Course Announcements

- Due Friday (11:59 PM)
 - o D4
 - o Q4
 - o A2
- PLEASE be precise in autograded notebooks!!!

Grading underway: Project Proposals

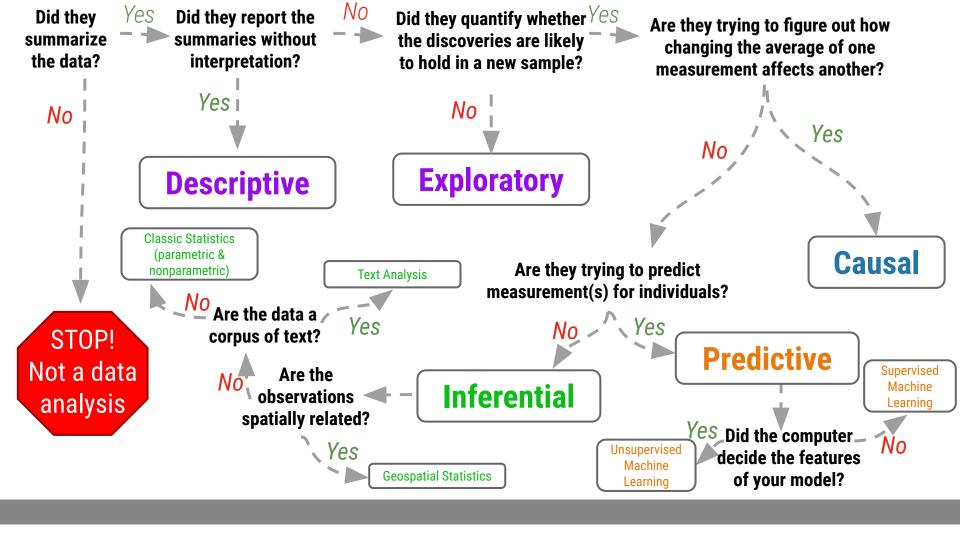
Inferential analysis

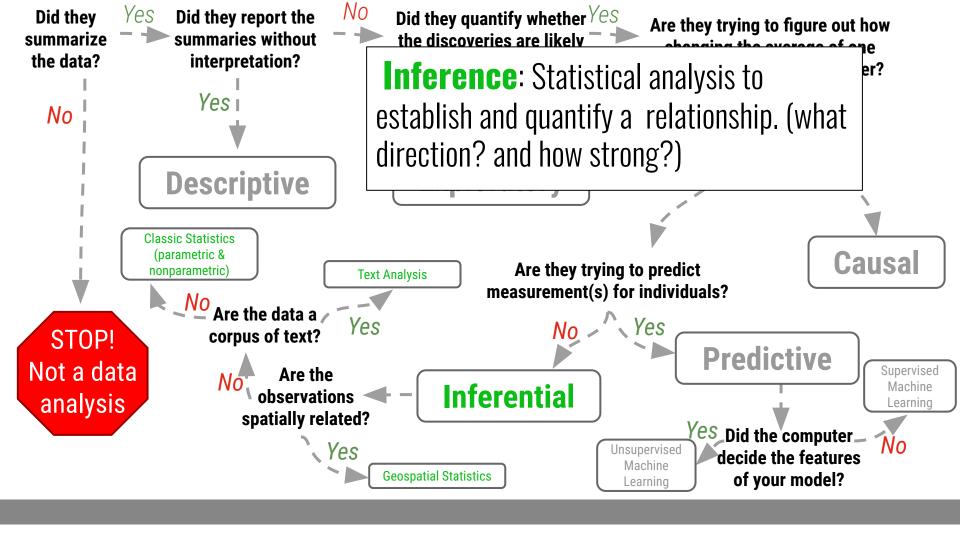
Jason G. Fleischer, Ph.D. **Asst. Teaching Professor** Department of Cognitive Science, UC San Diego



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- Problem: Does Sesame Street affect kids brain development?
- **Data science question:** What is the relationship between watching Sesame Street and test scores among children?
- **Type of analysis:** Inferential analysis



Sesame Street viewership



?? Test scores

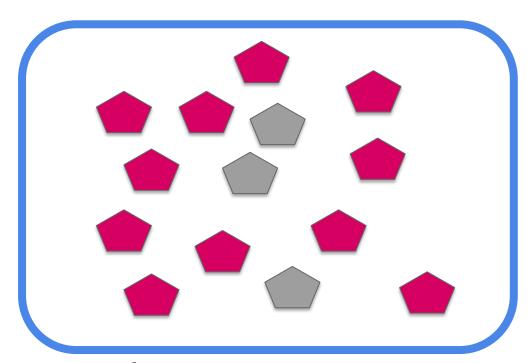
Establishing & Stating Your Null and Alternative Hypotheses Helps Guide Your Analysis

Null Hypothesis:

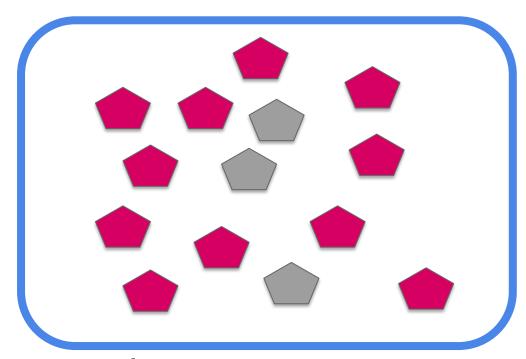
 H_0 : Sesame Street has *no effect* on kids brain development

<u>Alternative Hypothesis</u>:

H_a: Watching Sesame Street *has an effect* on kids' brain development



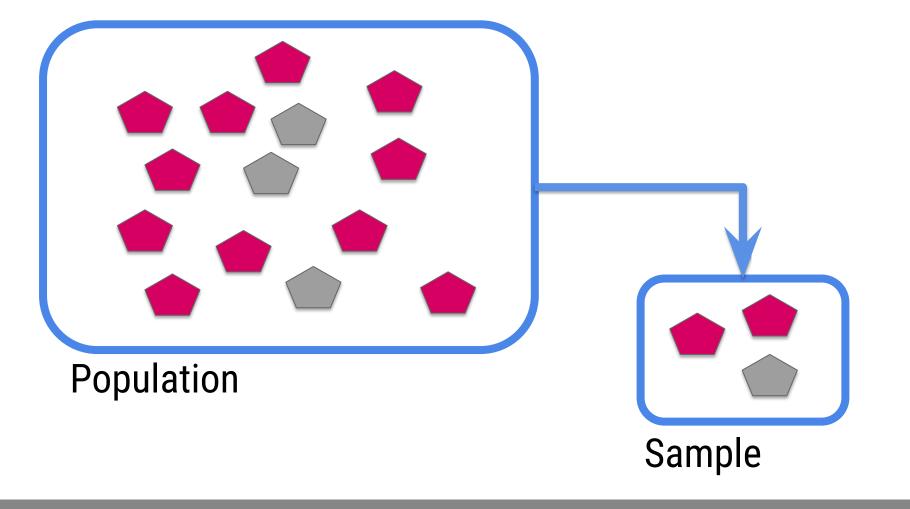
Population

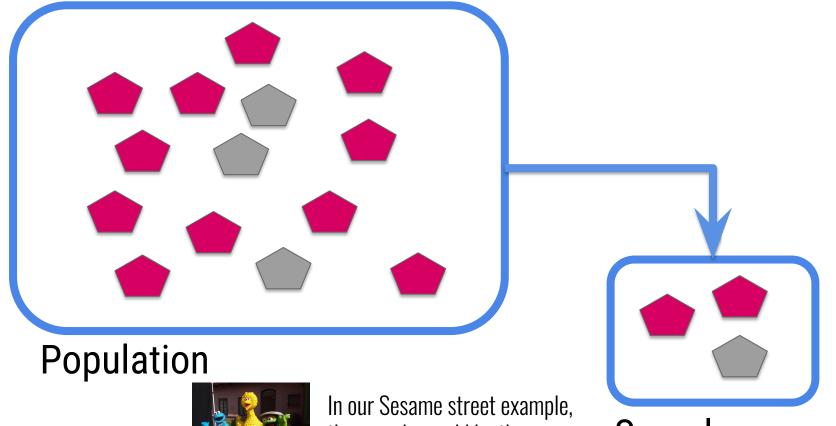


Population



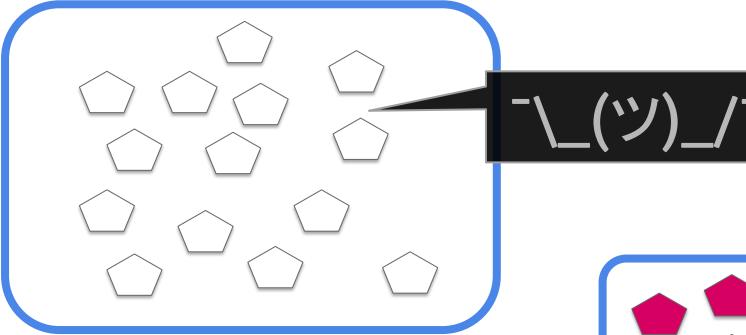
In our Sesame street example, the <u>population</u> would be all children



