



# 15-110 PRINCIPLES OF COMPUTING – F19

## LECTURE 17: FUNCTIONS 1

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# Functions: callable, named subprograms (procedures)

- **Function:** informally, a *subprogram*
  - we write a sequence of statements and give that sequence a name
  - the instructions can then be executed at any point in a program by referring to the function name

```
def function_name(arguments):  
    function_body  
    return something
```

**User function  
definition**

**Calling (invoking)  
the function**

```
def happy():  
    print("Happy birthday to you!")  
  
name = 'Fred'  
print('Hello ' + name + '!')  
happy()  
happy()  
happy()
```

**Built-in function  
(python standard library)**

# All functions return something

---

```
def function_name(arguments):  
    function_body
```

is implemented as:



```
def function_name(arguments):  
    function_body  
    return None
```

All function calls return something, `None` when left unspecified in the function body

# Built-in functions (Python standard library)

<code>abs()</code>	<code>delattr()</code>	<code>hash()</code>	<code>memoryview()</code>	<code>set()</code>
<code>all()</code>	<code>dict()</code>	<code>help()</code>	<code>min()</code>	<code>setattr()</code>
<code>any()</code>	<code>dir()</code>	<code>hex()</code>	<code>next()</code>	<code>slice()</code>
<code>ascii()</code>	<code>divmod()</code>	<code>id()</code>	<code>object()</code>	<code>sorted()</code>
<code>bin()</code>	<code>enumerate()</code>	<code>input()</code>	<code>oct()</code>	<code>staticmethod()</code>
<code>bool()</code>	<code>eval()</code>	<code>int()</code>	<code>open()</code>	<code>str()</code>
<code>breakpoint()</code>	<code>exec()</code>	<code>isinstance()</code>	<code>ord()</code>	<code>sum()</code>
<code>bytearray()</code>	<code>filter()</code>	<code>issubclass()</code>	<code>pow()</code>	<code>super()</code>
<code>bytes()</code>	<code>float()</code>	<code>iter()</code>	<code>print()</code>	<code>tuple()</code>
<code>callable()</code>	<code>format()</code>	<code>len()</code>	<code>property()</code>	<code>type()</code>
<code>chr()</code>	<code>frozenset()</code>	<code>list()</code>	<code>range()</code>	<code>vars()</code>
<code>classmethod()</code>	<code>getattr()</code>	<code>locals()</code>	<code>repr()</code>	<code>zip()</code>
<code>compile()</code>	<code>globals()</code>	<code>map()</code>	<code>reversed()</code>	<code>__import__()</code>
<code>complex()</code>	<code>hasattr()</code>	<code>max()</code>	<code>round()</code>	

<https://docs.python.org/3/library/functions.html>

# Categories of functions

---

## Returning values or not

- Functions that do something and do *not* return anything (return None)
- Functions that do something and do return something different than None

## Input arguments or not / Changing arguments or not

- Functions that do something based on input parameters
  - Functions that also change the value of the input parameters (only for mutable types!)
  - Functions that do not change the value of the input parameters
- Functions that do something *not* based on input parameters

# Making effects outside of the function (mutable inputs)

- Function `my_sort()` returns `None`, but it does change its input parameter `L`, which is of mutable type
- The function `my_sorted()` does return a NEW list, `LL` and doesn't change the input list `L`

```
def my_sort(L):  
    L.sort()  
  
def my_sorted(L):  
    LL = sorted(L)  
    return LL  
  
unsorted = [1,5,0,-1, 4, -100]  
unsorted2 = unsorted.copy()  
  
my_sort(unsorted)  
print(unsorted)  
  
L = my_sorted(unsorted)  
print(L)
```

# Functions: organizing the code, putting aside functionalities

---

- Functions are a fundamental way to *organize* the code into **procedural elements** that can be *reused*
- Functions provide **structure and organization**, that facilitate:



# Decomposition: simple interactive game example

Goal: design a simple *Guess the number* game where the user inputs three integer numbers and the system checks if she/he has guessed the right number or not

```
value_list = []
n = 0
while n < 3:
    input_str = input('Input an integer number: ')
    if input_str.isdigit():
        v = int(input_str)
        value_list.append(v)
        n += 1

prod = 1
for v in value_list:
    prod *= v
if not (prod % 13):
    print("You guessed it right!!!")
else:
    print("Wrong guess...")
```



Rule (hidden to the player):

- Win iff the product of the three numbers is divisible by 13



# Decomposition: example

---

get three numbers  
from user inputs and  
put them in a list

```
value_list = []  
n = 0  
while n < 3:  
    input_str = input('Input an integer number: ')  
    if input_str.isdigit():  
        v = int(input_str)  
        value_list.append(v)  
        n += 1
```

take the numbers in  
the list and make their  
product

```
prod = 1  
for v in value_list:  
    prod *= v
```

check the correctness  
of the number and  
output the message

```
if not (prod % 13):  
    print("You guessed it right!!!")  
else:  
    print("Wrong guess...")
```

