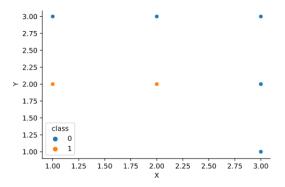
DATA 301: Decision Trees A Supervised Algorithm

Topics

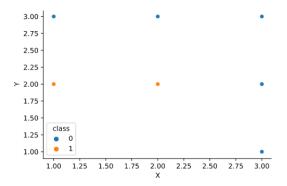
Demonstration
Impurity
Choosing which feature to split on scikit-learn

What if data is not linearly separable?



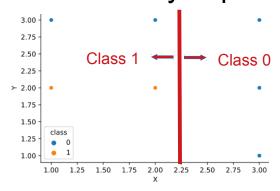
For this data you cannot draw a line that cleanly separates class 0 from class 1

What if data is not linearly separable?



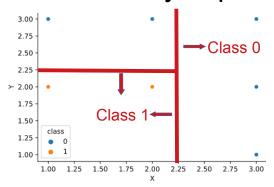
But you can use multiple line segments to do so.

What if data is not linearly separable?



But you can use multiple line segments to do so. The first

What if data is not linearly separable?



But you can use multiple line segments to do so. The first
The second

Easy to do for 2 dimensions, what about 4 or 8 dimensions? How to do this algorithmically? Especially since data looks like this.

	X	Y	class
0	1	3	а
1	2	3	a
2	3	3	а
3	1	2	b
4	2	2	b
5	3	2	а
6	3	1	а

Using 2 common algorithms:

- entropy and information gain
- gini impurity

We will use gini impurity for this class. It's calculated with the following equation

```
gini_impurity=1- (probability class A)**2 - (probability class B)**2 - (probability class C)**2 ... (probability class n)**2
```

	X	Y	class
0	1	3	а
1	2	3	а
2	3	3	а
3	1	2	b
4	2	2	b
5	3	2	а
6	3	1	а

Back to the problem
We want to predict class using features X and Y

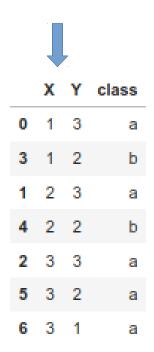
Where to start?



Back to the problem
We want to predict class using features X and Y

Where to start?

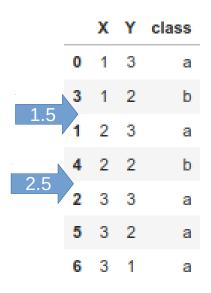
Start with first column (X)



Back to the problem
We want to predict class using features X and Y

Where to start?

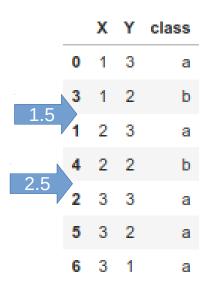
Start with first column (X)
Sort it ascending



Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)
Sort it ascending
Find midpoints between adjacent values

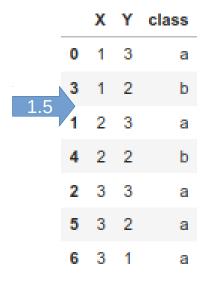


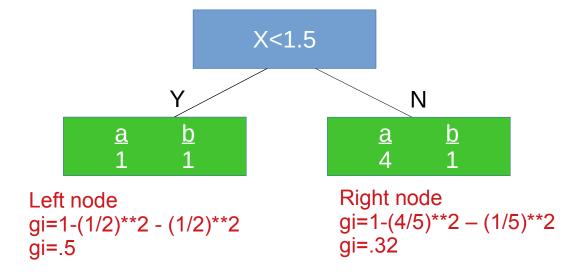
Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)
Sort it ascending
Find midpoints between adjacent values
Find gini impurity using each of these midpoints