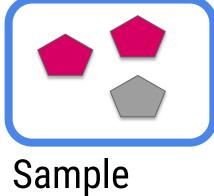


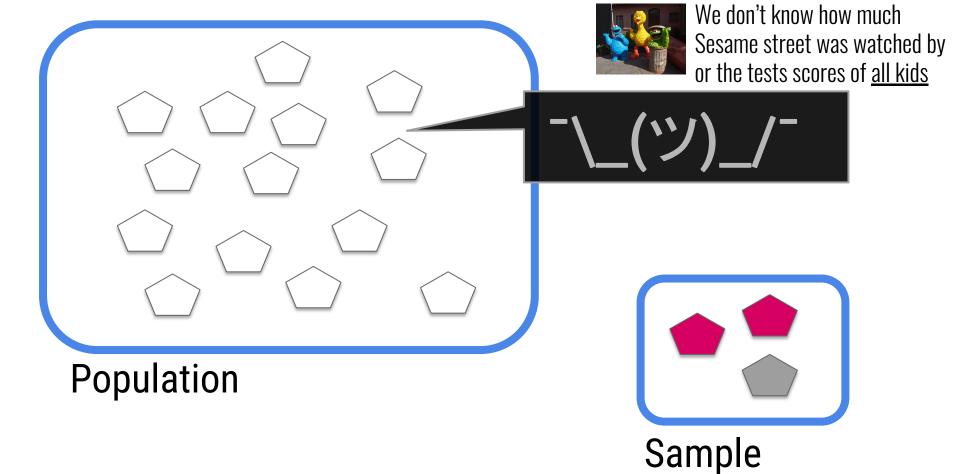
the <u>sample</u> would be the children included in the study

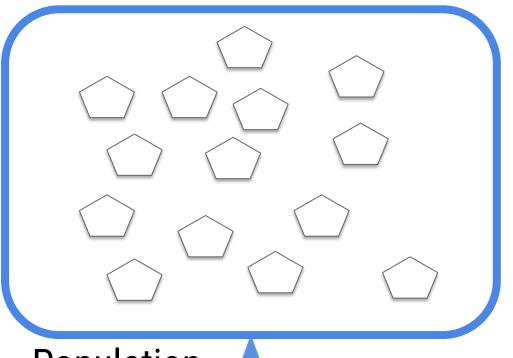
Sample



Population



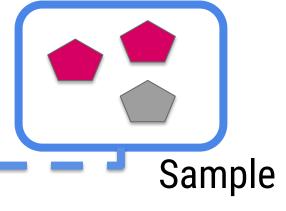




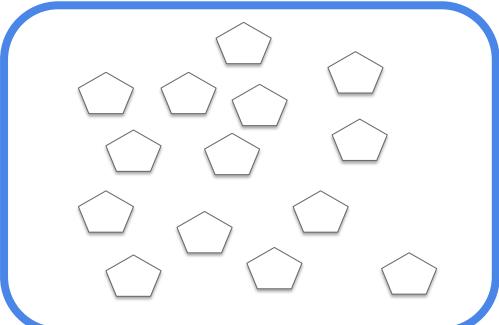
Based on the relationship we see in our sample, we can <u>infer</u> the answer to our question in our population

Population





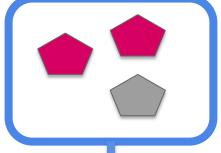
Inference!





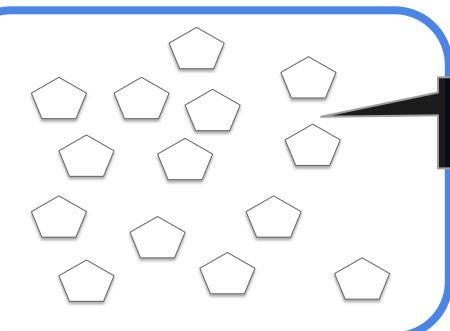
So we look at Sesame street viewing and test scores in a representative sample of kids





Inference!

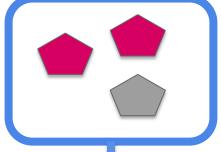
Sample



Best guess



So we look at Sesame street viewing and test scores in a representative sample of kids

