O(1) - CONSTANT TIME

The Lightning Fast Algorithm - Always the Same Speed!

CS 101 - Fall 2025

What is O(1) - Constant Time?



• The Superpower of Algorithms

O(1) means the algorithm takes the same amount of time no matter how much data

Real-World Analogy: * Like a valet parking service - you hand over your ticket and get your car back instantly * Whether there are 10 cars or 10,000 cars in the lot, it takes the same time! * The valet has a direct system to find your exact car

Performance Guarantee

- 10 items \rightarrow 1 step
- $100 \text{ items} \rightarrow 1 \text{ step}$
- $1,000,000 \text{ items} \to 1 \text{ step}$
- Same speed forever!

Key Insight

The algorithm has a "shortcut" that goes directly to the answer without checking other data!

Magic Question:

"Can I get the answer without looking at most of the data?"

What Makes O(1) So Fast?

The Secret Ingredients

O(1) algorithms use smart data organization and direct access patterns

Hash Tables (Dictionaries/Sets)

```
# Python dictionary uses hash function
student_grades = {
    "Alice": 95,
    "Bob": 87,
    "Charlie": 92
}

# Hash function calculates EXACTLY where
# "Alice" is stored in memory
grade = student_grades["Alice"] # O(1)!
```

How it works:

- 1. Hash function: "Alice" \rightarrow memory location 147
- 2. Go directly to location 147
- 3. Get the value (95)
- 4. Done! No searching needed!

Array Indexing

Mathematical Magic:

- Memory address = Base + $(2 \times 4 \text{ bytes})$ = Direct jump!
- No need to check scores[0] or scores[1]
- Jump straight to the answer!

Interactive O(1) Dictionary Demo

```
See O(1) in Action!
```

Try looking up different students' grades. Notice how it's always instant, no matter which student you choose!

Python O(1) Examples - The Fast Ones!

Dictionary Operations

```
# Creating a gradebook
gradebook = {
    "Alice": 95,
    "Bob": 87,
    "Charlie": 92,
    "Diana": 88
}
# All of these are O(1) - instant!
alice_grade = gradebook["Alice"] # Lookup: 0(1)
gradebook["Eve"] = 90
                                    # Insert: 0(1)
gradebook["Bob"] = 89
                                    # Update: 0(1)
del gradebook["Charlie"]
                                     # Delete: 0(1)
# Check if student exists
if "Diana" in gradebook:
                                      # Membership: O(1)
    print("Diana is in the class!")
print(f"Class size: {len(gradebook)}") # Length: 0(1)
```

List Operations (by index)

```
# Student scores list
scores = [95, 87, 92, 78, 85, 91, 88]

# These are O(1) - direct access
first_score = scores[0]  # Get first: O(1)
last_score = scores[-1]  # Get last: O(1)
middle_score = scores[3]  # Get by index: O(1)
```

```
print(f" Scores BEFORE update = {scores}")
                                      # Update by index: O(1)
scores[2] = 94
                                      # overwrite previous value
print(f" Scores AFTER update = {scores}")
# Stack operations (end of list)
scores.append(96)
                                      # Add to end: O(1)
final_score = scores.pop()
                                    # Remove from end: O(1)
print(f"Total scores: {len(scores)}") # Length: O(1)
```

Important Note

Not all list operations are O(1)!

- scores.insert(0, 100) is O(n) inserting at beginning
- scores.remove(87) is O(n) searching for value
- 87 in scores is O(n) searching through list

Set Operations - Another O(1) Champion!

Note

Are there differences in search times?

Set Basics

```
# Create a set of student IDs
enrolled_students = {101, 102, 103, 104, 105}
# All O(1) operations
enrolled_students.add(106)
                                   # Add: O(1)
enrolled_students.remove(103)
                                   # Remove: 0(1)
# The magic of O(1) membership testing!
if 104 in enrolled_students: # Check: O(1)
   print("Student 104 is enrolled!")
```

```
# Compare with list - this would be O(n)
student_list = [101, 102, 103, 104, 105]
if 104 in student_list: # O(n) - slow!
    print("Found in list (but slowly)")
```

Real Performance Difference

```
import time
# Large dataset
                                # 100k numbers
large_list = list(range(100000))
large_set = set(range(100000))
                                     # Same 100k numbers
target = 99999 # Last item (worst case)
# Timing list search - O(n)
start = time.time()
found = target in large_list
                                  # Checks all 100k!
list_time = time.time() - start
# Timing set search - O(1)
start = time.time()
                             # Instant!
found = target in large_set
set_time = time.time() - start + 0.001 # Add error time
print(f"List search: {list_time:.6f} seconds")
print(f"Set search: {set_time:.6f} seconds")
print(f"Set is {list_time/set_time:.0f}x faster!")
```

Partner Activity: O(1) Experiments!

