1_x	1976435.0	5.673000e-01	1.234400e+00	-0.9935	-1.548000e-01	2.964000e-01	8.916000e-01	8.916000e-01 1.914000e+01
ret_36_12_x	1972590.0	3.838000e-01	9.482000e-01	-0.9864	-1.546000e-01	2.006000e-01	6.490000e-01	6.490000e-01 1.702520e+01
ret_48_12_x	1821582.0	5.938000e-01	5.938000e-01 1.256400e+00	-0.9918	-1.358000e-01	3.161000e-01	9.172000e-01	9.172000e-01 1.811810e+01
ret_48_1_x	1826053.0	7.976000e-01	7.976000e-01 1.577300e+00	-0.9965	-1.285000e-01	4.175000e-01	4.175000e-01 $1.176300e+00$ $1.772000e+01$	1.772000e+01
$ret601_x$	1691563.0	1.064400e+00 $2.014800e+00$	2.014800e+00	-0.9985	-9.170000e-02	5.486000e-01	$5.486000e{-}01 \left 1.492300e{+}00 \right 2.754720e{+}01$	2.754720e+01
${\rm ret_60_12_x}$	1686573.0	8.258000e-01	8.258000e-01 1.611700e+00	-0.9960	-1.096000e-01	4.364000e-01	4.364000e-01 $1.200000e+00$ $2.063640e+01$	2.063640e+01
$ret_60_36_x$	1680619.0	3.857000e-01	9.340000e-01	-0.9860	-1.429000e-01	2.072000e-01	6.479000e-01	6.479000e-01 1.808570e+01
seas_1_1an_x	2426517.0	1.420000e-02	1.421000e-01	-0.6705	-6.040000e-02	7.600000e-03	7.560000e-02	$7.600000e-03 \bigg \ \ 7.560000e-02 \bigg 1.823500e+00 \bigg $

	count	mean	std	mim	25%	20%	75%	max
seas_1_1na_x	1870192.0	1.490000e-02	4.360000e-02	-0.2355	-7.800000e-03	1.280000e-02	3.460000e-02	3.871000e-01
seas_2_5an_x	1599992.0	1.520000e-02	6.790000e-02	-0.2970	-2.260000e-02	1.180000e-02	4.810000e-02	6.337000e-01
at_gr1_x	2426455.0	2.641000e-01	9.239000e-01	-0.7398	4.800000e-03	9.050000e-02	2.391000e-01	3.163840e+01
ca_gr1_x	2184566.0	3.206000e-01	3.206000e-01 1.336600e+00	-0.8313	-3.830000e-02	9.400000e-02	2.815000e-01	2.815000e-01
nca-gr1-x	2183067.0	3.950000e-01	3.950000e-01 1.682300e+00	-0.8737	-1.530000e-02	8.250000e-02	2.844000e-01	2.844000e-01 5.781320e+01
lt_gr1_x	2408077.0	3.042000e-01	9.791000e-01	-0.8021	-2.990000e-02	8.560000e-02	2.894000e-01	2.894000e-01 1.783760e+01
cl_gr1_x	2190296.0	2.996000e-01	8.898000e-01	-0.8494	-6.490000e-02	1.114000e-01	3.701000e-01	3.701000e-01 $1.634630e+01$
$ncl-gr1_x$	2075342.0	9.926000e-01	5.509500e+00	-1.0000	-1.023000e-01	3.970000e-02	3.376000e-01	3.376000e-01 1.990000e+02
be_gr1_x	2311345.0		3.178000e-01 1.301000e+00	-0.9166	5.900000e-03	9.660000e-02	2.271000e-01	2.271000e-01 3.373330e+01
$debt_gr1_x$	2158693.0	7.838000e-01	7.838000e-01 4.707200e+00	-1.0000	-1.456000e-01	1.900000e-02	3.292000e-01	3.292000e-01 1.090000e+02
${ m sale_gr1_x}$	2362404.0	2.228000e-01	6.711000e-01	-0.9960	5.000000e-03	1.032000e-01	2.478000e-01	2.478000e-01 1.370570e+01
cogs_gr1_x	2358805.0	2.142000e-01	6.122000e-01	-0.9619	-4.700000e-03	1.032000e-01	2.613000e-01	2.613000e-01 1.190030e+01
sga-gr1.x	1997437.0	1.844000e-01	3.963000e-01	-1.0000	1.340000e-02	1.044000e-01	2.389000e-01	2.389000e-01 6.765800e+00
opex_gr1_x	2387208.0	1.949000e-01	4.470000e-01	-0.7668	7.900000e-03	1.058000e-01	2.505000e-01	2.505000e-01 7.187400e+00
capx_gr1_x	2147147.0	6.016000e-01	2.183000e+00	-1.3370	-2.236000e-01	1.144000e-01	6.251000e-01	6.251000e-01 3.425000e+01
inv_gr1_x	1910333.0	2.595000e-01	9.931000e-01	-1.0000	-6.850000e-02	8.260000e-02	2.909000e-01	2.909000e-01 1.698080e+01
at_gr3_x	2114339.0	9.104000e-01	9.104000e-01 2.670800e+00	-0.8797	8.870000e-02	3.426000e-01	8.167000e-01	8.167000e-01 6.899070e+01
ca_gr3_x	1898998.0	9.832000e-01	9.832000e-01 3.187300e+00	-0.9099	2.890000e-02	3.230000e-01	8.289000e-01	8.289000e-01 7.748590e+01
nca_gr3_x	1897746.0	1.592100e+00 $6.786800e+00$	6.786800e+00	-0.9628	4.280000e-02	3.455000e-01	3.455000e-01 $1.005000e+00$ $1.792615e+02$	1.792615e + 02
lt_gr3_x	2091277.0	$\overline{}$	135900e+00 3.376000e+00	-0.8936	3.580000e-02	3.474000e-01	9.457000e-01	9.457000e-01 5.633890e+01
$ cl_gr3_x $	1906078.0		9.845000e-01 $2.656400e+00$	-0.9194	9.000000e-03	3.652000e-01		9.754000e-01 $4.535460e+01$

	count	mean	std	mim	25%	20%	12%	max
ncl_gr3_x	1803330.0	4.168200e+00 2.242620e+01	2.242620e+01	-1.0000	-1.231000e-01	2.914000e-01	2.914000e-01 1.285200e+00 8.32333e+02	8.323333e+02
be_gr3_x	1998122.0	1.009400e+00	1.009400e+00 3.275200e+00	-0.9384	7.210000e-02	3.326000e-01	7.902000e-01 6.699660e+01	6.699660e+01
debt_gr3_x	1882647.0	3.622500e+00 $2.086590e+01$	2.086590e+01	-1.0000	-2.165000e-01	2.251000e-01	2.251000e-01 $1.145100e+00$ $4.310000e+02$	4.310000e+02
sale_gr3_x	2063618.0	8.605000e-01	8.605000e-01 2.814400e+00	-1.0000	7.210000e-02	3.286000e-01	7.527000e-01 8.620390e+01	8.620390e+01
cogs_gr3_x	2052669.0	7.935000e-01	7.935000e-01 2.179500e+00	-1.0000	4.870000e-02	3.267000e-01	7.894000e-01 4.537560e+01	4.537560e+01
sga_gr3_x	1713690.0		6.540000e-01 1.324200e+00	-1.0000	9.470000e-02	3.366000e-01	7.294000e-01 2.400000e+01	2.400000e+01
opex_gr3_x	2073541.0		7.171000e-01 1.625000e+00	-0.8979	7.650000e-02	3.367000e-01	7.689000e-01 2.833740e+01	2.833740e+01
capx_gr3_x	1846897.0	1.692700e+00	692700e+00 5.902400e+00	-1.2088	-2.368000e-01	3.214000e-01	3.214000e-01 $1.355700e+00$ $1.128462e+02$	1.128462e + 02
cash_gr1a_x	2396920.0	1.480000e-02	1.380000e-01	-1.1898	-1.600000e-02	2.800000e-03	3.520000e-02	8.303000e-01
inv_gr1a_x	2351255.0	1.250000e-02	5.090000e-02	-0.3723	-7.000000e-04	7.000000e-04	2.250000e-02	2.978000e-01
rec_gr1a_x	2363716.0	2.190000e-02	6.430000e-02	-0.4405	-2.700000e-03	1.190000e-02	4.270000e-02	3.340000e-01
ppeg-gr1a_x	2178200.0	5.240000e-02	1.039000e-01	-0.8431	8.900000e-03	3.670000e-02	8.330000e-02	5.756000e-01
lti_gr1a_x	2205853.0	5.400000e-03	4.060000e-02	-0.4964	0.0000000e+00	0.0000000e+00	1.100000e-03	3.478000e-01
intan-gr1a_x	2110874.0	1.080000e-02	6.690000e-02	-0.9608	-7.000000e-04	0.0000000e+00	1.700000e-03	5.336000e-01
debtst_gr1a_x	2395084.0	3.900000e-03	6.220000e-02	-0.5236	-5.000000e-03	0.0000000e+00	1.320000e-02	4.847000e-01
ap_gr1a_x	2267822.0	1.460000e-02	4.890000e-02	-0.2766	-3.900000e-03	6.100000e-03	2.540000e-02	2.945000e-01
txp-gr1a_x	2057276.0	9.000000e-04	1.130000e-02	-0.0902	-9.000000e-04	0.0000000e+00	2.200000e-03	9.250000e-02
debtlt_gr1a_x	2411829.0	1.770000e-02	9.970000e-02	-0.6085	-1.080000e-02	0.0000000e+00	3.540000e-02	5.760000e-01
txditc_gr1a_x	2135161.0	2.300000e-03	1.280000e-02	-0.1302	0.0000000e+00	0.0000000e+00	4.800000e-03	8.330000e-02
coa_gr1a_x	2167569.0	3.450000e-02	1.005000e-01	-0.7908	-4.200000e-03	2.200000e-02	7.140000e-02	4.923000e-01
col_gr1a_x	2191221.0	1.980000e-02	6.480000e-02	-0.4855	-5.500000e-03	1.350000e-02	4.240000e-02	3.834000e-01

	count	mean	std	mim	25%	20%	75%	max
cowc_gr1a_x	2146736.0	1.440000e-02	8.680000e-02	-0.6052	-1.810000e-02	9.000000e-03	4.750000e-02	4.185000e-01
ncoa_gr1a_x	2185140.0	4.890000e-02	1.438000e-01	-1.8841	-5.500000e-03	2.970000e-02	9.040000e-02	7.494000e-01
ncol_gr1a_x	2174709.0	6.300000e-03	3.310000e-02	-0.3605	-1.100000e-03	1.900000e-03	1.180000e-02	3.338000e-01
nncoa_gr1a_x	2147813.0	4.270000e-02	1.424000e-01	-1.8841	-9.700000e-03	2.500000e-02	8.290000e-02	7.692000e-01
oa-gr1a-x	2167557.0	8.310000e-02	2.025000e-01	-2.5884	-3.400000e-03	6.800000e-02	1.668000e-01	8.176000e-01
ol-gr1a_x	2174709.0	2.620000e-02	8.090000e-02	-0.6433	-4.900000e-03	2.070000e-02	5.460000e-02	5.422000e-01
fna_gr1a_x	2497393.0	5.700000e-03	6.030000e-02	-0.7055	0.0000000e+00	0.0000000e+00 0.0000000e+00	0.000000e+00	6.896000e-01
fnl-gr1a_x	2418391.0	2.150000e-02	1.353000e-01	-1.2296	-1.620000e-02	1.000000e-04	5.400000e-02	5.400000e-02 1.130300e+00
nfna-gr1a-x	2418391.0	-1.580000e-02	1.552000e-01	-1.1078	-5.900000e-02	-9.000000e-04	2.760000e-02	2.760000e-02 1.384100e+00
gp-gr1a_x	2387365.0	3.580000e-02	1.161000e-01	-0.8663	-2.200000e-03	2.080000e-02	7.290000e-02	7.290000e-02 1.372100e+00
ebitda_gr1a_x	2390711.0	9.700000e-03	9.740000e-02	-0.8685	-1.050000e-02	9.300000e-03	3.840000e-02	3.840000e-02 1.237100e+00
ebit_gr1a_x	2392217.0	5.200000e-03	9.760000e-02	-0.8536	-1.310000e-02	6.700000e-03	3.280000e-02	3.280000e-02 1.345400e+00
ope-gr1a.x	2056758.0	9.400000e-03	1.005000e-01	-0.9869	-1.390000e-02	1.090000e-02	3.950000e-02	3.950000e-02 1.233300e+00
ni_gr1a_x	2402691.0	8.000000e-04	1.303000e-01	-1.6889	-1.340000e-02	3.900000e-03	2.430000e-02	2.430000e-02 2.739400e+00
nix_gr1a_x	2402691.0	6.000000e-04	1.422000e-01	-1.8549	-1.540000e-02	3.800000e-03	2.570000e-02	2.570000e-02 2.791300e+00
dp-gr1a.x	2309627.0	3.900000e-03	1.560000e-02	-0.3935	-0.3935 -0.000000e+00	2.500000e-03	7.500000e-03	7.500000e-03 1.932000e-01
fincf_gr1a_x	2053075.0	1.220000e-02	2.465000e-01	-2.0255	-5.480000e-02	2.700000e-03	7.330000e-02	7.330000e-02 1.485100e+00
ocf_gr1a_x	2334713.0	1.000000e-04	1.397000e-01	-0.9941	-4.190000e-02	2.900000e-03	4.640000e-02	4.640000e-02 1.151200e+00
fcf_gr1a_x	2181931.0	-7.300000e-03	1.637000e-01	-1.1368	-6.050000e-02	-4.000000e-04	5.020000e-02	5.020000e-02 1.202900e+00
nwc_gr1a_x	2164316.0	2.640000e-02	1.763000e-01	-1.4272	-2.650000e-02	1.650000e-02	7.240000e-02	9.090000e-01
eqnetis_gr1a_x	2052797.0	1.170000e-02	2.127000e-01	-1.9975	-1.000000e-02	0.000000e+00	1.380000e-02 1.207600e+00	1.207600e+00