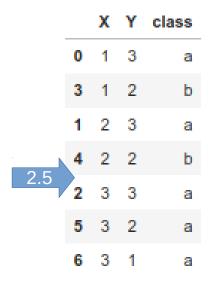
gini_impurity=1- (probability class A)**2 - (probability class B)**2

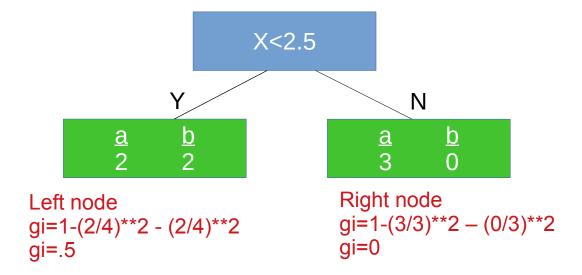




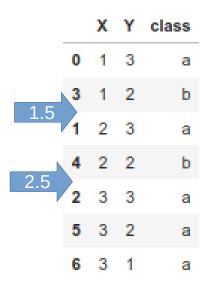
Gini impurity for column X at split 1.5 is a weighted average though Weights = (total values in node)/(total values in both nodes)

gini_impurity=1- (probability class A)**2 - (probability class B)**2





Gini impurity for column X at split 2.5 is a weighted average though Weights = (total values in node)/(total values in both nodes)



Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)

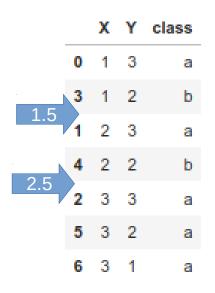
Sort it ascending

Find midpoints between adjacent values

Find gini impurity using each of these midpoints

Choose split with lowest value

Col X \rightarrow Choose split 2.5 with GI=.28



Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)

Sort it ascending

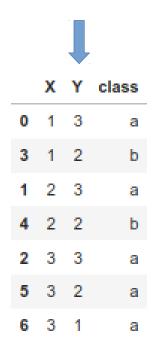
Find midpoints between adjacent values

Find gini impurity using each of these midpoints

Choose split with lowest value

Col X \rightarrow Choose split 2.5 with GI=.28

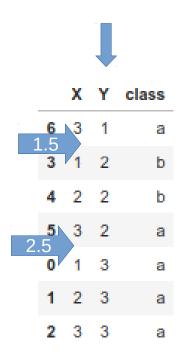
Repeat for all other columns (except the target 'class')



Back to the problem
We want to predict class using features X and Y

Where to start?

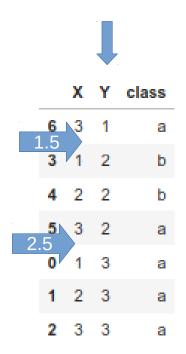
Choose column (Y)



Back to the problem
We want to predict class using features X and Y

Where to start?

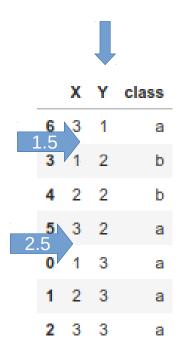
Choose column (Y)
Sort it ascending



Back to the problem
We want to predict class using features X and Y

Where to start?

Choose column (Y)
Sort it ascending
Find midpoints between adjacent values



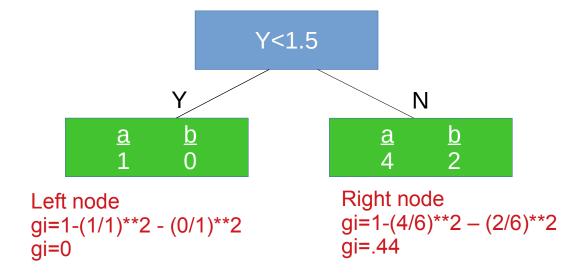
Back to the problem
We want to predict class using features X and Y

Where to start?

