



# **Functional Dependencies & Normalization for Relational DBs**

Chapter 6

# Contents

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G rpnbs argn

Dsl argn j bcnc l bcl agc q

L mpk jgx rgn

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# Contents

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## 1 Introduction

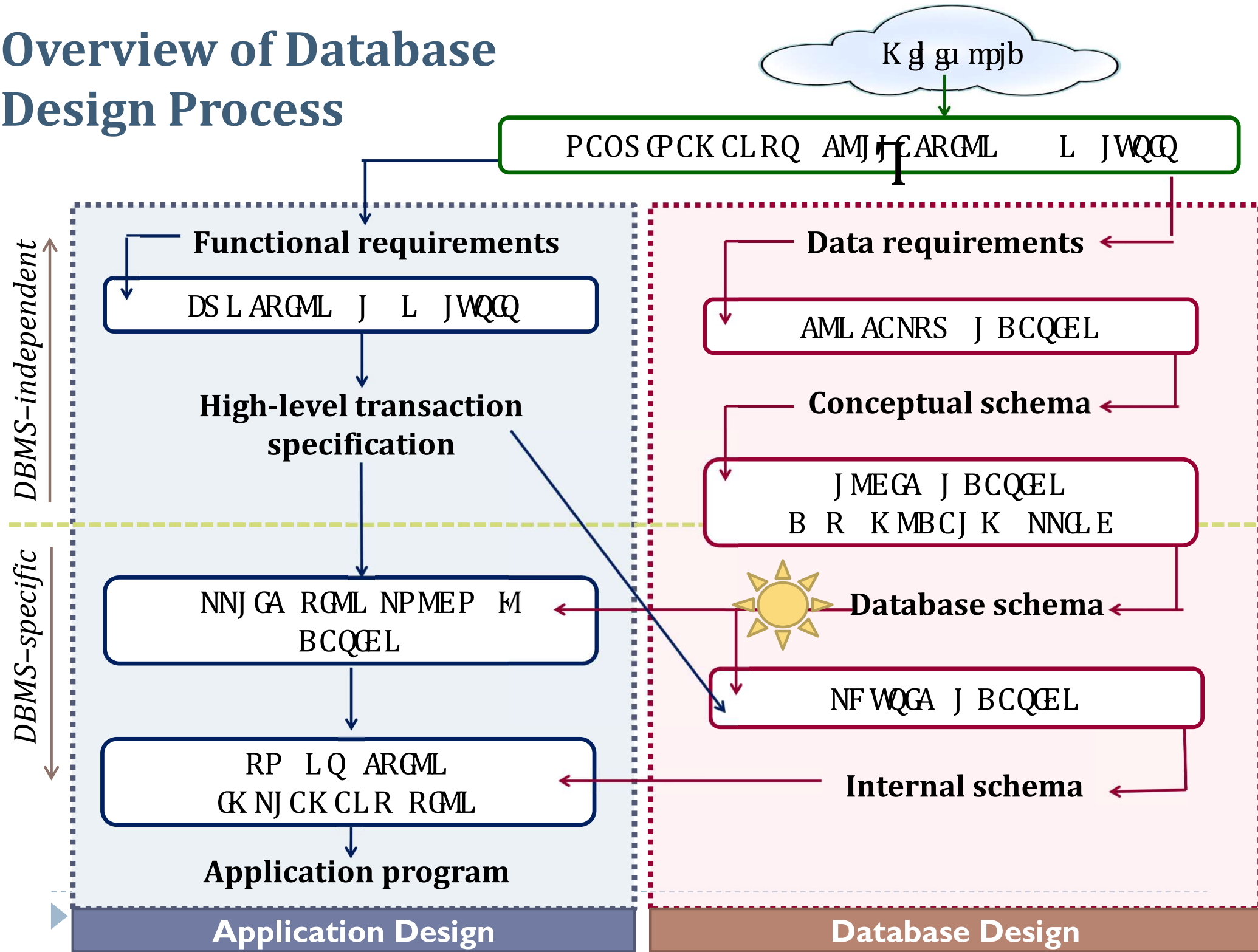
Dsl argm j bcnc1 bcl agc q

L mpk jgx rgm

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# Overview of Database Design Process



# Introduction

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- ▶ C af pcj rgnl qaf ck aml qgrq md lsk cpmd  
rrpg srcq l b rf c pcj rgnl j b r qc qaf ck aml qgrq  
md lsk cpmd pcj rgnl qaf ck q
- ▶ rrpg srcq pc epns ncb rmdmpk pcj rgnl qaf ck
- ▶ Lccb qmk c dmpk j k c qs pc ndu f wml c epns ng e md  
rrpg srcq g rm pcj rgnl qaf ck k w c crrcprf l  
l mrf cp



# Introduction

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- ▶ Embl cqq k c qs pcq
- ▶ K i g e qs pc rf r rf c qck l rgaq mdrf c rrpq srcq gq ajc p  
g rf c qaf ck
- ▶ Pcbsl b l r g dnpk rgm g rs njcq l b S nb rc l nk jgcq  
k mbgga rgm bcjcrgm g qcprgm
- ▶ Pcbsa g e rf c L S J J t jscq g rs njcq
- ▶ Bgq jjmu g e rf c nmqg ggrwmdcl cp rg e qns pgrs qrs njcq



# Introduction

- **Redundant information** g rs njcq rf c rrpq src t js cq  
ncpr g g e rm n prgas j pbcn prk cl r BLSK CP  
BL KC BK EPQQL pc pcnc rcb dmpct cpwck njmcc  
u f mu mpi q dmp rf r bcn prk cl r

EMP\_DEPT

Ename	Ssn	Bdate	Address	Dnumber	Dname	Dmgr_ssn
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5	Research	333445555
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5	Research	333445555
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4	Administration	987654321
Wallace, Jennifer S.	987654321	1941-06-20	291 Berry, Bellaire, TX	4	Administration	987654321
Narayan, Ramesh K.	666884444	1962-09-15	975 FireOak, Humble, TX	5	Research	333445555
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5	Research	333445555
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4	Administration	987654321
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1	Headquarters	888665555



# Introduction

- ▶ **Update anomalies** k mbgga rgn bcjcrgn g qcprgn
  - ▶ K mbgga rgn
    - ▶ qrf c k l ecpmd bcnr af l ecqu c f t c rmsnb rc k l w t js cq aampbg e rmck njmwccqu mpi g e dprf r bcnr
    - ▶ C qwrnk i c rf c B **inconsistent**

EMP\_DEPT

Ename	<u>Ssn</u>	Bdate	Address	Dnumber	Dname	Dmgr_ssn
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5	Research	333445555
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5	Research	333445555
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# Introduction

- ▶ Bcjcrgrm gl mpe H k cq C jc t cq u c bcjcrc f gqrs njc  
l b jmqc rf c cvgrg e mdbcnr rf c l k c mdbcnr l b  
u f mggrf c k l ecpmdbcnr

EMP\_DEPT

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# Introduction

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- ▶ G qc prgm
  - ▶ F mu a l u c apc rc bcn prk cl r cdhpc l wck njm wccq  
pc qqgel cb rmgr

EMP\_DEPT

Ename	<u>Ssn</u>	Bdate	Address	Dnumber	Dname	Dmgr_ssn
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5	Research	333445555
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# Introduction

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- ▶ Pcb sag e rf c L S J J t jscqg rs njcq
- ▶ Ck njmccql mr qqg el cb rm l wbcnr u qrc rf c qmp ec  
qn ac
- ▶ Mrf cpbgdhas jrgc q eepce rgm mcp rgm q c e AMS LR  
QS K l b hmg q



# Introduction

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- ▶ Bgg j jmu g e rf c nm qg ggrw decl cp rg e qns pgs qrs njcq