	count	mean	std	mim	25%	20%	15%	max
dltnetis-gr1a-x	2373431.0	-3.100000e-03	1.313000e-01	-0.7874	-2.580000e-02	0.000000e+00	2.250000e-02	7.003000e-01
dstnetis_gr1a_x	2290818.0	7.000000e-04	8.970000e-02	-0.8063	-1.090000e-02	0.000000e+00	1.870000e-02	7.197000e-01
dbnetis_gr1a_x	2374474.0	-2.600000e-03	1.670000e-01	-1.0269	-4.130000e-02	0.000000e+00	4.330000e-02	4.330000e-02 1.017900e+00
netis_gr1a_x	2052412.0	8.700000e-03	2.717000e-01	-2.0764	-6.040000e-02	1.700000e-03	7.550000e-02	7.550000e-02 1.539900e+00
eqnpo-gr1a-x	2047069.0	-1.040000e-02	2.148000e-01	-1.1821	-1.480000e-02	0.0000000e+00	1.310000e-02	1.310000e-02 1.940900e+00
tax_gr1a_x	2398103.0	3.100000e-03	2.840000e-02	-0.2157	-3.800000e-03	1.000000e-03	1.140000e-02	2.047000e-01
eqbb_gr1a_x	1893504.0	1.700000e-03	3.370000e-02	-0.3806	0.000000e+00	0.000000e+00	3.000000e-04	2.809000e-01
eqis_gr1a_x	2000469.0	1.360000e-02	2.117000e-01	-2.0255	-2.500000e-03	0.000000e+00	5.700000e-03	5.700000e-03 1.226200e+00
div_gr1a_x	2382722.0	1.100000e-03	1.270000e-02	-0.2183	0.000000e+00	0.000000e+00	1.200000e-03	2.439000e-01
eqpo-gr1a.x	1891334.0	2.900000e-03	4.380000e-02	-0.4620	-1.000000e-04	0.000000e+00	4.100000e-03	3.915000e-01
capx_gr1a_x	2184434.0	7.400000e-03	5.440000e-02	-0.4868	-7.300000e-03	2.300000e-03	1.940000e-02	4.471000e-01
be_gr1a_x	2311289.0	4.620000e-02	1.699000e-01	-2.0718	1.600000e-03	3.510000e-02	8.970000e-02	8.561000e-01
cash_gr3a_x	2081646.0	2.960000e-02	1.755000e-01	-2.5781	-1.260000e-02	9.500000e-03	6.320000e-02	9.052000e-01
inv_gr3a_x	2033267.0	2.900000e-02	8.700000e-02	-0.6971	0.000000e+00	6.800000e-03	5.550000e-02	4.115000e-01
rec_gr3a_x	2047864.0	4.970000e-02	1.082000e-01	-0.7795	1.400000e-03	3.280000e-02	8.960000e-02	4.887000e-01
ppeg_gr3a_x	1890568.0	1.277000e-01	2.118000e-01	-2.1282	3.190000e-02	1.080000e-01	2.163000e-01	9.231000e-01
lti_gr3a_x	1864897.0	1.290000e-02	7.040000e-02	-0.6566	0.0000000e+00	0.000000e+00	8.800000e-03	4.683000e-01
intan_gr3a_x	1784074.0	2.520000e-02	1.171000e-01	-1.7938	-1.7938 -0.000000e+00	0.000000e+00	2.360000e-02	6.632000e-01
debtst_gr3a_x	2078323.0	8.500000e-03	7.970000e-02	-0.8315	-6.500000e-03	3.000000e-04	2.440000e-02	5.514000e-01
ap_gr3a_x	1936459.0	3.440000e-02	8.510000e-02	-0.4973	-3.000000e-04	1.600000e-02	4.880000e-02	4.801000e-01
txp_gr3a_x	1751204.0	1.900000e-03	1.400000e-02	-0.0976	-1.200000e-03	0.000000e+00 $4.400000e-03$	4.400000e-03	1.079000e-01

	count	mean	std	mim	25%	20%	75%	max
${\rm debtlt_gr3a_x}$	2098723.0	4.090000e-02	1.579000e-01	-1.1700	-1.120000e-02	1.060000e-02	1.011000e-01	7.496000e-01
txditc_gr3a_x	1843283.0	6.200000e-03	2.480000e-02	-0.2172	0.000000e+00	0.000000e+00	1.330000e-02	1.273000e-01
coa_gr3a_x	1880953.0	7.660000e-02	1.701000e-01	-1.4412	6.100000e-03	6.190000e-02	1.549000e-01	6.791000e-01
col-gr3a_x	1907173.0	4.420000e-02	9.650000e-02	-0.9653	4.300000e-03	3.750000e-02	8.380000e-02	4.559000e-01
cowc_gr3a_x	1861920.0	3.210000e-02	1.338000e-01	-1.0405	-2.130000e-02	2.260000e-02	9.140000e-02	5.604000e-01
ncoa-gr3a_x	1899708.0	1.091000e-01	2.575000e-01	-4.5815	1.230000e-02	1.026000e-01	2.250000e-01	8.112000e-01
ncol_gr3a_x	1887939.0	1.640000e-02	5.970000e-02	-0.5782	-0.000000e+00	9.000000e-03	3.080000e-02	4.104000e-01
nncoa_gr3a_x	1861492.0	9.300000e-02	2.474000e-01	-3.9391	1.200000e-03	8.690000e-02	2.030000e-01	8.094000e-01
oa_gr3a_x	1880920.0	1.840000e-01	3.641000e-01	-5.1474	4.560000e-02	2.082000e-01	3.829000e-01	9.247000e-01
ol_gr3a_x	1887939.0	6.020000e-02	1.295000e-01	-1.1795	1.270000e-02	5.900000e-02	1.138000e-01	6.233000e-01
fna_gr3a_x	2302373.0	1.560000e-02	8.920000e-02	-1.1421	0.000000e+00	0.0000000000000000000000000000000000000	0.000000e+00	7.162000e-01
fnl_gr3a_x	2105333.0	4.560000e-02	2.040000e-01	-1.8999	-1.910000e-02	2.600000e-02	1.304000e-01	8.753000e-01
nfna_gr3a_x	2105333.0	-3.150000e-02	2.282000e-01	-1.3255	-1.318000e-01	-2.310000e-02	4.440000e-02	4.440000e-02 2.048000e+00
gp_gr3a_x	2074121.0	7.850000e-02	1.870000e-01	-1.2858	4.200000e-03	5.550000e-02	1.554000e-01	1.554000e-01 1.274100e+00
ebitda_gr3a_x	2079592.0	2.410000e-02	1.330000e-01	-1.0362	-8.600000e-03	2.410000e-02	7.360000e-02	7.360000e-02 1.478800e+00
ebit_gr3a_x	2081034.0	1.490000e-02	1.346000e-01	-1.1637	-1.460000e-02	1.620000e-02	6.010000e-02	6.010000e-02 1.985300e+00
ope_gr3a_x	1772515.0	2.290000e-02	1.350000e-01	-1.1140	-1.410000e-02	2.540000e-02	7.260000e-02	7.260000e-02 1.382600e+00
ni_gr3a_x	2095331.0	5.500000e-03	1.607000e-01	-2.0040	-1.480000e-02	8.900000e-03	4.110000e-02	4.110000e-02 3.365400e+00
nix_gr3a_x	2095331.0	5.200000e-03	1.722000e-01	-2.2144	-1.670000e-02	8.800000e-03	4.270000e-02	4.270000e-02 3.330500e+00
dp-gr3a_x	1998657.0	9.200000e-03	2.780000e-02	-0.6566	5.000000e-04	7.400000e-03	1.760000e-02	3.627000e-01
ocf_gr3a_x	2026157.0	1.030000e-02	1.536000e-01	-0.9623	-3.950000e-02	1.100000e-02		$6.680000e-02 \left 1.459300e+00 \right $

	count	mean	std	mim	25%	20%	15%	max
fcf_gr3a_x	1875380.0	-2.300000e-03	1.806000e-01	-0.9594	-6.520000e-02	3.500000e-03	6.430000e-02	6.430000e-02 1.668700e+00
nwc_gr3a_x	1880705.0	5.470000e-02	2.333000e-01	-3.1433	-2.400000e-02	4.470000e-02	1.438000e-01	9.475000e-01
dltnetis_gr3a_x	2057295.0	-7.000000e-03	1.381000e-01	-0.9437	-3.150000e-02	0.000000e+00	2.360000e-02	8.602000e-01
dstnetis_gr3a_x	1975805.0	-1.000000e-04	7.960000e-02	-0.7776	-1.420000e-02	0.000000e+00	1.680000e-02	6.541000e-01
dbnetis-gr3a_x	2058325.0	-7.400000e-03	1.681000e-01	-1.2437	-4.610000e-02	0.000000e+00	4.140000e-02	4.140000e-02 1.075700e+00
tax_gr3a_x	2090131.0	6.500000e-03	3.600000e-02	-0.2190	-4.800000e-03	2.700000e-03	1.970000e-02	2.106000e-01
div_gr3a_x	2069485.0	2.200000e-03	1.420000e-02	-0.2110	0.000000e+00	0.000000e+00	4.200000e-03	2.609000e-01
capx_gr3a_x	1877910.0	1.340000e-02	6.720000e-02	-0.6838	-6.700000e-03	6.500000e-03	3.240000e-02	3.679000e-01
capx_at_x	2305667.0	6.630000e-02	7.300000e-02	-0.0305	1.920000e-02	4.470000e-02	8.570000e-02	6.092000e-01
spi_at_x	2376699.0	-1.010000e-02	4.960000e-02	-1.3123	-2.700000e-03	0.0000000000000000000000000000000000000	0.000000e+00	1.961000e-01
xido-at_x	2513016.0	-5.000000e-04	1.800000e-02	-0.4152	0.0000000e+00	0.0000000e+00 0.0000000e+00	0.000000e+00	1.762000e-01
nri_at_x	2375825.0	-1.080000e-02	6.070000e-02	-1.5759	-4.600000e-03	0.0000000e+00 0.0000000e+00	0.0000000e+00	2.675000e-01
gp_sale_x	2468341.0	8.440000e-02	8.440000e-02 3.062100e+00	-124.7476	2.080000e-01	3.345000e-01	5.045000e-01	9.763000e-01
ebitda_sale_x	2470375.0	-3.073000e-01 $4.409900e+00$	4.409900e+00	-171.6176	5.970000e-02	1.272000e-01	2.277000e-01	7.373000e-01
ebit_sale_x	2470818.0	-3.840000e-01 $4.578500e+00$	4.578500e+00	-185.0447	3.170000e-02	8.990000e-02	1.721000e-01	6.154000e-01
pi_sale_x	2473639.0	-4.469000e-01 4.876400e+00	4.876400e+00	-184.2990	1.190000e-02	7.260000e-02	1.445000e-01	7.101000e-01
ni_sale_x	2474362.0	-4.693000e-01 $4.796100e+00$	4.796100e+00	-184.2990	7.200000e-03	4.550000e-02	9.440000e-02	5.566000e-01
nix_sale_x	2472905.0	-4.745000e-01 4.848700e+00	4.848700e+00	-184.2990	6.200000e-03	4.620000e-02	9.640000e-02	6.508000e-01
ocf_sale_x	2414346.0	-3.439000e-01 3.755000e+00	3.755000e+00	-140.2577	-1.520000e-02	5.800000e-02	1.448000e-01	1.448000e-01 1.412300e+00
fcf_sale_x	2267091.0	-5.418000e-01 $4.134400e+00$	4.134400e+00	-125.9694	-1.053000e-01	-1.100000e-03	6.670000e-02	6.670000e-02 1.210500e+00
gp_at_x	2503159.0	3.011000e-01	2.895000e-01	-1.2660	1.023000e-01	2.659000e-01	4.563000e- 01	$4.563000 e-01 \left 1.412300 e+00 \right $

