C.01.01.Z1 – Biblioteca Simplificada de Gás Ideal

Aplicação em FTHA – Finite Time Heat Addition Otto Engine Model

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https://github.com/CNThermSci/ApplThermSci

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Equação de Estado (EoS): Comportamento $P-T-v$

$$Pv = RT \qquad\qquad P\bar{v} = \bar{R}T \qquad \rightarrow$$

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Equação de Estado (EoS): Comportamento $P - T - v$

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Cada equação com forma nas bases mássica, e molar, com $R = \bar{R}/M$ — armazenar $\bar{R}$ e M!

Modelo de $\bar{c}_p(T)$ Polinomial:

$$\bar{c}_p(T) = \sum_{i=1}^{4} a_i T^{i-1}, \qquad T_{min} \leqslant T \leqslant T_{max} \quad \rightarrow$$

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Armazenar a_i, T_{min} e T_{max} e saber as conversões (i) $a_i \to b_i$ e (ii) $\bar{c}_{p,v}(T) \to c_{p,v}(T)$.

Modelo de $\bar{c}_p(T)$ Polinomial: $\bar{u}(T)$

$$\bar{u}(T) = \int_{T_{ref}}^{T} \bar{c}_v(T)\, dT = \int_{T_{ref}}^{T} \sum_{i=1}^{4} b_i T^{i-1}\, dT, \qquad T_{min} \leqslant T \leqslant T_{max} \qquad \rightarrow$$

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Modelo de $\bar{c}_p(T)$ Polinomial: $\bar{h}(T) = \bar{u}(T) + \bar{R}T$

$$\bar{h}(T) = \int_{T_{ref}}^{T} \bar{c}_p(T)\, dT + \bar{R}T_{ref} = \int_{T_{ref}}^{T} \sum_{i=1}^{4} a_i T^{i-1}\, dT + \bar{R}T_{ref}, \quad T_{min} \leqslant T \leqslant T_{max} \qquad \rightarrow$$

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Modelo de $\bar{c}_p(T)$ Polinomial: $P_r(T)$ e $v_r(T)$

$$\left(\frac{P_2}{P_1}\right)_s = \frac{P_{r2}}{P_{r1}}$$

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$$P_r(T) \equiv e^{\bar{s}^\circ(T)/\bar{R}} \qquad P_r(T) = e^{s^\circ(T)/R}$$

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- Sem requisitos adicionais de armazenamento!

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- Sem conversões de base!

Generalização de Coeficientes:

$$\bar{c}_p(T) = a_1 + a_2 T + a_3 T^2 + a_4 T^3, \qquad T_{min} \leqslant T \leqslant T_{max} \qquad \rightarrow$$

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Photo by Josh Sorenson from Pexels