## CMPS 2200 Recitation 02

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	e (Team Member 1):e (Team Member 2):
In thi	s recitation, we will investigate recurrences.
Some	of your answers will go in answers.md. Other prompts will require you to edit main.py.
	back to the README.md for instruction on git, how to test your code, and how to submit properly to l the points you've earned.
Rec	urrences
as a f certai the re	ss, we've started looking at recurrences and how to we can establish asymptotic bounds on their values unction of $n$ . In this lab, we'll write some code to generate recursion trees (via a recursive function) for an kinds of recurrences. By summing up nodes in the recurrence tree (that represent contributions to ecurrence) we can compare their total cost against the corresponding asymptotic bounds. We'll focus or rences of the form:
	W(n) = aW(n/b) + f(n)
where	e(W(1) = 1.
	1. (2 point) In main.py, you have stub code which includes a function simple_work_calc. Implement this function to return the value of $W(n)$ for arbitrary values of $a$ and $b$ with $f(n) = n$ .
	2. (2 point) Test that your function is correct by calling from the command-line pytesmain.py::test_simple_work by completing the test cases and adding 3 additional ones.
	3. (2 point) Now implement work_calc, which generalizes the above so that we can now input $a$ , $b$ and a function $f(n)$ as arguments. Test this code by completing the test cases in test_work and adding a more cases.
	4. (2 point) Now, derive the asymptotic behavior of $W(n)$ using $f(n) = 1$ , $f(n) = n$ , and $f(n) = n$ with $a = 2$ and $b = 2$ . Then, generate actual values for $W(n)$ for your code and confirm that the trend match your derivations.
	Enter your answer in answers.md
	5. (4 points) Now that you have a nice way to empirically generate values of $W(n)$ , we can look at the relationship between $a$ , $b$ , and $f(n)$ . Suppose that $f(n) = n^c$ . What is the asymptotic behavior of $W(n)$ if $c < \log_b a$ ? What about $c > \log_b a$ ? And if they are equal? Modify test_compare_work to compare empirical values for different work functions (at several different values of $n$ ) to justify your answer.
	Enter your answer in answers.md
	6. (3 points) $W(n)$ is meant to represent the running time of some recursive algorithm. Suppose we always had $a$ processors available to us and we wanted to compute the span of the same algorithm. In other words, assume that we always have enough processors for every generated subproblem. Implement the function $\operatorname{span\_calc}$ to compute the empirical span, where the work of the algorithm is given by $W(n)$ . Implement $\operatorname{test\_compare\_span}$ to create a new comparison function for comparing span functions. Derive the asymptotic expressions for the span of the recurrences you used in problem above. Confirm that everything matches up as it should.

Enter your answer in answers.md