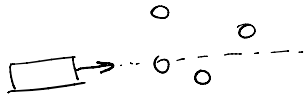


# Collision Avoidance documentation

Friday, January 25, 2019 6:10 PM

Idea:

Use gradient descent to determine the ideal steering angle



Robot's environment  $\rightarrow$  model each landmark as a Gaussian function

$$J = \underset{\Theta}{\operatorname{argmin}} \left[ \int_x P(\Theta, x) dx + \frac{1}{2} \|\Theta - \delta\|^2 \right]$$

basically, we want to pick the trajectory associated with the steering angle  $\Theta$  that has the fewest obstacles (we're integrating the probability of there being an obstacle at arclength  $x$  on trajectory  $\Theta$ )

We also want to steer as little as possible which is why we add the regularizer  $\frac{1}{2} \|\Theta - \delta\|^2$ ,  $\delta$  is our current steering angle.

The robot should also attempt to steer towards its goal as well, so after this step we run the standard controller.

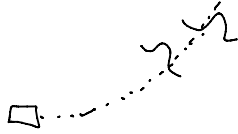
$$\Theta_{t+1} \leftarrow \Theta_t + \gamma \nabla J$$

$$\begin{aligned} \nabla J &= \frac{dJ}{d\Theta} = \frac{d}{d\Theta} \left( \int_x P(\Theta, x) dx + \frac{1}{2} \|\Theta\|^2 \right) \\ &= \frac{d}{d\Theta} \left( \int_x P(\Theta, x) dx \right) + \|\Theta\| \\ &= \int_x \frac{d}{d\Theta} (P(\Theta, x)) dx + \|\Theta\| \end{aligned}$$

$\frac{d}{d\Theta} (P(\Theta, x))$  is the derivative of a Gaussian whose mean  
i.e. all the obstacles along

$\frac{d}{d\theta}(P(\theta, x))$  is the derivative of a Gaussian whose mean is an obstacle, so basically take all the obstacles along that trajectory and add their derivatives up

we also need to consider the following:



in this situation it's ok because the 2 obstacles will cancel each other out. Therefore, we also need to add on a scaling term for the distance between the buggy and the obstacle, prioritizing closer obstacles.

MATLAB Sim:

