

The Kochen-Specker Theorem reduces Bell's argument on the noncontextuality of observables in quantum mechanics to a proof using a set of 117-three dimensional vectors in Hilbert space with no Kochen-Specker (KS) coloring. Since then, several KS uncolorable vector sets have been constructed, including a set of vectors whose rank-1 projection matrices have entries in the rational subring  $\mathbb{Z}[1/462]$  found by Cortez and Reyes. The vectors that were generated correspond to the set  $\mathcal{S}(N)$ , for  $N = 462$ , which is defined as a subset of  $\mathbb{Z}^3$  that contains vectors whose norm squared divides a power of  $N$ . However, the iterative processes used to generate the set of vectors  $\mathcal{S}(462)$  becomes computationally expensive when trying to prove whether sets of vectors such as  $\mathcal{S}(6)$  are KS uncolorable. To reduce the runtime of such procedures, we develop an algorithm that replaces some iterative processes with Python functions with at most  $O(n)$  complexity. Furthermore, we leverage methods that solve Diophantine equations of the form  $i^2 + j^2 + k^2 = N$  to more efficiently construct the necessary orthogonal basis vectors. By implementing this algorithm, we are able to identify a contradiction in our proof earlier on and minimize the possibility that the procedure does not halt.