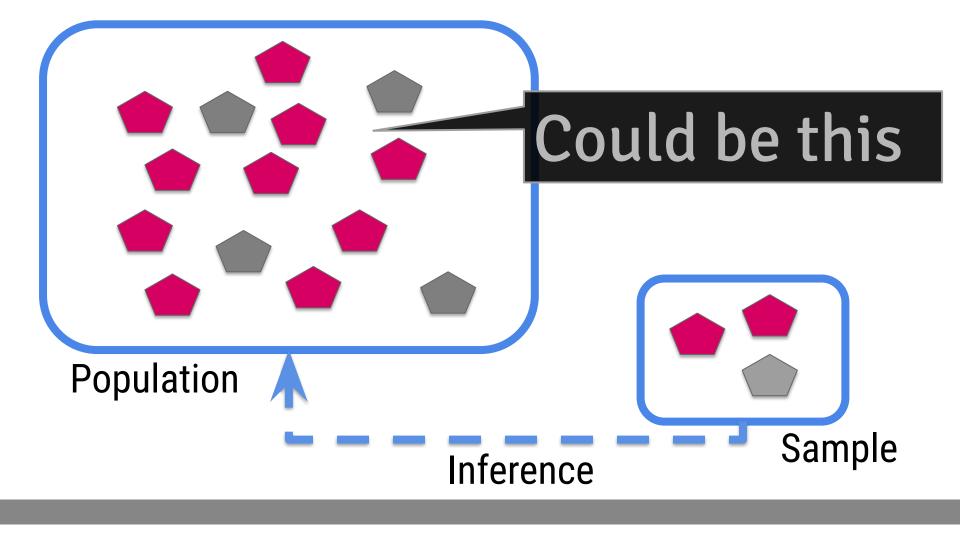


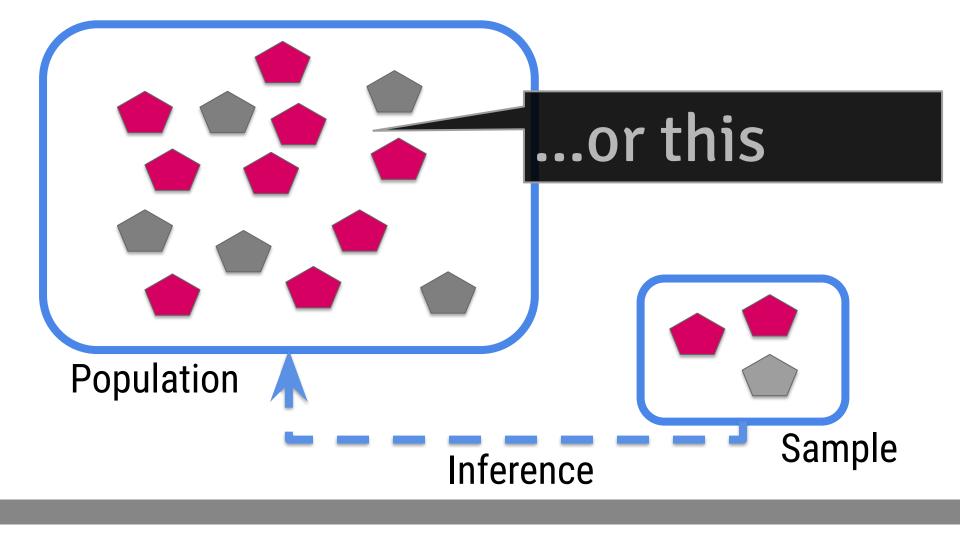
Population

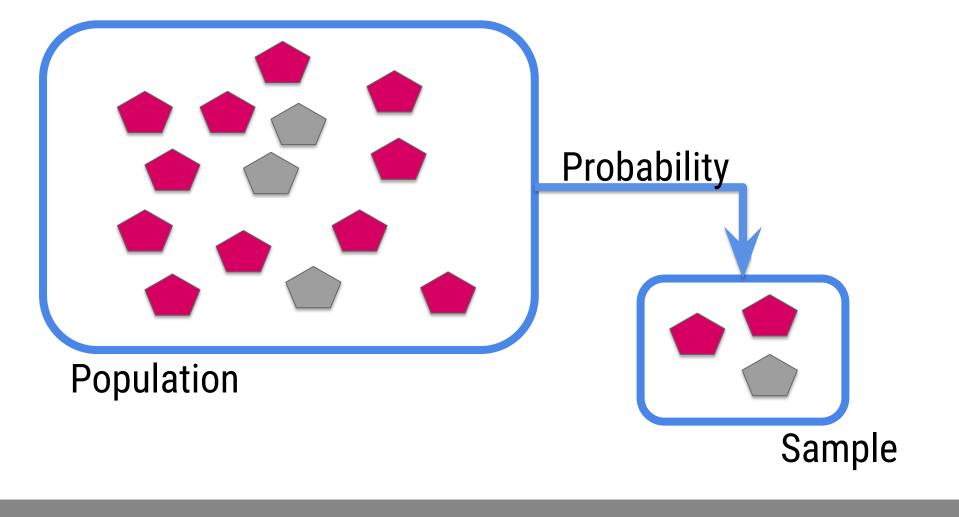


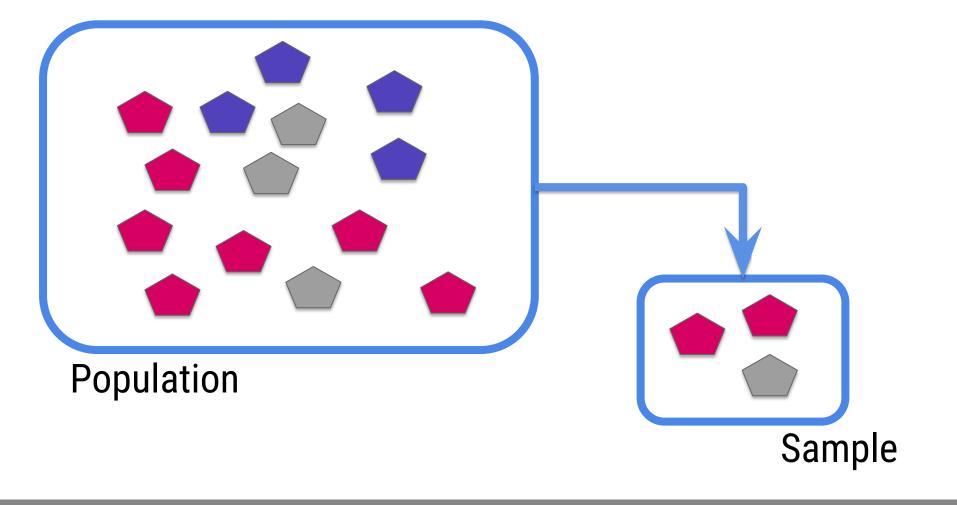
Inference!

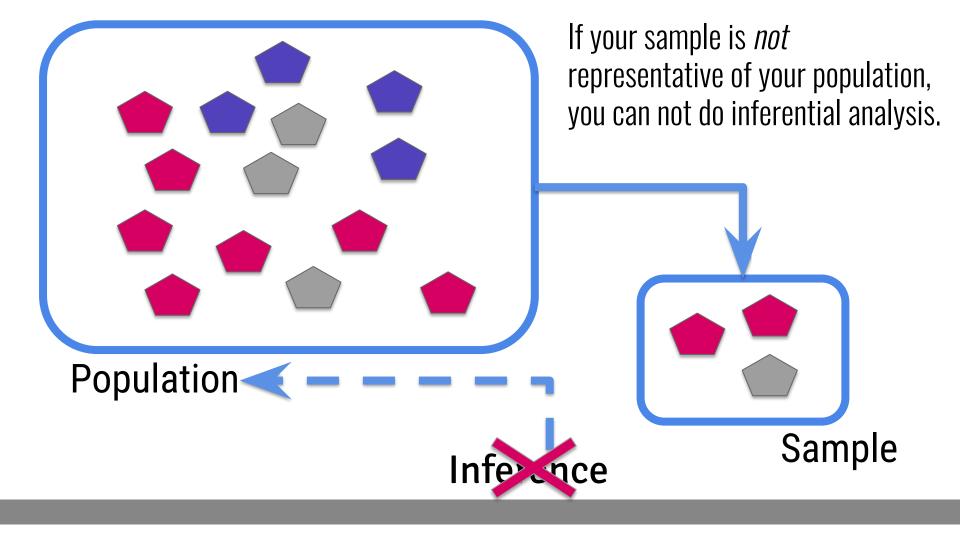
Sample











Approaches to Inference

CORRELATION

ASSOCIATION BETWEEN VARIABLES

i.e. Pearson Correlation, Spearman Correlation, chi-square test

COMPARISON OF MEANS

DIFFERENCE IN MEANS BETWEEN VARIABLES

i.e. t-test, ANOVA

REGRESSION

DOES CHANGE IN ONE VARIABLE MEAN CHANGE IN ANOTHER?

I.e. simple regression, multiple regression

NON-PARAMETRIC TESTS

FOR WHEN ASSUMPTIONS IN THESE OTHER 3 CATEGORIES ARE NOT MET

i.e. Wilcoxon rank-sum test, Wilcoxon sign-rank test, sign test

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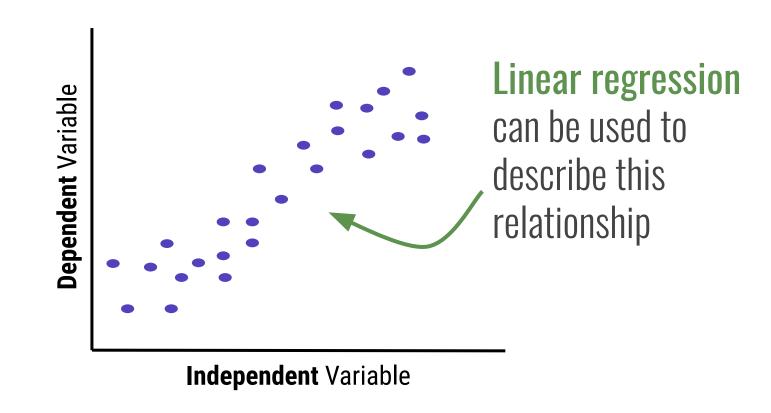
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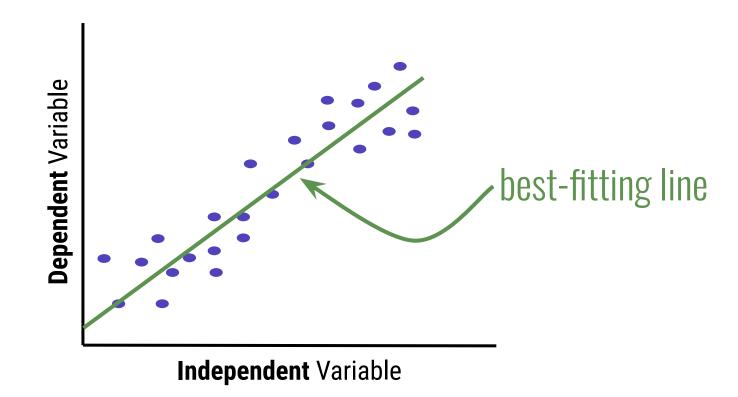
I.e. simple regression, multiple regression

