

Discrete Structures: Programming Constructs CMPSC 102

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Fall 2022

Week 3

Slides 02

Let's Discuss

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Let's Discuss

Loops

While

For

Newton's
Method

Quadratic
Roots

Solutions

Key Questions

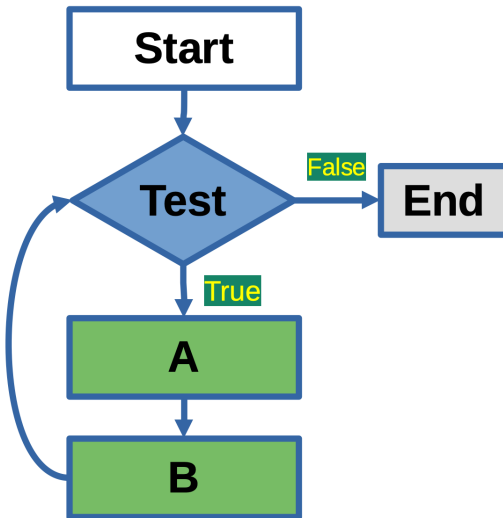
How do I use **iteration** and **conditional logic** in a Python program to perform computational tasks like processing a file's contents and mathematical tasks like using Newton's method to approximate the square root of a number?

Learning Objectives

To **remember** and **understand** some discrete mathematics and Python programming concepts, setting the stage for exploring of discrete structures.

Loops for Iteration

A loop is a way to reuse code blocks



The While Loop

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```
index = 0
while (index < 10): # condition
    print(f"Count :{index}")
    index += 1 # add one to index
```

Output

Count :0
Count :1
Count :2
Count :3
Count :4
Count :5
Count :6
Count :7
Count :8
Count :9

The for ... in range() Loop

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```
for index in range(10):  
    print(f"Count :{index}")
```

Output

```
Count :0  
Count :1  
Count :2  
Count :3  
Count :4  
Count :5  
Count :6  
Count :7  
Count :8  
Count :9
```

Newton's Method

Mathematical loops to find square roots

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Loops

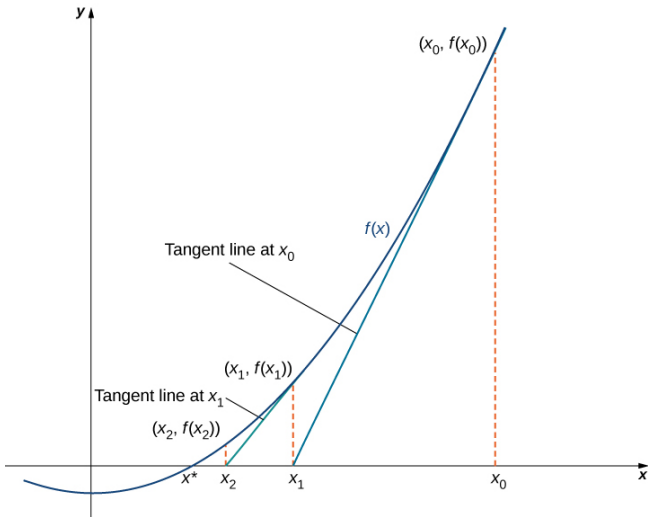
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The While Loop Application

Finding a Square Root

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```
n = 4
guess = 1.0
while abs(n - guess*guess) > 0.0001:
    guess = guess - (guess*guess - n)/(2*guess)
print(f"n = {n} : guess = {guess}")
```

- Iteratively **guesses** the square root until **within tolerance**
- The while loop uses 'abs' for computing an absolute value
- This loop computes the root as 2.0000000929222947
- The `math.sqrt(n)` function confirms this approximation!
- Any questions about this way to approximate a square root?

The While Loop Application

Finding a Square Root

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```
n = 4
guess = 1.0
while abs(n - guess*guess) > 0.0001:
    guess = guess - (guess*guess - n)/(2*guess)
print(f"n = {n} : guess = {guess}")
```

Output

```
n = 4 : guess = 2.5
n = 4 : guess = 2.05
n = 4 : guess = 2.000609756097561
n = 4 : guess = 2.0000000929222947
```