Choose column (Y)
Sort it ascending
Find midpoints between adjacent values
Find gini impurity using each of these midpoints

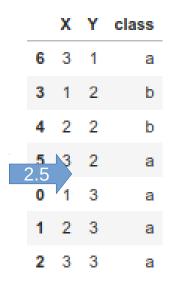
gini_impurity=1- (probability class A)**2 - (probability class B)**2

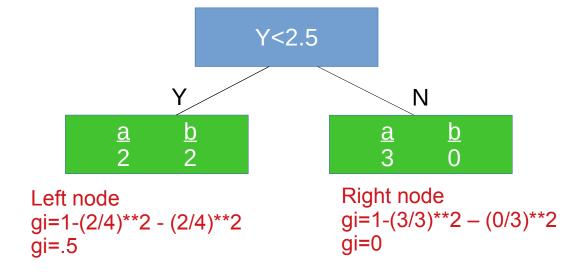
		X	Y	class
. 1	6 5	3	1	a
	3	1	2	b
	4	2	2	b
	5	3	2	а
	0	1	3	a
	1	2	3	а
	2	3	3	а



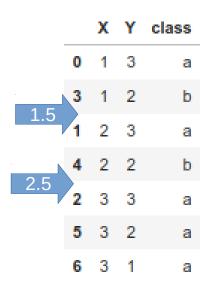
Gini impurity for column Y at split 2.5 is a weighted average though Weights = (total values in node)/(total values in both nodes)

gini_impurity=1- (probability class A)**2 - (probability class B)**2





Gini impurity for column X at split 2.5 is a weighted average though Weights = (total values in node)/(total values in both nodes)



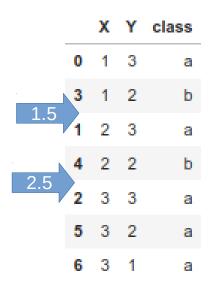
Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)
Sort it ascending
Find midpoints between adjacent values
Find gini impurity using each of these midpoints

1.5 => GI=.37

2.5=> GI=.28



Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)

Sort it ascending

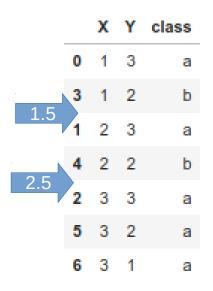
Find midpoints between adjacent values

Find gini impurity using each of these midpoints

Choose split with lowest value

Col X \rightarrow Choose split 2.5 with GI=.28

Col Y→ Choose split 2.5 with GI=.28



Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)

Sort it ascending

Find midpoints between adjacent values

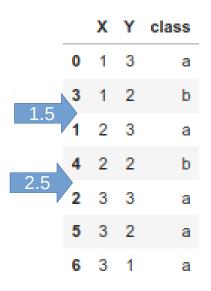
Find gini impurity using each of these midpoints

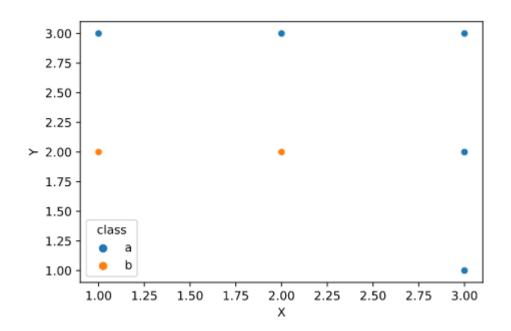
Choose split with lowest value

Col X \rightarrow Choose split 2.5 with GI=.28

Col Y→ Choose split 2.5 with GI=.28

Why are they both the same?

