Programming Languages

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1/59

Scanning and Parsing

Scanner: translate source code to tokens (e.g., < int >, +, < id >)

• Report lexical errors like illegal characters and illegal symbols.

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Scanner: translate source code to tokens (e.g., < int >, +, < id >)

• Report lexical errors like illegal characters and illegal symbols.

Parser: read token stream and reconstruct the derivation.

• Reports parsing errors – i.e., source that is not derivable from the grammar. E.g., mismatched parenthesis/braces, nonsensical statements (x = 1 +;)

What is Syntax Analysis aka Parsing?

- After lexical analysis (scanning), we have a series of tokens.
- In syntax analysis (or parsing), we want to interpret what those tokens mean.

3/59

What is Syntax Analysis aka Parsing?

- After lexical analysis (scanning), we have a series of tokens.
- In syntax analysis (or parsing), we want to interpret what those tokens mean.
- Goal: Recover the structure described by that series of tokens.
- Goal: Report errors if those tokens do not properly encode a structure.

3 / 59

Formal Languages

- An alphabet is a set \sum of symbols that act as letters.
- A language over \sum is a set of strings made from symbols in \sum .

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- When scanning, our alphabet is ASCII or Unicode characters. We produced tokens.
- When parsing, our alphabet is the set of tokens produced by the scanner.

Grammar

Grammar consists of the following::

- 1 a set of terminals (same as an alphabet)
- 2 a set of non-terminal symbols, including a starting symbol
- 3 a set of rules

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Grammar consists of the following::

- 1 a set of terminals (same as an alphabet)
- 2 a set of non-terminal symbols, including a starting symbol
- a set of rules
- \bullet Strings are derived from a grammar (e.g., S \to aS \to aaS \to aabA \to aab)
- At each step, a non-terminal is replaced by the sentential form on the right-hand side of a rule (a sentential form can contain non-terminals and/or terminals)
- Grammars generate languages

Sentential Form

- If $S \to *\alpha$, the string α is called a sentential form of the grammar.
- In the derivation $S \to \beta_1 \to \beta_2 \to ... \to \beta_n$, each of the β_i are sentential forms.
- A sentential form in a rightmost derivation is called a right-sentential form (similarly for leftmost and left-sentential).

Context-Free Grammar

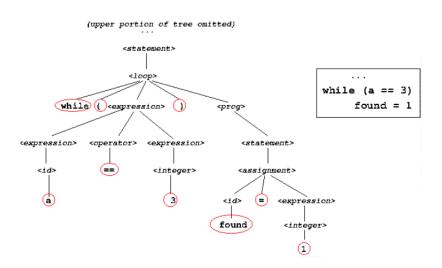
- A context-free grammar (or CFG) is a formalism for defining languages.
- A grammar is said to be context-free if every rule has a single non-terminal on the left-hand side
- This means you can apply the rule in any context.

Context-Free Grammar

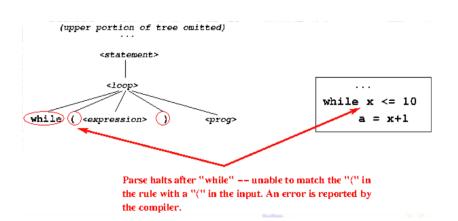
Formally, a context-free grammar (as is the regular grammar) is a collection of four objects:

- A set of nonterminal symbols (or variables),
- A set of terminal symbols,
- A set of production rules saying how each nonterminal can be converted by a string of terminals and nonterminals, and
- A start symbol that begins the derivation.

Sample Parse Tree (portion)



Sample Parse Tree (failed)



Grammars for Java (version 8) and Python3

```
Java: Overview of notation used:
  https:
  //docs.oracle.com/javase/specs/jls/se8/html/jls-2.html
```

- Java: The full syntax grammar:
 https:
 //docs.oracle.com/javase/specs/jls/se8/html/jls-19.html
- Python: The full grammar: https://docs.python.org/3/reference/grammar.html

Parsing Algorithms

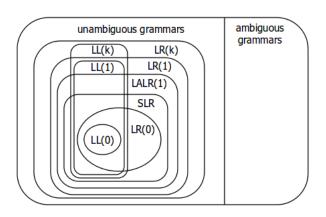
LL Parsing (Left to right scan, Leftmost derivation)

- Top-down: start with grammar start symbol, work your way down until you get to terminals
- Generates a leftmost derivation (the leftmost derivation assuming unambiguous grammar)

Parsing Algorithms

- LL Parsing (Left to right scan, Leftmost derivation)
 - Top-down: start with grammar start symbol, work your way down until you get to terminals
 - Generates a leftmost derivation (the leftmost derivation assuming unambiguous grammar)
- LR Parsing (Left to right scan, Rightmost derivation (reverse rightmost))
 - Bottom-up: apply productions in reverse to convert the user's program to the start symbol
 - ullet Almost all practical programming languages have an LR(1) grammar

Language Hierarchies



Bottom-up Parsing Strategies

Beginning with the user's program, try to apply productions in reverse to convert the program back into the start symbol

Top-down Parsing Strategies

- Begin at root with a start symbol of the grammar
- Repeatedly pick a non-terminal and expand
- Success when expanded tree matches input

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- LL(k)

Beginning with the start symbol, try to guess the productions to apply to end up at the user's program.

Challenges in Top-down Parsing

- Top-down parsing begins with virtually no information.
- Begins with just the start symbol, which matches every program.
- How can we know which productions to apply?

Challenges in Top-down Parsing

- Top-down parsing begins with virtually no information.
- Begins with just the start symbol, which matches every program.
- How can we know which productions to apply?
 - Guess and backtrack if we are wrong backtracking algorithms (BFS/DFS).
 - Based on remaining input, predict (without backtracking) which production to use - predictive algorithms (LL(1))

A Simple Predictive Parser: LL(1)

Top-down, predictive parsing:

- L: Left-to-right scan of the tokens
- L: Leftmost derivation
- (1): One token of lookahead

A Simple Predictive Parser: LL(1)

Top-down, predictive parsing:

- L: Left-to-right scan of the tokens
- L: Leftmost derivation
- (1): One token of lookahead
- Construct a leftmost derivation for the sequence of tokens.
- When expanding a non-terminal, we predict the production to use by looking at the next token of the input. The decision is forced.

LL(1) Algorithm: FYI

Suppose a grammar has start symbol S and LL(1) parsing table T. We want to parse string ω .

- Initialize a stack containing S \$.
- Repeat until the stack is empty:
 - Let the next character of ω be t.
 - If the top of the stack is a terminal r:
 - If r and t don't match, report an error.
 - Otherwise consume the character t and pop r from the stack.
 - Otherwise, the top of the stack is a non-terminal A:
 - If T[A,t] is undefined, report an error.
 - Replace the top of the stack with T[A,t].

Lox Interpreter Parser: Top Down

- Starts from the top or outermost grammar rule
- Goes down into the nested subexpressions
- Gets to the leaves of the syntax tree

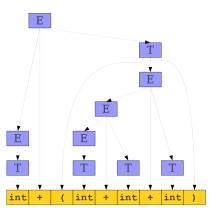
Bottom Up Parsing



Idea: Apply productions in reverse to convert the user's program to the start symbol.

Bottom Up Parsing





Bottom Up Parsing

```
\mathbf{E} \to \mathbf{T}
                             int + (int + int + int)
\mathbf{E} \to \mathbf{E} + \mathbf{T}
                         \Rightarrow T + (int + int + int)
T \rightarrow int
                         \Rightarrow E + (int + int + int)
T \rightarrow (E)
                         \Rightarrow E + (T + int + int)
                         \Rightarrow E + (E + int + int)
                         \Rightarrow E + (E + T + int)
                         \Rightarrow E + (E + int)
                         \Rightarrow E + (E + T)
                         \Rightarrow \mathbf{E} + (\mathbf{E})
                         \Rightarrow \mathbf{E} + \mathbf{T}
                         \Rightarrow \mathbf{E}
```

Bottom-Up Parsing

- The handle of the right-sentential form is a substring corresponding to the right-hand side of the production that produced it from the previous step in the rightmost derivation.
- Handle can also be represented as the production and the position of the last symbol being replaced.
- A left-to-right, bottom-up parse works by iteratively searching for a handle, then reducing the handle.