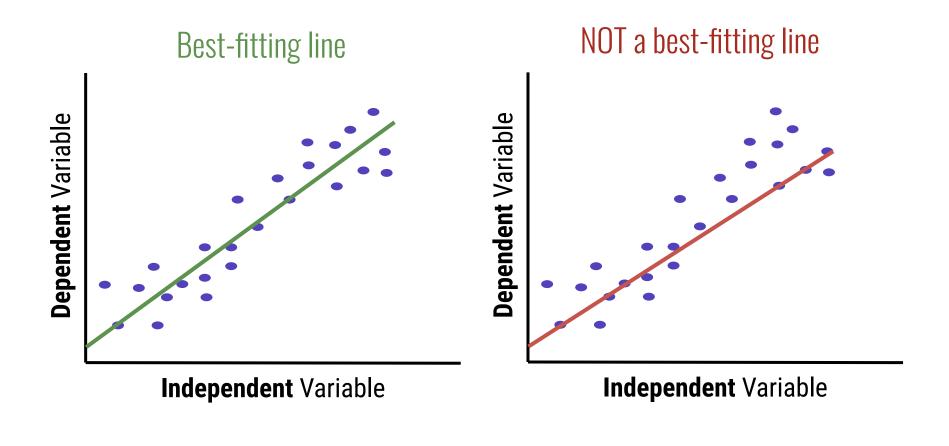
NON-PARAMETRIC TESTS

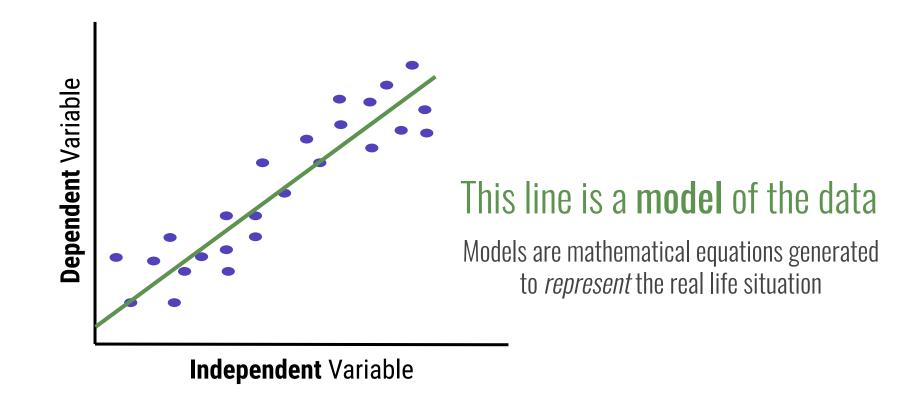
FOR WHEN ASSUMPTIONS IN THESE OTHER 3 CATEGORIES ARE NOT MET

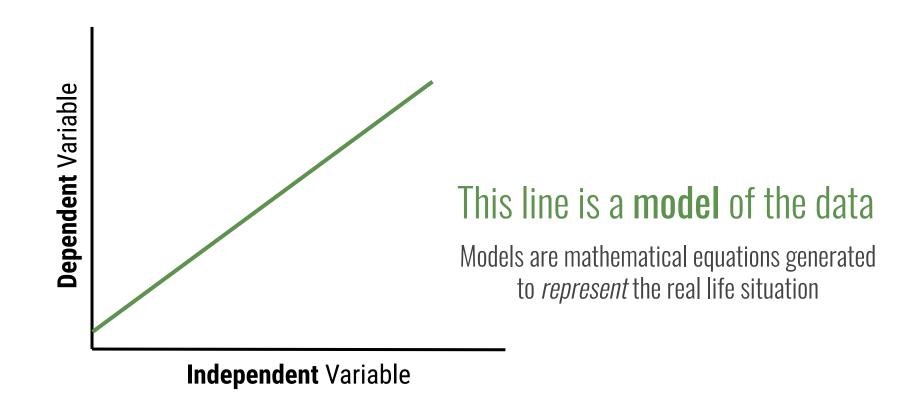
i.e. Wilcoxon rank-sum test, Wilcoxon sign-rank test, sign test