# Decomposition: example

---

- ✓ It can be observed that the overall task is (naturally) **composed by at least three independent sub-tasks**
- ✓ In fact, the defined computation is composed by three groups of statements each aimed at realizing a specific sub-task
  - These three groups of statements can be conveniently *isolated*, organized into *different functions*, and then *merged* to obtain the same overall result
- ✓ Each function corresponds to the creation of a **primitive** for the task, that can be used in the computation

# Decomposition: example

---

```
def get_user_numbers():  
    value_list = []  
    n = 0  
    while n < 3:  
        input_str = input('Input an integer number: ')  
        if input_str.isdigit():  
            v = int(input_str)  
            value_list.append(v)  
            n += 1  
    return value_list
```

```
def make_product(values):  
    prod = 1  
    for v in values:  
        prod *= v  
    return prod
```

```
def check_guess(input_val):  
    if not (input_val % 13):  
        print(" You guessed it right!!!")  
    else:  
        print(" Wrong guess...")
```

```
numbers = get_user_numbers()  
guess_number = make_product(numbers)  
check_guess(guess_number)
```

# Decomposition: example

```
def get_user_numbers():  
    value_list = []  
    n = 0  
    while n < 3:  
        input_str = input('Input an integer number: ')  
        if input_str.isdigit():  
            v = int(input_str)  
            value_list.append(v)  
            n += 1  
    return value_list
```

```
def make_product(values):  
    prod = 1  
    for v in values:  
        prod *= v  
    return prod
```

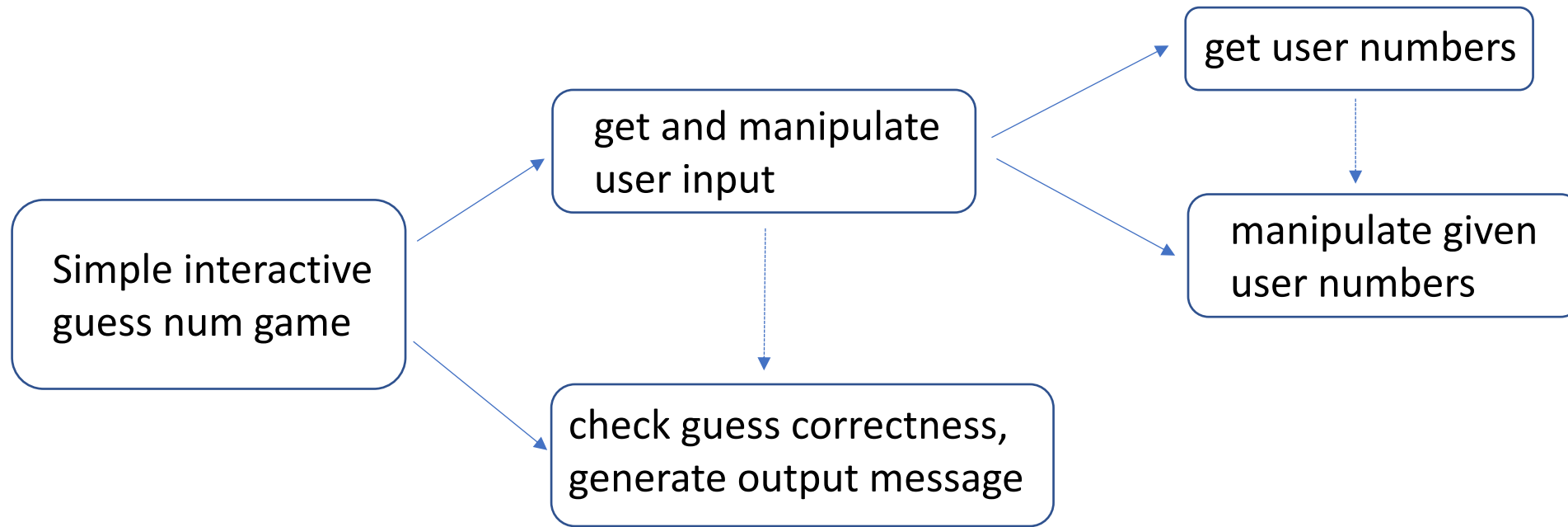
```
def check_guess (input_val):  
    if not (input_val % 13):  
        print("You guessed it right!!!")  
    else:  
        print("Wrong guess...")
```

```
numbers = get_user_numbers()  
guess_number = make_product(numbers)  
check_guess(guess_number)
```