Instructions: Find a partner and complete these experiments together. Discuss your observations!

Experiment 1: Dictionary vs List Race

```
import time
import random
```

```
# Create test data with your partner
def create_test_data(size):
    data = [f"student_{i}" for i in range(size)]
    data_dict = {name: f"grade_{i}" for i, name in enumerate(data)}
   return data, data_dict
# Partner A: Test small dataset (100 items)
# Partner B: Test large dataset (10,000 items)
sizes = [100, 10000] # Choose one each
for size in sizes:
    data_list, data_dict = create_test_data(size)
    target = f"student_{size-1}" # Last item (worst case)
    # Time list search (O(n))
    start = time.time()
   found = target in data_list
   list_time = time.time() - start
    # Time dict search (O(1))
    start = time.time()
    found = target in data_dict
    dict_time = time.time() - start
   print(f"Size {size}:")
   print(f" List search: {list_time:.6f} seconds")
   print(f" Dict search: {dict_time:.6f} seconds")
    # zero division precaution: add 0.001 to denominator
    print(f" Dict is {list_time/(dict_time+0.001):.0f}x faster!")
```

Discussion Questions:

- What happened to the performance difference as data size increased?
- Why doesn't dictionary search time change much?

Experiment 2: Hash Table Investigation

```
# Build a student grade system together
student_grades = {}

# Partner A: Add students with IDs 1-1000
# Partner B: Add students with IDs 1001-2000
```

```
def add_students(start_id, end_id, grades_dict):
    import time
    start = time.time()
    for i in range(start_id, end_id + 1):
        grades_dict[f"student_{i}"] = random.randint(70, 100)
    end = time.time()
    return end - start
# Time your additions
partner_a_time = add_students(1, 1000, student_grades)
partner_b_time = add_students(1001, 2000, student_grades)
# Now test random lookups
def test_lookups(grades_dict, num_tests=100):
    import time
    start = time.time()
    for _ in range(num_tests):
        random_id = random.randint(1, 2000)
        grade = grades_dict.get(f"student_{random_id}", "Not found")
    return time.time() - start
lookup_time = test_lookups(student_grades)
print(f"Adding 1000 students: ~{partner_a_time:.4f} seconds each")
print(f"100 lookups in {len(student_grades)} students: {lookup_time:.6f} seconds")
```

Partner Discussion:

- Did adding more students slow down individual lookups?
- How would this compare with a simple list of 2000 students?

O(1) Scenario Analysis: Group Discussion Prompts

i Class Discussion Questions

Work in groups of 3-4. Discuss these scenarios and be ready to share insights!

Important

Discuss with your group:

- 1. **Social Media Apps**: When you open Instagram/TikTok, your profile loads instantly regardless of how many users the app has. What O(1) operations make this possible?
- 2. **Online Shopping**: Amazon can instantly tell you if an item is in stock, even with millions of products. How might they achieve O(1) inventory checks?
- 3. Video Games: In a multiplayer game with thousands of players, you can instantly see your own stats. What data structure enables O(1) player data retrieval?
- 4. **School Systems**: Your student portal shows your GPA instantly, even though the school has thousands of students. What makes this O(1)?

Group Challenge: Design a simple system for one of these scenarios using Python dictionaries. How would you organize the data for O(1) access?

O(1) Scenario Analysis: Critical Thinking

i Class Discussion Questions

Work in groups of 3-4. Discuss these scenarios and be ready to share insights!

Important

Discuss with your group:

- 5. **Trade-off Analysis**: O(1) operations often require extra memory (like hash tables). When is this trade-off worth it? When might it not be?
- 6. **Failure Cases**: Can you think of situations where a dictionary lookup might NOT be O(1)? (Hint: Think about hash collisions)
- 7. **Design Decisions**: You're building an app that needs to store user preferences. Would you use a list or dictionary? Why? How would your choice affect performance with 1 user vs 1 million users?

8. **Performance Prediction**: If a dictionary lookup takes 0.001 seconds with 1,000 items, how long should it take with 1,000,000 items? Why?

Your Turn: Practice O(1) Operations!



Individual Coding Exercises

After your group discussions, try these hands-on exercises to solidify your understanding.

