

Discrete Structures: CMPSC 102

Oliver BONHAM CARTER

Let's Discuss

Setup VENV

IZ: J. . C.C.

Proper SubSets

Union and Intersection

Probability

Solution

# Discrete Structures: CMPSC 102

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Spring 2024 Week 9





## Let's Discuss

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### **Key Questions**

How do I implement finite sets in Python so that I can calculate and use probabilities?

### Learning Objectives

To **remember** and **understand** some concepts about **sets**, as implemented by SymPy, supporting the calculation of probabilities.



# Mathematical Sets in Python Programs

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- Set theory is useful in mathematics and computer science
- The Sympy package gives an implementation of finite sets
  - Remember, sets are "containers" for other elements
  - The sets in Sympy are finite sets, called FiniteSet
  - These sets have the same properties as built-in sets
  - FiniteSet has a few features not provided by set
  - A probability is the likelihood that an event will occur
  - We can use either set or FiniteSet to study probabilities
- Investigate probability after exploring an alternative approach to sets



# Setting Up Virtual Environment

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### Create a project directory (outside of lassDocs/)

mkdir projects cd projects

### Create virtual environment using Python

python3 -m venv myenv
# see the file tree
find

find . -not -path '\*/\.\*' # UNIX only
dir /s # Windows?

#### Activate myenv the virtual environment

source myenv/bin/activate

#### **Install Dependencies**

pip install sympy



Import sympy

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### Get into a Python instance from terminal

python3

#### Creating a finite set

```
#_____import sympy as sy
#
```

```
empty_set = sy.FiniteSet()
```

```
empty_set = sy.FiniteSet()
print(f"{empty_set} :: {type(empty_set)}")
```

# EmptySet :: <class 'sympy.sets.sets.EmptySet'>

#### Creating a finite set

```
import sympy as sy
```

```
finite_set = sy.FiniteSet(2, 4, 6, 8, 10)
print(f"{finite_set} :: {type(empty_set)}")
# <class 'sympy.sets.sets.EmptySet'>
```



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### Creating a Set from a List or Tuple

```
#______
import sympy as sy
#
mylist = [2, 4, 6, 8, 10]
finite_set = sy.FiniteSet(*mylist)
print(finite_set)
#
tuple = (2, 4, 6, 8, 10)
finite_set = sy.FiniteSet(*tuple)
print(finite_set)
```

- All approaches call the FiniteSet constructor
- Can construct a FiniteSet out of a list or a tuple
- What is the purpose of the "\*" in this program?



# The purpose of using "\*" in set()

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We use the "\*" operator for iterable unpacking. For instance, it is used to unpack the elements of the list (mylist) and pass them as separate arguments to the sy.FiniteSet constructor.

```
import sympy as sy
mylist = [1, 2, 3, 4, 5]
```

```
# Without *, crashes
finite_set_without_star = sy.FiniteSet(mylist)
print(f"Without *: {finite_set_without_star}")
```



# The purpose of using "\*" in set()

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```
# With *
finite_set_with_star = sy.FiniteSet(*mylist)
print(f"With *: {finite_set_with_star}")
```

- sy.FiniteSet(\*mylist) is equivalent to explicitly writing
   sy.FiniteSet(1, 2, 3, 4, 5)
- The \* operator unpacks the elements from the list and provides them as separate arguments to the function or constructor.
- Useful when you have a list of values that you want to pass individually to a function or constructor that expects multiple arguments.



# **Understanding Outputs**

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```
Output of Finite Set Creation Program
import sympy as sy
#
# Explicit FiniteSet:
sy.FiniteSet(2, 4, 6, 8, 10)
#
# Empty FiniteSet:
EmptySet
#
# FiniteSet from Tuple:
sy.FiniteSet(2, 4, 6, 8, 10)
#
# FiniteSet Containing Tuple:
sy.FiniteSet((2, 4, 6, 8, 10))
```



# Why do we need this dependency?

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#### Math and Programming Differences

- Programmers cannot use sets like mathematicians do!
- Python programs cannot store an infinite set
- Finite sets must fit into a computer's finite memory
- Programs need a procedure for constructing the set
- Different programming languages and packages have other restrictions. For instance, recall that Python programs cannot create sets that contain mutable elements like lists! Why do you think that this is the case?
- So, what are the **benefits** of using sets in Python programs?
- Importantly, sets come with some super-useful default operations!
- Thankfully, sympy contains even more basic operations!