The For Loop Application

Finding a Square Root

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```
n = 4
guess = 1.0
for i in range(5):
    abs(n - guess*guess) > 0.0001
    guess = guess - (guess*guess - n)/(2*guess)
print(f"n = {n} : guess = {guess}")
```

Output

```
n = 4 : guess = 2.5
n = 4 : guess = 2.05
n = 4 : guess = 2.000609756097561
n = 4 : guess = 2.0000000929222947
```

Quadratic Root Calculation

(Back to where we were ...)

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Quadratic Equation

$$ax^2 + bx + c = 0 \quad (1)$$

Quadratic Formula

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (2)$$

Special Note

Note the $x_{1,2}$ to imply that there are **two** solutions (i.e., x_1 and x_2) to find for a second degree equation as observed from the x^2 .

Our Solution From Class

Function: `main()`

```
def main():  
    """Docstring: driver of the program;  
        deals with user"""  
    print("Quadratic equation solver:")  
    print("Enter your a,b,c integer values below")  
  
    # Get inputs from user  
    prompt = " Enter a :"  
    a_int = int(input(prompt))  
    prompt = " Enter b :"  
    b_int = int(input(prompt))  
    prompt = " Enter c :"  
    c_int = int(input(prompt))
```

Our Solution From Class

Continuing Function main()

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```
# want to check that values are integers
print(f" the types for a,b,c resp are:
{type(a_int)}, {type(b_int)}, {type(c_int)}")
print("preparing root calculation ...")
# call quadratic formula solver
root1,root2 = calcQuadratic(a_int, b_int, c_int)
# end of main()
```

Our Solution From Class

Function quadSolver()

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```
def quadSolver(a,b,c):  
    """function to apply quadratic  
        forumula to find roots"""  
    a=int(a)  
    b=int(b)  
    c=int(c)  
    print(f"\tReceived a={a}, b={b}, c={c}")  
  
    # sqrt of discriminant  
    D = (b * b - 4 * a * c) ** 0.5  
    x_one = (-b + D) / (2 * a) # first root  
    x_two = (-b - D) / (2 * a) # second root  
    return x_one, x_two  
# end of quadSolver()
```

Another Solution

Function main()

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```
def main(  
    """Driver Function"""  
    a: float = typer.Option(1),  
    b: float = typer.Option(2),  
    c: float = typer.Option(2)  
    console.print(f"Calculating roots with:")  
    console.print(f"    a = {a}")  
    console.print(f"    b = {b}")  
    console.print(f"    c = {c}")  
    x_one, x_two =  
        rootfind.  
        calc_quad_eqn_roots(a, b, c)  
    console.print(f"    x_one = {x_one}")  
    console.print(f"    x_two = {x_two}")
```

Another Solution

Function `calc_quad_eqn_roots()`

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```
def calc_quad_eqn_roots(a: float, b: float, c: float):  
    """Calculate roots of quadratic equation."""  
    D = (b * b - 4 * a * c) ** 0.5  
    x_one = (-b + D) / (2 * a)  
    x_two = (-b - D) / (2 * a)  
    return x_one, x_two
```

- Three floating-point inputs: a , b , and c
- Two floating-point outputs: x_{one} and x_{two}
- How does it calculate the roots of a quadratic equation?

- **How do we test functions to ensure correctness?**

Creating Solutions

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```
def squareArea(s: float ) -> float:  
    return s*s # area of square is s*s  
# end of squareArea()
```

What inputs s are acceptable?

- integers?
- floats?
- booleans?
- strings?
- imaginary numbers? $(1 + 3j)$

```
def main(in_str):
    # passes
    sideLength = 5
    print(f"Length {sideLength},
          area: {squareArea(sideLength)}")

    # does not pass since some values are not ints or floats
    testValues_list = [2,0,-3,2 + 5j, True, "radius"]
    for val in testValues_list:
        print(f"Length {val}, area: {squareArea(val)}")
    # end main()
```

Can we calculate with the values in testValues_list?

```
import sys
if __name__ == '__main__':
    main(sys.argv[1:])

main()
```