	count	mean	std	mim	25%	20%	15%	max
ebitda_at_x	2505194.0	7.710000e-02	1.992000e-01	-2.1076	2.950000e-02	1.080000e-01	1.699000e-01	5.122000e-01
ebit_at_x	2506116.0	4.100000e-02	1.986000e-01	-2.1142	1.820000e-02	7.130000e-02	1.269000e-01	4.730000e-01
fi_at_x	2185678.0	1.660000e-02	2.114000e-01	-2.6041	2.010000e-02	6.410000e-02	9.800000e-02	3.716000e-01
cop_at_x	2259456.0	1.333000e-01	1.925000e-01	-1.1882	3.940000e-02	1.365000e-01	2.302000e-01	2.302000e-01 1.940400e+00
ni_at_x	2514966.0	-5.000000e-03	2.045000e-01	-2.8828	3.400000e-03	3.510000e-02	7.410000e-02	3.332000e-01
ope-be-x	2108352.0	1.569000e-01	5.427000e-01	-8.8149	9.490000e-02	2.136000e-01	3.261000e-01	3.261000e-01 3.725100e+00
ni_be_x	2444347.0	-1.990000e-02	5.962000e-01	-10.7541	1.720000e-02	9.500000e-02	1.504000e-01	1.504000e-01 1.450500e+00
nix_be_x	2444347.0	-2.270000e-02	6.187000e-01	-11.9515	1.490000e-02	9.590000e-02	1.526000e-01	1.526000e-01 1.558300e+00
ocf_be_x	2375509.0	4.150000e-02	5.350000e-01	-7.2459	-3.990000e-02	1.089000e-01	2.199000e-01	2.199000e-01 4.068700e+00
fcf_be_x	2219533.0	-1.352000e-01	6.520000e-01	-9.8959	-2.117000e-01	-4.000000e-03	1.206000e-01	1.206000e-01 2.895100e+00
gp-bev-x	2404319.0		6.940000e-01 1.236500e+00	-11.0645	2.172000e-01	4.625000e-01	8.366000e-01	8.366000e-01 1.753110e+01
ebitda_bev_x	2406313.0	5.730000e-02	5.730000e-02 1.310800e+00	-38.6063	9.750000e-02	1.837000e-01	2.972000e-01	2.972000e-01 3.290900e+00
ebit_bev_x	2406990.0	-2.510000e-02 1.386000e+00	1.386000e+00	-41.0563	5.220000e-02	1.282000e-01	2.282000e-01	2.282000e-01 2.800000e+00
fi_bev_x	2116451.0	-8.600000e-02 1.345800e+00	1.345800e+00	-38.5103	4.190000e-02	9.910000e-02	1.608000e-01	1.608000e-01 2.274200e+00
cop_bev_x	2188818.0	3.139000e-01	8.344000e-01	-8.9448	8.920000e-02	2.259000e-01	4.111000e-01	4.111000e-01 1.607970e+01
gp-ppen_x	2466653.0	2.766900e+00 6.510900e+00	6.510900e+00	-130.5385	4.559000e-01	1.518900e+00	$1.518900e{+00} \ 3.353000e{+00} \ 1.035052e{+02}$	1.035052e + 02
ebitda_ppen_x	2468488.0	-1.134000e-01 $1.280070e+01$	1.280070e+01	-558.0000	1.689000e-01	4.726000e-01	$4.726000e{-}01 \left 1.116300e{+}00 \right 3.389320e{+}01$	3.389320e+01
fcf_ppen_x	2270795.0	-8.658000e-01 1.104610e+01	1.104610e+01	-423.4211	-3.778000e-01	-1.180000e-02	3.338000e-01	3.338000e-01 3.272670e+01
fincf_at_x	2181057.0	6.050000e-02	2.270000e-01	-0.9085	-4.100000e-02	1.800000e-03	8.120000e-02	8.120000e-02 1.643700e+00
netis_at_x	2180970.0	2.900000e-02	2.576000e-01	-1.3681	-4.860000e-02	0.000000e+00	5.940000e-02	5.940000e-02 1.592800e+00
eqnetis_at_x	2181226.0	5.680000e-02	1.918000e-01	-0.3507	-8.000000e-04	6.000000e-04	1.520000e-02	$1.520000e-02 \left 1.488800e+00 \right $

	count	mean	std	mim	25%	20%	75%	max
eqis-at-x	2142004.0	7.050000e-02	1.912000e-01	-0.1034	0.0000000e+00	3.200000e-03	2.280000e-02	2.280000e-02 1.535600e+00
dbnetis_at_x	2487875.0	-2.120000e-02	1.573000e-01	-1.3624	-3.980000e-02	-8.000000e-04	2.270000e-02	6.456000e-01
dltnetis_at_x	2487184.0	-2.430000e-02	1.364000e-01	-1.2268	-3.180000e-02	-2.200000e-03	1.200000e-03	5.184000e-01
dstnetis_at_x	2428021.0	3.500000e-03	6.050000e-02	-0.4789	-5.100000e-03	0.000000e+00	1.130000e-02	4.836000e-01
eqnpo_at_x	2177364.0	-4.470000e-02	1.949000e-01	-1.4673	-1.110000e-02	8.000000e-04	2.020000e-02	4.462000e-01
eqbb_at_x	2059717.0	1.250000e-02	3.500000e-02	-0.0026	0.0000000e+00	0.000000e+00	5.300000e-03	4.018000e-01
div_at_x	2500964.0	1.160000e-02	2.170000e-02	0.0000	0.000000e+00	1.900000e-03	1.660000e-02	3.183000e-01
oaccruals_at_x	2261617.0	-1.580000e-02	1.522000e-01	-2.2637	-7.200000e-02	-1.830000e-02	4.760000e-02	6.719000e-01
oaccruals_ni_x	2260635.0	-5.853000e-01 $6.180500e+00$	6.180500e+00	-71.4418	-71.4418 -1.208700e+00	-2.712000e-01	6.967000e-01	6.967000e-01 8.515790e+01
taccruals_at_x	2240180.0	-3.100000e-02	2.045000e-01	-2.4802	-9.100000e-02	-1.180000e-02	4.930000e-02	4.930000e-02 1.294200e+00
taccruals_ni_x	2238904.0	2238904.0 $\left -1.448100e + 00 \right 8.683400e + 00$	8.683400e+00	-131.5096	-131.5096 -1.516600e+00	-1.946000e-01	7.622000e-01	7.622000e-01 6.728570e+01
noa_at_x	2142866.0	6.816000e-01	4.649000e-01	-1.1515	4.896000e-01	6.884000e-01	8.418000e-01	8.418000e-01 1.038840e+01
be-bev_x	2368048.0	1.343100e+00 2.666700e+00	2.666700e+00	0.0326	5.543000e-01	8.086000e-01	8.086000e-01 $1.190400e+00$ $6.053070e+01$	6.053070e + 01
debt_bev_x	2416506.0	4.732000e-01	6.162000e-01	0.0000	1.399000e-01	3.804000e-01	6.012000e-01	6.012000e-01 1.276120e+01
cash_bev_x	2397575.0	8.357000e-01	8.357000e-01 3.110100e+00	0.0000	3.800000e-02	1.245000e-01	4.276000e-01	4.276000e-01 8.007360e+01
pstk_bev_x	2418755.0	2.720000e-02	1.704000e-01	0.0000	0.0000000e+00	0.000000e+00	$0.000000e{+}00 \boxed{0.000000e{+}00} \boxed{7.089400e{+}00}$	7.089400e+00
debtlt_bev_x	2412477.0	3.446000e-01	4.482000e-01	0.0000	5.390000e-02	2.671000e-01	4.815000e-01	4.815000e-01 9.026500e+00
debtst_bev_x	2403343.0	1.233000e-01	2.903000e-01	0.0000	3.200000e-03	3.390000e-02	1.172000e-01	1.172000e-01 5.633000e+00
int_debt_x	1959042.0	1.258000e-01	3.153000e-01	0.0000	5.310000e-02	7.610000e-02	1.063000e-01	1.063000e-01 7.750000e+00
int_debtlt_x	1874541.0		3.393000e-01 1.552500e+00	0.0000	6.360000e-02	9.400000e-02	1.485000e-01	1.485000e-01 4.145000e+01
ebitda_debt_x	2242375.0	2.161600e+00 $2.312980e+01$	2.312980e+01	-362.2105	1.666000e-01	3.959000e-01		9.501000e-01 $5.562212e+02$

	count	mean	std	mim	25%	20%	75%	max
profit_cl_x	2270271.0	4.298000e-01	$4.298000e-01 \left 1.566600e+00 \right $	-11.9038	2.114000e-01	5.648000e-01	5.648000e-01 1.016300e+00 6.155300e+00	6.155300e+00
ocf_cl_x	2269486.0		5.390000e-02 1.456200e+00	-14.9568	-1.363000e-01	2.183000e-01	5.993000e-01	5.993000e-01 5.976400e+00
ocf_debt_x	2189764.0	$\overline{}$.253200e+00 1.968000e+01	-264.1167	-7.590000e-02	1.564000e-01	5.185000e-01	5.185000e-01 4.307215e+02
cash_lt_x	2487462.0		7.781000e-01 2.113200e+00	0.0000	4.150000e-02	1.312000e-01	5.084000e-01	2.990910e+01
inv_act_x	2124755.0	2.719000e-01	2.276000e-01	0.0000	4.860000e-02	2.538000e-01	4.448000e-01	9.113000e-01
rec_act_x	2130411.0	3.499000e-01	2.071000e-01	0.0000	1.990000e-01	3.479000e-01	4.754000e-01	9.455000e-01
debtst_debt_x	2235158.0	2.916000e-01	3.181000e-01	0.0000	3.900000e-02	1.578000e-01	4.582000e-01	4.582000e-01 1.000000e+00
cl_lt_x	2271050.0	5.408000e-01	2.822000e-01	0.0172	3.033000e-01	5.188000e-01	7.861000e-01	7.861000e-01 1.000000e+00
debtlt_debt_x	2251637.0	7.215000e-01	3.158000e-01	0.0000	5.637000e-01	8.571000e-01	9.724000e-01	9.724000e-01 1.000000e+00
lt_ppen_x	2467297.0		413180e+01 4.095230e+01	0.0809	1.032300e+00	2.019600e+00	2.019600e+00 5.768200e+00 7.630447e+02	7.630447e+02
debtlt_be_x	2439883.0	7.140000e-01	7.140000e-01 1.464700e+00	0.0000	3.360000e-02	3.025000e-01	7.618000e-01	2.225160e+01
opex_at_x	2503218.0	9.413000e-01	8.196000e-01	0.0029	3.295000e-01	7.872000e-01	$7.872000e{-}01 \left 1.304500e{+}00 \right 7.158500e{+}00$	7.158500e+00
nwc_at_x	2253296.0	2.724000e-01	2.457000e-01	-0.7924	8.520000e-02	2.536000e-01	4.349000e-01	9.547000e-01
debt_at_x	2514980.0	2.331000e-01	2.095000e-01	0.0000	5.090000e-02	1.957000e-01	3.591000e-01	1.428700e+00
debt_be_x	2444508.0	9.825000e-01	1.972300e+00	0.0000	9.520000e-02	4.426000e-01	4.426000e-01 $1.023800e+00$ $3.440000e+01$	3.440000e+01
ebit_int_x	2038745.0		266250e+01 1.784445e+02	-3702.0000	1.253300e+00	4.003000e+00	$4.003000e+00 \left 1.124330e+01 \right 3.302250e+03$	3.302250e+03
inv_days_x	2394275.0	8.869850e+01 1.683021e+02	1.683021e+02	0.0000	9.009300e+00	5.392190e+01	$5.392190e{+01} 1.091676e{+02} 3.574195e{+03}$	3.574195e+03
rec_days_x	2403668.0	3.602296e + 02	9.967740e+02	0.0000	3.863530e+01	5.827670e+01	$5.827670e{+01} 8.822010e{+01} 7.354934e{+03}$	7.354934e+03
ap_days_x	2314657.0	1.459695e + 03	7.489965e+03	0.7812	2.587680e+01	4.209780e+01	$4.209780e{+01} \left 7.865320e{+01} \right 1.412089e{+05}$	1.412089e+05
cash_conversion_x	1836443.0	1.256743e + 02	2.122532e+02	0.0000	4.172550e+01	8.193360e+01	8.193360e+01 $1.398610e+02$ $3.521431e+03$	3.521431e+03
cash_cl_x	2262167.0		1.419800e + 00 3.231200e + 00	0.0000	1.124000e-01	3.726000e-01	$3.726000e-01 \Big 1.177400e+00 \Big 3.650000e+01$	3.650000e+01

	count	mean	std	mim	25%	20%	75%	max
caliq_cl_x	2241081.0	2.487700e+00 3.827100e+00	3.827100e+00	0.0581	9.004000e-01	1.378900e+00	1.378900e+00 $2.376600e+00$ $4.066670e+01$	4.066670e+01
ca_cl_x	2252774.0	3.162200e+00 $3.912700e+00$	3.912700e+00	0.0824	1.372500e+00	2.102000e+00	2.102000e+00	4.119530e+01
inv_turnover_x	1990611.0	1.861590e + 01 4.951140e + 01	4.951140e+01	0.0438	2.956600e+00	5.130900e+00	$5.130900e+00 \left 1.205000e+01 \right 7.307939e+02$	7.307939e+02
at_turnover_x	2482416.0	1.084900e+00	9.318000e-01	0.0000	3.768000e-01	9.269000e-01	$9.269000e{-}01 \left 1.525100e{+}00 \right 9.298300e{+}00$	9.298300e+00
rec_turnover_x	2400338.0	1.234110e+01 2.636800e+01	2.636800e+01	0.0000	4.039600e+00	6.187900e+00	$6.187900e+00 \left 9.236800e+00 \right 2.787135e+02$	2.787135e+02
ap_turnover_x	2229997.0	1.163840e+01 $1.238900e+01$	1.238900e+01	-0.1258	4.826800e+00	8.918500e+00	8.918500e+00 $1.434510e+01$ $1.336129e+02$	1.336129e + 02
sale_bev_x	2408388.0	2.269200e+00 $2.923100e+00$	2.923100e+00	0.0000	7.623000e-01	1.580300e+00	1.580300e+00	3.887110e+01
sale_be_x	2437063.0	2.732600e+00 $3.718300e+00$	3.718300e+00	0.0000	9.001000e-01	1.758000e+00	1.758000e+00 3.096000e+00 5.438940e+01	5.438940e+01
div_ni_x	1963756.0	3.126000e-01	5.775000e-01	0.0000	0.0000000e+00	1.650000e-01		4.135000e-01 1.293670e+01
sale_nwc_x	2017664.0	9.746900e+00 2.267620e+01	2.267620e+01	0.0000	2.066900e+00	3.971600e+00	3.971600e+00 $7.750900e+00$ $3.110241e+02$	3.110241e+02
tax_pi_x	1999061.0	3.279000e-01	3.117000e-01	-7.2981	2.705000e-01	3.654000e-01	4.329000e-01	4.329000e-01 5.548900e+00
cash_at_x	2496082.0	1.581000e-01	2.035000e-01	0.0000	2.580000e-02	7.260000e-02	2.026000e-01	9.799000e-01
ni-emp-x	2332173.0	2332173.0 $\left -1.044570e + 01 \right 1.898294e + 02$	1.898294e+02	-3810.3810	4.055000e-01	4.200600e+00	$4.200600e+00 \left 1.703640e+01 \right 1.438498e+03$	1.438498e+03
sale_emp_x	2328826.0	2.691786e + 02 $5.003031e + 02$	5.003031e+02	0.0000	6.301400e+01	1.411000e+02	1.411000e + 02	7.782523e+03
sale_emp_gr1_x	2120715.0	1.123000e-01	4.553000e-01	-0.9563	-3.330000e-02	5.300000e-02		1.513000e-01 7.027000e+00
emp_gr1_x	2048454.0	7.670000e-02	2.504000e-01	-1.3333	-3.060000e-02	4.520000e-02		1.538000e-01 1.483100e+00
ni_inc8q_x	1837805.0	3.116800e+00 $3.262400e+00$	3.262400e+00	0.0000	0.0000000e+00	2.000000e+00	2.000000e+00 $7.000000e+00$ $8.000000e+00$	8.0000000e+00
noa-gr1a.x	2130139.0	1.277000e-01	4.002000e-01	-0.7366	-1.750000e-02	4.940000e-02	1.574000e-01	1.574000e-01 1.075230e+01
ppeinv_gr1a_x	2130674.0	1.104000e-01	2.282000e-01	-0.5663	9.400000e-03	5.870000e-02	1.436000e-01	1.436000e-01 3.078700e+00
lnoa_gr1a_x	2042945.0	3.180000e-02	9.170000e-02	-0.5778	-3.800000e-03	1.370000e-02	4.740000e-02	7.544000e-01
$capx_sr^2x$	1996106.0	1.219100e+00 $4.305300e+00$	4.305300e+00	-1.4277	-2.477000e-01	2.272000e-01	$2.272000\text{e-}01 \Big 1.043000\text{e+}00 \Big 7.697220\text{e+}01$	7.697220e+01

