

## NOTES AND FORMULAS

**Low precision formulas for the Sun**

The following are low precision formulas for the Sun. On this page, the time argument  $n$  is the number of days of TT from J2000.0. UT can be used with negligible error.

The low precision formulas for the apparent right ascension and declination of the Sun yield a precision better than 1'.0 between the years 1950 and 2050.

$$\begin{aligned} n &= \text{JD} - 2451545.0 = 6938.5 + \text{day of year (from B4-B5)} + \text{fraction of day from 0}^{\text{h}} \text{ TT} \\ \text{Mean longitude of Sun, corrected for aberration: } L &= 280^{\circ}.460 + 0^{\circ}.985\,6474\,n \\ \text{Mean anomaly: } g &= 357^{\circ}.528 + 0^{\circ}.985\,6003\,n \end{aligned}$$

Put  $L$  and  $g$  in the range  $0^{\circ}$  to  $360^{\circ}$  by adding multiples of  $360^{\circ}$ .

$$\begin{aligned} \text{Ecliptic longitude: } \lambda &= L + 1^{\circ}.915 \sin g + 0^{\circ}.020 \sin 2g \\ \text{Ecliptic latitude: } \beta &= 0^{\circ} \\ \text{Obliquity of ecliptic: } \epsilon &= 23^{\circ}.439 - 0^{\circ}.000\,0004\,n \\ \text{Right ascension: } \alpha &= \tan^{-1}(\cos \epsilon \tan \lambda); (\alpha \text{ in same quadrant as } \lambda) \end{aligned}$$

Alternatively, right ascension,  $\alpha$ , may be calculated directly from:

$$\begin{aligned} \text{Right ascension: } \alpha &= \lambda - f t \sin 2\lambda + (f/2)t^2 \sin 4\lambda \\ \text{where } f &= 180/\pi \quad \text{and} \quad t = \tan^2(\epsilon/2) \\ \text{Declination: } \delta &= \sin^{-1}(\sin \epsilon \sin \lambda) \end{aligned}$$

The low precision formula for the distance of the Sun from Earth,  $R$ , in au, yields a precision better than 0.0003 au between the years 1950 and 2050.

$$R = 1.000\,14 - 0.016\,71 \cos g - 0.000\,14 \cos 2g$$

The low precision formulas for the equatorial rectangular coordinates of the Sun, in au, yield a precision better than 0.015 au between the years 1950 and 2050.

$$\begin{aligned} x &= R \cos \lambda \\ y &= R \cos \epsilon \sin \lambda \\ z &= R \sin \epsilon \sin \lambda \end{aligned}$$

The low precision formula for the Equation of Time,  $E$ , in minutes, yields a precision better than 3'.5 between 1950 and 2050.

$$E = (L - \alpha), \text{ in degrees, multiplied by } 4$$

Other useful quantities:

$$\begin{aligned} \text{Horizontal parallax: } &0^{\circ}.0024 \\ \text{Semidiameter: } &0^{\circ}.2666/R \\ \text{Light-time: } &0^{\text{d}}.0058 \end{aligned}$$