Exercise 1: Phone Book

```
# Create your own phone book
phone_book = {}
# Add contacts (O(1) each)
phone_book["Mom"] = "555-0123"
phone_book["Pizza Place"] = "555-PIZZA"
phone_book["Best Friend"] = "555-9999"
# Look up numbers instantly
print(f"Mom's number: {phone_book['Mom']}")
# Your task: Add 5 more contacts and
# time how long it takes to look them up!
import time
start = time.time()
# Add your lookups here
end = time.time()
print(f"Lookup time: {end - start} seconds")
```

Exercise 2: Student Checker

```
# Create sets for different classes
math_class = {"Alice", "Bob", "Charlie"}
science_class = {"Bob", "Diana", "Eve"}
history_class = {"Alice", "Eve", "Frank"}
# Check enrollment instantly (O(1))
student = "Alice"
```

```
enrolled_classes = []
# Check to see whether item is in dictionary
# add subject name to new list if student is enrolled
if student in math_class:
    enrolled_classes.append("Math")
if student in science_class:
    enrolled_classes.append("Science")
if student in history_class:
    enrolled_classes.append("History")
print(f"{student} is in: {enrolled_classes}")
# Your task: Check enrollment for all students
# and see how fast it is!
```

When NOT to Use O(1) Approaches



 \triangle O(1) Has Limitations!

While O(1) is amazing, it's not always possible or practical.

When O(1) Won't Work

```
# These operations CANNOT be O(1):
scores = [95, 87, 92, 78, 85]
# Finding maximum - must check all values
                        # O(n) - no shortcut!
max_score = max(scores)
# Counting specific values
count_90s = scores.count(90) # O(n) - must check all
# Finding an item in unsorted list
position = scores.index(92) # O(n) - no direct path
# Sorting data
scores.sort()
                                # O(n log n) - complex!
```

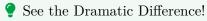
Why?

No way to know the answer without examining the data!

Trade-offs to Consider

```
# Memory vs Speed Trade-off
students = ["Alice", "Bob", "Charlie", "Diana"]
# Option 1: List (less memory, slower search)
if "Bob" in students: # O(n) - slow search
   print("Found Bob!")
# Option 2: Set (more memory, faster search)
# Note: Sets contain only unique items.
# Although time and energy is required to complete
# operations involved with creating sets ...
                              # Uses more memory
student_set = set(students)
if "Bob" in student_set:
                               # 0(1) - fast search!
   print("Found Bob!")
# Choice depends on:
# - How often do you search?
# - How much memory do you have?
# - How large is your data?
```

Comparing O(1) to Other Complexities



Let's compare O(1) to other complexities with real numbers.

Data Size	O(1)	O(log n)	O(n)	$O(n^2)$	Real-World Impact
10 items 100 items	1 step 1 step	~3 steps ~7 steps	10 steps 100 steps	100 steps 10,000 steps	All feel instant O(1) still instant
1,000 items	1 step	~10 steps	1,000 steps	1,000,000 steps	Only $O(1)$ stays fast
1,000,000 items	1 step	~20 steps	1,000,000 steps	1	

The O(1) Advantage

Dictionary lookup with 1 million entries = Same speed as with 10 entries! This is why Google can search billions of web pages instantly - they use hash tables and other O(1) techniques!

Summary: O(1) - The Algorithm Superhero!

? Key Takeaways

O(1) - Constant Time is the gold standard of algorithm efficiency!

What Makes O(1) Special

- Always the same speed no matter how much data
- Direct access patterns no searching required
- Smart data structures hash tables, arrays
- Real-world applications Google search, databases, caches

Python O(1) Champions:

- Dictionary operations: dict[key], dict[key] = value
- Set operations: item in set, set.add(item)
- List indexing: list[0], list[-1]
- Stack operations: list.append(), list.pop()

Programming Wisdom

```
# Choose your data structure wisely!

# For frequent lookups
use_dict = {"key": "value"}  # 0(1) lookup

# not_list = ["key", "value"]  # 0(n) lookup

# For membership testing
use_set = {1, 2, 3, 4, 5}  # 0(1) testing
# not_list = [1, 2, 3, 4, 5]  # 0(n) testing

# For indexed access
use_list = [1, 2, 3, 4, 5]  # 0(1) by index
# Perfect for stacks and queues
```

Remember: O(1) is not always possible, but when it is, it's magical!

Next: Exploring O(log n) - The Smart Searcher!

Coming Up Next

 $O(\log n)$ - Logarithmic Time * Binary search and divide-and-conquer strategies * Why "halving" is so powerful * Interactive binary search demonstrations * When $O(\log n)$ beats O(n) by huge margins

Questions to Think About: * When might you need to give up O(1) for O(log n)? * How can "smart searching" be almost as good as direct access? * What's the trade-off between data organization and search speed?

Ready to see how smart algorithms can be nearly as fast as O(1)?