- Even better:

```
def get_number():  
    values = get_user_numbers()  
    number = make_product(values)  
    return number  
  
guess_number = get_guess_number()  
check_guess(guess_number)
```

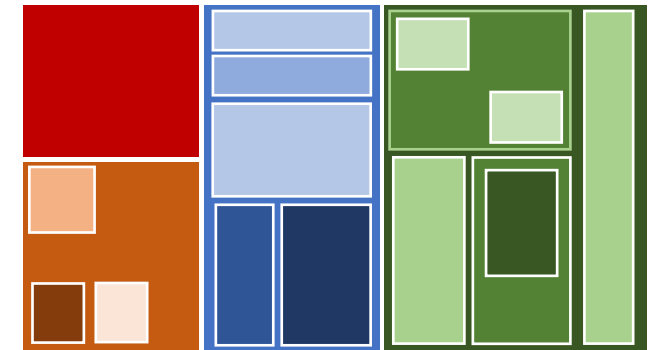
# Decomposition using functions



Problem to solve  
(monolithic view)

**Decompose** in multiple (smaller / easier) sub-problems, possibly nested, and then merge the sub-problems

**Divide-and-conquer**



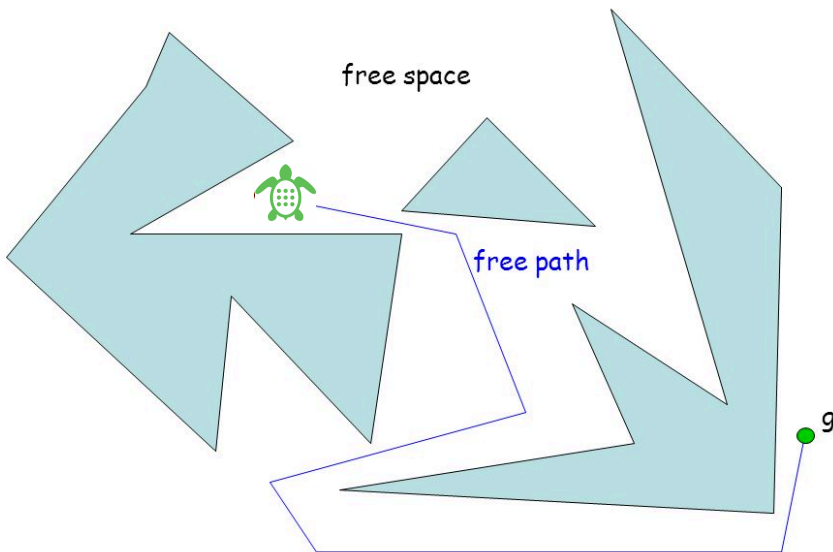
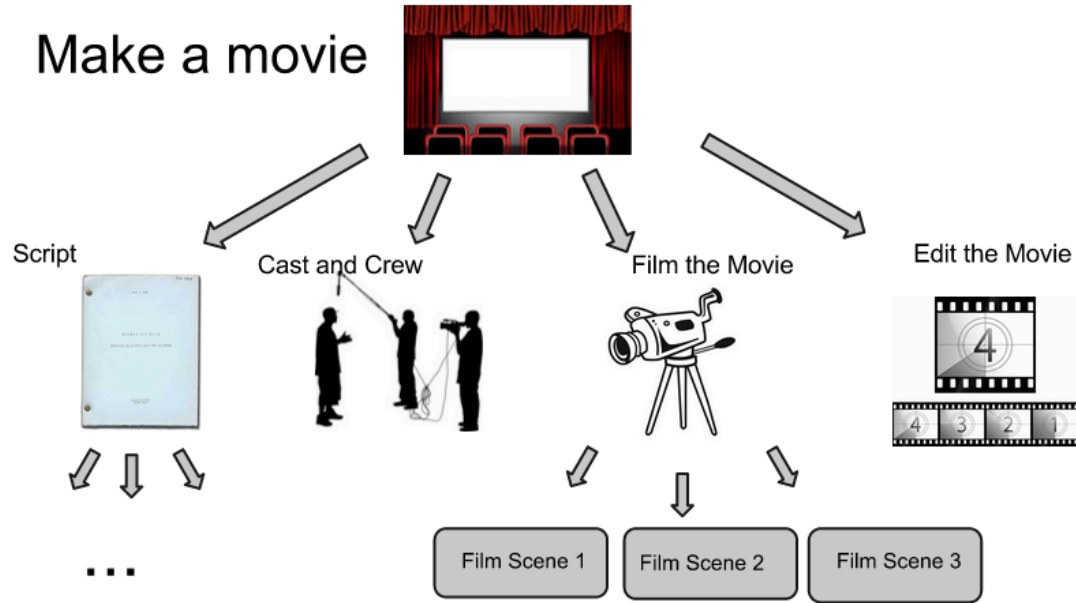
# Gains from decomposition using functions

