

Discrete Structures: CMPSC 102

BONHAM CARTER

Let's Discuss

Setup VENV

Kinds of Set

Proper SubSets

Union and Intersection

Probability

Solution

# Discrete Structures: CMPSC 102

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Spring 2024 Week 9





### Let's Discuss

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### **Key Questions**

How do I implement finite sets in Python so that I can calculate and use probabilities?

### Learning Objectives

To **remember** and **understand** some concepts about **sets**, as implemented by SymPy, supporting the calculation of probabilities.



## Mathematical Sets in Python Programs

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- Set theory is useful in mathematics and computer science
- The Sympy package gives an implementation of finite sets
  - Remember, sets are "containers" for other elements
  - The sets in **Sympy** are finite sets, called **FiniteSet**
  - These sets have the same properties as built-in sets
  - FiniteSet has a few features not provided by set
  - A probability is the likelihood that an event will occur
  - We can use either set or FiniteSet to study probabilities
- Investigate probability after exploring an alternative approach to sets



### Setting Up Virtual Environment

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### Create a project directory (outside of lassDocs/)

mkdir projects cd projects

#### Create virtual environment using Python

python3 -m venv myenv
# see the file tree

find . -not -path '\*/\.\*' # UNIX only

dir /s # Windows?

#### Activate myenv the virtual environment

source myenv/bin/activate

#### **Install Dependencies**

pip install sympy



# Creating Sets Import sympy

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### Get into a Python instance from terminal

python3

#### Creating a finite set

```
#_____import sympy as sy
```

#

```
empty_set = sy.FiniteSet()
print(f"{empty_set} :: {type(empty_set)}")
```

# EmptySet :: <class 'sympy.sets.sets.EmptySet'>

#### Creating a finite set

```
import sympy as sy
```

```
finite_set = sy.FiniteSet(2, 4, 6, 8, 10)
print(f"{finite_set} :: {type(empty_set)}")
# <class 'sympy.sets.sets.EmptySet'>
```



## **Creating Sets**

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#### Creating a Set from a List or Tuple

```
"-----
import sympy as sy
#
mylist = [2, 4, 6, 8, 10]
finite_set = sy.FiniteSet(*mylist)
print(finite_set)
#
tuple = (2, 4, 6, 8, 10)
finite_set = sy.FiniteSet(*tuple)
print(finite_set)
```

- All approaches call the FiniteSet constructor
- Can construct a FiniteSet out of a list or a tuple
- What is the purpose of the "\*" in this program?



# The purpose of using "\*" in set()

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We use the "\*" operator for iterable unpacking. For instance, it is used to unpack the elements of the list (mylist) and pass them as separate arguments to the sy.FiniteSet constructor.

```
import sympy as sy
mylist = [1, 2, 3, 4, 5]
```

```
# Without *, crashes
finite_set_without_star = sy.FiniteSet(mylist)
print(f"Without *: {finite_set_without_star}")
```



# The purpose of using "\*" in set()

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```
# With *
finite_set_with_star = sy.FiniteSet(*mylist)
print(f"With *: {finite_set_with_star}")
```

- sy.FiniteSet(\*mylist) is equivalent to explicitly writing sy.FiniteSet(1, 2, 3, 4, 5)
- The \* operator unpacks the elements from the list and provides them as separate arguments to the function or constructor.
- Useful when you have a list of values that you want to pass individually to a function or constructor that expects multiple arguments.



## Working with FiniteSet()

Why do we need this dependency?

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#### Math and Programming Differences

- Programmers cannot use sets like mathematicians do!
- Python programs cannot store an infinite set
- Finite sets must fit into a computer's finite memory
- Programs need a procedure for constructing the set
- Different programming languages and packages have other restrictions. For instance, recall that Python programs cannot create sets that contain mutable elements like lists! Why do you think that this is the case?
- So, what are the **benefits** of using sets in Python programs?
- Importantly, sets come with some super-useful default operations!
- Thankfully, sympy contains even more basic operations!



## **Creating Sets**

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```
Using Finite Sets in Sympy
```

```
#_____
from sympy import FiniteSet
#
list = [1, 2, 3, 2]
finite_set = FiniteSet(*list)
print(finite_set)
#
for element in finite_set: # iteration
    print(element)
```

- What is the output of print(finite\_set) ?
- What is the output of print(element) in the for loop?
- How do these two output segments differ?



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```
Subset Relationships with Finite Sets
```

```
from sympy import FiniteSet
#
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3)
#
subset = one.is_proper_subset(two)
print(subset)
subset = two.is_proper_subset(one)
print(subset)
```

- What is the mathematical definition of a proper subset?
- What is the purpose of the is\_proper\_subset function?
- What is the output of the print(subset) function calls?



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#### Subsets with Finite Sets

- Is one a proper subset of three ?
- Is three a proper subset of one ?
- What is the output of the print(subset) ?



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```
from sympy import FiniteSet
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3)
three = FiniteSet(1, 2, 3, 4)
#
# Set one proper subset set two:
one.is_proper_subset(two) # False
#
# Set two proper subset set one:
two.is_proper_subset(one) # False
#
# Set one proper subset set three:.
one.is_proper_subset(three) # True
#
# Set three proper subset set one:
three.is_proper_subset(one) # False
```



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```
Union and Intersection with Finite Sets
```

```
#______
from sympy import FiniteSet
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3, 4)
#
intersection = one.intersection(two)
print(intersection)
#
union = one.union(two)
print(union)
```

- What is the meaning of one.union(two) ?
- What is the meaning of one.intersection(two)?



## Relationships As a Venn Diagram

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### Union and Intersection with Finite Sets

```
#_____
one = FiniteSet(1, 2, 3)
two = FiniteSet(1, 2, 3, 4)
#
intersection = one.intersection(two)
print(intersection) # {1, 2, 3}
print(len(intersection)) # 3 (understand your output!!)
#
union = one.union(two)
print(union) #{1, 2, 3, 4}
print(len(union)) # 4 (understand your output!!)
```





### Probability Intersection

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A die can roll prime numbers ( $\{2, 3, 5\}$ ) or odd numbers ( $\{1, 3, 5\}$ ). What are the chances of a die roll is both prime **AND** odd? To determine this, you calculate the probability of the **intersection** of the two event sets over all possible outcomes.  $E = A \cap B = \{2, 3, 5\} \cap \{1, 3, 5\} = \{3, 5\}$ 

### Probability of Event A AND Event B

- The 'intersect' function connects to a logical 'AND' operation
- The output of this program is 0.333333333333333. Why?



# Probability Union

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Solution

A die can roll prime numbers ( $\{2, 3, 5\}$ ) or odd numbers ( $\{1, 3, 5\}$ ). What are the chances of a die roll is both prime **OR** odd? To determine this, you calculate the probability of the **union** of the two event sets over all possible outcomes.  $E = A \cup B = \{2, 3, 5\} \cup \{1, 3, 5\} = \{1, 2, 3, 5\}$ 

### Probability of Event A **OR** Event B

```
#______
six_sided = FiniteSet(1, 2, 3, 4, 5, 6)
roll_one = FiniteSet(2, 3, 5)
roll_two = FiniteSet(1, 3, 5)
event = roll_one.union(roll_two)
prob = len(event) / len(six_sided) # over all outcomes
print(prob)
```

- The 'union' function connects to a logical 'OR' operation
- The output of this program is 0.666666666666666. Why?



# Creating Solutions Check out your sandbox!

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