	count	mean	std	mim	25%	20%	75%	max
saleq_gr1_x	2256822.0	2.428000e-01	8.315000e-01	-1.0000	-1.270000e-02	9.890000e-02	2.606000e-01	2.606000e-01 1.574840e+01
niq-be_x	2153966.0	5.000000e-04	1.393000e-01	-2.0216	1.600000e-03	2.420000e-02	4.290000e-02	6.993000e-01
niq-at_x	2218680.0	-2.200000e-03	6.080000e-02	-0.6672	0.0000000e+00	8.200000e-03	2.060000e-02	1.818000e-01
niq-be-chg1-x	1961181.0	-7.700000e-03	1.339000e-01	-2.0038	-1.650000e-02	-6.000000e-04	1.090000e-02	1.090000e-02 1.227600e+00
niq-at-chg1_x	2044996.0	3.000000e-04	5.400000e-02	-0.4547		-7.100000e-03 -0.000000e+00	5.600000e-03	8.413000e-01
dsale_dinv_x	1796036.0	-4.380000e-02	8.780000e-01	-19.4778	-1.460000e-01	2.150000e-02	1.949000e-01	1.949000e-01 5.598300e+00
dsale_drec_x	2136436.0	-3.080000e-02	6.202000e-01	-7.3996	-1.418000e-01	1.500000e-03	1.418000e-01	1.418000e-01 7.637700e+00
dgp_dsale_x	2120443.0	2.720000e-02	5.405000e-01	-5.9700	-7.530000e-02	2.300000e-03	8.380000e-02	8.380000e-02 1.201120e+01
dsale_dsga_x	1827645.0	2.310000e-02	3.643000e-01	-2.2251	-8.920000e-02	-1.000000e-04		9.360000e-02 6.963700e+00
saleq_su_x	1944544.0		1.618000e-01 1.699500e+00	-16.0960	-8.666000e-01	1.532000e-01	$1.532000e{-}01 \left 1.125000e{+}00 \right 3.358810e{+}01$	3.358810e+01
miq-su_x	1972831.0	-1.123000e-01	1.123000e-01 1.940400e+00	-50.8463	-7.565000e-01	5.100000e-03	7.529000e-01	7.529000e-01 2.019490e+01
capex_abn_x	1806456.0	1.173000e-01	9.626000e-01	-1.1469	-3.685000e-01	-6.920000e-02	2.932000e-01	2.932000e-01 1.196350e+01
op-atll_x	2415570.0	1.320000e-01	2.472000e-01	-6.9463	4.860000e-02	1.355000e-01	2.227000e-01	2.227000e-01 1.125400e+00
gp_atll_x	2413733.0	3.639000e-01	3.763000e-01	-1.9036	1.162000e-01	3.032000e-01	5.356000e-01	5.356000e-01 2.788000e+00
ope_bell_x	2010286.0	2.202000e-01	6.575000e-01	-13.6285	1.063000e-01	2.425000e-01	3.880000e-01	3.880000e-01 4.617600e+00
cop_atll_x	2237311.0	1.409000e-01	2.863000e-01	-3.8344	4.500000e-02	1.505000e-01	2.563000e-01	2.563000e-01 1.923400e+00
pi_nix_x	1959639.0	1.615000e+00	6.861000e-01	0.1059	1.340700e+00	1.572900e+00	1.572900e+00 $1.777900e+00$ $1.989360e+01$	1.989360e+01
ocf_at_x	2449158.0	1.150000e-02	1.872000e-01	-1.8184	-2.140000e-02	4.090000e-02	1.033000e-01	5.979000e-01
op_at_x	2505194.0	1.113000e-01	1.575000e-01	-1.2330	4.200000e-02	1.205000e-01	1.892000e-01	5.662000e-01
ocf_at_chg1_x	2333855.0	2.300000e-03	1.627000e-01	-1.0782	-4.770000e-02	-1.000000e-04		4.630000e-02 1.390100e+00
at_be_x	2452393.0	$2452393.0 \Big \ \ 3.714900e + 00 \Big 4.779700e + 00$	4.779700e+00	1.0000	1.0000 1.469000e+00	$2.029600e + 00 \left 3.240900e + 00 \left 5.963100e + 01 \right \right.$	3.240900e+00	5.963100e+01

	count	mean	std	mim	25%	20%	75%	max
niq_saleq_std_x	1902197.0	1.360600e+00 1.149800e+01	1.149800e+01	0.0008	1.930000e-02	4.260000e-02	1.236000e-01	$1.236000e-01 \left 3.177766e+02 \right $
roe_be_std_x	1799259.0	1.611000e-01	4.732000e-01	0.0021	2.230000e-02	4.760000e-02	1.133000e-01	1.133000e-01 9.225400e+00
tangibility_x	2201788.0	6.502000e-01	1.916000e-01	0.0025	5.540000e-01	6.638000e-01	7.614000e-01	7.614000e-01 1.684700e+00
earnings_variability_x	1752776.0	8.639000e-01	8.639000e-01 1.037400e+00	0.0243	2.577000e-01	5.765000e-01	$5.765000e{-}01 \left 1.052900e{+}00 \right 1.145280e{+}01$	1.145280e+01
aliq_at_x	2174808.0	8.263000e-01	8.005000e-01	0.1044	5.792000e-01	6.946000e-01		8.423000e-01 2.803980e+01
f_score_x	1978727.0	4.911500e+00 $1.728500e+00$	1.728500e+00	0.0000	4.000000e+00	5.000000e+00	6.0000000e+00	9.0000000e+00
o_score_x	2127585.0	-1.902100e+00 $ 3.035200e+00 $	3.035200e+00	-9.3872	$-3.598500e + 00 \left -2.309000e + 00 \left -8.857000e - 01 \right 2.287030e + 01$	-2.309000e+00	-8.857000e-01	2.287030e+01
z_score_x	2126989.0	5.526800e+00 9.357000e+00	9.357000e+00	-37.3359	1.992200e+00	$3.446700e{+00} \left 5.637300e{+00} \right 1.744239e{+02}$	5.637300e+00	1.744239e+02
intrinsic_value_x	1899809.0	1.317903e+03 $5.258077e+03$	5.258077e+03	0.0982	3.489040e+01	1.295681e+02	5.706605e + 02	1.130984e+05
kz_index_x	2167838.0	2167838.0 $\left -1.126290e + 01 \right 5.190800e + 01$	5.190800e+01	-1723.5716	$-1723.5716 \left -6.936600e + 00 \right -1.467200e + 00$	-1.467200e+00	5.962000e-01	5.962000e-01 8.903350e+01
gpoa_ch5_x	1799428.0	-5.000000e-03	1.939000e-01	-1.1201	-7.080000e-02	-2.900000e-03	5.560000e-02	5.560000e-02 1.669700e+00
roe_ch5_x	1718355.0	-1.400000e-02	5.543000e-01	-7.5143	-7.570000e-02	-6.100000e-03	5.400000e-02	5.400000e-02 7.791500e+00
roa_ch5_x	1824336.0	4.900000e-03	1.917000e-01	-1.6595	-3.640000e-02	-1.800000e-03	2.650000e-02	2.650000e-02 3.283900e+00
cfoa_ch5_x	1759171.0	1.520000e-02	1.825000e-01	-0.9610	-5.570000e-02	2.500000e-03	7.100000e-02	7.100000e-02 2.175100e+00
gmar_ch5_x	1777826.0	4.200000e-02	9.593000e-01	-24.3597	-4.330000e-02	2.700000e-03	5.140000e-02	5.140000e-02 3.059480e+01
ni_ar1_x	1798398.0	2.127000e-01	6.110000e-01	-3.9640	-1.463000e-01	1.674000e-01	5.078000e-01	5.078000e-01 9.144200e+00
ni_ivol_x	1798398.0	5.090000e-02	1.054000e-01	0.0003	7.900000e-03	1.910000e-02	4.640000e-02	4.640000e-02 1.756800e+00
at_me_x	2522907.0	2.710400e+00 $4.953100e+00$	4.953100e+00	0.0086	5.788000e-01	$1.230200e{+}00 $	2.687400e+00	1.923122e+02
be_me_x	2452453.0	7.411000e-01	7.141000e-01	0.0050	3.072000e-01	5.729000e-01	9.557000e-01	9.557000e-01 2.516310e+01
debt_me_x	2515141.0	7.136000e-01	7.136000e-01 1.647800e+00	0.0000	3.610000e-02	2.333000e-01	7.145000e-01	7.145000e-01 6.550580e+01
netdebt_me_x	2515141.0		4.707000e-01 $1.480500e+00$	-3.4965	-6.240000e-02	1.146000e-01	5.472000e-01	$5.472000e{-01} 5.866260e{+01} $

	$\left \begin{array}{c} count \end{array}\right $	mean	std	mim	25%	20%	75%	max
cash_me_x	2496218.0	2.459000e-01	5.843000e-01	0.0000	3.340000e-02	9.500000e-02	2.301000e-01	$2.301000e{-}01 \left 1.478940e{+}01 \right $
sale_me_x	2509790.0	1.848400e+00 $3.088100e+00$	3.088100e+00	0.0000	3.854000e-01	9.080000e-01	$9.080000e$ -01 $\left 2.049100e$ +00 $\left 7.507530e$ +01	7.507530e+01
gp-me-x	2504145.0	4.729000e-01	6.845000e-01	-5.3506	1.503000e-01	2.955000e-01	5.587000e-01	5.587000e-01 1.896990e+01
ebitda_me_x	2506237.0	1.594000e-01	2.707000e-01	-5.8474	5.650000e-02	1.331000e-01	2.363000e-01	2.363000e-01 5.597900e+00
ebit_me_x	2507305.0	9.600000e-02	2.455000e-01	-7.4186	3.000000e-02	9.500000e-02	1.716000e-01	1.716000e-01 $3.506600e+00$
ope-me-x	2183835.0	1.085000e-01	2.516000e-01	-8.0248	3.920000e-02	1.084000e-01	1.911000e-01	1.911000e-01 3.793500e+00
ni_me_x	2517298.0	1.200000e-03	3.459000e-01	-18.9294	5.500000e-03	4.900000e-02	8.530000e-02	9.917000e-01
nix_me_x	2517298.0	-1.200000e-03	3.693000e-01	-20.3694	4.100000e-03	4.920000e-02	8.650000e-02	8.650000e-02 1.036200e+00
cop_me_x	2259562.0	2.183000e-01	5.014000e-01	-3.5452	4.550000e-02	1.406000e-01	2.768000e-01	2.768000e-01 2.124680e+01
ocf_me_x	2450553.0	4.280000e-02	2.747000e-01	-5.6691	-1.830000e-02	5.360000e-02	1.205000e-01	1.205000e-01 5.711200e+00
fcf_me_x	2303306.0	-7.030000e-02	3.536000e-01	-8.5448	-1.065000e-01	-2.600000e-03	5.530000e-02	5.530000e-02 4.202300e+00
div_me_x	2501593.0	1.780000e-02	2.950000e-02	0.0000	0.000000e+00	3.900000e-03	2.660000e-02	2.660000e-02 1.049700e+00
eqbb_me_x	2059868.0	1.380000e-02	3.780000e-02	-0.0037	0.000000e+00	0.000000e+00	7.800000e-03	8.704000e-01
eqis-me-x	2142182.0	4.550000e-02	1.388000e-01	-0.1339	1.000000e-04	3.500000e-03	1.830000e-02	1.830000e-02 5.839400e+00
edbo-me-x	2058263.0	3.150000e-02	5.660000e-02	-0.0013	0.0000000e+00	1.120000e-02	4.150000e-02	4.150000e-02 1.725500e+00
ednpo-me-x	2177501.0	-1.430000e-02	1.450000e-01	-6.1142	-8.100000e-03	1.200000e-03	3.130000e-02	3.130000e-02 1.442900e+00
eqnetis_me_x	2181408.0	3.130000e-02	1.401000e-01	-0.6866	-1.400000e-03	7.000000e-04	1.260000e-02	1.260000e-02 5.679700e+00
at_mev_x	2480516.0	1.759600e+00 $3.280300e+00$	3.280300e+00	0.0085	5.638000e-01	$1.008000e+00 \left 1.587100e+00 \right 6.916660e+01$	1.587100e+00	6.916660e+01
bev_mev_x	2404633.0	6.919000e-01	5.487000e-01	0.0009	3.194000e-01	6.308000e-01	9.482000e-01	9.482000e-01 1.692550e+01
ppen_mev_x	2459710.0	3.322000e-01	3.872000e-01	0.0000	5.950000e-02	1.893000e-01	4.753000e-01	4.753000e-01 6.654400e+00
be_mev_x	2410201.0	6.153000e-01	8.336000e-01	0.0050	2.513000e-01	4.357000e-01	7.057000e-01	7.057000e-01 2.914710e+01