CK N NPMH QQL NL sk cp F ns pq CL k c NL k c NJ na rgm

CK N J MAQ CL k c NJ na rgm

CK N NPMH QQL NL sk cp F ns pq NL k c NJ na rgm

- ▶ Ecl cp rgm mdg t jgb l b qns pgs qb r bs pg e HML Q  
NJ na rgm ggrfc rrpq src rf r pcj rcq CK N J MAQ l b  
CK N NPMH l b NJ na rgm ggl cgrf cp npgk pwi cwl np  
dnp cgel i cwgl cgrf cp CK N J MAQ np CK N NPMH



# Introduction

- Background of the relational database model

EMP\_LOCS

Ename	Plocation
Smith, John B.	Bellaire
Smith, John B.	Sugarland
Narayan, Ramesh K.	Houston
English, Joyce A.	Bellaire
English, Joyce A.	Sugarland
Wong, Franklin T.	Sugarland
Wong, Franklin T.	Houston
Wong, Franklin T.	Stafford
Zelaya, Alicia J.	Stafford
Jabbar, Ahmad V.	Stafford
Wallace, Jennifer S.	Stafford
Wallace, Jennifer S.	Houston
Borg, James E.	Houston

EMP\_PROJ1

Ssn	Pnumber	Hours	Pname	Plocation
123456789	1	32.5	ProductX	Bellaire
123456789	2	7.5	ProductY	Sugarland
666884444	3	40.0	ProductZ	Houston
453453453	1	20.0	ProductX	Bellaire
453453453	2	20.0	ProductY	Sugarland
333445555	2	10.0	ProductY	Sugarland
333445555	3	10.0	ProductZ	Houston
333445555	10	10.0	Computerization	Stafford
333445555	20	10.0	Reorganization	Houston
999887777	30	30.0	Newbenefits	Stafford
999887777	10	10.0	Computerization	Stafford
987987987	10	35.0	Computerization	Stafford
987987987	30	5.0	Newbenefits	Stafford
987654321	30	20.0	Newbenefits	Stafford
987654321	20	15.0	Reorganization	Houston
888665555	20	NULL	Reorganization	Houston

# Introduction

- Bgg jjmu g e rf c nmqqg ggwmdcl cp rg e qns pgn s q  
rs njcq

Ssn	Pnumber	Hours	Pname	Plocation	Ename
123456789	1	32.5	ProductX	Bellaire	Smith, John B.
* 123456789	1	32.5	ProductX	Bellaire	English, Joyce A.
123456789	2	7.5	ProductY	Sugarland	Smith, John B.
* 123456789	2	7.5	ProductY	Sugarland	English, Joyce A.
* 123456789	2	7.5	ProductY	Sugarland	Wong, Franklin T.
666884444	3	40.0	ProductZ	Houston	Narayan, Ramesh K.
* 666884444	3	40.0	ProductZ	Houston	Wong, Franklin T.
* 453453453	1	20.0	ProductX	Bellaire	Smith, John B.
453453453	1	20.0	ProductX	Bellaire	Smith, John B.

# Introduction

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- ▶ Embl cqq k c qs pcq
  - ▶ Pcbsl b l r g dmpk rgm g rs njcq
  - ▶ Snb rc l nk jgcq k nb gda rgm bcjcrgm g qcprgm
  - ▶ Pcbs ag e rf c LSJJ t jscqg rs njcq
  - ▶ Bgq jjm g e rf c nm qg ggrw mdecl cp rg e qns pgn s qrs njcq

👉 **Normalization**



# Introduction

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- ▶ Lmpk jgx rgn f c jnqB bcqgel cpq bcrcpk g c rf c cqr  
pcj rgn qaf ck q
- ▶ dmpk jdp k cu mpi dmp l jwxg e pcj rgn qaf ck q qcb ml  
rf c gpi cwq l b ml rf c d l argn j bcnc l bcl agc q k ml e rf c g  
rrpg srcq
- ▶ qcpgc q ml mpk j dmpk rcqrq rf r a l c a ppgc b ns r ml  
g bg gbs j pcj rgn qaf ck q qmrf r rf c pcj rgn j b r qc a l  
c l mpk jgxcb rm l wbcqgpc b bcepcc
- ▶ Gr gq qcb ml rf c anl acnr ml mpk j dmpk LD LD LD  
ALD LD LD
- ▶ Gr gq nprmacqq u f gaf cl qs pcq rf r rf c b r gq qrp s ars pcb g  
qs af u wrf r rrp g srcq pc epns ncb u gf rf c NI  
rrpg srcq rf r bml mr bgpcarjwbcnc l b ml NI k w c  
cvrp arc b rmdmpk l cu pcj rgn





# Introduction

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► Rf cpc pc ru mgk nmpr l r npmcprgcq mdbcank nmrgm q

l m bbgc npjm qjcqq cqq mdrf c amppcqnml bg e hmg  
npcqcpt rgm mdrf c dsl argm j bcnci bcl agc q

► L mrc rf r npmcprw gq cvrpck cjwgc nmpr l r l b a l l m r  
c q apgac b Npmcprw gq jcqq qrpq ecl r l b k w c  
q apgac b



# Contents

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$\mathbb{Q}$  rpnbs argn

## **2 Functional dependencies**

L mpk jgx rgn

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# Functional Dependencies (FDs)

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- ▶ **Definition of FDs**

- ▶  $B \twoheadrightarrow G \mid B \twoheadrightarrow G \mid n \mid \text{prg} \mid j \mid \text{bcncl} \mid \text{bcl} \mid \text{agc} \mid q$
- ▶  $G \twoheadrightarrow \text{dpcl} \mid \text{ac} \mid P \mid s \mid j \mid \text{cq} \mid \text{dnp} \mid \text{DB} \mid q$
- ▶  $C \twoheadrightarrow s \mid g \mid j \mid \text{cl} \mid \text{ac} \mid m \mid Q \mid \text{crq} \mid m \mid \text{DB} \mid q$
- ▶  $K \twoheadrightarrow g \mid g \mid k \mid j \mid Q \mid \text{crq} \mid m \mid \text{DB} \mid q$



# Functional Dependencies (FDs)

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- ▶  $\text{DBq} \rightarrow \text{pc s qcb r m q n c a g w}$   
 $\text{d n p k j k c q s p c q m d r f c e m m b l c q q m d p c j r g n j}$   
 $\text{b c q g e l q}$
- ▶  $\text{DBq} \rightarrow \text{l b i c w q p c s q c b r m b c d g c l m p k j d n p k q d n p}$   
 $\text{p c j r g n q}$
- ▶  $\text{DBq} \rightarrow \text{p c a m q r p g r q r f r p c b c p g c b d n k r f c k c l g e}$   
 $\text{l b g r c p p c j r g n q f g n q m d r f c b r r r p g s r c q}$
- ▶  $\text{q c r m d r r p g s r c q} \rightarrow \text{q c r m d r r p g s r c q}$  **functionally determines**  $\text{q c r m d r r p g s r c q}$   
 $\text{W g d r f c t j s c m d V b c r c p k g c q s l g o s c t j s c}$   
 $\text{d n p W}$

$X \rightarrow Y$

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# Functional Dependencies (FDs)

---

- ▶  $V \rightarrow W$  f mjbq gdu f cl ct cpru mrs njc qf t c r f c q k c t j s c dmp  
V r f c w k s q r f t c r f c q k c t j s c dmp W
  - ▶ Dmp l wru mrs njc q r l b r g l wpcj rgnl g q r l ac p P  
Gdr V r V r f cl r W r W
  - ▶  $V \rightarrow W$  g P qnc ag g c q aml qrp g r m j j pcj rgnl g q r l ac q p P
  - ▶ Cv k njc q
    - ▶ qmag j qc as p g w l s k c p b c r c p k g c q c k n j m w c c l k c  
QQL  $\rightarrow$  CL k c
    - ▶ npml car l s k c p b c r c p k g c q n p m l car l k c l b j n a rgnl  
NL s k cp  $\rightarrow$  NL k c NJ n a rgnl
    - ▶ ck n j m w c c qql l b n p m l car l s k c p b c r c p k g c q r f c f n s p q n c p  
u c c i r f r r f c c k n j m w c c u m p i q m l r f c n p m l car  
QQL NL s k cp  $\rightarrow$  F n s p q
- 



# Functional Dependencies (FDs)

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- ▶  $\{A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z\} \twoheadrightarrow \{A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z\}$



# Functional Dependencies (FDs)

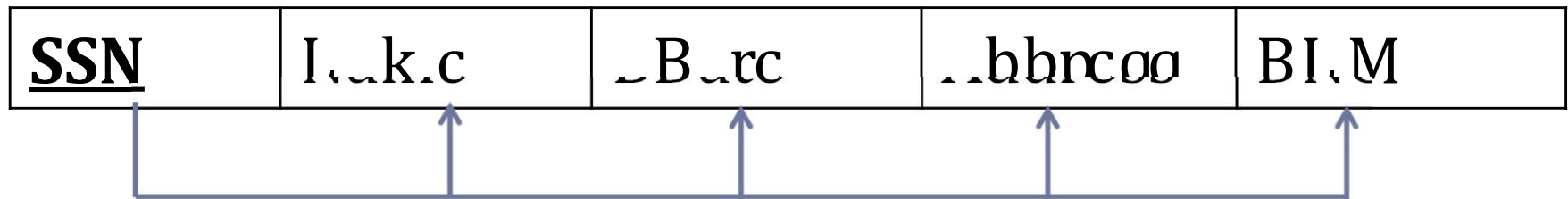
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- ▶  $B \rightarrow C, G \rightarrow H$  in  $DB$
- ▶ **Direct, indirect, partial dependencies**
- ▶  $G \rightarrow H$  in  $DB$
- ▶  $C \rightarrow H$  in  $DB$
- ▶  $K \rightarrow L$  in  $DB$

# Functional Dependencies (FDs)

- Direct and fully dependency**
  
 $QQL \rightarrow L \text{ k c } B \text{ rc } \text{ bbpcqq } BLM$

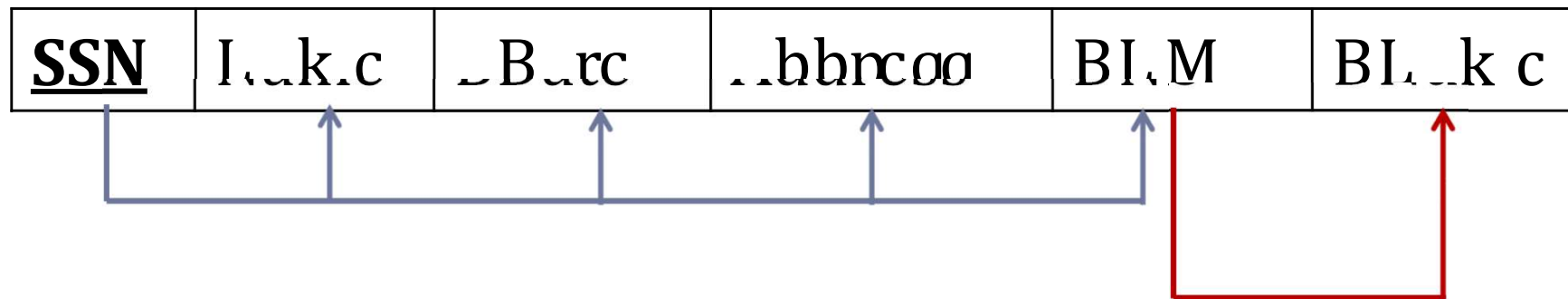
CK NJ MCCC





# Functional Dependencies (FDs)

- ▶ **Indirect dependency** T jsc nd l rrpq src gq l mr  
bcrcpk g cb bgrcarjw wrf c npgk pwi cw  
BLM  $\rightarrow$  BL k c
- ▶ QQL  $\rightarrow$  Bl k c gq *transitive dependency* rf pns ef BLM  
CK N BCNR



# Functional Dependencies (FDs)

## Partial dependency

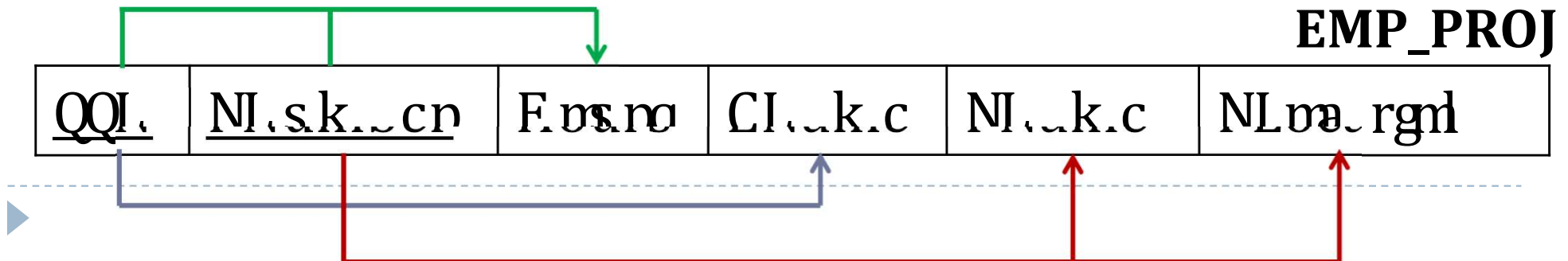
- Amk nmqgc bcrckp g l r k m p r f l m c t j s c g p c o s g p c b  
 r m b c r c p k g c r f c t j s c m d l m r f c p r r p g s r c r f c  
 ank g r g n m d t j s c q g a j j c b ank nmqgc bcrckp g l r  
 QQL NLsk cp g CK N NPMH QQL NLsk cp  $\rightarrow$  Fns pq
- N prg j bcnc l bcl aw g d r f c t j s c m d l r r p g s r c b m c q l m r  
 bcnc l b m l c l r g p c ank nmqgc bcrckp g l r s r m j w  
 n p r m d g r f c p c j r g n q f g n g i l m u l q r f c n prg j  
 bcnc l bcl aw

QQL  $\rightarrow$  CL k c

Nl s k cp  $\rightarrow$  NL k c NJ m a r g n l

**EMP\_PROJ**

<u>QQL</u>	<u>Nl.s.k.c</u>	<u>Fns</u>	<u>CL.k.c</u>	<u>Nl.k.c</u>	<u>NLmæ.rgnl</u>
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# Functional Dependencies (FDs)

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- ▶  $B \rightarrow C \mid G \mid M \mid DB$
- ▶  $B \rightarrow C \mid G \mid M \mid DB \mid A \mid N \mid P \mid R \mid J \mid B \mid C \mid N \mid C \mid L \mid B \mid C \mid L \mid A \mid G \mid Q$
- ▶ **Inference Rules for FDs**
- ▶  $C \rightarrow S \mid G \mid J \mid C \mid L \mid A \mid C \mid M \mid Q \mid C \mid R \mid Q \mid M \mid D \mid B \mid Q$
- ▶  $K \rightarrow G \mid G \mid K \mid J \mid Q \mid C \mid R \mid Q \mid M \mid D \mid B \mid Q$



# Functional Dependencies (FDs)

---

- ▶ Eg cl qcr mDBq D u c a l g d p bbgm j DBq rf r  
f mjb u f cl ct cprf c DBq g Df mjb
- ▶ **Armstrong's inference rules:**
  - ▶ **IR1. (Reflexive)**  $G \mid W \subseteq V \text{ rf cl } V \rightarrow W$
  - ▶ **IR2. (Augmentation)**  $G \mid V \rightarrow W \text{ rf cl } VX \rightarrow WX$   
 $L \text{ m r g m } VX \text{ q r l b q d m p } V \cup X$
  - ▶ **IR3. (Transitive)**  $G \mid V \rightarrow W \text{ l b } W \rightarrow X \text{ rf cl } V \rightarrow X$



# Functional Dependencies (FDs)

- ▶ Qmk c bbggnl j g d pcl ac ps jcqrf r pc s qc d j
  - ▶ **Decomposition:**  $GdV \rightarrow W \text{ rf cl } V \rightarrow W \text{ b } V \rightarrow X \quad \vdash$
  - ▶ **Union:**  $GdV \rightarrow W \text{ b } V \rightarrow X \text{ mcl } V \rightarrow W \quad \vdash$
  - ▶ **Pseudotransitivity:**  $GdV \rightarrow W \text{ b } U \rightarrow W \rightarrow X \text{ mcl } U \rightarrow V \rightarrow X \quad \vdash$
- ▶ Rf c j qr rf pcc g d pcl ac ps jcq qu cjj q l wmr f cp  
 g d pcl ac ps jcq a l c bcbs acb dmk  $\mathcal{P}$   $\mathcal{P}$  l b  $\mathcal{P}$   
 ank njcrcl cqq npmcpw
- ▶ **Armstrong's inference rules:**
  - ▶ **IR1. (Reflexive)**  $GdW \subseteq V \text{ rf cl } V \rightarrow W$
  - ▶ **IR2. (Augmentation)**  $GdV \rightarrow W \text{ rf cl } VX \rightarrow WX$   
 $L \text{ m rgnl } VX \text{ qr l bq dnp } V \cup X$
  - ▶ **IR3. (Transitive)**  $GdV \rightarrow W \text{ l b } W \rightarrow X \text{ rf cl } V \rightarrow X$

# Functional Dependencies (FDs)

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- ▶ A functional dependency  $F^+$  in a relation  $r$  is a set of attributes  $A$  such that for any two tuples  $t_1, t_2$  in  $r$ , if  $t_1[A] = t_2[A]$  then  $t_1[B] = t_2[B]$ .
- ▶ A functional dependency  $X^+$  in a relation  $r$  is a set of attributes  $X$  such that for any two tuples  $t_1, t_2$  in  $r$ , if  $t_1[X] = t_2[X]$  then  $t_1[Y] = t_2[Y]$ .
- ▶  $X^+$  is a functional dependency in a relation  $r$  if and only if  $X^+ \subseteq F^+$ .

# Exercise

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- ▶ Am qgbc p pcj rgm  $R A, B, C, D, E$  u gf rf c dhjmu g e  
bcncl bcl agcq D

$\rightarrow A$

$AB \rightarrow C$

$BC \rightarrow$

- ▶ Dg b B

- ▶ Dg b D



# Functional Dependencies (FDs)

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- ▶  $B \rightarrow C, G \rightarrow M$  in DB
- ▶  $B \rightarrow C, A \rightarrow B, C \rightarrow A, D \rightarrow E, F \rightarrow G, H \rightarrow I, J \rightarrow K, L \rightarrow M, N \rightarrow O, P \rightarrow Q, R \rightarrow S, T \rightarrow U, V \rightarrow W, X \rightarrow Y, Z \rightarrow AA$
- ▶  $A \rightarrow B, C \rightarrow D, E \rightarrow F, G \rightarrow H, I \rightarrow J, K \rightarrow L, M \rightarrow N, O \rightarrow P, Q \rightarrow R, S \rightarrow T, U \rightarrow V, W \rightarrow X, Y \rightarrow Z, AA \rightarrow BB$
- ▶ **Equivalence of Sets of FDs**
- ▶  $K \rightarrow G, G \rightarrow K, J \rightarrow Q, Q \rightarrow J$  in DB





# Functional Dependencies (FDs)

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- ▶  $R \cup S \models F^+ \iff R \models F^+ \text{ and } S \models F^+$  **equivalent**
- ▶  $R \models F^+ \iff R \models F$
- ▶  $D \text{ covers } E \iff G^+ \subseteq F^+$
- ▶  $D \text{ is a subset of } E \iff D \text{ is a subset of } E \text{ and } D \models F^+ \implies E \models F^+$  **equivalent**
- ▶  $R \models F^+ \iff R \models F$

# Functional Dependencies (FDs)

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- ▶  $qcr \rightarrow mDBq$   $gk \rightarrow gk$   $j \rightarrow j$   $glg \rightarrow q$   $rgg \rightarrow c$   $dcq \rightarrow rf$   $c \rightarrow c$   $hjm \rightarrow u$   $g \rightarrow e$   
 $am \rightarrow b$   $grgm \rightarrow q$
- ▶  $Ct \rightarrow cpw$   $bcncl \rightarrow bcl$   $awg \rightarrow Df$   $q \rightarrow q$   $qg \rightarrow ejc$   $rrpg \rightarrow src$   $dmp \rightarrow grq$   $PF \rightarrow Q$
- ▶  $U \rightarrow c$   $a \rightarrow l$   $l \rightarrow m$   $pc \rightarrow k$   $nt \rightarrow c$   $l \rightarrow w$   $bcncl \rightarrow bcl$   $aw \rightarrow pmk$   $D \rightarrow l$   $b \rightarrow f$   $t \rightarrow c$   $qcr \rightarrow m$   
 $bcncl \rightarrow bcl$   $ag \rightarrow c$   $q \rightarrow rf$   $r \rightarrow g$   $cos \rightarrow g$   $j \rightarrow cl$   $r \rightarrow rmD$
- ▶  $U \rightarrow c$   $a \rightarrow l$   $l \rightarrow m$   $pc \rightarrow nj$   $ac \rightarrow l$   $w \rightarrow b$   $cncl \rightarrow bcl$   $aw \rightarrow V \rightarrow g$   $Du \rightarrow gf$   
 $bcncl \rightarrow bcl$   $aw \rightarrow W \rightarrow u$   $f \rightarrow cpc$   $W \rightarrow pmcp$   $qs \rightarrow qcr$   $m \rightarrow V$   $W \rightarrow W$   
 $qs \rightarrow qcr$   $m \rightarrow V$   $l \rightarrow b$   $q \rightarrow gj$   $f \rightarrow t$   $c \rightarrow qcr$   $m \rightarrow b$   $cncl \rightarrow bcl$   $ag \rightarrow c$   $q \rightarrow rf$   $r \rightarrow g$   
 $cos \rightarrow g$   $j \rightarrow cl$   $r \rightarrow rmD$

# Functional Dependencies (FDs)

---

- ▶  $C \rightarrow P, W, Q, R, M, D, B, Q, F$     $Q \rightarrow L, C, O, S, G$     $J \rightarrow C, L, R, K, G, G, K$     $J \rightarrow Q, C, R$
- ▶  $R \rightarrow F, C, P, C, A, L$     $C \rightarrow Q, C, T, C, P, J, C, O, S, G$     $J \rightarrow C, L, R, K, G, G, K$     $J \rightarrow Q, C, R, Q$
- ▶  $R \rightarrow F, C, P, C, G, L, M, Q, G, K, N, J, C$     $J \rightarrow E, M, P, G, F, K, D, H, P, A, N, K, N, S, R, G, E$     $K \rightarrow G, G, K$     $J \rightarrow Q, C, R, M, D, B, Q, R, F$     $R \rightarrow G, G, C, O, S, G$     $J \rightarrow C, L, R, R, M$     $Q \rightarrow C, R, D, M, D, B, Q$
- ▶  $R \rightarrow M, Q, W, L, R, F, C, Q, G, X, C$     $Q \rightarrow C, R, M, D, P, C, J, R, G, M$     $Q \rightarrow U, C$     $Q \rightarrow Q, S, K, C, R, F$     $R \rightarrow U, C$   
 $Q \rightarrow R, P, U, G, F$     $Q \rightarrow C, R, M, D, B, C, N, C, L, B, C, L, A, G, C, Q, R, F$     $R \rightarrow G, G$    **minimal set**



# Contents

---

---

Q rpnbs argn

Dsl argn j bcnc1 bcl agc q

## **3 Normalization**

---



# Normalization

---

- ▶ **Normalization** Rf c nprmacqq mdecomposing  
sl q rggd armpw b pcj rgnl q w pc i g e s n rf cgp  
rrpg srcqg rmqk jjcp pcj rgnl q
- ▶ Lmpk j dmpk S qg e i cwq l b DBq m pcj rgnl rm  
acprgdwu f crf cp pcj rgnl qaf ck ggg n prgas j p  
lmpk j dmpk
- ▶ Lmpk jgx rgnl gga ppgcb nsr g np argac qmrf r rf c  
pcqs jrg e bcqgel q pc mdf gef os jgw l b k ccr rf c  
bcqgp jc nprmcprgcq
- ▶ Rf c b r qc bcqgel cpq need not lmpk jgxc rmrf c  
f gef cqr nmqg jc lmpk j dmpk LD AL Dmp LD



# Normalization

---

- ▶ Ru ml cu am acnrq
  - ▶ **Prime attribute** k s qr c k ck cpmd qmk c a l b gb rc i cw
  - ▶ **Nonprime attribute** g l m npg k c rrp g s rc g g l m k ck cpmd l wa l b gb rc i cw



# Normalization

---

- ▶ LD l b bcnc1 bcl awn~~pm~~ jck q
- ▶ LD qmjt cq n prg j bcnc1 bcl aw
- ▶ LD qmjt cq g bgpcar bcnc1 bcl aw
- ▶ ALD u cjj l m~~pk~~ jgxc b pcj rgm q

# Normalization

---

- ▶ **First normal form (1NF):** rf cpc gq m jwm c t js c r  
rf c g rcpqcargm mdc af pmu l b amjs k l md pcj rgm  
l mqcr t js cb rrpq srcq g LD  
→ Bgq jjmu q ank nmqrc rrpq srcq k s jrg js cb  
rrpq srcq l b **nested relations**
- ▶ Rm c n pr ndr f c dnpk j bcd g rgm md pcj rgm g rf c  
qga d r pcj rgm j k mbcj



# 1NF

(a)

## DEPARTMENT

Dname	<u>Dnumber</u>	Dmgr_ssn	Dlocations

(b)

## DEPARTMENT

<u>Dname</u>	<u>Dnumber</u>	<u>Dmgr_ssn</u>	Dlocations
Research	5	333445555	{Bellaire, Sugarland, Houston}
Administration	4	987654321	{Stafford}
Headquarters	1	888665555	{Houston}

(c)

## DEPARTMENT

Dname	<u>Dnumber</u>	Dmgr_ssn	<u>Dlocation</u>
Research	5	333445555	Bellaire
Research	5	333445555	Sugarland
Research	5	333445555	Houston
Administration	4	987654321	Stafford
Headquarters	1	888665555	Houston

# 1NF

---

**EMP\_PROJ**

SSN	ENAME	PROJS	
		PNUMBER	HOURS

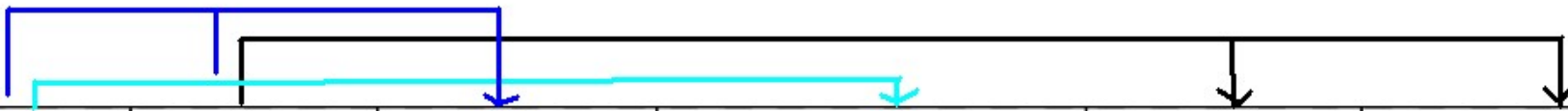
**EMP\_PROJ**

Ssn	Ename	Pnumber	Hours
123456789	Smith, John B.	1	32.5
		2	7.5
666884444	Narayan, Ramesh K.	3	40.0
453453453	English, Joyce A.	1	20.0
		2	20.0



# 1NF

## EMP\_PROJ



<u>SSN</u>	<u>PNUMBER</u>	HOURS	ENAME	PNAME	PLOCATION
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford

# 1NF

---

CK N NPMH QQL NL s k cp F ns pq CL k c NL k c NJ na rgn

QQL NL s k cp  $\rightarrow$  F ns pq

QQL  $\rightarrow$  CL k c

NL s k cp  $\rightarrow$  NL k c NJ na rgn



# 1NF

---

CK N NPMH QQL NLsk cp Fms pq

CK N QQL CL k c

NPMH NLsk cp NL k c NJ ma rgml

QQL NL S K CP  $\rightarrow$  F M S P Q

QQL  $\rightarrow$  CL K C

NL S K CP  $\rightarrow$  NL K C NJ MA RGML



# Normalization

---

- ▶ L D l b bcnc l bcl awn p m jck q
- ▶ **2NF – solves partial dependency**
- ▶ L D q m j t c q g b g p c a r bcnc l bcl aw
- ▶ AL D u c j j l m p k r j g x c b p c j r g m q



# Normalization

---

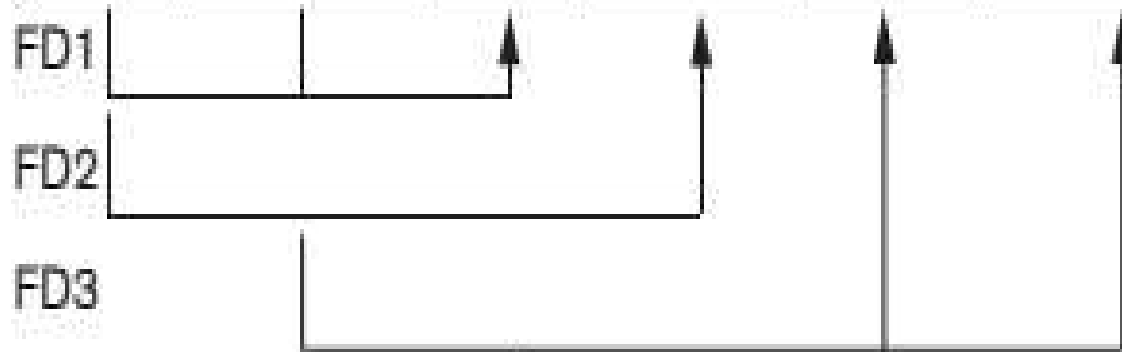
- ▶ Qcaml b l mpk j dmpk L D jj rpg srcq k s qr c d j j w  
d l argm j j w b c n c l b c l r m r f c n p g k p w i c w
- ▶ L D q m j t c q n p r g j b c n c l b c l a w n p m j c k g L D
- ▶ K c r f m b g b c l r g d w n p g k p w i c w q l b e p m s n r r p g s r c q  
r f r p c j r c r m r f c i c w r m e c r f c p r m d m p k q c n p r c l c u  
p c j r g m q



# 2NF

EMP\_PROJ

<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
------------	----------------	-------	-------	-------	-----------



2NF Normalization

EP1

<u>Ssn</u>	<u>Pnumber</u>	Hours
------------	----------------	-------



EP2

<u>Ssn</u>	Ename
------------	-------



EP3

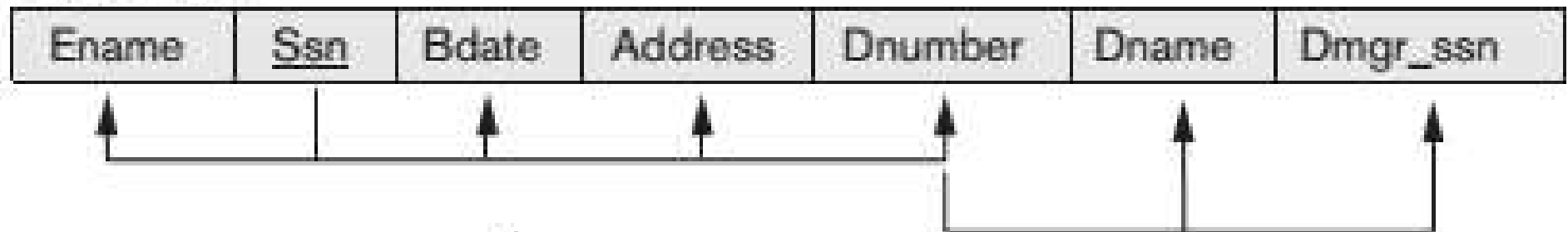
<u>Pnumber</u>	Pname	Plocation
----------------	-------	-----------





# 2NF

## EMP\_DEPT



## EMP\_DEPT ➤ Problem with 2NF

Ename	<u>Ssn</u>	Bdate	Address	Dnumber	Dname	Dmgr_ssn
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5	Research	333445555
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5	Research	333445555
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4	Administration	987654321
Wallace, Jennifer S.	987654321	1941-06-20	291 Berry, Bellaire, TX	4	Administration	987654321
Narayan, Ramesh K.	666884444	1962-09-15	975 FireOak, Humble, TX	5	Research	333445555
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5	Research	333445555
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4	Administration	987654321
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1	Headquarters	888665555

# Normalization

---

- ▶ LD l b bcnc l bcl awn p m jck q
- ▶ LD qm j t c q n p r g j bcnc l bcl aw
- ▶ **3NF – solves indirect dependency**
- ▶ AL D u c j j l m p k r j g x c b p c j r g m q



# Normalization

- ▶ pcj rgm qaf ck P ggg **third normal form 3NF** glg  
 ggg LD and l ml m npgk rrpq src g P gq  
 rp l qgg c jwbcncl bcl r m rfc npgk pwi cw

## NOTE:

G V  $\rightarrow$  W l b W  $\rightarrow$  X u gf V qrf c npgk pwi cwu c am qgbc  
 rf gq npm jck m jwgd Wgql mr a l bgb rc i cwU f cl Wgq  
 a l bgb rc i cwrf cpc gq l mnpm jck u gf rfc rp l qgg c  
 bcnc l bcl aw

C e Am qgbc pCK N QQL Ck n Q j pw

F cpc QQL  $\rightarrow$  Ck n  $\rightarrow$  Q j pw l b Ck n gq a l bgb rc i cw

# Normalization

---

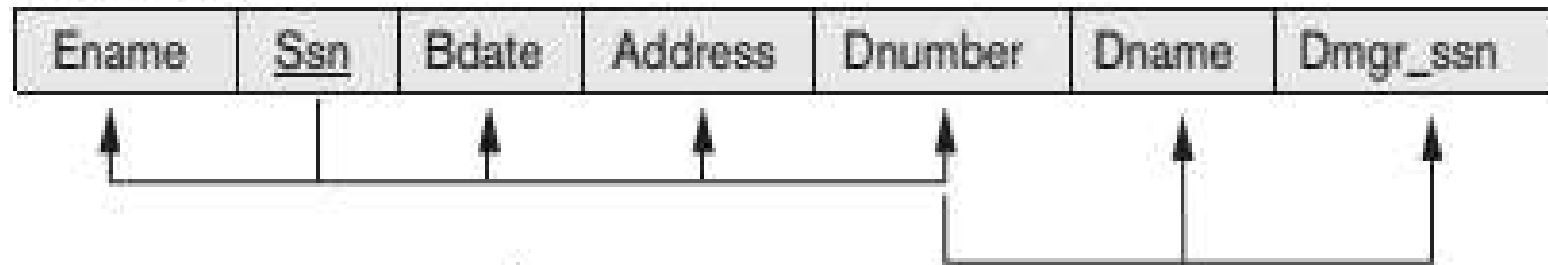
- ▶ L D qmjt c q g b g car rp l q g g c bcnc l bcl ag c q n p m jck  
g LD l b LD
- ▶ K crf mb g bcl r g w j j rp l q g g c bcnc l bcl ag c l b c af  
rp l q g g c bcnc l bcl awu g j d m p k l cu p c j r g m u g f  
l m n p g k r r p g s r c q n p r g a g n r g e g r f c rp l q g g c  
bcnc l bcl aw l b r f c r r p g s r c u f g a f b c r c p k g c q m r f c p q  
q r f c r r p g s r c q d m p r f c l cu p c j r g m



# 3NF

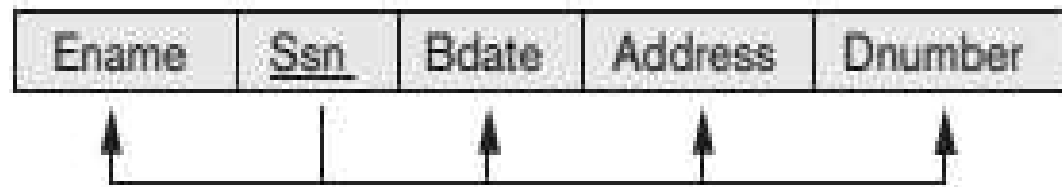
---

EMP\_DEPT

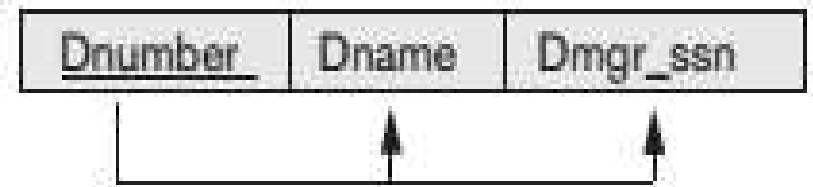


3NF Normalization

ED1



ED2



# Exercise

---

Am qgbcprf c sl g cpq j pcj rgm P A, B, C, D, E, F, G, H, I, J  
l b rf c qcr mdc l argm j bcnc l bcl agc q

1.  $A, B \rightarrow C$
2.  $A \rightarrow D, E$
3.  $B \rightarrow F$
4.  $F \rightarrow G H$
5.  $D \rightarrow I J$

U f r ggrf c i c w dmp R? Bcank nmqc R g rm LD rf cl LD  
pcj rgm q



# Normalization

---

- ▶ **1NF and dependency problems**
- ▶ **2NF – solves partial dependency**
- ▶ **3NF – solves indirect dependency**
- ▶ **4NF – solves multi-valued dependency**



# SUMMARY OF NORMAL FORMS based on Primary Keys

Summary of Normal Forms Based on Primary Keys and Corresponding Normalization

Normal Form	Test	Remedy (Normalization)
First (1NF)	Relation should have no multivalued attributes or nested relations.	Form new relations for each multi-valued attribute or nested relation.
Second (2NF)	For relations where primary key contains multiple attributes, no nonkey attribute should be functionally dependent on a part of the primary key.	Decompose and set up a new relation for each partial key with its dependent attribute(s). Make sure to keep a relation with the original primary key and any attributes that are fully functionally dependent on it.
Third (3NF)	Relation should not have a nonkey attribute functionally determined by another nonkey attribute (or by a set of nonkey attributes). That is, there should be no transitive dependency of a nonkey attribute on the primary key.	Decompose and set up a relation that includes the nonkey attribute(s) that functionally determine(s) other nonkey attribute(s).



# General Normal Form Definitions

---

- ▶ Rf c    nt c bcdg ggm q am qgbcprf c npgk   pwi cwm jw
- ▶ Rf c dhjmu g e k npc ecl cp j bcdg ggm qr i c g rm  
aans l r pcj rgm qu gf k sjrgnjc a l bgo rc i cwq



# General Normal Form Definitions

---

- ▶  $\rho \subseteq \rho'$  is a **second normal form (2NF)** if and only if for every non-prime attribute  $A$  in  $\rho$ ,  $A$  is fully functionally dependent on some prime attribute  $B$  in  $\rho'$ .  
 $\rho \subseteq \rho'$  is a **third normal form (3NF)** if and only if for every non-prime attribute  $A$  in  $\rho$ ,  $A$  is fully functionally dependent on some prime attribute  $B$  in  $\rho'$  or  $A$  is a prime attribute in  $\rho'$ .



# Normalization

---

- ▶ LD l b bcnc1 bcl awn~~pm~~ jck q
- ▶ LD qmjt cq n prg j bcnc1 bcl aw
- ▶ LD qmjt cq g bg~~pc~~ar bcnc1 bcl aw
- ▶ **BCNF – well-normalized relations**



# Normalization

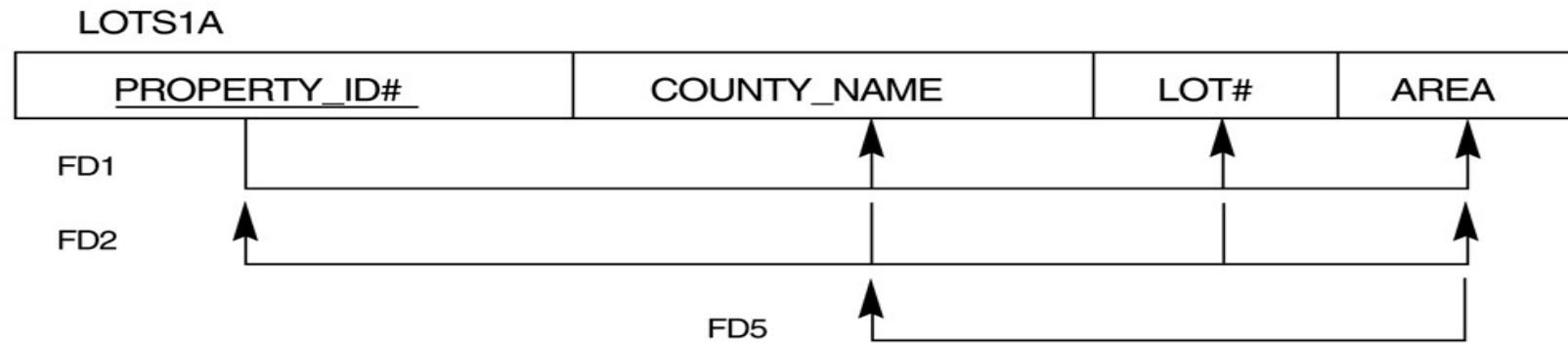
---

- ▶ **Boyce-Codd Normal Form (BCNF)**  
A DB is in BCNF if for every non-trivial FD  $V \rightarrow W$ ,  $V$  is a superkey.



# BCNF

(a)



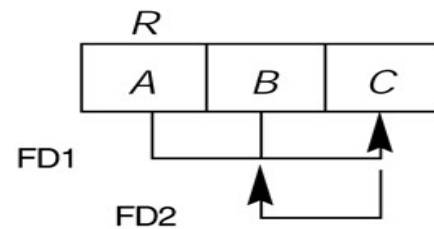
LOTS1AX



LOTS1AY



(b)



# BCNF

- RC AF Qrs bcl r Ans pqc G qrp s armp

FD1: {Student, Course} → Instructor

FD2:<sup>12</sup> Instructor → Course

## TEACH

Student	Course	Instructor
Narayan	Database	Mark
Smith	Database	Navathe
Smith	Operating Systems	Ammar
Smith	Theory	Schulman
Wallace	Database	Mark
Wallace	Operating Systems	Ahamad
Wong	Database	Omiecinski
Zelaya	Database	Navathe
Narayan	Operating Systems	Ammar

# BCNF

---

► Rf pcc nmqg jc n gpq

1. {Student, Instructor} and {Student, Course}.
2. {Course, Instructor} and {Course, Student}.
3. {Instructor, Course} and {Instructor, Student}.

► jj rf pcc bcank nmqggnl qlose the functional  
dependency *FD1* Rf c bcqgp jc bcank nmqggnl ndrnf nqc  
hsqr qf mu l gq ca sqc gu gj l nr ecl cp rc qns pgn s q  
rs njcq dcp hmg



# Nonadditive Join Decomposition into BCNF Schemas

---

**Algorithm 16.5.**  $Decompose(R, F)$  returns a set of BCNF schemas  $\{R_1, \dots, R_n\}$  such that  $R = R_1 \bowtie \dots \bowtie R_n$  and  $F = F_1 \cup \dots \cup F_n$  where  $F_i$  is the set of functional dependencies on  $R_i$ .

**Input:**  $R$  is a relation schema,  $F$  is a set of functional dependencies on  $R$ .

1.  $Q \leftarrow R$
2.  $U \leftarrow F$

while  $Q$  is not in BCNF do  
 choose a functional dependency  $f \in U$  such that  $f$  is not in BCNF  
 let  $R_1$  and  $R_2$  be the two schemas obtained by decomposing  $Q$  using  $f$   
 let  $U_1$  and  $U_2$  be the sets of functional dependencies on  $R_1$  and  $R_2$  respectively  
 let  $Q \leftarrow R_1$  and  $U \leftarrow U_1 \cup U_2$





# Contents

---

---

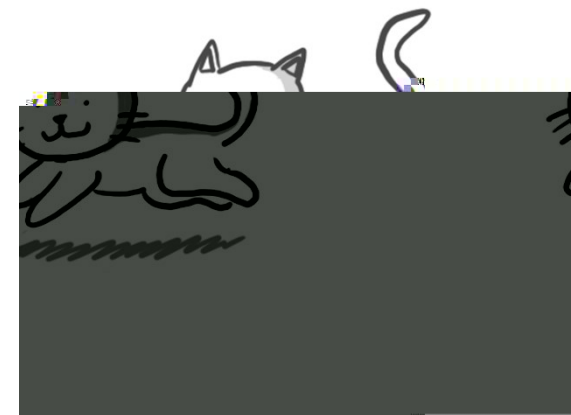
G rpnbs argn

Dsl argn j bcnc l bcl agc q

L mpk jgx rgn

---





# Exercise

Am qgbcprf c sl g cpq j pcj rgm P A, B, C, D, E, F, G, H, I, J  
 l b rf c qcr mdc l argm j bcnc l bcl agc q

1)  $A, B \rightarrow C$

2)  $B, D \rightarrow E, F$

3)  $A, D \rightarrow G, H$

4)  $A \rightarrow I$

5)  $H \rightarrow J$  Bcamk nmqc R g rm LD rf cl LD pcj rgm q

Second (2NF)

For relations where primary key contains multiple attributes, no nonkey attribute should be functionally dependent on a part of the primary key.

Decompose and set up a new relation for each partial key with its dependent attribute(s). Make sure to keep a relation with the original primary key and any attributes that are fully functionally dependent on it.

Third (3NF)

Relation should not have a nonkey attribute functionally determined by another nonkey attribute (or by a set of nonkey attributes). That is, there should be no transitive dependency of a nonkey attribute on the primary key.

Decompose and set up a relation that includes the nonkey attribute(s) that functionally determine(s) other nonkey attribute(s).

# Exercise

---

- ▶ Am qgbcprf c pcj rgm

## **BOOK (Book\_Name, Author, Edition, Year)**

- ▶ qcb m ank k m qcl qcl bcpqr l bg e mdrf c b r  
u f r pc rf c nm qg jc a l bg rc i cw q mdrf g pcj rgm

Book_Name	Author	Edition	Copyright_Year
DB_fundamentals	Navathe	4	2004
DB_fundamentals	Elmasri	4	2004
DB_fundamentals	Elmasri	5	2007
DB_fundamentals	Navathe	5	2007



# Exercise

Rp l e F zaf l f m RNF AK  
**PHIẾU ĐIỂM - Học kỳ 1 năm 2008**

- ▶ *MSSV:*
- ▶ *Tên sinh viên:* Lesw l T l
- ▶ *Địa chỉ:* l RV zaf l f m
- ▶ *Khoa:* l f m f a i rfs rk zwr l f

Mã môn học	Tên môn học	Nhóm	Số TC	Điểm KT	Điểm thi	Điểm tổng kết
	ARBJ ER	RL				
	AQBJ	A				

- ▶ *Ghi chú:* R wr l e k l f a q a f q a g k i g k rp ty  
g k rf gi f zalf s g k r lei r arlf b rp l g k  
l R g k rf gty azaf q l yw

# Key finding algorithms

Extended part

# Key and super key

---

- ▶ **Superkey** of R: A set of attributes **SK** of **R** such that no two tuples in any valid relation instance  $r(R)$  will have the same value for SK. That is, for any distinct tuples  $t_1$  and  $t_2$  in  $r(R)$ ,  $t_1[SK] \neq t_2[SK]$
- ▶ **Key** of R: A "**minimal**" **superkey**; that is, a superkey  $K$  such that removal of any attribute from  $K$  results in a set of attributes that is not a superkey
- ▶ If  $K$  is a **key** of  $R$ , then  $K$  **functionally determines all attributes** in  $R$



# Key-finding algorithm (1)

---

**Input:** *A relation  $R$  and a set of functional dependencies  $F$  on the attributes of  $R$ .*

**Output:** *a key  $K$  of  $R$*

1. Set  $K$  to contain all attributes in  $R$
2. For each attribute  $A$  in  $K$  {  
compute  $(K - A)^+$  with respect to  $F$ ;  
if  $(K - A)^+$  contains all attributes in  $R$ , then  
    set  $K := K - \{A\}$   
};





## Key-finding algorithm (1)

---

- ▶ In algorithm (1), we start by setting  $K$  to all the attributes of  $R$ ; we then remove one attribute at a time and check whether the remaining attributes still form a superkey.
- ▶ The algorithm (1) determines only **one key** out of the possible candidate keys for  $R$ ; the key returned depends on the order in which attributes are removed from  $R$  in step 2.



## Key-finding algorithm (2)

---

**Input:** A relation  $R$  and a set of functional dependencies  $F$  on the attributes of  $R$ .

**Output:** all candidate keys of  $R$

Let:

- ▶  $U$  contain **all** attributes of  $R$
- ▶  $U_l$  contain attributes of  $R$  that occur **only** on the **left-hand side** of FDs in  $F$
- ▶  $U_r$  contain attributes of  $R$  that occur **only** on the **right-hand side** of FDs in  $F$
- ▶  $U_b$  contain attributes of  $R$  that occur on **both sides** of FDs in  $F$

Note:

- ▶  $U_l \cap U_r = \emptyset$ ,  $U_l \cap U_b = \emptyset$  and  $U_r \cap U_b = \emptyset$
  - ▶  $U_l \cup U_r \cup U_b = U$
  - ▶ For every attribute  $A \in U$ , if  $A \in U_l$ , then  $A$  **must be** part of every candidate key of  $R$ .
  - ▶ For every attribute  $A \in U$ , if  $A \in U_r$ , then  $A$  will **not** be part of any candidate key of  $R$ .
- 



## Key-finding algorithm (2)

---

**Input:** A relation  $R$  and a set of functional dependencies  $F$  on the attributes of  $R$ .

**Output:** all candidate keys of  $R$

1. Determine  $U_l$ ,  $U_r$  and  $U_b$
2. If  $U_l^+ = U$  under  $F$ , then  $U_l$  forms the only key of  $R$  and the algorithm stops here.  
Else: move to step 3 //  $U_l^+ \neq U$  under  $F$
3. Consider every subsets  $U_{bi}$  of  $U_b$ :  $U_{bi} \subset U_b$   
For each  $U_{bi}$ , if  $(U_l \cup U_{bi})^+ = U$  under  $F$ , then  $K_i = (U_l \cup U_{bi})$  is a candidate key of  $R$  (\*)

(\*) If  $K_i = (U_l \cup U_{bi})$  is a candidate key of  $R$ , then we need not to check  $U_{bj} \subset U_b$  where  $U_{bi} \subset U_{bj}$



## Key-finding algorithm (2)

---

- ▶ A simple categorization of attributes into the sets  $U_l$ ,  $U_r$  and  $U_b$  allows to distinguish between those attributes that will participate in the candidate keys of a relational database schema and those that do not.
- ▶ The algorithm (2) finds all candidate keys.



# Exercise 1

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Am qgbcprf c sl g cpq j pcj rgm P     $A, B, C, D, E, F$     l b  
rf c qcr mdc l argm    j bcnc l bcl agc q

1)  $A \rightarrow B$

2)  $C, D \rightarrow A$

3)  $B, C \rightarrow D$

4)  $A, E \rightarrow F$

5)  $C, E \rightarrow D$

U f r g r f c i c w d m p R?



## Exercise 2

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Am qgbcprf c sl g cpq j pcj rgm P A, B, C, D, E, F l b  
rf c qcr mdc l argm j bcnc l bcl agc q

1)  $A, D \rightarrow B$

2)  $A, B \rightarrow E$

3)  $C \rightarrow D$

4)  $B \rightarrow C$

5)  $A, C \rightarrow F$

U f r ggrf c i c w d m P? B c a n k n m q c R g r m L D r f c l L D  
pcj rgm q Ecl cp j L m p k j D m p k B c d g g r m q



## Exercise 3

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Am qgbcprf c sl g cpq j pcj rgm P A, B, C, D, E, F l b rf c qcr  
 mdc l argm j bcnc l bcl agc q

1)  $A \rightarrow$

2)  $C \rightarrow$  , D

3)  $A, F \rightarrow A, E$

U f r g r f c i c w d m p R? B c a n k n m q c R g r m L D L D l b A L D  
 pcj rgm q

$\rightarrow$

$A \rightarrow$

$A \rightarrow B$

$D \rightarrow A$

$D \rightarrow B$



Which of the following dependencies may hold in the above relation

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A	B	C	TUPLE#
10	b1	c1	1
10	b2	c2	2
11	b4	c1	3
12	b3	c1	4
12	b3	c1	4
13	b1	c1	5

- i.  $A \rightarrow B$ ,   ii.  $B \rightarrow C$ ,   iii.  $C \rightarrow B$ ,   iv.  $B \rightarrow A$ ,   v.  $C \rightarrow A$
- 





# QUIZ 2

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- ▶ Leywi g k rp
- ▶ Ml jg c l cJ
  - ▶ Rp a l e f g k a s
  - ▶ Rf geg l n f r
- ▶ L g b s l e
  - ▶ Af l e P c j r g n j j e c p
  - ▶ Af l e Q O J
  - ▶ Af l e L m p k j g x r g n

