



So far, we've talked about systems that "just" react. Even with systems that have memory, we can't say they're learning. Because they never change their policies. Even Bayesian networks don't really "learn" as much as process sensory data with diff. conditions.

That's because we need some way of assigning value to an action. Was this the right or wrong choice? Does this work or not work? This is called UTILITY.

Utility, as a concept, comes from economics. Often, it's talked about abstractly, i.e. it has no unit. But concretely it's often operationalized as price.


you
have
chocolate
bar


I
want
it

→ we negotiate. → $\text{Value} =$
 $\text{\$ price}$
 $=$
 $\text{\$1.00}$

so we can say the chocolate bar
is worth \$1.00 and must therefore
give me \$0.00 of utility.

I want to point out a divergence between his model and reality.

1. Humans can predict, recall, learn. $\$1 \neq \1.00 if your $\$1/\1000 vs. $\$1/1000000$.
2. Most things don't have a value.
"money can't buy you love" is literally true.
3. Even within strict preference models, price shifts. E.g. Kelowna.

But utility is (potentially) comparable.
So, it is the basis of our modelling.

Blacksmith in Dist. Kingdom.

Purse $\frac{\text{lab.}}{\text{prod.}} = \text{Labour Per unit of Value}$
10 coins

prod = +1 to value and inventory.

1 unit of raw = \$1.

King ^{Bezos.} has set up a distribution network.

Each day, a cart will stop. You can:

- 1) go and sell what you've made.
- 2) Buy a ^{raw.} product material.
- 3) wait and do nothing
- 4) spend the day producing something.

you tell the cart man every day for tomorrow.

Buy sell wait produce.
-1 +2 ϕ ϕ

obviously:

sell > wait = produce > buy = profits

If your policy is strictly $\arg\max(\text{profits})$,
you would never make or buy anything!

Instead:

coin?	prod?	wait?	action.
Y	N	N	buy

★ fill out the rest.

Let's say the coin is now true random.

You probably need a more complex
policy. e.g.

★ coin < 2 coin > 10 ... etc.

and you need to pick when it "washed"!

now let's say you need to schedule ppl.

produce now is -10 and needs advance
commitment. But sell is now
+40 because of efficiency.
coin still random.

★ schedule policy.

Now let's say that the costs "look" (4)
 random, but there actually is a pattern.
 The pattern is mostly consistent but not
 perfectly. How do you learn the best
 policy?

Introduce Q-learning, a type of reinforcement learning.

$Q: S \times A \rightarrow \mathbb{R}$ → reward
↓ ↘
 state action buy, sell, wait,
produce.

coin inv. raw inv. prod.

The idea is ~~then~~ to make a big table
 of future reward so:

$\frac{c}{10} \quad \frac{r}{0} \quad \frac{prod}{1} \times \text{sell} \rightarrow +40$

may be true in a moment, but might
 be long-run costly if faced with a choice
 to buy raw. why?

$\frac{c}{100} \quad \frac{r}{0} \quad \frac{prod}{0} \quad \times \text{sell} \rightarrow 0$

so abstract utility s.t.

$\frac{c}{100} \quad \frac{r}{0} \quad \frac{prod}{1} \times \text{sell} < \frac{c}{10} \quad \frac{r}{0} \quad \frac{prod}{1} \times \text{buy}$

⑤

★ Time table so that ~~that~~ a 5-day week can be "planned" using just utility values.

This is hard. Essentially impossible to design by hand w/o very restricted circumstances.

Translate to the robot. How could

★ you reward + punish your robot?

COGS 300

Distribution 02

NOV 6/25 ①

Warm up: Draw networks with "islands" ... what does it take to make an island into a ... "peninsula"?



vs.



Meet the profs 2hr @ 5pm
Koerner's.

utility = value

$u(\text{action}) = \text{value}$

stick figure ~ stick figure \$1.00

(2)

$$\frac{1}{1000} = \$100 = 20$$

equal pref.

1. $\$1/1000$ $\$1/1000000$

2. "money unit by you love."

3. Kahneman

Blacksmith iron \rightarrow products



sell > wait = produce > buy

X $\arg\max(\text{actions}) \rightarrow \text{sell}$

	coin?	prod?	raw?	→ action ^③
policy	Y	N	N	buy
	Y	Y	N	→ sell
	Y	N	Y	→ produce
	N	Y	N	→ sell
	N	N	N	→ wait

what if cost is random?

$c < 2$ vs. $c > 10$

make a new policy table.

$c < 2 \rightarrow \text{sell}$

$p? = y$

$c > 10$

$\rightarrow \text{prod.}$

$p > 20$

$-5^{\text{th}} \text{ prod.}$

for the next week, you hire labourers. 4 iron \rightarrow 10 prod.

④
-5 because you're paying to produce
but you get +10 products.

			<u>c</u>	<u>raw</u>	<u>prod</u>
sell	+10		$\frac{c}{10}$	$\frac{raw}{5}$	$\frac{prod}{20}$
buy	-1	X			
produce	-5				
wait	0		<u>100</u>	<u>0</u>	<u>0</u>

↳ what else can you track
it costs aren't actually
random but just
appear so?

<u>day</u>	<u>c</u>	<u>raw</u>	<u>prod.</u>	<u>utility</u>	<u>action</u>
7th Nov	10	5	25	\$10	sell

⋮
Reinforcement Learning
Q-learning

$$Q: S \times A \rightarrow \mathbb{R}$$

state

actions

Reward

coin	raw	prod.
1	0	0
0	1	0
6	0	1

actions → Reward

sell

buy

buy → -1 Reward

buy, produce, sell → (+10)

1. State tracking?
2. Actions?
3. Reward?