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- Gains resulting from decomposing the problem in functional blocks and defining functions / primitives to handle the computation in each block:
  - ✓ A better **understanding of the task** and of **our computational approach** to its solution
  - ✓ **Readability**: we can now *read* what's going on (using self-explanatory names for the functions)
  - ✓ **Easiness of testing**: each function can be tested for correctness / performance in standalone
  - ✓ **Easiness of maintenance and updating**: we can improve / change the code of each new primitive function independently from other program parts (as long as inputs and return types stay the same)
  - ✓ We can now even **split the job** to design the individual functions to multiple programmers, *in parallel!*

# Examples of problem decompositions

## Make a movie



rotate in place  $+110^\circ$   
 move forward 5m  
 rotate in place  $+80^\circ$   
 move forward 6m  
 rotate in place  $+95^\circ$   
 move forward 7.5m  
 rotate in place  $-95^\circ$   
 move forward 2.5m  
 rotate in place  $-105^\circ$   
 move forward 9m  
 rotate in place  $-85^\circ$   
 move forward 2.8m

Original problem

Draw a figure

Level 0

Subproblems

Draw a circle

Draw a triangle

Draw intersecting lines

Level 1

Detailed subproblems

Draw intersecting lines

Draw a base

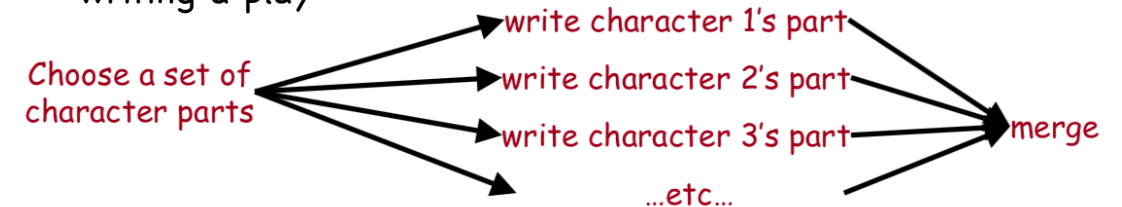
Level 2

## designing a restaurant menu



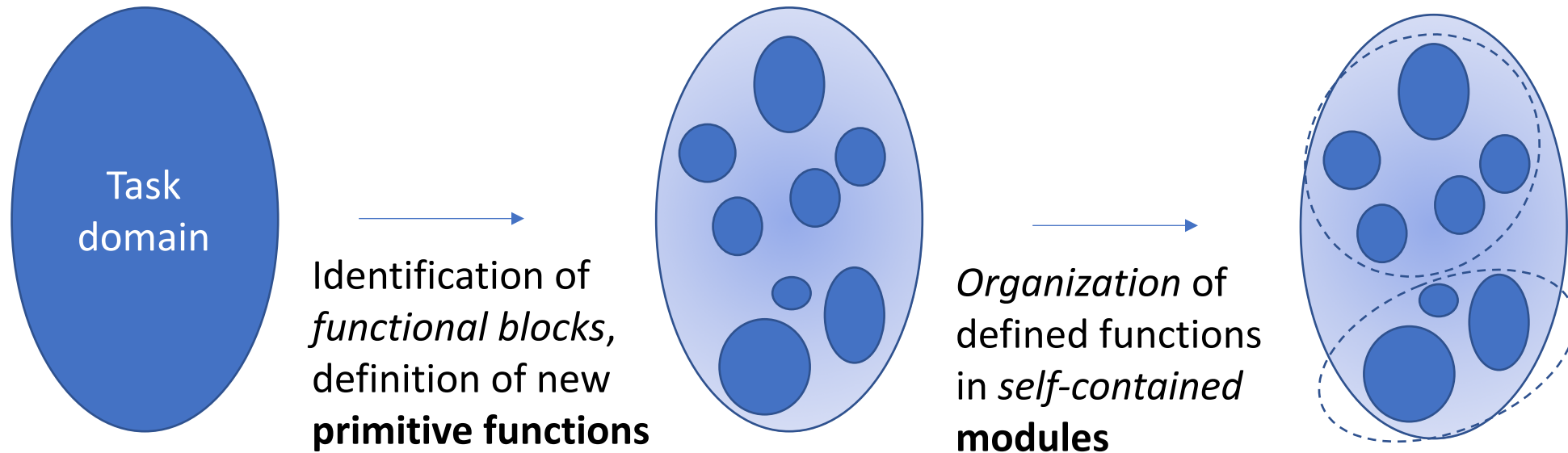
Not always fully feasible or straightforward!