Shift/Reduce Algorithm

- One type of bottom-up parsers are called shift/reduce parsers.
- Idea: Split the input into two parts:
 - Left substring is our work area; all handles must be here.
 - Right substring is input we have not yet processed; consists purely of terminals.
- At each point, decide whether to:
 - Move a terminal across the split (shift)
 - Reduce a handle (reduce)

Shift/Reduce Algorithm

$$\mathbf{E} \rightarrow \mathbf{F}$$
 $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{F}$
 $\mathbf{F} \rightarrow \mathbf{F} \star \mathbf{T}$
 $\mathbf{F} \rightarrow \mathbf{T}$
 $\mathbf{T} \rightarrow \mathbf{int}$
 $\mathbf{T} \rightarrow (\mathbf{E})$

Shift/Reduce Algorithm

$$E \rightarrow F$$
 $E \rightarrow E + F$
 $F \rightarrow F * T$
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 $T \rightarrow int$
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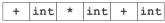


26 / 59

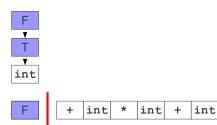
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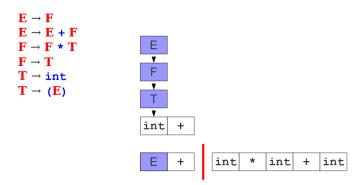




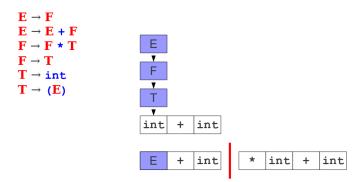


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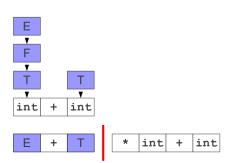


30 / 59

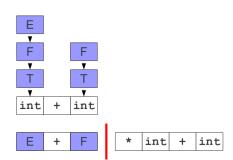


31/59

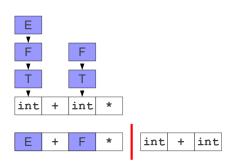
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$$E \rightarrow F$$

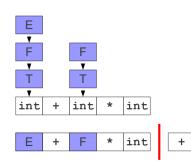
$$E \rightarrow E + F$$

$$F \rightarrow F * T$$

$$F \rightarrow T$$

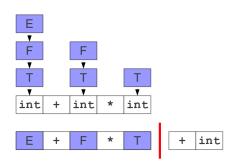
$$T \rightarrow int$$

$$T \rightarrow (E)$$

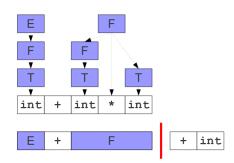


int

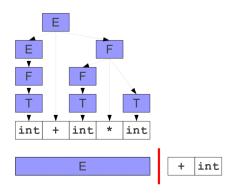
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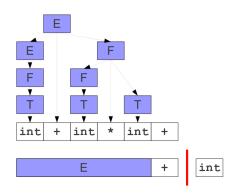
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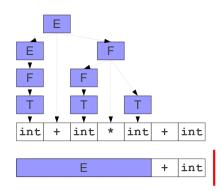
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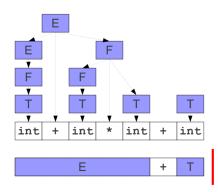




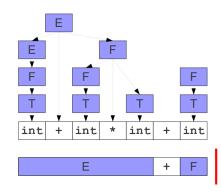
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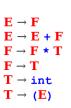


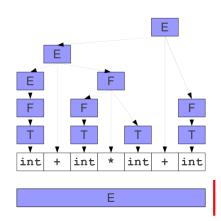
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Activity 3.2: Shift/Reduce Algorithm

Trace through the shift-reduce algorithm given the input: https://forms.gle/fvSRJFqpnTeBskKx6

44 / 59

Observations

- Since reductions are always at the right side of the left area, we never need to shift from the left to the right.
- No need to "uncover" something to do a reduction.
- Consequently, shift/reduce parsing means
 Shift: Move a terminal from the right to the left area.
 Reduce: Replace some number of symbols at the right side of the left area.

Observations

- All activity in a shift/reduce parser is at the far right end of the left area.
- Idea: Represent the left area as a stack.

