

Discrete Structures: CMPSC 102

BONHAM CARTER

Let's Discuss

Rules

Juive

Further Learning

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Oliver BONHAM-CARTER

Spring 2024 Week 07





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Key Questions

How do I place an equation and a system of logic into Python code?

Learning Objectives

To **remember** and **understand** some the concepts involved with placing mathematical logic into code.



An Easy, *Hard* Problem

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A problem for which Mathematics is not ready. Paul Erdös



Rules: the Collatz or Hailstone Problem

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$$f(x) = \begin{cases} \frac{n}{2} & \text{if } n \equiv 0 \pmod{2} \\ 3n+1 & \text{if } n \equiv 1 \pmod{2} \end{cases}$$

- The 3x+1 problem concerns an iterated function
- The question is to determine whether the function always reaches a value of 1 when starting from any positive integer.



Trajectory

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$$f(x) = \begin{cases} \frac{n}{2} & \text{if n is even} \\ 3n+1 & \text{if n is odd} \end{cases}$$

- Start = 4 (is even)
 - $f(4) = \frac{4}{2} = 2$ (is even)
 - $f(2) = \frac{2}{2} = 1$ (stop here)
- Last three elements of sequence: {4, 2, 1}
- Start = 5 (is odd)
 - f(5) = 3(5) + 1 = 16 (is even)
 - $f(16) = \frac{16}{2} = 8$ (is even)
 - $f(8) = \frac{8}{2} = 4$ (is even) • $f(4) = \frac{4}{2} = 2$ (is even)
 - $f(2) = \frac{2}{3} = 1$ (stop here)
- Last three elements of sequence: {4, 2, 1}



Trajectory

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```
Seed Number: 7
2.
                 even
3.
4.
      34
                 even
5.
      17
6.
      52
                 even
7.
      26
                 even
8.
      13
9.
      40
                 even
10.
      20
11.
      10
12.
13.
      16
                 even
14.
      8
                 even
15.
      4
                 even
16.
17.
```

```
Seed Number: 15
1.
      15
2.
      46
3.
4.
      70
                 even
5.
      35
6.
      106
                 even
      53
      160
8.
9.
      80
                 even
10.
      40
                 even
11.
      20
                 even
12.
      10
13.
      5
14.
      16
                 even
15.
      8
                 even
16.
      4
                 even
17.
                 even
18.
```

```
Seed Number:
                  70
1.
      70
                 even
2.
      35
3.
      106
                 even
4.
      53
      160
5.
      80
6.
                 even
7.
      40
                 even
8.
      20
                 even
9.
      10
10.
11.
      16
12.
      8
                 even
13.
      4
                 even
14.
      2
                 even
15.
      1
```

• All sequences end with {8, 4, 2, 1}



Trajectory

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[+] Seed Number: 106 106 53 3. 160 even 80 5. 40 20 6. 10 8. 16 even 10. even 11. 12. 13.

[+] Se	ed Numbe	r: 600
1.	600	even
2.	300	even
3.	150	even
4.	75	odd
5.	226	even
6.	113	
7.	340	even
8.	170	even
9.	85	
10.	256	even
11.	128	even
12.	64	even
13.	32	even
14.	16	even
15.	8	even
16.	4	even
17.	2	even
18.	1	

39.	29	odd
40.	88	even
41.	44	even
42.	22	even
43.	11	
44.	34	even
45.	17	
46.	52	even
47.	26	even
48.	13	
49.	40	even
50.	20	even
51.	10	even
52.	5	
53.	16	even
54.	8	even
55.	4	even
56.	2	even

• All sequences end with {8, 4, 2, 1}



Your Task!

06_survey_theeXPlusOne_starter

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Make your own sequence builder

- Add functionality to model system of equations to build a sequence
- Allow user to input seed numbers
- Output to screen the 3xplus1 sequence
- Allow program to run without errors.

https://classroom.github.com/a/_XVhojpu





Further Learning

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Further Learning Wikipedia: Collatz Conjecture

• https://en.wikipedia.org/wiki/Collatz_conjecture

- The Simplest Math Problem No One Can Solve Collatz Conjecture
 - https://www.youtube.com/watch?v=094y1Z2wpJg
- UNCRACKABLE? The Collatz Conjecture Numberphile
 - https://www.youtube.com/watch?v=5mFpVDpKX70



Collatz Conjecture in Sets

File: collatz_sets.py

```
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```

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```
def collatz_conjecture(n):
    sequence = set()
    while n != 1:
       if n in sequence:
            # Detected a cycle, exit to avoid infinite loop
            break
        sequence.add(n)
       if n % 2 == 0:
            n = n // 2
        else:
            n = 3 * n + 1
    sequence.add(n)
    return sequence
def main():
    try:
        starting_number = int(input("Enter a positive integer: "))
        if starting_number <= 0:
            raise ValueError("Please enter a positive integer.")
        collatz_sequence = collatz_conjecture(starting_number)
        print(f"Collatz sequence starting from {starting_number}:")
        print(collatz sequence)
        print(f"Length of the sequence: {len(collatz sequence)}")
    except ValueError as ve:
        print(f"Error: {ve}")
if __name__ == "__main__":
   main()
```



Collatz Conjecture in Lists

File: collatz_lists.py

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```
def collatz conjecture(n):
    sequence = [n]
    while n != 1:
       if n % 2 == 0:
           n = n // 2
        else:
           n = 3 * n + 1
        sequence.append(n)
    return sequence
def main():
    # Get user input for the starting number
    starting_number = int(input("Enter a positive integer: "))
    if starting number <= 0:
        print("Please enter a positive integer.")
        return
    # Generate and print the Collatz sequence
    result_sequence = collatz_conjecture(starting_number)
    print(f"The Collatz sequence starting with {starting number}")
    print(f"{result_sequence}")
    print(f"Length of the sequence: {len(result_sequence)}")
if name == " main ":
   main()
```



Creating Solutions

Go check out the fun code about sets in the sandbox/!

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