CS550: Massive Data Mining and Learning
Homework 2

Christos Mitropoulos - cm1012
email c.mitro@rutgers.edu

Github repository:
https://github.com/CMitropoulos/MassiveDataMining/tree/master/Homework3

Submission Instructions

Assignment Submission Include a signed agreement to the Honor Code with this assignment. Assignments are due at 11:59pm. All students must submit their homework via Sakai. Students can typeset or scan their homework. Students also need to include their code in the final submission zip file. Put all the code for a single question into a single file.

Late Day Policy Each student will have a total of *two* free late days, and for each homework only one late day can be used. If a late day is used, the due date is 11:59pm on the next day.

Honor Code Students may discuss and work on homework problems in groups. This is encouraged. However, each student must write down their solutions independently to show they understand the solution well enough in order to reconstruct it by themselves. Students should clearly mention the names of all the other students who were part of their discussion group. Using code or solutions obtained from the web is considered an honor code violation. We check all the submissions for plagiarism. We take the honor code seriously and expect students to do the same.

Discussion Group (People with whom you discussed ideas used in your answers):

On-line or hardcopy documents used as part of your answers:

I acknowledge and accept the Honor Code.

(Signed) Christos Mitropoulos

Answer to Question 1(a)

Answer to Question 1(b)

Answer to Question 1(c)

Answer to Question 2(a)

Answer to Question 2(b)

Answer to Question 2(c)

Answer to Question 3(a)

By definition C_i is a clique if there are fewer than two nodes in it. In any other case, any two nodes in C_i have an edge between them since they have i as a common factor.

Answer to Question 3(b)

i must be a prime number $\leq 1,000,000$

- If i is $\leq 1,000,000$ but isn't prime, let j be a factor of i and 1 ¡ j ¡ i. Node j is not in C_i, however it has an edge to every member of C_i, since it has j as a common factor. Therefore, C_i is not maximal.

- If i is $\geq 1,000,000$ then C_i is the empty clique and adding one node will make it a 1-clique, which is not maximal.

- If i is prime and $\leq 1,000,000$ then there is no node outside C_i that has an edge to the node i itself. Suppose there was a node j like that. Then i and j have a common factor other than 1, which can only be i, since i is prime. This makes j a multiple of i since j has i as a factor and therefore j is already in C_i.

Answer to Question 3(c)

i and i+1 are always relatively prime. If they had a common factor p¿1 then (i+1) - i =1 must also be divisible by p and this is impossible for any p¿1. Only one of the 2,3,4,5,6,7,8,9,... can be in a clique. The largest possible clique has 500,000 members as C_2.
There are no cliques other than C_2 that have 500,000 members. For a clique to have 500,000 members, it must contain 2 or 3, since otherwise the clique will have at most 499,999 members. If it contains 3, then all other members must have 3 as a factor (3 being a prime) and there less than 499,999 elements that are divisible by 3.