## writing a play



# Decomposition by creation of self-contained modules

- Decomposition can be realized at different granularity, depending on the task domain



A function is a module with one single component

Each module provides a set of (related) functionalities:

- ✓ **Reusability** in different tasks or different parts of the program
- ✓ High-level of **abstraction**



# Reusability

---

- **Code reusability:** In addition to convenient code decomposition in functional blocks, the use of functions is essential to avoid to repeat the same fragment of code over and over in the same program, as well as to allow to reuse the same functional blocks in different programs

- E.g, we want to write a program that prints out the lyrics to the “Happy Birthday” song:

Happy birthday to you!

Happy birthday to you!

Happy birthday, dear <insert-name>. Happy birthday to you!

- Without functions we would write something like the following code to wish happy birthday to Fred:

```
print("Happy birthday to you!")  
print("Happy birthday to you!")  
print("Happy birthday, dear", 'Fred.')  
print("Happy birthday to you!")
```

- If we want to wish happy birthday to Lucy too, now we have to duplicate the code ... ☹️

# Reusability

---

```
print("Happy birthday to you!")
print("Happy birthday to you!")
print("Happy birthday, dear", 'Fred.')
print("Happy birthday to you!")
```

```
print("Happy birthday to you!")
print("Happy birthday to you!")
print("Happy birthday, dear", 'Lucy.')
print("Happy birthday to you!")
```

We don't want all this duplicated code!

```
def happy():
    print("Happy birthday to you!")

def sing(person):
    happy()
    happy()
    print "Happy Birthday, dear", person + "."
    happy()
```

- ✓ Now `sing(person)` can be reused for wishing happy birthday to *any* person!
- ✓ `sing()` and `happy()` could be included in a new *birthday module* ...

# Functions, parameters, scope, stack frames

---

```
def sing(person):  
    happy()  
    happy()  
    print "Happy Birthday, dear", person + "."  
    happy()
```

- ✓ Defines an *abstraction*: it describes a computation that applies to any person (passed as a string), as defined through the input parameter `person`
- ✓ **Formal parameters** (*arguments*) play a central role to let a function being applied in different contexts
  - Have the parameters **local or global scope** as variables?
  - Do they *live* inside and/or outside of the function when the function is being called?

# Local scope of variables: happy birthday example

---

```
def happy():  
    print "Happy birthday to you!"  
  
def sing(person):  
    happy()  
    happy()  
    print "Happy Birthday, dear", person + "."  
    happy()
```

```
sing("Fred")  
print()  
sing("Lucy")
```

```
sing("Fred")  
print("The song was for ", person)  
sing("Lucy")
```

Ok!

# Local Scoping: where do function variables live?

Examples from the class notebook: read them, understand them, run them, play with them ...

```
def avg_two(x, y):  
    x += 1  
    y += 1  
    print(x,y)  
    avg = (x + y) / 2  
    return avg
```

```
x = 2  
y = 5  
s = avg_two(x, y)  
print(s, x, y)
```

```
def avg(n_list):  
    val = sum(n_list) / len(n_list)  
    #print("Avg is:", val)  
    return val
```

```
def happy():  
    a = print("Happy birthday!")  
    print(a)
```

```
x = [1,2,3,4,5]  
y = avg(x)  
print(y)  
a = 5  
y = (y + a)/2  
print(y)  
happy()
```

```
def avg(n_list):  
    for i in range(len(n_list)):  
        n_list[i] += 1  
    val = sum(n_list) / len(n_list)  
    return val
```

```
x = [1,2,3,4]  
res = avg(x)  
print(res)  
print(x)
```

```
def avg_two(x, y):  
    x += 1  
    y += 1  
    print(x,y)  
    avg = (x + y) / 2  
    return avg
```

```
def prod_three(a,b,c):  
    return a * b * c
```

```
def no_sense():  
    a = 2 + hhh  
    b = 3  
    return a * b
```

```
hh = 6  
print(no_sense())  
hhh = 3
```

# Functions, parameters, scope, stack frames

---

What happens inside the computer when a function is called?