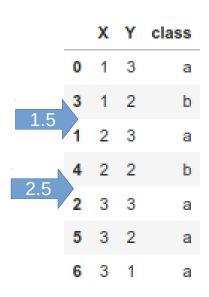


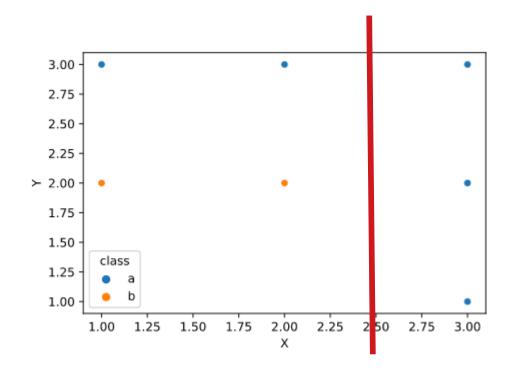


Why are they both the same?

Because it doesn't matter whether we split on X=2.5 or Y=2.5,

we still have 3 a's on 1 side and 2 a's and 2 b's on the other

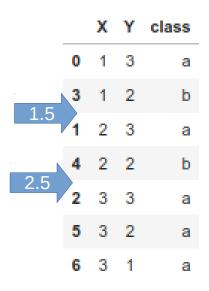


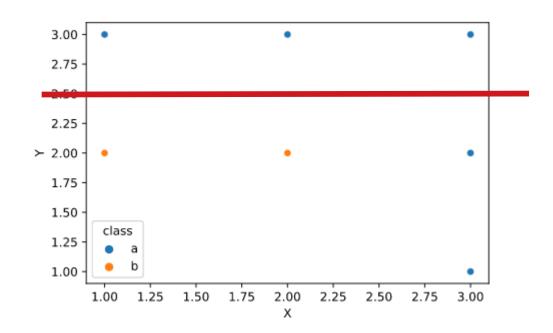


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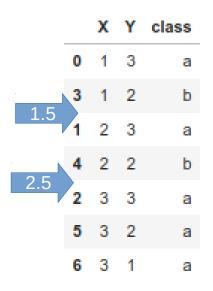




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Back to the problem
We want to predict class using features X and Y

Where to start?

Start with first column (X)

Sort it ascending

Find midpoints between adjacent values

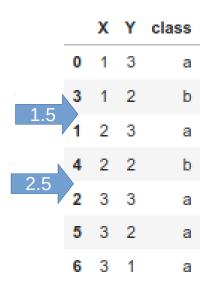
Find gini impurity using each of these midpoints

Choose split with lowest value

Col X \rightarrow Choose split 2.5 with GI=.28

Col Y→ Choose split 2.5 with GI=.28

Why are they both the same?



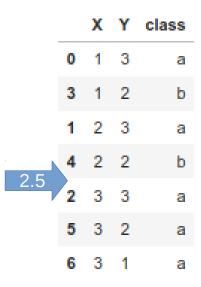
Back to the problem
We want to predict class using features X and Y

Where to start?

Keep splitting the dataset until;

- 1. a node has a gini impurity less than any of the column splits, in which case leave it as is
- 2. a node has a gini impurity of 0, in which case leave it as is since it only has 1 class
- 3. you reach the maximum depth of branches. (Maximum depth is a hyperparameter)

Scikitlearns Decision Tree



Scikitlearn Decision Tree

```
from sklearn import tree
df2=df.to numpy();
clf = tree.DecisionTreeClassifier()
clf.fit(X=df2[:,:-1],y=df2[:,-1]);
tree.plot tree(clf);
#for root node; gi= 1-(5/7)**2 -(2/7)**2=0.408
                         X[1] \le 2.5
                         gini = 0.408
                         samples = 7
                        value = [5, 2]
               X[0] \le 2.5
                                     gini = 0.0
                gini = 0.5
                                    samples = 3
              samples = 4
                                   value = [3, 0]
              value = [2, 2]
      gini = 0.0
                           qini = 0.0
    samples = 2
                         samples = 2
   value = [0, 2]
                        value = [2, 0]
```

Summary

- How to split by eye
- What gini impurity is
- How to use gini impurity to find the best features to split on and the best split points (it approximates a humans split by eye approach by splitting on midpoints of adjacent features)
- Scikit learns decision tree