	count	mean	std	mim	25%	20%	75%	max
cash_mev_x	2460357.0	2.333000e-01	6.611000e-01	0.0000	2.350000e-02	6.940000e-02	1.825000e-01	1.825000e-01 $1.486960e+01$
sale_mev_x	2472091.0	1	.265200e+00 1.765600e+00	0.0000	3.146000e-01	7.343000e-01	$7.343000e{-}01 \left 1.550900e{+}00 \right 3.775600e{+}01$	3.775600e+01
gp_mev_x	2467238.0	3.453000e-01	4.647000e-01	-2.4081	1.209000e-01	2.305000e-01	4.284000e-01	4.284000e-01 1.314000e+01
ebitda_mev_x	2469299.0	1.012000e-01	2.101000e-01	-5.5869	5.090000e-02	1.060000e-01	1.669000e-01	1.669000e-01 2.711700e+00
ebit_mev_x	2470075.0	6.010000e-02	2.226000e-01	-6.8743	2.670000e-02	7.470000e-02	1.222000e-01	1.222000e-01 2.601300e+00
cop_mev_x	2243652.0	1.516000e-01	2.798000e-01	-2.3844	4.200000e-02	1.203000e-01	2.126000e-01	2.126000e-01 8.747500e+00
ocf_mev_x	2431339.0	3.150000e-02	1.968000e-01	-4.7377	-1.650000e-02	4.340000e-02	9.350000e-02	9.350000e-02 2.334400e+00
fcf_mev_x	2286863.0	-3.800000e-02	2.261000e-01	-6.0410	-8.630000e-02	-2.300000e-03		4.670000e-02 1.728000e+00
debt_mev_x	2480615.0	3.008000e-01	3.502000e-01	0.0000	4.020000e-02	2.106000e-01		4.607000e-01 7.224300e+00
pstk_mev_x	2479267.0	1.480000e-02	5.860000e-02	0.0000	0.0000000e+00	0.0000000e+00	$0.0000000e+00 \boxed{0.0000000e+00} \boxed{1.220500e+00}$	1.220500e+00
debtlt_mev_x	2476104.0	2.224000e-01	2.443000e-01	0.0000	1.400000e-02	1.446000e-01	3.542000e-01	3.542000e-01 2.411300e+00
$_{\rm debtst_mev_x}$	2461067.0	8.090000e-02	2.125000e-01	0.0000	9.000000e-04	1.690000e-02	7.010000e-02	7.010000e-02 5.292900e+00
dltnetis_mev_x	2453443.0	-3.150000e-02	1.853000e-01	-3.5613	-3.440000e-02	-1.900000e-03	1.200000e-03	1.200000e-03 6.324000e-01
dstnetis_mev_x	2393968.0	4.100000e-03	9.390000e-02	-1.0163	-4.800000e-03	0.000000e+00	1.110000e-02	1.110000e-02 1.122900e+00
dbnetis_mev_x	2454176.0	-2.880000e-02	2.223000e-01	-4.4848	-4.210000e-02	-6.000000e-04	2.280000e-02	2.280000e-02 1.188800e+00
netis_mev_x	2164671.0	-8.300000e-03	2.729000e-01	-4.6395	-5.040000e-02	0.0000000e+00		5.030000e-02 5.358400e+00
fincf_mev_x	2164802.0	3.700000e-02	2.405000e-01	-2.3006	-4.040000e-02	1.300000e-03	7.090000e-02	7.090000e-02 6.822000e+00
aliq_mat_x	2036506.0	5.016000e-01	2.661000e-01	0.0270	3.052000e-01	4.793000e-01	6.504000e-01	6.504000e-01 3.973200e+00
eq_dur_x	2193667.0	1.598720e+01	5.630900e+00	0.2861	1.413720e+01	1.612420e+01	$1.612420e{+01} 1.764670e{+01} 3.430355e{+02}$	3.430355e+02
beta_60m_x	2090801.0	1.153800e+00	6.856000e-01	-1.7467	6.897000e-01	1.081600e+00	$1.081600e{+00} \left 1.528500e{+00} \right 4.912400e{+00}$	4.912400e+00
ivol_capm_60m_x	2090801.0	1.172000e-01	6.560000e-02	0.0288	7.050000e-02	1.002000e-01	1.002000e-01 1.454000e-01 5.392000e-01	5.392000e-01

	count	mean	std	mim	25%	20%	75%	max
resff3.12.1.x	2274040.0	-2.210000e-02	2.736000e-01	-1.1550	-1.908000e-01	-8.900000e-03	1.610000e-01	7.899000e-01
resff3_6_1_x	2273172.0	-5.420000e-02	5.396000e-01	-2.9537	-3.435000e-01	-2.040000e-02	2.734000e-01	2.734000e-01 1.925800e+00
mispricing_mgmt_x	2414716.0	4.896000e-01	1.856000e-01	0.0147	3.610000e-01	5.047000e-01	6.284000e-01	9.427000e-01
mispricing_perf_x	2649116.0	5.208000e-01	2.065000e-01	0.0099	3.773000e-01	5.270000e-01	6.749000e-01	9.881000e-01
zero_trades_21d_x	2568596.0	9.102000e-01	2.670500e+00	0.0000	1.800000e-03	3.700000e-03	7.200000e-03	7.200000e-03 2.100980e+01
dolvol_126d_x	2527407.0	1.272436e+07	5.041472e+07	36.1000	6.023594e+04	3.756701e+05 $3.493927e+06$ $1.038495e+09$	3.493927e+06	1.038495e+09
$dolvol_var_126d_x$	2527340.0	1.275800e+00	7.751000e-01	0.2622	7.587000e-01	$1.088500e{+00} \left 1.545100e{+00} \right 8.289100e{+00}$	1.545100e+00	8.289100e+00
$turnover_126d_x$	2527415.0	4.300000e-03	6.800000e-03	0.0000	9.000000e-04	2.200000e-03	5.300000e-03	2.857000e-01
turnover_var_126d_x	2527348.0	1.251900e+00	7.609000e-01	0.2796	7.459000e-01	1.058700e+00	1.058700e+00 1.509700e+00 7.678300e+00	7.678300e+00
zero_trades_126d_x	2527415.0	9.170000e-01	9.170000e-01 2.511100e+00	0.0000	1.900000e-03	4.000000e-03	1.771000e-01	1.771000e-01 1.949730e+01
zero_trades_ $252d_x$	2472485.0	9.236000e-01	9.236000e-01 2.470600e+00	0.0001	2.000000e-03	4.300000e-03	2.625000e-01	2.625000e-01 1.910030e+01
bidaskhl 21d x	2474735.0	1.470000e-02	1.810000e-02	0.0011	5.6000000e-03	9.400000e-03	1.710000e-02	5.318000e-01
rvolhl_21d_x	2474735.0	2.130000e-02	1.570000e-02	0.0000	1.100000e-02	1.720000e-02	2.680000e-02	1.854000e-01
beta_21d_x	2469080.0	8.736000e-01	1.205700e+00	-11.1429	2.238000e-01	8.042000e-01	8.042000e-01 1.458000e+00 1.276490e+01	1.276490e+01
ivol_capm_21d_x	2469080.0	2.710000e-02	1.960000e-02	0.0018	1.400000e-02	2.160000e-02	3.380000e-02	2.415000e-01
iskew_capm_21d_x	2469046.0	2.407000e-01	8.745000e-01	-3.5665	-2.542000e-01	2.053000e-01	7.097000e-01	7.097000e-01 3.715300e+00
coskew_21d_x	2469074.0	-1.530000e-02	3.111000e-01	-1.4678	-2.232000e-01	-2.070000e-02	1.886000e-01	1.886000e-01 1.347500e+00
beta_dimson_21d_x	2469080.0	9.503000e-01	9.503000e-01 1.950600e+00	-19.3713	4.290000e-02	8.515000e-01	$8.515000e-01 \left 1.798400e+00 \right 2.341690e+01$	2.341690e+01
ivol_ff3_21d_x	2469080.0	2.640000e-02	1.930000e-02	0.0018	1.360000e-02	2.100000e-02	3.300000e-02	2.340000e-01
iskew_ff3_21d_x	2469068.0	1.990000e-01	7.943000e-01	-3.1203	-2.632000e-01	1.696000e-01	6.344000e-01	6.344000e-01 3.455800e+00
ivol_hxz4_21d_x	2332649.0	2.680000e-02	1.960000e-02	0.0018	1.370000e-02	2.130000e-02	3.350000e-02	2.397000e-01

	count	mean	std	mim	25%	20%	75%	max
skew_hxz4_21d_x	2332643.0	1.777000e-01	7.585000e-01	-3.0805	-2.681000e-01	1.513000e-01	6.005000e-01	6.005000e-01 $3.275600e+00$
rmax5_21d_x	2469033.0	3.860000e-02	2.910000e-02	0.0022	1.960000e-02	3.050000e-02	4.810000e-02	3.544000e-01
rmax1_21d_x	2469033.0	6.730000e-02	5.830000e-02	0.0035	3.110000e-02	5.000000e-02	8.280000e-02	8.996000e-01
rvol_21d_x	2469080.0	2.970000e-02	2.060000e-02	0.0018	1.590000e-02	2.400000e-02	3.690000e-02	2.515000e-01
rskew_21d_x	2469038.0	2.439000e-01	8.740000e-01	-3.5810	-2.529000e-01	2.077000e-01		7.136000e-01 3.808400e+00
ami_126d_x	2427976.0	2	.294900e+00 1.277990e+01	0.0000	6.300000e-03	8.310000e-02	7.621000e-01	7.621000e-01 7.242321e+02
beta_252d_x	2434576.0	8.972000e-01	6.011000e-01	-1.8325	4.682000e-01	8.481000e-01	8.481000e-01 $1.259200e+00$ $4.013900e+00$	4.013900e+00
ivol_capm_252d_x	2434576.0	2.910000e-02	1.710000e-02	0.0050	1.700000e-02	2.480000e-02		3.650000e-02 1.684000e-01
betadown_252d_x	2406390.0	1.001300e+00	7.817000e-01	-3.9821	5.127000e-01	9.352000e-01	9.352000e-01 $1.414000e+00$ $5.699200e+00$	5.699200e+00
$\rm prc_highprc_252d_x$	2434268.0	7.724000e-01	1.997000e-01	0.0167	6.610000e-01	8.272000e-01		9.318000e-01 1.000000e+00
rvol_252d_x	2434576.0	3.110000e-02	1.740000e-02	0.0052	1.870000e-02	2.680000e-02	3.870000e-02	1.690000e-01
$_{\rm corr_1260d_x}$	1904407.0	3.603000e-01	1.650000e-01	-0.0374	2.362000e-01	3.573000e-01	4.786000e-01	8.219000e-01
betabab_1260d_x	1893789.0	1.075600e+00	5.871000e-01	-0.3259	6.475000e-01	$1.000500e{+}00 \mid 1.410600e{+}00 \mid 4.274900e{+}00$	1.410600e+00	4.274900e+00
$\rm rmax5_rvol_21d_x$	2343331.0	1.232900e+00	5.049000e-01	0.1125	8.720000e-01	1.159900e+00	1.159900e + 00 1.512600e + 00 4.328700e + 00	4.328700e+00
age_x	2739928.0	2.184690e + 02 $1.888040e + 02$	1.888040e+02	1.0000	7.900000e+01	1.590000e+02	1.590000e+02 3.000000e+02 1.115000e+03	1.115000e+03
qmj_x	1825615.0	8.990000e-02	9.763000e-01	-1.7027	-7.318000e-01	1.204000e-01	9.350000e-01	9.350000e-01 1.701100e+00
qmj_prof_x	2502382.0	9.110000e-02	9.846000e-01	-1.7036	-7.339000e-01	1.300000e-01	9.456000e-01	9.456000e-01 1.698800e+00
qmj -growth_x	1825622.0	3.610000e-02	9.739000e-01	-1.7018	-7.911000e-01	4.900000e-02	8.716000e-01	8.716000e-01 1.702100e+00
qmj_safety_x	2579701.0	8.730000e-02	9.713000e-01	-1.7012	-7.189000e-01	1.215000e-01	9.239000e-01	9.239000e-01 1.708800e+00
m r	2739928.0	6.400000e-03	1.555000e-01	-1.0113	-6.530000e-02	-1.400000e-03		6.680000e-02 1.988170e+01
ri	2739928.0 1	1.770830e+01	.770830e+01 $6.890425e+02$	-0.2196	6.348000e-01	$6.348000e{-}01 \Big \ 1.290100e{+}00 \Big 3.413100e{+}00 \Big 1.527087e{+}05$	3.413100e+00	1.527087e+05