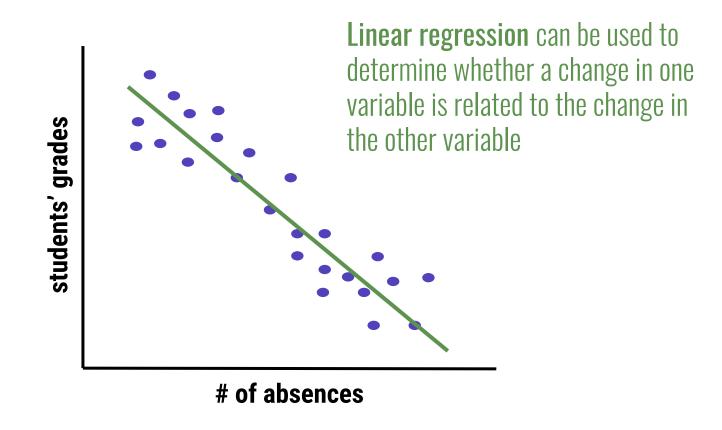


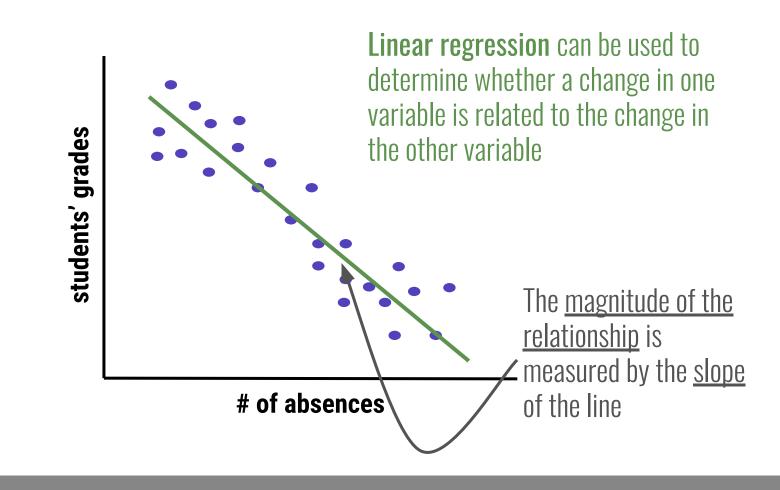


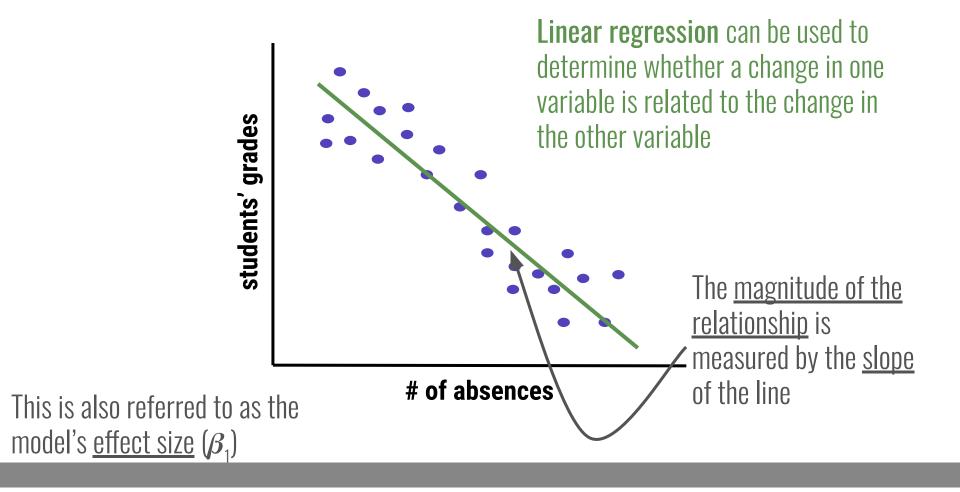


"All models are wrong, but some are useful"

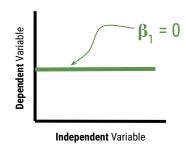
-George Box (British Statistician, *JASA* 1976)



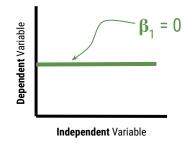


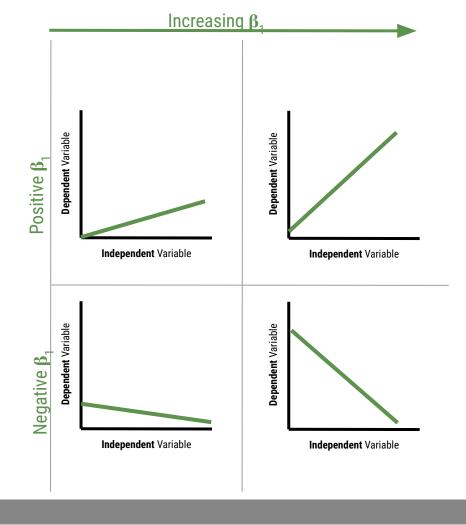


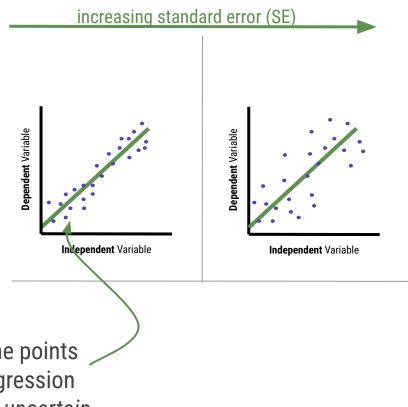
Effect size (β_1) can be estimated using the slope of the line