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- All activity in a shift/reduce parser is at the far right end of the left area.
- Idea: Represent the left area as a stack.
- Shift: Push the next terminal onto the stack.
- Reduce: Pop some number of symbols from the stack, then push the appropriate non-terminal.

Reduce when we know we have a handle.

Finding Handles

- Where do we look for handles?
 - At the top of the stack.

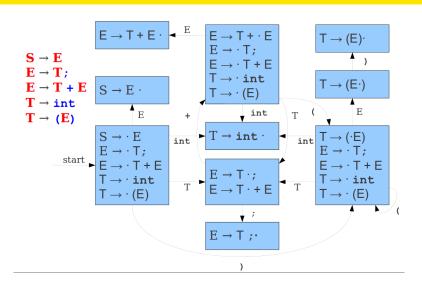
Finding Handles

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Finding Handles

- Where do we look for handles?
 - At the top of the stack.
- How do we search for possible handles?
 - Build a handle-finding automaton.
- How do we recognize handles?
 - Once we have found a candidate handle, how do we check that it really is the handle?

A Deterministic Automaton



Handle Recognition

- Our automaton will tell us all places where a handle might be.
- However, if the automaton says that there might be a handle at a given point, we need a way to confirm this.

Handle Recognition

- Our automaton will tell us all places where a handle might be.
- However, if the automaton says that there might be a handle at a given point, we need a way to confirm this.
- We can use predictive bottom-up parsing: Have a deterministic procedure for guessing where handles are.
- There are many predictive algorithms, each of which recognize different grammars.

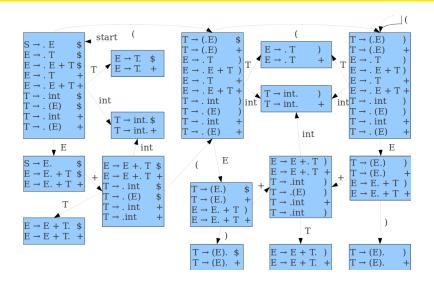
- Bottom-up predictive parsing with:
 - L:Left-to-right scan
 - R:Rightmost derivation
 - (1): One token lookahead
- Tries to intelligently find handles by using a lookahead token at each step.

- Guess which series of productions we are reversing.
- Use this information to maintain information about what lookahead to expect.
- When deciding whether to shift or reduce, use lookahead to disambiguate.

- How do we know what lookahead to expect at each state?
- Observation:
 - There are only finitely many productions we can be in at any point.
 - There are only finitely many positions we can be in each production.
 - There are only **finitely many lookahead sets** at each point.

- How do we know what lookahead to expect at each state?
- Observation:
 - There are only finitely many productions we can be in at any point.
 - There are only finitely many positions we can be in each production.
 - There are only **finitely many lookahead sets** at each point.
 - Construct an automaton to track lookaheads!

A Deterministic LR(1) Automata



53 / 59

Representing LR(1) Automata

- LR(1) parsers are usually represented via two tables: an action table and a goto table.
- The action table maps each state to an action:
 - shift, which shifts the next terminal, and
 - reduce $A \rightarrow \omega$, which performs reduction.

Representing LR(1) Automata

- LR(1) parsers are usually represented via two tables: an action table and a goto table.
- The action table maps each state to an action:
 - shift, which shifts the next terminal, and
 - reduce $A \rightarrow \omega$, which performs reduction.
- Any state of the form $A \to \omega \cdot$ does that reduction; everything else shifts.
- The goto table maps state/symbol pairs to a next state.
- This is just the transition table for the automaton.

LR Parsing table

| (1) (2) | Е | \rightarrow | Ε | + | Т | |
|------------|---|---------------|---|---|---|--|
| (2) | F | \rightarrow | т | | | |

 $(3) T \rightarrow (E)$

| State | | Action | | Goto Goto | | | | |
|-------|----|--------|----|-----------|--------|----|----------|--|
| Olato | | Action | | | | | <u> </u> | |
| | id | + | (|) | \$ | E | T | |
| 0 | S4 | | S3 | | | S1 | S2 | |
| 1 | | S5 | | | accept | | | |
| 2 | R2 | R2 | R2 | R2 | R2 | | | |
| 3 | S4 | | S3 | | | S6 | S2 | |
| 4 | R4 | R4 | R4 | R4 | R4 | | | |
| 5 | S4 | | S3 | | | | S8 | |
| 6 | | S5 | | S7 | | | | |
| 7 | R3 | R3 | R3 | R3 | R3 | | | |
| 8 | R1 | R1 | R1 | R1 | R1 | | | |