	count	mean	std	mim	25%	20%	75%	max
m r-f001m	2717410.0	-3.000000e-04	1.452874e+03	-11994.7451	3.000000e-04 1.452874e+03 -11994.7451 -6.730875e+02 -6.488730e+01 -6.730875e+02 -6.488730e+01 -6.730875e+02 -6.488730e+01 -6.730875e+02 -6.488730e+01 -6.730875e+02 -6.730875e+02 -6.730875e+01 -6.730875e+02 -6.730875e+01 -6.730876e+01		5.622922e+02 1.975796e+05	1.975796e + 05
$r_{-}f002m$	2694932.0		1.453405e+03	-12093.2324	$-4.000000e-04 \ 1.453405e+03 \ -12093.2324 \ -6.719280e+02 \ -6.400750e+01 \ -6.400750e+01$	-6.400750e+01	5.623110e + 02 1.340182e + 05	1.340182e + 05
$r_{-}f003m$	2672377.0	-5.000000e-04	1.452500e+03	-12181.5869	$1.452500e{+03} -12181.5869 -6.704744e{+02} -6.279780e{+01}$		5.626841e+02 1.023323e+05	1.023323e+05
$r_{-}f004m$	2649956.0	3.000000e-04	1.467237e+03	-12221.2090	$1.467237e+03 \left -12221.2090 \right -6.701777e+02 \left -6.287600e+01 \right $		5.621040e+02	1.259151e + 05
$r_{-}f005m$	2627466.0		1.471883e+03	-12192.0312	$1.000000e-04 \left 1.471883e+03 \right -12192.0312 \left -6.696848e+02 \right -6.289280e+01$	-6.289280e+01	5.614439e + 02 1.259212e + 05	1.259212e + 05
$r_{-}f006m$	2604896.0	3.000000e-04	1.479795e+03	-12242.7471	$1.479795e+03 \begin{array}{r rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		5.606614e+02	1.259316e + 05
$r_{-}f007m$	2582271.0	6.000000e-04	6.000000e-04 $1.481432e+03$ -12249.9131		-6.683008e+02 $-6.239580e+01$		5.602472e+02 1.895877e+05	1.895877e+05
$r_{-}f008m$	2559645.0	-4.000000e-04	1.494461e+03	-12270.5273	$-4.000000e-04 \ 1.494461e+03 \ -12270.5273 \ -6.684138e+02 \ -6.289780e+01 \ -6.289780e+01$		5.595248e+02 1.975297e+05	1.975297e+05
r_f009m	2536940.0	1	1.497932e+03	-12302.8760	$7.000000e-04 \left 1.497932e+03 \right -12302.8760 \left -6.676816e+02 \right -6.255130e+01$		5.583124e + 02 1.975135e + 05	1.975135e + 05
$r_{-}f010m$	2514233.0	0	1.505680e + 03	-12306.7148	$.0000000e + 00 \\ \boxed{1.505680e + 03} \\ \boxed{-12306.7148} \\ \boxed{-6.674777e + 02} \\ \boxed{-6.674777e + 02} \\ \boxed{-6.308580e + 01} \\ \boxed{5.573524e + 02} \\ \boxed{1.975094e + 05} \\ \boxed{-6.308580e + 01} \\ \boxed{-6.308680e + 01}$	-6.308580e+01	5.573524e+02	1.975094e+05
r_f011m	2491745.0	0	.000000e+00 $1.511348e+03$ -12250.5898	-12250.5898	-6.675006e+02 -6.366780e+01		5.557687e+02 1.975246e+05	1.975246e + 05
$r_{-}f012m$	2469229.0	-4.000000e-04	1.506349e + 03	-12207.8350	$-4.000000e-04 \ 1.506349e+03 \ -12207.8350 \ -6.657420e+02 \ -6.324470e+01$		5.550534e+02	1.975047e+05
r_f013m	2446715.0	-1.000000e-04	1.515108e+03	-12176.1465	$-1.000000e-04 \\ 1.515108e+03 \\ -12176.1465 \\ -6.655490e+02 \\ -6.655490e+02 \\ -6.377990e+01 \\ 5.530358e+02 \\ 1.974958e+05 \\ 2.530358e+05 \\ 1.974958e+05 \\ 2.530358e+05 \\ 2.530368e+05 \\ 2.530368e+05 \\ 2.530368e+05 \\ 2.530368e+05 \\ 2.53088e+05 \\ 2.530388e+05 \\ 2.5303888e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\ 2.5303888e+05 \\ 2.530388e+05 \\ 2.5303888e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\ 2.530388e+05 \\$	-6.377990e+01	5.530358e+02	1.974958e + 05
r_f014m	2424394.0	2.000000e-04	1.510473e+03 -11440.9531	-11440.9531	-6.651825e+02 $-6.383700e+01$		5.523057e+02 1.974974e+05	1.974974e + 05
$r_{-}f015m$	2402314.0	-1.000000e-04	1.512811e+03	-11449.6279	$1.512811e+03 \ $		5.507740e + 02 1.974900e + 05	1.974900e+05
$r_{-}f016m$	2380363.0	2.000000e-04	1.515042e+03	-11449.5361	$2.000000e-04 \ \ 1.515042e+03 \ \ -11449.5361 \ \ -6.646672e+02 \ \ -6.581010e+01$	-6.581010e+01	5.496704e+02 1.974964e+05	1.974964e + 05
$r_{-}f017m$	2358474.0	-1.000000e-04	1.518632e+03	-11473.9346	$1.518632e + 03 \\ -11473.9346 \\ -6.650385e + 02 \\ -6.704440e + 01$		5.478585e + 02 1.974688e + 05	1.974688e+05
$r_{-}f018m$	2336696.0	1.000000e-04	1.522247e+03	-11924.3223	$1.522247\mathrm{e} + 03 \ -11924.3223 \ -6.646155\mathrm{e} + 02 \ -6.711870\mathrm{e} + 01$		5.465416e + 02 1.974814e + 05	1.974814e + 05
r_f019m	2315092.0	1.000000e-04	1.522928e+03	-11477.0908	$1.522928e + 03 \\ -11477.0908 \\ -6.638971e + 02 \\ -6.765280e + 01 \\ -6.765280e + 01$	-6.765280e+01	5.454422e+02 1.974768e+05	1.974768e + 05
$r_{-}f020m$	2293683.0	<u>'</u>	1.526165e+03	-11837.1934	$1.000000e-04 \ \ 1.526165e+03 \ \ -11837.1934 \ \ -6.631345e+02 \ \ -6.773940e+01$		5.443864e+02 1.974707e+05	1.974707e+05
r_f021m	2272416.0 -0	-0.000000e+00	1.525184e + 03	-11830.5957	$.000000e + 00 \left 1.525184e + 03 \right - 11830.5957 \left -6.630684e + 02 \left -6.768750e + 01 \right 5.435944e + 02 \left 1.974645e + 05 \right + 1000000e + 100 \left 1.974645e + 100 \right + 1000000e + 100 \left 1.974645e + 100 \right + 1000000e + 100 \left 1.974645e + 100 \right + 10000000e + 100 \left 1.974645e + 100 \right + 1000000e + 100 \left 1.974645e + 100 \right + 1000000e + 100 \left 1.974645e + 100 \right + 1000000e + 100 \left 1.974646e + 100 \left 1.974646e + 100 \right + 1000000e + 100 \left 1.974646e $	-6.768750e+01	5.435944e+02	1.974645e + 05

	count	mean	std	mim	25%	20%	75%	max
$ ho_{ m r-f022m}$	2251211.0	1.000000e-04	1.000000e-04 $1.521066e+03$ -11822.4795	-11822.4795	-6.620583e + 02 $-6.732170e + 01$	-6.732170e+01	5.424589e+02 $1.974786e+05$	1.974786e + 05
$r_{-}f023m$	2230142.0	-0.000000e+00	1.521688e+03	-11815.7969	$.0000000e + 00 \ 1.521688e + 03 \ -11815.7969 \ -6.616403e + 02 \ -6.751140e + 01 \ -6.751140e + 01 \ -6.8686e + 01 \ -6.8$	-6.751140e+01	5.414223e+02 $1.974742e+05$	1.974742e + 05
$r_{-}f024m$	2209316.0	-0.000000e+00	.000000e+00 1.520726e+03 -11948.9941	-11948.9941	-6.596912e+02 $-6.725050e+01$	-6.725050e+01	5.403683e+02 1.974745e+05	1.974745e+05
$ m r$ _f025 $ m m$	2188719.0	1.000000e-04	1.521428e+03 -11828.5732		-6.593975e+02 -6.767100e+01	-6.767100e+01	5.392651e+02 1.974657e+05	1.974657e+05
$r_{-}f026m$	2168242.0	0.0000000e+00	1.522714e+03	-11837.6758	$.0000000e+00 \left 1.522714e+03 \right -11837.6758 \left -6.583010e+02 \right -6.773110e+01$	-6.773110e+01	5.379360e+02 1.974702e+05	1.974702e+05
$r_{-}f027m$	2147901.0	1.000000e-04	1.511179e+03	-11839.1934	$1.511179e+03 \ $	-6.728920e+01	5.372294e+02	1.895889e+05
$r_{-}f028m$	2127702.0	1.000000e-04	1.507530e + 03	-11834.7500	$1.000000e-04 \ \ 1.507530e+03 \ \ -11834.7500 \ \ -6.557527e+02 \ \ -6.652340e+01$	-6.652340e+01	5.364533e+02 $1.895897e+05$	1.895897e+05
$r_{-}f029m$	2107711.0	1.000000e-04	1.502109e + 03	-11846.0547	1.502109e + 03 - 11846.0547 - 6.544728e + 02 - 6.637620e + 01		5.357737e+02 1.896120e+05	1.896120e + 05
$r_{-}f030m$	2087915.0	-1.000000e-04	1.000000e-04 1.498496e+03 -11853.5107	-11853.5107	-6.531980e + 02 -6.626840e + 01	-6.626840e+01	5.346227e+02 $1.896178e+05$	1.896178e+05
$r_{-}f031m$	2068400.0	0	1.492586e + 03	-11866.2324	$.0000000e + 00 \ 1.492586e + 03 \ -11866.2324 \ -6.525869e + 02 \ -6.630400e + 01 \ -6.630400e$	-6.630400e+01	5.336425e+02 1.596513e+05	1.596513e + 05
$r_{-}f032m$	2049032.0	0.0000000e+00	.000000e+00 1.489238e+03 -11872.9951	-11872.9951	-6.517037e+02 -6.576680e+01	-6.576680e+01	5.334434e+02 $1.596468e+05$	1.596468e+05
r_f033m	2029771.0		$1.000000e-04 \left 1.488224e+03 \right -11889.0117$	-11889.0117	-6.510807e+02 -6.590900e+01	-6.590900e+01	5.329744e+02	1.596441e+05
$r_{-}f034m$	2010873.0	1.000000e-04	1.484454e + 03	-11889.4648	$1.000000e-04 \left 1.484454e+03 \right -11889.4648 \left -6.505530e+02 \right -6.600180e+01 \left 5.321952e+02 \right 1.339924e+05 \left 1.339924e+05 \right + 1188988888888888888888888888888888888$	-6.600180e+01	5.321952e+02	1.339924e+05
$r_{-}f035m$	1991985.0	0.0000000e+00	1.481871e+03	-11888.5801	$1.481871e+03 \ -11888.5801 \ -6.497461e+02 \ -6.637680e+01$	-6.637680e+01	5.308284e+02	1.339871e+05
$ m r_f036m$	1973277.0		$.0000000e+00 \left 1.480547e+03 \right -11901.7588$		-6.487253e+02 -6.560970e+01	-6.560970e+01	5.307343e+02	1.339843e+05
$ m r_f037m$	1954719.0	0	1.474733e+03	-11808.9707	$.0000000e + 00 \left 1.474733e + 03 \right -11808.9707 \left -6.477959e + 02 \right -6.532040e + 01$	-6.532040e+01	5.303346e+02 1.105830e+05	1.105830e + 05
$r_{-}f038m$	1936335.0	0	1.470288e+03	-11795.4795	$.0000000e+00 \left 1.470288e+03 \right -11795.4795 \left -6.465491e+02 \right -6.499620e+01$	-6.499620e+01	5.294399e+02 1.105891e+05	1.105891e + 05
r_f039m	1918045.0	-0.0000000e+00	.000000e+00 $1.466709e+03$ -11661.7285	-11661.7285	-6.456418e+02 $-6.549740e+01$	-6.549740e+01	5.287186e+02 1.105892e+05	1.105892e + 05
$r_{-}f040m$	1900119.0	0	1.464523e+03	-11641.5117	$.0000000e+00 \\ \boxed{1.464523e+03} \\ \boxed{-11641.5117} \\ \boxed{-6.446006e+02} \\ \boxed{-6.542780e+01}$	-6.542780e+01	5.281598e + 02 $1.105945e + 05$	1.105945e + 05
$r_{-}f041m$	1882204.0	-0.0000000e+00	1.461618e + 03	-11620.1201	$.0000000e+00 \\ \boxed{1.461618e+03} \\ \boxed{-11620.1201} \\ \boxed{-6.434552e+02} \\ \boxed{-6.541130e+01}$	-6.541130e+01	5.274347e+02 1.105990e+05	1.105990e + 05
r_{-} f042m	1864406.0 0		1.461010e+03	-11649.9248	$.0000000e+00 \left 1.461010e+03 \right -11649.9248 \left -6.426281e+02 \left -6.453170e+01 \right 5.271555e+02 \left 1.105945e+0581e+05 \right + 1.105945e+0581e+0581e+0581e+0681e$	-6.453170e+01	5.271555e+02	1.105945e + 05

