

Handout: Rasterizing Lines

A. Naive approach: use line equation, _____

```
// first octant,  $0 < m < 1$ 
```

```
m = _____
```

```
b = _____
```

```
for( x = ____; x ≤ ____; ++x )    ←
```

```
    y = _____
```

```
    plot( x, _____ )    ← choose the pixel _____
```

Inefficient due to _____ .

B. Improvement:

```
Yi    = _____
```

```
Yi+1  = _____ + b
```

```
        = ____ ( _____ ) + b
```

```
        = _____
```

```
        = _____
```

```
Yi+1  = _____    ← next value of y obtained by _____
```

C. Pseudo-code:

```
// first octant,  $0 < m < 1$ , line from  $(x_1, y_1)$  to  $(x_2, y_2)$ 
```

```
compute ____
```

```
compute ____
```

No multiplies \Rightarrow this is called an

```
plot( __, __ )
```

" _____ "

```
compute ____
```

or, a "DDA":

```
y = ____
```

" _____ "

```
while( _____ )
```

```
    increment  $x_1$  by ____
```

```
    increment y by ____
```

```
    plot(  $x_1$ , _____ )
```

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```
// DDA, all octants (lab assignment implements!):
```

```
compute ____
```

```
compute ____
```

```
plot( __, __ )
```

```
// Shallow slope case (can be either ____ or ____ ):
```

```
if ____ < slope < ____
```

```
    compute m
```

```
    // Do we increment or decrement x ?
```

```
    dx < 0  $\Rightarrow$  _____ , otherwise _____
```

```
    // Make slope + or -
```

```
    m = _____
```

```
    y = _____
```

```
    while( _____ )
```

```
        increment  $x_1$  by _____
```

```
        increment y by _____
```

```
        plot(  $x_1$ , floor(y + 0.5) )
```

```
else // Steep slope case: _____
```

```
    // same algorithm as above, except
```

```
    // switch _____ and _____, _____ and _____
```

```
    plot(floor(x + 0.5),  $y_1$  )
```

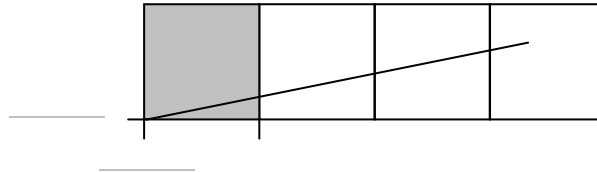
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Bresenham's Algorithm (1st octant illustrates the general idea but extends to all octants)

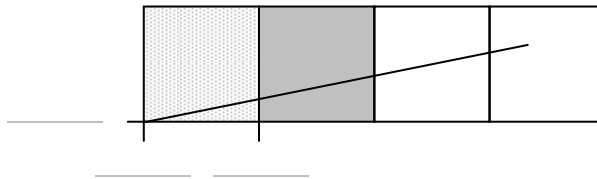
1st octant \Rightarrow _____. Rasterizing a line from _____ to _____.

Starting at _____, increment _____ each time.

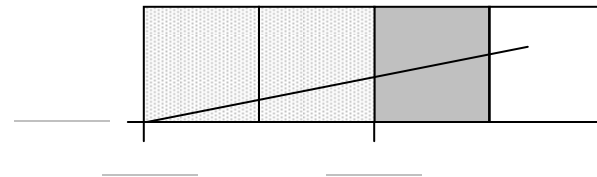
Question: As we move to the right, _____?



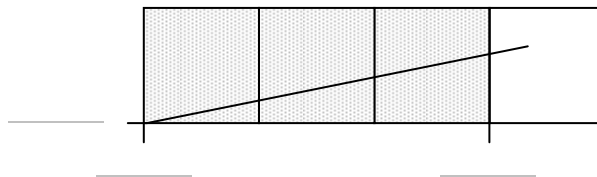
Keep track of _____ the distance from _____ to _____ of the line at _____.



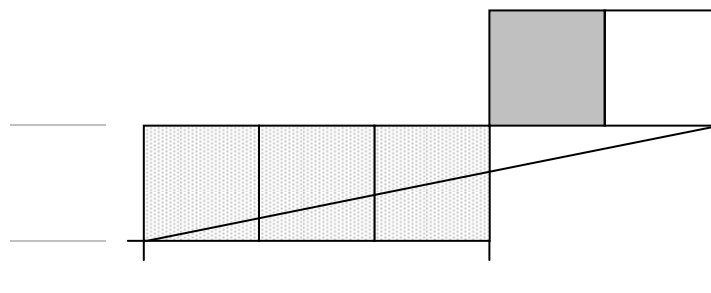
Each time we _____, we _____ by _____:



When the error value _____, the line is closer to _____ ...



... so we _____, and reset the error term, making it relative to the new scanline by _____:



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Naïve Bresenham(x_1 , y_1 , x_2 , y_2) // First octant only!

```
dx = _____
dy = _____
e = _____
de = _____ <-- _____
y = _____
for( x from _____ )
    plot( __, __ )
    e = _____
    if( _____ ) <-- _____
        _____
        e = _____ <-- _____
```

Improved Bresenham(x_1 , y_1 , x_2 , y_2) // First octant only!

```
dx = | $x_2$  -  $x_1$ |
dy = | $y_2$  -  $y_1$ |
e = 0
_____ <-- _____
y =  $y_1$ 
for( x from  $x_1$  to  $x_2$  )
    plot(x,y)
    e = e + de
    if( _____ ) <-- _____
        ++y
    e = _____ <-- _____
```

Integer Bresenham(x_1 , y_1 , x_2 , y_2) // First octant only!

```
dx = | $x_2$  -  $x_1$ |
dy = | $y_2$  -  $y_1$ |
e = 0
de = dy
y =  $y_1$ 
for( x from  $x_1$  to  $x_2$  )
    plot(x,y)
    e = e + de
    if( _____ ) <-- _____
        ++y
    e = e - dx
```

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Swapping _____ (reflection about $y = x$) when _____
converts _____ to the steep slope case above.

Bresenham(x_1 , y_1 , x_2 , y_2) // First and second octants only

steep = _____ > _____ (boolean flag)

if(steep)

dx = _____

dy = _____

e = _____

de = _____

y = _____

for(x from x_1 to x_2)

if(steep) _____ else _____

e = _____

if(_____)

++y

e = _____

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Remaining octants: _____ and/or _____, as appropriate.

Bresenham(x_1 , y_1 , x_2 , y_2) // All octants (lab implements):

```
steep =  $|y_2 - y_1| > |x_2 - x_1|$ 
```

```
if( steep )
```

```
    swap( $x_1$ ,  $y_1$ )
```

```
    swap( $x_2$ ,  $y_2$ )
```

```
if( _____ )
```

```
    _____
```

```
    _____
```

```
dx = _____
```

```
dy =  $|y_2 - y_1|$ 
```

```
e = 0
```

```
de = dy
```

```
y =  $y_1$ 
```

```
if( _____ ) _____ else _____
```

```
for( x from  $x_1$  to  $x_2$  )
```

```
    if( steep ) plot( $y$ , $x$ ) else plot( $x$ , $y$ )
```

```
    e = e + de
```

```
    if(  $2e \geq dx$  )
```

```
        y += _____
```

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$$e = e - dx$$