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```
Using Finite Sets in Sympy
```

```
#______
from sympy import FiniteSet
#
list = [1, 2, 3, 2]
finite_set = FiniteSet(*list)
print(finite_set)
#
for element in finite_set:
    print(element)
```

- What is the output of print(finite\_set) ?
- What is the output of print(element) in the for loop?
- How do these two output segments differ?



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### Subset Relationships with Finite Sets

```
from sympy import FiniteSet

#
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3)

#
subset = one.is_proper_subset(two)
print(subset)
subset = two.is_proper_subset(one)
print(subset)
```

- What is the mathematical definition of a **proper subset**?
- What is the purpose of the is\_proper\_subset function?
- What is the output of the print(subset) function calls?



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#### Subsets with Finite Sets

```
#______
from sympy import FiniteSet
one = FiniteSet(1, 2, 3)
three = FiniteSet(1, 2, 3, 4)
#
subset = one.is_proper_subset(three)
print(subset)
subset = three.is_proper_subset(one)
print(subset)
```

- Is one a proper subset of three ?
- Is three a proper subset of one ?
- What is the output of the print(subset) ?



# Determining Subsets with Sympy

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```
from sympy import FiniteSet
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3)
three = FiniteSet(1, 2, 3, 4)
#
# Set one proper subset set two:
one.is_proper_subset(two) # False
#
# Set two proper subset set one:
two.is_proper_subset(one) # False
#
# Set one proper subset set three:.
one.is_proper_subset(three) # True
#
# Set three proper subset set one:
three.is_proper_subset(one) # False
```



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```
Union and Intersection with Finite Sets
```

```
#______
from sympy import FiniteSet
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3, 4)
#
intersection = one.intersection(two)
print(intersection)
#
union = one.union(two)
print(union)
```

- What is the meaning of one.union(two)?
- What is the meaning of one.intersection(two)?



# As a Venn Diagram

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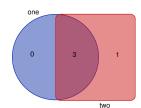
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### Union and Intersection with Finite Sets





# Probability

#### Intersection

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Solution

A die can roll prime numbers ( $\{2, 3, 5\}$ ) or odd numbers ( $\{1, 3, 5\}$ ). What are the chances of a die roll is both prime **AND** odd? To determine this, you calculate the probability of the **intersection** of the two event sets.  $E = A \cap B = \{2, 3, 5\} \cap \{1, 3, 5\} = \{3, 5\}$ 

### Probability of Event A AND Event B

```
#_______
six_sided = FiniteSet(1, 2, 3, 4, 5, 6)
roll_one = FiniteSet(2, 3, 5)
roll_two = FiniteSet(1, 3, 5)
event = roll_one.intersect(roll_two)
prob = len(event) / len(six_sided)
print(prob)
```

- The 'intersect' function connects to a logical 'AND' operation
- The output of this program is 0.333333333333333. Why?



# Probability

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Solution

A die can roll prime numbers ( $\{2, 3, 5\}$ ) or odd numbers ( $\{1, 3, 5\}$ ). What are the chances of a die roll is both prime **OR** odd? To determine this, you calculate the probability of the **union** of the two event sets.  $E = A \cup B = \{2, 3, 5\} \cup \{1, 3, 5\} = \{1, 2, 3, 5\}$ 

### Probability of Event A OR Event B

```
#______
six_sided = FiniteSet(1, 2, 3, 4, 5, 6)
roll_one = FiniteSet(2, 3, 5)
roll_two = FiniteSet(1, 3, 5)
event = roll_one.union(roll_two)
prob = len(event) / len(six_sided)
print(prob)
```

- The 'union' function connects to a logical 'OR' operation
- The output of this program is 0.666666666666666. Why?



# **Creating Solutions**

Check out your sandbox!

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Solutions