1. The **calling program** *suspends* at the point of the call and *jumps* to the program instruction with the definition of the function
2. A new **memory area** is allocated (stacked/*pushed* on the **run-time stack**) for the function (**call frame**)
3. The formal parameters of the function **get assigned the values supplied** by the actual parameters in the call, and get *pushed on the run-time stack* (**variable frame**)
4. The **body of the function is executed**, function **variables get pushed on the run-time stack**
5. At the end of the body or at return instruction, all call and variable frames are **popped out the stack**
6. Control returns **to the point just after where the function was called**

... complicated (maybe) ... let's skip the technical details

# Local scope of variables: happy birthday example

---

```
def happy():  
    print "Happy birthday to you!"  
  
def sing(person):  
    happy()  
    happy()  
    print "Happy Birthday, dear", person + "."  
    happy()
```

```
def main():  
    sing("Fred")  
    print()  
    sing("Lucy")  
  
main()
```

# Scope of variables: happy birthday example

---

Control being transferred from `main()` to `sing(person)`

```
def main():  
    sing("Fred")  
    print  
    sing("Lucy")  
  
def sing(person):  
    happy()  
    happy()  
    print "Happy birthday, dear", person + ". "  
    happy()
```

The diagram illustrates the flow of control between two functions. In the `main()` function, the line `sing("Fred")` is followed by a line break and then `print`. An arrow originates from the `sing("Fred")` call and points to the `def sing(person):` definition, indicating that the execution of `main()` is paused to execute the `sing` function.

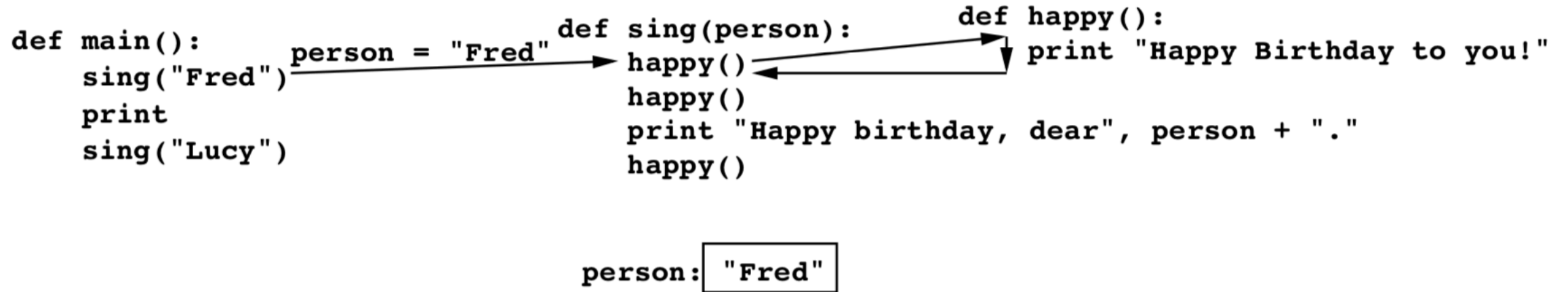
person: "Fred"



# Scope of variables: happy birthday example

---

Execution of `sing("Fred")` starts, and the control gets further passed to `happy()`

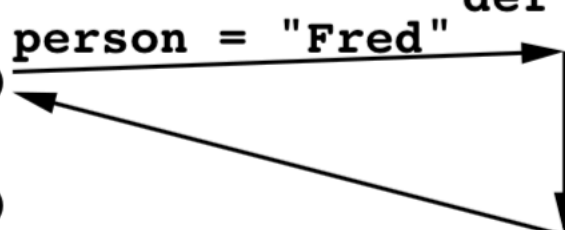


# Scope of variables: happy birthday example

---

Call of `sing("Fred")` is completed, and the control passes back to `main()`

```
def main():  
    sing("Fred")  
    print  
    sing("Lucy")  
  
def sing(person):  
    happy()  
    happy()  
    print "Happy birthday, dear", person + "."  
    happy()
```



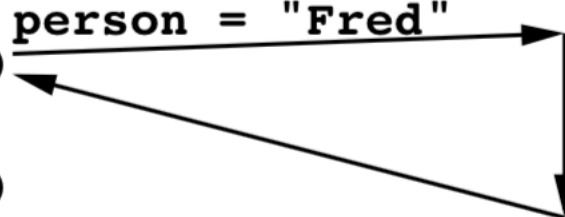
The diagram illustrates the execution flow between the `main()` and `sing(person)` functions. An arrow originates from the `sing("Fred")` call within the `main()` function and points to the start of the `sing(person)` function definition. Another arrow originates from the end of the `sing(person)` function (after the final `happy()` call) and points back to the `sing("Fred")` call in `main()`, indicating the return of control to the caller.