	count	mean	std	mim	25%	20%	75%	max
r_f043m	1846808.0	0.	1.458799e+03	-11647.5039	$0000000e+00 \left 1.458799e+03 \left -11647.5039 \right -6.419841e+02 \left -6.478650e+01 \right 5.264048e+02 \left 1.105988e+0586e+0586e+0586e+06866e+068666e+0686e+0686e+0686e+0686e+0686e+0686e+0686e+0686e+0686e+0686e+06866e+06866e+06866e+0686666666666$.6.478650e+01	5.264048e+02	1.105988e + 05
r_f044m	1829434.0		1.456109e+03	-11657.0537	$1.000000e-04 \left 1.456109e+03 \right -11657.0537 \left -6.405219e+02 \right -6.464430e+01 \left 5.260392e+02 \right 1.105983e+05 \left 1.105983e+05 \right -1165983e+05 \left 1.1059886e+05 \right -1165986e+05 \left 1.1059886e+05 \right -1165986e+05 \left 1.1059886e+05 \right -1165986e+05 \left 1.1059886e+05 \right -1165986e+05 \left 1.105986e+05 \right -1165966e+05 \left 1.105986e+05 \right -1165966e+05 \left 1.105966e+05 \right -1165966e+05 \left 1.10596$	6.464430e+01	5.260392e+02	1.105983e + 05
r_f045m	1812186.0	0.	1.455769e+03	-11657.0459	0000000e+00 $1.455769e+03$ -11657.0459 $-6.401905e+02$	-6.447610e+01	5.255322e+02 1.105999e+05	1.105999e+05
r_f046m	1795157.0		1.457390e+03	-11652.4551	0000000 + 00 $1.4573900 + 03$ -11652.4551 $-6.4031300 + 02$ $-6.4556700 + 01$		5.250655e+02 1.105960e+05	1.105960e + 05
r_f047m	1778282.0 -0.		1.460243e+03	-11658.8438	$0000000e+00 \\ \boxed{1.460243e+03} \\ -11658.8438 \\ \boxed{-6.401207e+02} \\ \boxed{-6.554230e+01} \\ \boxed{5.242169e+02} \\ \boxed{1.105929e+05} $	-6.554230e+01	5.242169e+02	1.105929e+05
r_f048m	1761604.0		1.455848e+03	-11682.4463	$0000000e+00 \\ \boxed{1.455848e+03} \\ -11682.4463 \\ \boxed{-6.391160e+02} \\ \boxed{-6.477180e+01}$.6.477180e+01	5.234120e+02	1.105901e+05
$r_{-}f049m$	1745155.0		1.455978e + 03	-11670.7920	$1.000000e-04 \left 1.455978e+03 \right -11670.7920 \left -6.382848e+02 \right -6.515990e+01 \left 5.229612e+02 \right 1.105818e+05 \left 1.105818e+05 \right + 1.105818e+0.05 \left 1.105818e+0.05 \right + 1.105818e+0.0$	-6.515990e+01	5.229612e+02	1.105818e + 05
$r_{-}f050 \mathrm{m}$	1728738.0	0	1.454388e+03	-11632.7188	$.0000000e+00 \\ \boxed{1.454388e+03} \\ -11632.7188 \\ \boxed{-6.375092e+02} \\ \boxed{-6.496860e+01} \\ \boxed{5.226442e+02} \\ \boxed{1.105831e+05} \\ \boxed{1.105831e+05} \\ \boxed{-6.496860e+01} \\ \boxed{-6.49680e+01} \\ \boxed{-6.496860e+01} \\ \boxed{-6.4968600e+01} \\ \boxed{-6.4968600e+01} \\ \boxed{-6.4968600e+01} \\ \boxed{-6.4968600e+01} \\ \boxed{-6.4968600e+01} \\ \boxed$.6.496860e+01	5.226442e+02	1.105831e+05
$r_{-}f051m$	1712469.0		1.452841e+03	-11632.8320	$1.000000e-04 \left 1.452841e+03 \right -11632.8320 \left -6.363624e+02 \right -6.464440e+01 \left 5.219601e+02 \right 1.105796e+05 = 0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.000000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.00000e+0.0000000e+0.00000e+0.00000e+0.00000e+0.000000e+0.000000e+0.00000e+0.000000e+0.00000e+0.000000e+0.000000e+0.000000e+0.00000000$.6.464440e+01	5.219601e+02	1.105796e + 05
$r_{-}f052m$	1696257.0 -0.		1.447684e+03	-11634.2344	$0000000e+00 \\ \boxed{1.447684e+03} \\ -11634.2344 \\ \boxed{-6.354518e+02} \\ \boxed{-6.441250e+01} \\ \boxed{5.216530e+02} \\ \boxed{1.105797e+05} \\ \boxed{1.105796+05} \\ 1.10$.6.441250e+01	5.216530e+02	1.105797e+05
$r_{-}f053m$	1680291.0		1.446640e+03	-11599.9922	$0000000e+00 \\ \boxed{1.446640e+03} \\ -11599.9922 \\ \boxed{-6.352231e+02} \\ \boxed{-6.461350e+01}$	-6.461350e+01	5.207815e+02	1.105815e+05
r_f054m	1664527.0 -0.		1.447881e+03	-11610.1670	$0000000e+00 \\ \boxed{1.447881e+03} \\ -11610.1670 \\ \boxed{-6.343800e+02} \\ \boxed{-6.448220e+01}$		5.200620e+02 1.105856e+05	1.105856e + 05
$r_{-}f055m$	1648942.0		1.441350e+03	-11593.4238	$.0000000e+00 \\ \boxed{1.441350e+03} \\ -11593.4238 \\ \boxed{-6.328156e+02} \\ \boxed{-6.362880e+01} \\ \boxed{5.197030e+02} \\ \boxed{1.105916e+05} \\ \boxed{1.105916e+05} \\ \boxed{-6.362880e+01} \\ -6.$.6.362880e+01	5.197030e+02	1.105916e + 05
$r_{-}f056m$	1633612.0 0		1.439244e+03	-11559.6719	$0000000e+00 \hspace{0.2cm} \hspace{0.08cm} 1.439244e+03 \hspace{0.2cm} \hspace{0.08cm} -11559.6719 \hspace{0.2cm} \hspace{0.08cm} -6.322285e+02 \hspace{0.2cm} \hspace{0.08cm} -6.335630e+01 \hspace{0.2cm} $		5.195420e+02	1.105924e + 05
r_f057m	1618435.0		1.437575e+03	-11520.1182	$0000000e+00 \hspace{0.2cm} \left. 1.437575e+03 \right11520.1182 \left6.320952e+02 \right. \left6.346460e+01 \right. \\$		5.184686e + 02 1.105943e + 05	1.105943e+05
r_f058m	1603369.0	0	1.432364e+03	-11498.3047	$0000000e+00 \\ \boxed{1.432364e+03} \\ -11498.3047 \\ \boxed{-6.313463e+02} \\ \boxed{-6.371530e+01} \\ \boxed{5.178313e+02} \\ \boxed{1.105877e+05} \\ \boxed{1.105877e+05} \\ \boxed{-6.371530e+01} \\ \boxed{-6.37150e+01} \\ -6.3$.6.371530e+01	5.178313e+02	1.105877e+05
r_f059m	1588459.0	0.	1.432379e+03	-11524.8418	$0000000e+00 \\ \boxed{1.432379e+03} \\ -11524.8418 \\ \boxed{-6.294853e+02} \\ \boxed{-6.328710e+01} \\ \boxed{5.172325e+02} \\ \boxed{1.105811e+05} \\ \boxed{1.105811e+05} \\ \boxed{-6.328710e+01} \\ -6.3$.6.328710e+01	5.172325e+02	1.105811e + 05
$r_{-}f060 \mathrm{m}$	1573646.0		1.425208e+03	-11522.6631	$-1.000000e-04 \ \ 1.425208e+03 \ \ -11522.6631 \ \ -6.281742e+02 \ \ -6.214360e+01$.6.214360e+01	5.171097e+02 $1.105770e+05$	1.105770e+05
$r_{-}f061m$	1558831.0	0.	1.423086e+03	-11512.3076	$0000000e+00 \\ \begin{array}{ c c c c c c c c c c c c c c c c c c c$.6.188950e+01	5.169286e + 02 1.105791e + 05	1.105791e + 05
$r_{-}f062m$	1544091.0	0.	1.421962e+03	-11506.7881	$0000000e+00 \\ \boxed{1.421962e+03} \\ \boxed{-11506.7881} \\ \boxed{-6.266454e+02} \\ \boxed{-6.163530e+01} \\ \boxed{5.167087e+02} \\ \boxed{1.105750e+05} \\ \boxed{1.105750e+05} \\ \boxed{-6.163530e+01} \\ -$.6.163530e+01	5.167087e+02	1.105750e + 05
r_{-} f063 m	1529580.0 -0.	-0.000000e+00	1.421226e+03	-11490.2002	$.0000000e+00\left 1.421226e+03\left -11490.2002\right -6.257752e+02\left -6.118430e+01\right 5.159457e+02\left 1.105775e+0560000e+0160000e+016000e+016000e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+01600e+016000e+016000e+016000e+016000e+016000e+016000e+016000e+016000e+0160000e+016000e+016000e+016000e+016000e+016000e+016000e+0160000e+016$	-6.118430e+01	5.159457e + 02	1.105775e + 05

	count	mean	std	mim	25%	20%	75%	max
r_f064m	1515298.0	0	1.420464e+03	-11447.7783	$.0000000e+00 \left 1.420464e+03 \right -11447.7783 \left -6.246249e+02 \right -6.092020e+01$	-6.092020e+01	5.155374e + 02 1.105721e + 05	1.105721e+05
r_f065m	1501145.0	0	1.414488e+03	-11448.2666	$.0000000e+00 \\ \boxed{1.414488e+03} \\ \boxed{-11448.2666} \\ \boxed{-6.226816e+02} \\ \boxed{-6.009660e+01} \\ \boxed{5.149099e+02} \\ \boxed{1.105906e+05} \\ 1.105906e+$	-6.009660e+01	5.149099e+02	1.105906e+05
r_f066m	1487126.0	0	1.409900e+03	-11429.1436	$.0000000e+00 \left 1.409900e+03 \right -11429.1436 \left -6.217508e+02 \right -6.041790e+01$		5.136979e + 02 1.105791e + 05	1.105791e+05
r_f067m	1473347.0 -0		.00000000+000 1.4103590+03 -11395.8105		-6.213913e+02 $-5.986390e+01$	-5.986390e+01	5.135056e+02 1.105783e+05	1.105783e + 05
r_f068m	1459783.0 -0	-0.000000e+00	1.408494e+03	-11416.6279	$.0000000e+00 \left 1.408494e+03 \left -11416.6279 \right -6.212914e+02 \left -5.952610e+01 \right 5.132261e+02 \left 1.105899e+0516000 \right -1.105899e+0.0000000000000000000000000000000000$	-5.952610e+01	5.132261e+02	1.105899e + 05
r_f069m	1446378.0 -0		1.407508e+03	-11403.6064	$.0000000e+00 \left 1.407508e+03 \left -11403.6064 \right -6.206971e+02 \left -6.046170e+01186000 \right -6.046170e+011860000000000000000000000000000000000$	-6.046170e+01	5.122022e+02 1.105804e+05	1.105804e+05
r_f070m	1433053.0 -0	-0.000000e+00	1.407457e+03	-11369.1240	$.0000000e+00 \left 1.407457e+03 \right -11369.1240 \left -6.195969e+02 \right -6.033520e+01$	-6.033520e+01	5.112055e+02 $1.105780e+05$	1.105780e+05
$r_{-}f071m$	1419806.0		1.405462e+03	-11368.4258	$.0000000e + 00 \left 1.405462e + 03 \right - 11368.4258 \left -6.189065e + 02 \right - 6.046740e + 01$	-6.046740e+01	5.107696e + 02 $1.105753e + 05$	1.105753e + 05
r_f072m	1406604.0	-0.0000000e+00	1.400772e+03	-11371.8594	$.0000000e + 00 \\ \boxed{1.400772e + 03} \\ \boxed{-11371.8594} \\ \boxed{-6.173835e + 02} \\ \boxed{-5.969520e + 01}$	-5.969520e+01	5.105945e+02	1.105796e+05
r_f073m	1393602.0		1.400693e+03	-11396.2529	$.0000000e+00 \left 1.400693e+03 \left -11396.2529 \right -6.175958e+02 \left -6.000100e+01 \right \right $		5.098098e+02 1.105802e+05	1.105802e + 05
r_f074m	1380833.0	0	1.402398e+03	-11372.6416	$.0000000e + 00 \ 1.402398e + 03 \ -11372.6416 \ -6.169977e + 02 \ -6.035980e + 01 \ -6.035980e$	-6.035980e+01	5.092791e+02 1.105740e+05	1.105740e+05
r_f075m	1368264.0	0	.000000e+000 1.403089e+03 -11405.9805	-11405.9805	-6.166624e+02 $-6.033900e+01$	-6.033900e+01	5.087950e + 02 $1.105671e + 05$	1.105671e + 05
r_f076m	1355788.0	0	1.397425e+03	-11382.0527	$.0000000e + 00 \\ \boxed{1.397425e + 03} \\ \boxed{-11382.0527} \\ \boxed{-6.149069e + 02} \\ \boxed{-5.957630e + 01} \\ \boxed{5.083461e + 02} \\ \boxed{1.105749e + 05} \\ 1.1057$	-5.957630e+01	5.083461e+02	1.105749e+05
$r_{-}f077m$	1343377.0	0	1.395999e+03	-11382.4336	$.0000000 + 00 \left 1.3959990 + 03 \right -11382.4336 \left -6.1354130 + 02 \right -5.8956800 + 01$	-5.895680e + 01	5.081946e+02	1.105644e + 05
r_f078m	1331081.0	0	1.391616e+03	-11378.7529	$.0000000 + 00 \left 1.3916166 + 03 \right - 11378.7529 \left -6.1252506 + 02 \right -5.8665206 + 01$	-5.866520e+01	5.075152e + 02 1.105711e + 05	1.105711e+05
r_f079m	1318964.0 -0		1.388824e+03	-11362.2051	$.0000000e + 00 \left 1.388824e + 03 \left -11362.2051 \right -6.116483e + 02 \left -5.816850e + 01 \right 5.073903e + 02 \left 1.105640e + 05 \right -100000e + 000 \right -1000000e + 000 \left 1.000000e + 0.00000e + $	-5.816850e+01	5.073903e+02	1.105640e + 05
r_f080m	1307052.0		1.386874e+03	-11357.9014	$.0000000e+00 \left 1.386874e+03 \right -11357.9014 \left -6.107534e+02 \right -5.763730e+01$		5.068637e + 02	1.105745e + 05
r_f081m	1295317.0	0	1.381056e+03	-11383.5312	$.0000000 + 00 \left 1.381056 + 03 \left -11383.5312 \right -6.103754 + +02 \left -5.766870 e + 01 \right -1.381056 + 1.081000 + 1.0810000 + 1.08100000 + 1.081000000 + 1.081000000 + 1.0810000000 + 1.08100000000 + 1.08100000000 + 1.0810000000000 + 1.0810000000000000000000000000000000000$		5.064513e + 02 $1.105647e + 05$	1.105647e + 05
r_f082m	1283667.0	0	1.383347e+03	-11365.5000	$.0000000e + 00 \ \ 1.383347e + 03 \ \ -11365.5000 \ \ -6.103617e + 02 \ \ -5.777960e + 01$	-5.777960e+01	5.060737e + 02 1.105658e + 05	1.105658e + 05
r_f083m	1272047.0 -0	-0.0000000e+00	1.374520e+03	-11384.9004	$.0000000e + 00 \ \ 1.374520e + 03 \ \ -11384.9004 \ \ -6.086416e + 02 \ \ -5.797640e + 01$	-5.797640e+01	5.042909e + 02 1.105673e + 05	1.105673e + 05
r_f084m	1260498.0 0	0.0000000e+00	1.373337e+03	-11363.2959	$.000000e + 00 \left 1.373337e + 03 \left -11363.2959 \right - 6.076294e + 02 \left -5.762950e + 01 \right 5.040967e + 02 \left 1.105768e + 0586 + 05868e + 05868e + 05868e + 05868e + 05868e + 06868e + 068666e + 06868e + 068666e + 0686666e + 068666e + 068666e + 068666e + 068666e + 068666e + 0686666e + 0686666e + 0686666e + 0686666e + 0686666e + 0686666e + 06866666e + 0686666e + 06866666e + 068666666e + 068666666e + 068666666666e + 068666666e + 068666666e + 0686666666666e + 06866666666666$	-5.762950e+01	5.040967e+02	1.105768e + 05

