CMPS 2200 Assignment 1

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In this assignment, you will learn more about asymptotic notation, parallelism, functional languages, and algorithmic cost models. As in the recitation, some of your answer will go here and some will go in main.py. You are welcome to edit this assignment-01.md file directly, or print and fill in by hand. If you do the latter, please scan to a file assignment-01.pdf and push to your github repository.

1. Asymptotic notation

- 1a. Is $2^{n+1} \in O(2^n)$? Why or why not? .
 - · Yes become in O(n) relation constants are ignoral, i. O(2n+1) => 062n) which is a subset of 062n).
- 1b. Is $2^{2^n} \in O(2^n)$? Why or why not?
 - : Let become $\lim_{z \to \infty} (S_z) = \infty$ and $\lim_{z \to \infty} (S_z) = \infty$

0° 72° € 0(2°)

- 1c. Is $n^{1.01} \in O(\log^2 n)$?
 - · 1m 100 = = 0 (00 0 100 6 0 (leg2)
- 1d. Is $n^{1.01} \in \Omega(\log^2 n)$?
 - n DI & S2 (log2n) becase It asymptototrowally dominates 10g2n.
- 1e. Is $\sqrt{n} \in O((\log n)^3)$?
 - ino, The O((logn)), as In asymptotically commutes o (logn)).
- If. Is $\sqrt{n} \in \Omega((\log n)^3)$?

: Vn # 52 (log n3) because vin 7 log n3 for

1g. Consider the definition of "Little o" notation:

 $g(n) \in o(f(n))$ means that for every positive constant c, there exists a constant n_0 such that $g(n) \le c \cdot f(n)$ for all $n \ge n_0$. There is an analogous definition for "little omega" $\omega(f(n))$. The distinction between o(f(n))and O(f(n)) is that the former requires the condition to be met for every c, not just for some c. For example, $10x \in o(x^2)$, but $10x^2 \notin o(x^2)$.

Prove that $o(g(n)) \cap \omega(g(n))$ is the empty set.

$$o(g(n)) = \lim_{n \to \infty} \frac{f(n)}{g(n)} = 0$$

$$o' \cdot no such f(n) ext$$

$$w(g(n)) = \lim_{n \to \infty} f(n) = 0$$

$$o' \cdot o' \cdot o' \cdot o' \cdot g(n) \cap w(g(n)) \quad (s \neq 1)$$

$$w(g(n)) = \lim_{n \to \infty} f(n) = 0$$

$$f(n) = 0$$

2. SPARC to Python

Consider the following SPARC code:

$$\begin{array}{l} foo\ x=\\ \text{ if }\ x\leq 1\ \text{ then }\\ x\\ \text{ else }\\ \text{ let }(ra,rb)=(foo\ (x-1))\ ,\ (foo\ (x-2))\ \text{ in }\\ ra+rb\\ \text{ end.} \end{array}$$

- 2a. Translate this to Python code fill in the def foo method in main.py
- · 2b. What does this function do, in your own words?

3. Parallelism and recursion

Consider the following function:

E.g., longest_run([2,12,12,8,12,12,12,0,12,1], 12) == 3

- 3a. First, implement an iterative, sequential version of longest_run in main.py.
- 3b. What is the Work and Span of this implementation?

- 3c. Next, implement a longest_run_recursive, a recursive, divide and conquer implementation. This
 is analogous to our implementation of sum_list_recursive. To do so, you will need to think about
 how to combine partial solutions from each recursive call. Make use of the provided class Result.
- 3d. What is the Work and Span of this sequential algorithm?

 3e. Assume that we parallelize in a similar way we did with sum_list_recursive. That is, each recursive call spawns a new thread. What is the Work and Span of this algorithm?