# Scope of variables: happy birthday example

---

Call of `sing("Fred")` is completed, and the control passes back to `main()`,  
the variable `person` doesn't exist anymore in the program, and it can't be referred to in `main()`

```
def main():  
    sing("Fred")  
    print  
    sing("Lucy")  
  
def sing(person):  
    happy()  
    happy()  
    print "Happy birthday, dear", person + "."  
    happy()
```

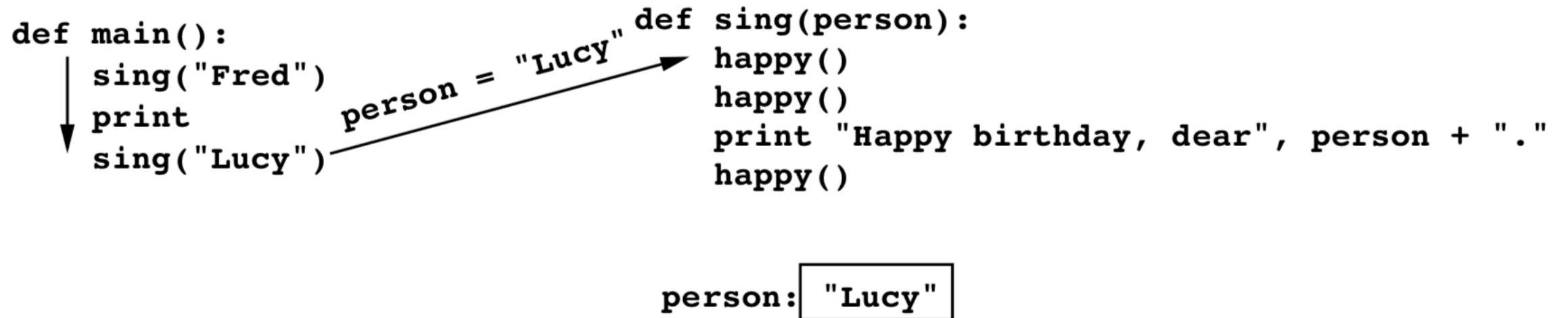


The diagram illustrates the execution flow between the `main()` function and the `sing(person)` function. An arrow points from the `sing("Fred")` call in `main()` to the start of the `sing(person)` function definition. Another arrow points from the end of the `sing(person)` function back to the line in `main()` following the `sing("Fred")` call, indicating the return of control.

# Scope of variables: happy birthday example

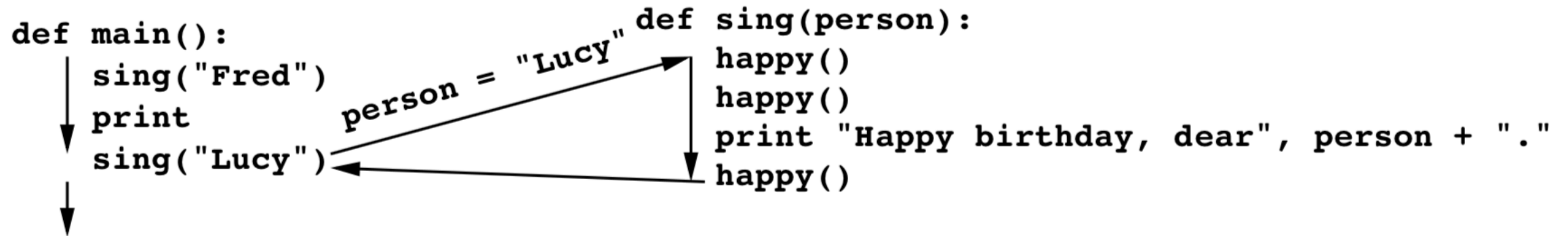
---

`main()` execution keeps going, and eventually `sing("Lucy")` is called, in this case a new parameter variable is allocated on the stack frame, with value "Lucy"



# Scope of variables: happy birthday example

`sing("Lucy")` is executed, and finally the control is passed back to `main()`, again all run-time stack data are cleared up and aren't anymore accessible in the program



## Moral:

All variables being created inside a function, live the time the function is being executed, therefore, they cannot be used outside the function

# How do we pass arguments to a function?

---

**def** function\_name(*arguments*):

*function\_body*

**return** *something*

- If we only need to pass one **single argument**, there's no much to say
- The situation is different when passing **multiple parameters** ...

```
def quadratic_roots(a, b, c):  
    x1 = -b / (2 * a)  
    x2 = sqrt(b**2 - (4 * a * c)) / (2 * a)  
    return (x1 + x2), (x1 - x2)
```

✓ Passing arguments as **positional arguments**

quadratic\_roots(31, 93, 62)

is different than:

quadratic\_roots(93, 31, 62)

**Order matters!**

✓ Passing arguments as **keyword arguments**

quadratic\_roots(a=31, b=93, c=62)

is the same as:

quadratic\_roots(b=93, a=31, c=62)

