
Algorithm 1: ProbSparse multi-head self-attention

Input : Tensor $X \in \mathbb{R}^{L \times d}$ for representations of behavior-specific sequences

Output: Final output representations $\text{PSA}(X) \in \mathbb{R}^{L \times d}$

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1 foreach head  $h = 1$  to  $H$  do  
2    $Q_h \leftarrow f_{Q_h}(X), K_h \leftarrow f_{K_h}(X), V_h \leftarrow f_{V_h}(X);$   
3   Randomly select  $u$  dot-product pairs from  $K_h$  as  $\bar{K}_h$ ,  
   where  $u = \alpha \ln L$ ;  
4   Calculate  $\bar{M}$  through Eq.(15) with  $Q_h$  and  $\bar{K}_h$ ;  
5   Select the top- $u$  queries under  $\bar{M}$  as  $\bar{Q}_h$ ;  
6   Calculate  $X_1^{(h)}$  through Eq.(16);  
7   Set  $X_0^{(h)} = \text{mean}(V_h)$ ;  
8    $\text{PSA}^{(h)}(X) \leftarrow [X_1^{(h)}, X_0^{(h)}]$ , which concatenates along  
   the row axis;  
9 end  
10  $\text{PSA}(X) \leftarrow \text{concat}(\text{PSA}^{(1)}(X), \dots, \text{PSA}^{(H)}(X))W_L;$   
11 return  $\text{PSA}(X)$ 
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