

control 03

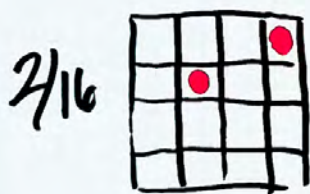
6065 300

Feb 03/26

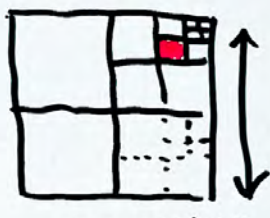
①

Warm up: discretizations + tiling.

Create different "grids": \longleftrightarrow



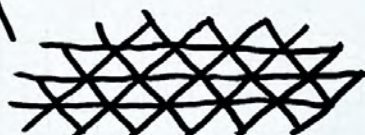
cartesian



recursive



polar



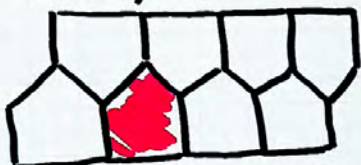
triangular



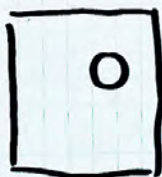
1D
linear

etc...

1/8



pentagon-ish



p (point
is
covered) ?

$r = 1 \text{ cm}$

$A = 21 \times 29.7 \text{ cm}^2$



← 22 →

↑ 33 ↓

$$22 \times 33 = 726$$

$$\frac{1}{150} - \frac{1}{726}$$

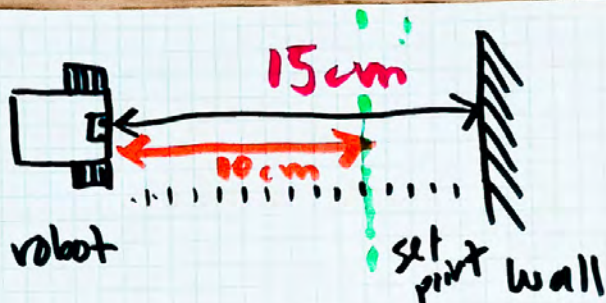
$$\frac{\pi r^2}{A} = \frac{1}{623.7}$$

$$0.0016$$

↑

$$r = 1 \text{ cm}$$
$$A = 21 \times 29.7 \text{ cm}^2$$

③



$$p(pos) = 1/15$$

go faster the farther we are
slower closer

out = map(dist, min, max, log hi);

PID = proportional integral derivative

current pos = pos = read();

set point = set = 5 cm;

error = pos - set;

output = out = c · error

"tuning"

err = 1 cm
out = 500

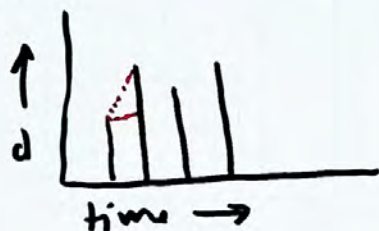
c = 500 err = 10
out = 5000

(4)

$c = 100$	$err = 10$	$out = 1000$
$c = 100$	$err = 1$	$out = 100$
$c = 17$	$err = 10$	$out = 170$
$c = 17$	$err = 1$	$out = 17$

Simulation + turning

d_0
 d_1
 d_2
 \vdots
 d_n



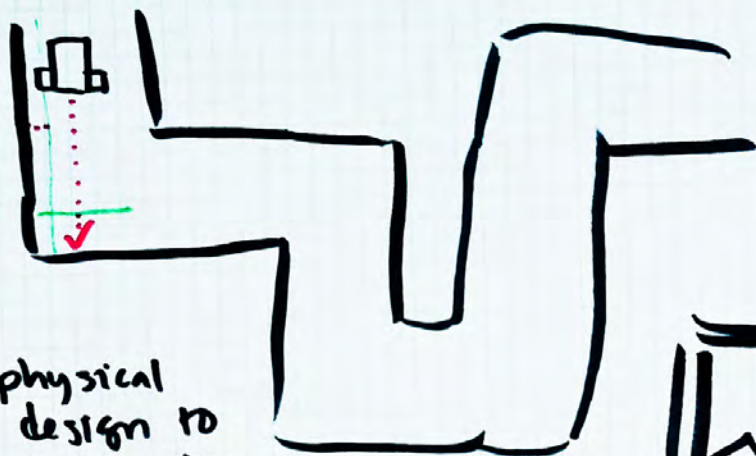
$$\frac{d_j - d_i}{1} = d_j - d_i$$

$$\Delta d$$

$$c \cdot \underset{P}{err} + a \cdot \underset{D}{\Delta err} + b \cdot \underset{I}{\sum err}$$