**Order doesn't matter!**

# Keyword arguments and the `help()` function

---

- Passing arguments as **keyword arguments** works because python **knows the name function arguments**, and therefore it can perform automatic matching without errors

```
quadratic_roots(a=31, b=93, c=62)
```

```
quadratic_roots(b=93, a=31, c=62)
```

```
quadratic_roots(c=62, b=93, a=31)
```

all give the same result, (-1.0, -2.0) in this case

→ We can ask python **help** on function's parameters using the `help(function_name)` function:

```
help(quadratic_roots)
```

would give as answer:

```
quadratic_roots(a,b,c)
```

Use of keyword arguments increases the clarity of a program!

```
random_password(upper=1, lower=1, digits=1, length=8) vs. random_password(1, 1, 1, 8)
```

# Positional arguments: different possible errors

---

- When passing arguments as **positional arguments** we need to be careful to **match the order** with which the parameters appear in the function definition!

- **Wrong computations** (no errors are issued by the interpreter!)

`quadratic_roots(31, 93, 62) → (-1.0, -2.0)`

`quadratic_roots(62, 93, 31) → (-0.5, -1.0)`

- **Run-time errors due to incorrect type** (program aborted!)

```
def sing(person, repetitions):  
    for i in range(repetitions):  
        happy()  
        happy()  
    print("Happy Birthday, dear", person + ".")  
    happy()
```

`sing(2, "Fred")`

Throws an error because a string object cannot be interpreted as an integer



# Default values for the arguments, equivalent function calls

---

- When defining a function, a **default value can be defined for each argument**
  - If a value argument for an argument with a default value is passed (either by position or by keyword) when the function is called, then the argument takes the provide value
  - Otherwise, the argument takes the default value
- `def sing(person="Fred", repetitions=2):`
  - ✓ `sing()`
  - ✓ `sing("Lucy")`
  - ✓ `sing("Lucy", 3)`
  - NO: `sing(3)`
- `def sing(person, repetitions=2):`
  - NO: `sing()`
  - ✓ `sing("Lucy")`
  - ✓ `sing("Lucy", 3)`
  - NO: `sing(3)`
- NO: `def sing(person="Fred", repetitions):` parameter assignments would be ambiguous

# Default values for making arguments optional

---

- The parameters with default values are de facto **optional**, in the absence of them they take the default value, that might be an empty value
  - `def sing(person, repetitions = 2):`
  - `def draw_rectangle(x1, x2, y1, y2, fill_color = None):`
  - `def move_forward(distance, velocity = 10):`

# Arbitrary number of arguments

---

- It might be the case that a function does some repetitive job and operates on a non well-defined number of arguments
- E.g., `print ( )` function
- We could use lists but it's not always nice, convenient, appropriate pack everything into a string
- Arbitrary sequence of arguments can be passed with the notation `*arguments`

```
def longlen(*strings):  
    max = 0  
    for s in strings:  
        if len(s) > max:  
            max = len(s)  
    return max
```

```
longlen('apple', 'banana', 'cantaloupe', 'cherry') → 9  
longlen('red', 'blue', 'green') → 5
```

- Positional and keyword arguments should be placed first to the arbitrary ones

```
def my_func(a, b=True, *args):
```

# Passing functions as arguments!

---

- Function arguments can also include a **function, that can be then regularly invoked inside the function**

```
def parabola(x):  
    return -x*x + 2
```

```
def cubic(x):  
    return x*x*x + 2*x*x
```

```
def geometric(x):  
    return 1 / (1-x)
```

```
def line(x):  
    return x
```

```
def estimate_max_in_interval(f, low_val, high_val, samples):  
    x = low_val  
    step = (high_val - low_val) / samples  
    max_val = f(high_val)  
    for i in range(samples):  
        if f(x) > max_val:  
            max_val = f(x)  
        x += step  
    return max_val
```

```
print(estimate_max_in_interval(geometric, -2, -1, 100))
```

# Abstraction

- **Abstraction** in computing aims to **hide details that are not necessary in a given context**, preserving only the information that is relevant in the context: it is the process that allows to take a piece of code, *name it*, and use it as it were a *black-box*
- When we define a function we are performing an **abstraction**: we take a piece of code, including objects and expressions, we name it, and in principle we can use it, without caring about *how* the outputs are precisely obtained in the function body
- The only information relevant to use the function are its input parameters and the returning object types, the details about how processing is performed are hidden by the abstraction

```
def make_product(values):  
    prod = 1  
    for v in values:  
        prod *= v  
    return prod
```

```
def make_product(values):  
    p = 1  
    for i in range(len(values)):  
        p *= values[i]  
    return p
```

```
import numpy  
def make_product(values):  
    return numpy.prod(values)
```

- ❖ All these three functions do the same thing! All that matters for the user are the **type of the inputs**, `values`, and what the function **returns**. *How* things are done inside the function doesn't matter for using it!