LR Parsing table

| S→E |
|--------------|
| E→T E+T |
| T → id (E) |

| | | | , , , |
|-------------|-----------------|-----------------------------|--------------------------|
| Parse Stack | Remaining Input | Action | Input: (id + id) |
| | (id + id) \$ | Shift (| The state (that it stary |
| (| id + id) \$ | Shift id | |
| (id | + id) \$ | Reduce T → id | |
| (T | + id) \$ | Reduce E → T | |
| (E | + id) \$ | Shift + | |
| (E+ | id) \$ | Shift id | |
| (E+id |)\$ | Reduce T → id | |
| (E+T |)\$ | Reduce E → E+T; (Ignore: E→ | ·T) |
| (E |)\$ | Shift) | |
| (E) | \$ | Reduce T → (E) | |
| Т | \$ | Reduce E → T | |
| E | \$ | Reduce S → E | |
| s | \$ | Accept | |

LR Parser

| | | | | | | | | _ |
|----------|------------------|----|----|----|--------|----|----|-----|
| State on | on <u>Action</u> | | | | Goto | | 1 | |
| TOS | id | + | (|) | \$ | E | T |] (|
| 0 | S4 | | S3 | | | S1 | S2 |] (|
| 1 | | S5 | | | accept | | | 7. |
| 2 | R2 | R2 | R2 | R2 | R2 | | | (. |
| 3 | S4 | | S3 | | | S6 | S2 | (4 |
| 4 | R4 | R4 | R4 | R4 | R4 | | | 1 |
| 5 | S4 | | S3 | | | | S8 | 7 |
| 6 | | S5 | | S7 | | | | |
| 7 | R3 | R3 | R3 | R3 | R3 | | | |
| 8 | R1 | R1 | R1 | R1 | R1 | | | |

| $(1) E \rightarrow E + T$ | |
|---------------------------|--|
| (2) E → T | |
| (3) T → (E) | |
| (4) T \rightarrow id | |

| State stack | Remaining Input | Parser action |
|--------------|-----------------|---|
| S0 | id + (id)\$ | Shift S4 onto state stack, move ahead in input |
| S0S4 | + (id)\$ | Reduce 4) T → id, pop state stack, goto S2, input unchanged |
| S0S2 | + (id)\$ | Reduce 2) E → T, goto S1 |
| S0S1 | + (id)\$ | Shift S5 |
| S0S1S5 | (id)\$ | Shift S3 |
| S0S1S5S3 | id)\$ | Shift S4 (saw another id) |
| S0S1S5S3S4 |)\$ | Reduce 4) T → id, goto S2 |
| S0S1S5S3S2 |)\$ | Reduce 2) E → T, goto S6 |
| S0S1S5S3S6 |)\$ | Shift S7 |
| S0S1S5S3S6S7 | \$ | Reduce 3) T → (E), goto S8 |
| S0S1S5S8 | \$ | Reduce 1) F → F + T goto S1 * |

LR(1) Algorithm

• Begin with an empty stack and the input set to ω \$, where ω is the string to parse. Set **state** to the initial state.

LR(1) Algorithm

- Begin with an empty stack and the input set to ω \$, where ω is the string to parse. Set **state** to the initial state.
- Repeat the following:
 - Let the next symbol of input be t.
 - If action[state,t] is shift, then shift the input and set state=goto[state,t].
 - If action[state,t] is reduce $A \rightarrow \omega$:
 - Pop $|\omega|$ symbols off the stack; replace them with A.
 - Let the state atop the stack be top-state.
 - Set state=goto[top-state,A]
 - If action[state,t] is accept, then the parse is done.
 - If action[state,t] is error, report an error.

LALR(1)

Look Ahead LR Parser

- LR(1) produces numerous states.
- LALR(1): merge similar states:
 - same core (LR(0))
 - only differences in lookaheads