	count	mean	std	mim	25%	20%	75%	max
r_f085m	1249073.0 -0		1.374082e+03	-11402.5264	.000000e+00 $1.374082e+03$ -11402.5264 $-6.065834e+02$	-5.695480e+01	5.032051e+02 1.105750e+05	1.105750e + 05
$r_{-}f086m$	1237781.0	0	1.370850e+03	-11400.8906	$.0000000e + 00 \ \ 1.370850e + 03 \ \ -11400.8906 \ \ -6.059218e + 02 \ \ -5.657530e + 01$	-5.657530e+01	5.023136e+02 1.105727e+05	1.105727e+05
$r_{-}f087m$	1226562.0	-1.000000e-04	1.370446e+03 -11414.5410	-11414.5410	-6.048359e+02 $-5.619380e+01$		5.021124e + 02 1.105748e + 05	1.105748e + 05
r_f088m	1215483.0	0.000000e+00	1.369352e+03	-11404.8936	$.0000000 + 00 \left 1.369352 + +03 \right -11404.8936 \left -6.043073 + +02 \right -5.630440 e + 01$		5.014727e+02 1.105904e+05	1.105904e + 05
r_f089m	1204483.0	0	1.370709e+03	-11400.6182	$.0000000e+00 \left 1.370709e+03 \right -11400.6182 \left -6.037288e+02 \right -5.706160e+01$	-5.706160e+01	5.004432e+02 1.105700e+05	1.105700e+05
$ m r$ _f090 $ m m$	1193700.0	0	1.367878e+03	-11385.3594	$.0000000e + 00 \ 1.367878e + 03 \ -11385.3594 \ -6.028849e + 02 \ -6.028849e + 02 \ -6.028849e + 0.02 \ -6.028849e + 0$	-5.712190e+01 4.993200e+02		1.105744e + 05
$r_{-}f091m$	1183030.0		.000000e+00 $1.363581e+03$ -11358.1553	-11358.1553	$-6.016176e + 02 \left -5.622980e + 01 \right 4.984420e + 02 \left 1.105727e + 05880e + 01 \right + 0.00880e + 0$	-5.622980e+01	4.984420e+02	1.105727e+05
$r_{-}f092m$	1172486.0	0	1.360579e + 03	-11309.1123	$.0000000e + 00 \left 1.360579e + 03 \left -11309.1123 \right -6.002883e + 02 \left -5.573990e + 01 \right 4.975717e + 02 \left 1.105593e + 0575717e + 057717e + 057717e$	-5.573990e+01	4.975717e+02	1.105593e + 05
$r_{-}f093m$	1162055.0	0	.000000e+00 1.358095e+03 -11357.9609	-11357.9609	$-5.987974e + 02 \left -5.531470e + 01 \right 4.968514e + 02 \left 1.105644e + 05 \right + 0.0088514e + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.008888888 + 0.00888888 + 0.00888888 + 0.00888888 + 0.00888888 + 0.00888888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.0088888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.008888 + 0.00$	-5.531470e+01	4.968514e+02	1.105644e + 05
$r_{-}f094m$	1151736.0	0	1.352453e+03	-11317.3789	$.0000000e + 00 \\ \boxed{1.352453e + 03} \\ -11317.3789 \\ \boxed{-5.971700e + 02} \\ \boxed{-5.971700e + 02} \\ \boxed{-5.476540e + 01} \\ \boxed{4.963483e + 02} \\ \boxed{1.105683e + 05} \\ \boxed{1.105684e + 05} \\ 1.105684$	-5.476540e+01	4.963483e+02	1.105683e + 05
$ m r$ _f095 $ m m$	1141522.0	0	.000000e+00 $1.348188e+03$ -11309.7559	-11309.7559	-5.962652e + 02 -5.471390e + 01 4.951203e + 02	-5.471390e+01	4.951203e+02	1.105691e + 05
r_f096m	1131442.0 -0		1.342258e + 03	-11309.1016	$.0000000e+00 \\ \boxed{1.342258e+03} \\ -11309.1016 \\ \boxed{-5.944086e+02} \\ \boxed{-5.403380e+01} \\ \boxed{4.948370e+02} \\ \boxed{1.105662e+05} \\ \boxed{1.10562e+05} \\ $	-5.403380e+01	4.948370e+02	1.105662e + 05
$ m r_f097m$	1121493.0 -0		1.338318e+03	-11247.9277	$.0000000e + 00 \\ \boxed{1.338318e + 03} \\ \boxed{-11247.9277} \\ \boxed{-5.932616e + 02} \\ \boxed{-5.932616e + 02} \\ \boxed{-5.396110e + 01} \\ \boxed{4.937179e + 02} \\ \boxed{1.105643e + 05} \\ \boxed{1.105644e + 05} \\ 1.105$	-5.396110e + 01	4.937179e+02	1.105643e + 05
r_f098m	1111606.0	-0.0000000e+00	1.338118e+03 -11261.6719	-11261.6719	-5.919281e+02	-5.361060e+01 4.932585e+02		1.105735e + 05
r_f099m	1101788.0 -0		1.334361e+03	-11223.1240	$.0000000e + 00 \ 1.334361e + 03 \ -11223.1240 \ -5.905834e + 02 \ .$	$-5.352240e{+01} \left 4.921118e{+02} \right 1.105733e{+05}$	4.921118e+02	1.105733e + 05
r_f100m	1092121.0		.000000e+00 $1.331728e+03$ -11206.9795	-11206.9795	$-5.900486e + 02 \left -5.297250e + 01 \right 4.916311e + 02 \left 1.105714e + 05 \right $	-5.297250e+01	4.916311e+02	1.105714e + 05
r_f101m	1082539.0	0	.000000e+00 $1.332157e+03$ -11283.8125	-11283.8125	-5.892725e+02	$-5.268540e{+01} \left 4.909461e{+02} \right 1.105668e{+05}$	4.909461e+02	1.105668e + 05
$ m r_f102m$	1072947.0 -0		.000000e+00 $1.332334e+03$ -11282.4170	-11282.4170	-5.881101e+02	$-5.258020e{+}01 \left 4.907911e{+}02 \right 1.105829e{+}05$	4.907911e+02	1.105829e + 05
r_f103m	1063428.0	0.0000000e+00	.0000000e+00 $1.329495e+03$ -11285.6172	-11285.6172	$-5.869788e + 02 \left -5.248610e + 01 \right 4.906705e + 02 \left 1.105661e + 05 \right + 0.0008616e + 0.000$	-5.248610e+01	4.906705e+02	1.105661e + 05
r_f104m	1053983.0	0	.0000000e+00 $1.325444e+03$ -11298.3848	-11298.3848	$-5.862903e + 02 \left -5.239650e + 01 \right 4.899225e + 02 \left 1.105618e + 05 \right $	-5.239650e+01	4.899225e+02	1.105618e + 05
m r-f105 $ m m$	1044601.0 0	0.0000000e+00	1.323975e + 03	-11301.4951	$.000000e + 00 \left 1.323975e + 03 \left -11301.4951 \right -5.851770e + 02 \left -5.231380e + 01 \right 4.887940e + 02 \left 1.105658e + 0581770e + 1088180e + 1$	-5.231380e+01	4.887940e+02	1.105658e + 05

	count	mean	std	mim	25%	20%	75%	max
r_f106m	1035321.0	0.000000e+00	1.318717e+03	-11297.5840	$0.0000000 + 00 \left 1.318717e + 03 \left -11297.5840 \right -5.832391e + 02 \left -5.184850e + 01 \right 4.882903e + 02 \left 1.105617e + 0588850e + 01 \right + 0.000000e + 0.000000e + 0.0000000e + 0.0000000000$	-5.184850e+01	4.882903e+02	1.105617e+05
r_f107m	1026131.0	$1026131.0 \left -0.0000000e + 00 \right 1.311274e + 03 \left -11285.4033 \right -5.818715e + 02 \left -5.133990e + 01 \right 4.878159e + 02 \left 1.105708e + 05 \right -2.133990e + 0.000000e + 0.000000e + 0.000000e + 0.0000000e + 0.0000000e + 0.0000000e + 0.0000000e + 0.00000000e + 0.000000000e + 0.000000000e + 0.000000000e + 0.0000000000$	1.311274e + 03	-11285.4033	-5.818715e+02	-5.133990e+01	4.878159e+02	1.105708e+05
r_f108m	1017036.0	0.0000000e+00	1.305877e+03	-11274.5352	$0.0000000e+00 \\ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	-5.048810e+01	4.874828e+02	1.105686e + 05
r_f109m	1007990.0	1.000000e-04	1.294919e + 03	-11275.3604	$1.000000e-04 \left 1.294919e+03 \right -11275.3604 \left -5.771514e+02 \right -4.921990e+01 \left 4.869372e+02 \right 1.105662e+05 \left 1.105662e+05 \right +1.000000e+0.0000e+$	-4.921990e+01	4.869372e+02	1.105662e + 05
r_f110m	999001.0	- 1	1.289170e + 03	-11268.4707	$0.0000000e + 00 \\ 1.289170e + 03 \\ -11268.4707 \\ -5.755809e + 02 \\ -5.755809e + 02 \\ -4.920890e + 01 \\ 4.857903e + 02 \\ 1.105673e + 05 \\ 2.857903e + 05 \\ 1.105673e + 05 \\ 1.105674e + 05 \\ 1.1$	-4.920890e+01	4.857903e+02	1.105673e + 05
r_f111m	990052.0	-0.0000000e+00	1.290836e + 03	-11281.2275	$0.0000000e + 00 \\ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	-4.955900e+01	4.840651e+02	1.105661e + 05
r_f112m	981156.0	0.0000000e+00	1.287458e + 03	-11282.5312	$0.0000000e + 00 \\ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	-4.994070e+01	4.832928e+02	1.105664e + 05
r_f113m	972370.0	-1.000000e-04	1.284069e + 03	-11264.9014	$-1.000000e-04 \left 1.284069e+03 \right -11264.9014 \left -5.725287e+02 \right -4.965830e+01 \left 4.823773e+02 \right 1.105705e+0580e+0580e+0680$	-4.965830e+01	4.823773e+02	1.105705e + 05
r_f114m	963718.0		1.278476e + 03	-11253.8916	$0.0000000e+00 \\ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	-4.986240e+01	4.817620e+02	1.105646e + 05
r_f115m	955145.0	0.0000000e+00	1.275283e+03	-11264.3701	$0.0000000e + 00 \\ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	-4.919280e+01	4.812133e+02	1.105725e + 05
r_f116m	946626.0		1.272883e+03	-11263.4824	$0.0000000e+00 \\ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	-4.945870e+01	4.802682e+02	1.105707e+05
r_f117m	938160.0	0.0000000e+00	1.274644e+03	-11257.9434	$0.0000000e + 00 \\ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	-5.015010e+01	4.790787e+02	1.105761e+05
r_f118m	929764.0	0.0000000e+00	1.270645e+03	-11259.9062	$0.0000000e + 00 \\ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	-5.087480e+01	4.773846e+02	1.105775e+05
r_f119m	921481.0	-0.0000000e+00	1.270319e + 03	-11240.6992	$0.0000000e + 00 \\ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	-5.112130e+01	4.756199e+02	1.105739e + 05
r_f120m	913287.0	-0.0000000e+00	1.257670e + 03	-11251.2500	$0.0000000e + 00 \\ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	-4.977740e+01	4.754564e+02	1.105857e+05
train	2739928.0	3.998000e-01	4.994000e-01	0.0000	0.0000 0.0000000e+00 0.0000000e+00 1.000000e+00 1.000000e+00	0.000000e+00	1.000000e+00	1.000000e+00
test	2739928.0	6.002000e-01	4.994000e-01	0.0000	0.0000000e+00	1.000000e+00	$1.000000e+00 \mid 1.000000e+00 \mid 1.000000e+00$	1.000000e+00
dev	2739928.0	3.998000e-01	4.994000e-01	0.0000	$0.0000 \Big \ 0.0000000e+00 \Big \ 0.0000000e+00 \Big 1.000000e+00 \Big 1.000000e+00$	0.000000e+00	1.000000e+00	1.000000e+00

Table 3: Summary Statistics

15.4Code

All files, resources, and code is available for download from Github. The document listing function and class docstring is available for download here. Furthermore, the coding listings for this research essay follow. Try update.

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