CMPS 2200 Assignment 1 Name: Jake Lehner

In this assignment, you will learn more about asymptotic notation, parallelism, functional languages, and algorithmic cost models. As in the recitation, some of your answer will go here and some will go in main.py. You are welcome to edit this assignment-01.md file directly, or print and fill in by hand. If you do the latter, please scan to a file assignment-01.pdf and push to your github repository.

1. Asymptotic notation • 1a. Is $2^{n+1} \in O(2^n)$? Why or why not? $O(3^n)$, simce only the coefficient differs. 2" EO(2") => a" E M, which raise. Hence, 2" & O(2"). $\begin{array}{ll} \text{1c. Is } n^{1.01} \in O(\log^2 n)? \\ \text{Important } \left(\text{Important } n > \text{Impor$ 1e. Is $\sqrt{n} \in O((\log n)^3)$? 1f. Is $\sqrt{n} \in \Omega((\log n)^3)$?

• 1g. Consider the definition of "Little o" notation:

 $g(n) \in o(f(n))$ means that for **every** positive constant c, there exists a constant n_0 such that $g(n) \le c \cdot f(n)$ for all $n \ge n_0$. There is an analogous definition for "little omega" $\omega(f(n))$. The distinction between o(f(n)) and O(f(n)) is that the former requires the condition to be met for **every** c, not just for some c. For example, $10x \in o(x^2)$, but $10x^2 \notin o(x^2)$.

Prove that $o(g(n)) \cap \omega(g(n))$ is the empty set.

If $f(x) \in O(g(n))$, then $\{\forall C\}(\forall n > n_0)\{f(x) \in C \cdot g(x)\}$.

If $f(x) \in \omega(g(n))$, then $\{\forall C\}(\forall n > n_0)\{f(x) > C \cdot g(x)\}$.

Let the first statement be event.

A, and the second event B. We cam rewrite B as \overline{A} , since the inequalities have opposite signs. If both events are that the specific of A and A are that A are contradications of A are specific to A and A are contradications of A are specific to A are contradications of A and A are contradications.

```
\begin{array}{l} foo\ x=\\ \text{ if }\ x\leq 1\ \text{then}\\ x\\ \text{ else}\\ \text{ let }(ra,rb)=(foo\ (x-1))\ ,\ (foo\ (x-2))\ \text{in}\\ ra+rb\\ \text{ end.} \end{array}
```

- 2a. Translate this to Python code fill in the def foo method in main.py
- 2b. What does this function do, in your own words?

This function recursively calculates
the kth term of the fibonacci
sequence.

Consider the following function:

```
def longest_run(myarray, key)
    """
    Input:
        `myarray`: a list of ints
        `key`: an int
    Return:
        the longest continuous sequence of `key` in `myarray`
"""
```

E.g., $longest_run([2,12,12,8,12,12,0,12,1], 12) == 3$

- 3a. First, implement an iterative, sequential version of longest_run in main.py.
- 3b. What is the Work and Span of this implementation?

- 3c. Next, implement a longest_run_recursive, a recursive, divide and conquer implementation. This is analogous to our implementation of sum_list_recursive. To do so, you will need to think about how to combine partial solutions from each recursive call. Make use of the provided class Result.
- 3d. What is the Work and Span of this sequential algorithm?

• 3e. Assume that we parallelize in a similar way we did with sum_list_recursive. That is, each recursive call spawns a new thread. What is the Work and Span of this algorithm?