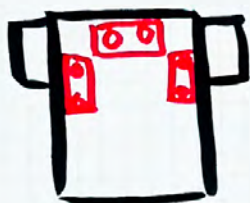


5



1. physical design to sense in maze

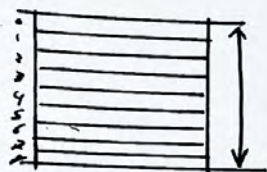
2. Algorithm for control



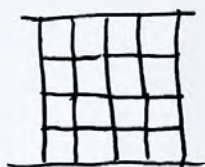
①

Control 03

Warm-up: Discretizations. + tiling



linear



cartesian

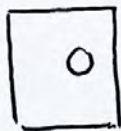


polar

recursive
cartesian

triangular

probability: if I throw a coin
onto a page, $P(\text{point is covered})$



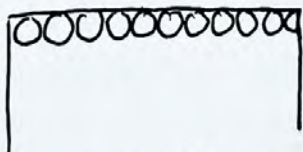
$$\frac{\text{area of coin}}{\text{area of page}} ?$$

$$p = \frac{\pi r^2}{A} = 1/623.7$$

$$r = 1 \text{ cm}$$

$$A = 21 \times 29.7 = 623.7$$

$r = 0.5$
 \hookrightarrow slower!



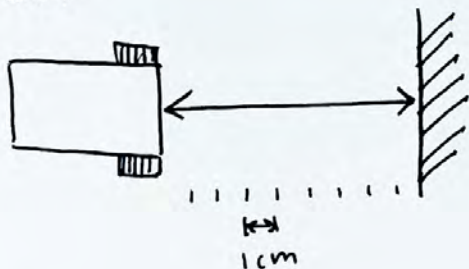
try it!

$\leftarrow 10 \rightarrow$
 $15 \updownarrow$

$$0.0066 \sim 0.0016 ?$$

$$\longleftrightarrow 1/150 \sim \frac{1}{623.7} ?$$

Robot.



$p(\text{Robot is @ 5cm})$

$$= 1/10$$

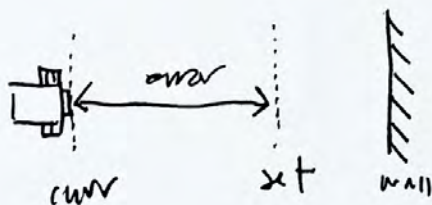
$$\frac{1 \text{ cm chunk}}{\# \text{ of chunks}}$$

→ robot doesn't "know," it has to guess.

Last time: alg. for driving to set point.

Key insight: go faster, further.

$\text{output} = \text{map}(\text{dist to set point,}$
 $\text{min dist, max dist,}$
 $\text{min motor, max motor}).$



$$\text{error} = \text{curr} - \text{set};$$

$$\text{output} = \text{map}(\text{error}, 0, 10, 0, 255);$$

→ but what about a diff. curve?

③

```


curr = read();
set = 5 cm; // cm
error = curr - set;
out = curr C * error
      ↑
    some constant
  
```


$C = 100$ $err = 5$ $out = 500$

$C = 50$ $err = 5$ $out = 250$

$C = 1/5$ $err = 5$ $out = 1$

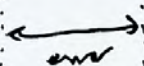
depends on your robot.

PWM  encoding

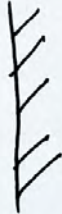
PID  control

control requires sensation + model.
to evaluate.

curr set

 err

↑
prediction.

 reference.

muscles
?

④


★ come up with a wall-following algorithm. + design

uses:

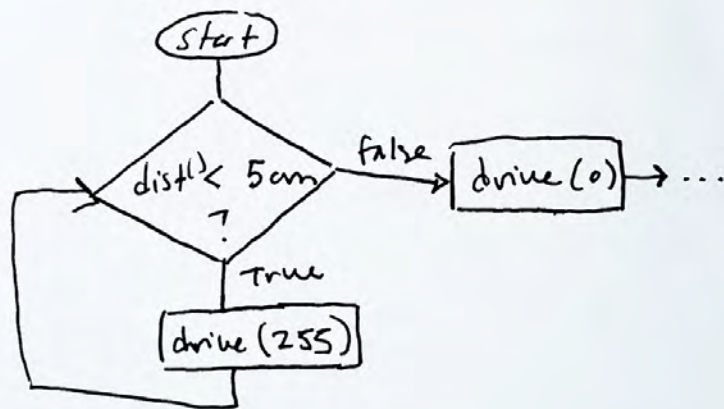


= straight

 inside

 outside.

- which sensors / where do you put them?
- which filters do you use, why?
- what is the algo?
- ↳ low level



why doesn't this "just work"?

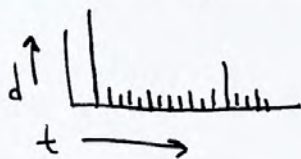
vs. PID version...

(5)

Shifting into a probabilistic
mindset...



How many measurements
until you're sure?



stability
of
signal

$$\Delta d = \text{change in } d = d_i - d_{i-1}$$

small Δd is small variation...
but also fragile!

$$\text{avg}(d_i : d_j) \quad \text{var}(\text{~~di~~ } d_i : d_j) \quad \text{etc.}$$

$$\vdots$$

$$p(\text{pos} \mid \text{measurement}) ?$$

$$\star \quad p(\text{pos})$$

$$p(\text{measurement}) ?$$