

**Table 3: Some notations and their corresponding explanations used in the paper.**

|   |  |
|---|--|
| $\mathcal{U} = \{u\}$   | the set of users   |
| $\mathcal{V} = \{v\}$   | the set of items   |
| $\mathcal{B}$   | the set of user behaviors  |
| $k$   | behavior types for the enumeration or illustration   |
| $v_u^\ell \in \mathcal{V}$  | the item interacted with by user $u$ at the $\ell$ -th time step   |
| $\mathbf{b}_u^\ell \in \mathbb{R}^{ \mathcal{B} }$                | the behavior set (multi-hot vector) involved in the interaction term of user $u$ at the $\ell$ -th time step   |
| $b_{u,k}^\ell \in \{0, 1\}$                                       | $b_{u,k}^\ell = 1$ if user $u$ has an interaction on item $v_u^\ell$ with the $k$ -th behavior at the $\ell$ -th time step, otherwise $b_{u,k}^\ell = 0$ |
| $\mathcal{S}_u = \{(v_u^\ell, \mathbf{b}_u^\ell)\}$               | the interaction sequence with behavior set of user $u$   |
| $d \in \mathbb{R}$  | latent dimension of embeddings   |
| $L \in \mathbb{R}$  | length of the user sequence  |
| $I \in \mathbb{R}^{ \mathcal{V}  \times d}$                       | the embedding look-up table for all the items  |
| $E \in \mathbb{R}^{L \times d}$                                   | the matrix form of item embeddings for the whole user sequence   |
| $P \in \mathbb{R}^{L \times d}$                                   | position embedding matrix  |
| $G \in \mathbb{R}^{ \mathcal{B}  \times d}$                       | global behavior embedding matrix   |
| $\mathcal{F} \in \mathbb{R}^{ \mathcal{U}  \times  \mathcal{B} }$ | user behavioral preference factor matrix   |
| $\mathbf{e}_{v_u^\ell} \in \mathbb{R}^{1 \times d}$               | item embedding of item $v_u^\ell$  |
| $\mathbf{p}_\ell \in \mathbb{R}^{1 \times d}$                     | position embedding at the $\ell$ -th time step   |
| $\boldsymbol{\beta}_u^\ell \in \mathbb{R}^d$                      | embedding of the behavior set corresponding to the interaction term of user sequence $\mathcal{S}_u$ at the $\ell$ -th time step                         |
| $B \in \mathbb{R}^{L \times d}$                                   | the matrix form of behavior set embeddings for the whole user sequence   |
| $\mathfrak{B} \in \mathbb{R}^{L \times  \mathcal{B} }$            | the matrix form of behavior set multi-hot vectors for the whole user sequence  |
| $\alpha$  | the sampling constant in PSA   |
| $C$   | the total number of blocks of L-MSAB   |
| $H$   | the total number of heads in PSA mechanism   |
| $\star \in \{(ib), (pb)\}$  | used to distinguish representations from different perspectives  |
| $\tilde{X} \in \mathbb{R}^{L \times d}$                           | the output representations from the DCBA layer   |
| $H \in \mathbb{R}^{L \times L}$                                   | Hamming distance attention weight matrix   |
| $M^s \in \mathbb{R}^{L \times  \mathcal{B} }$                     | scaling mask in UB-FEEL  |
| $M^e \in \mathbb{R}^{L \times  \mathcal{B} }$                     | embedding enhancement mask in UB-FEEL  |
| $M_\Delta \in \mathbb{R}^{u \times L}$                            | causality mask corresponding to the indices of the top- $u$ queries in PSA   |
| $\overline{X}_k^{(h)} \in \mathbb{R}^{u \times \frac{d}{H}}$      | the output representations with top- $u$ dominant queries under the $k$ -th behavior for head $h$ in PSA   |
| $\hat{X}_k \in \mathbb{R}^{L \times d}$                           | the output representations of L-MSAB under the $k$ -th behavior  |
| $\mathbf{y}^{\ell+1} \in \mathbb{R}^{1 \times d}$                 | non-user-personalized behavior set embedding at the $(\ell+1)$ -th time step   |
| $X^{\text{EMP}} \in \mathbb{R}^{L \times d}$                      | the output representations along EMP   |
| $X^{\text{IMP}} \in \mathbb{R}^{L \times d}$                      | the output representations along IMP   |