Effect size (β_1) can be estimated using the slope of the line



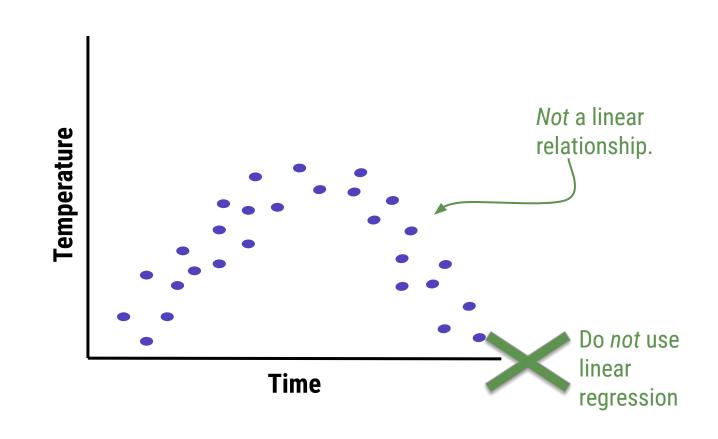




The *closer* the points are to the regression line, the *less uncertain* we are in our estimate

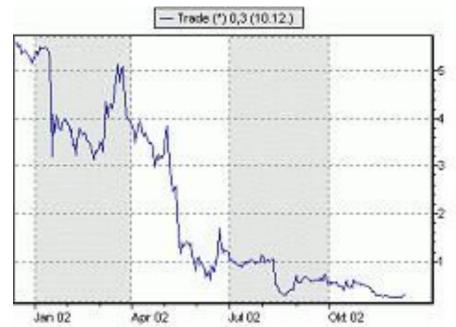
Assumptions of linear regression

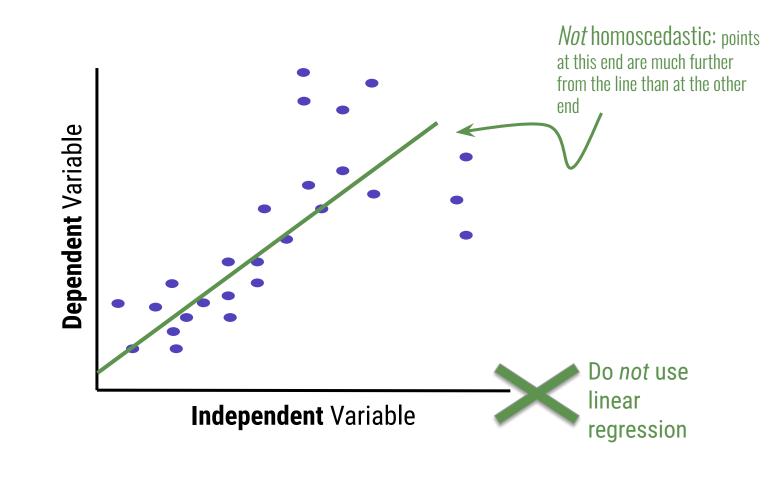
- 1. Linear relationship
- 2. No multicollinearity
- 3. No auto-correlation
- 4. Homoscedasticity



Linear regression assumes no multicollinearity. Multicollinearity occurs when the independent variables (in multiple linear regression) are too highly correlated with each other.

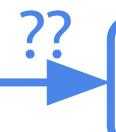
Autocorrelation occurs when the observations are *not* independent of one another (i.e. stock prices)





Does Poverty Percentage affect Teen Birth Rate?

Poverty Percentage



Teen Birth Rate

Null Hypothesis:

 H_0 : Poverty Rate does not affect Teen Birth Rate (β_1 =0)

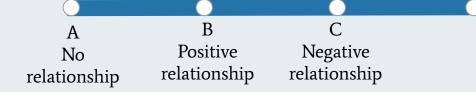
Alternative Hypothesis:

 H_a : Poverty Rate affects Teen Birth Rate ($\beta_1 \neq 0$)



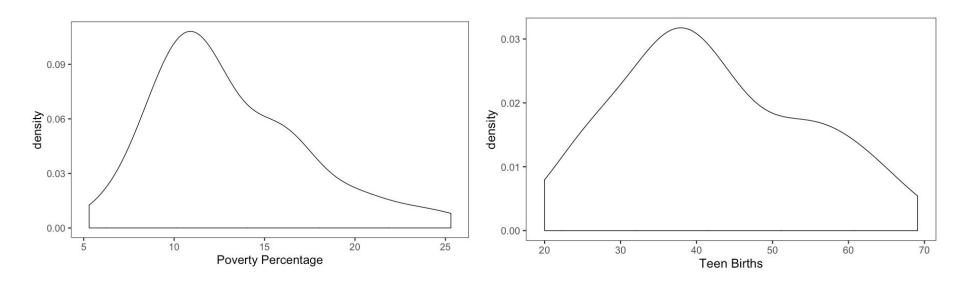
What is the relationship between Poverty Percentage & Teen Birth Rate?

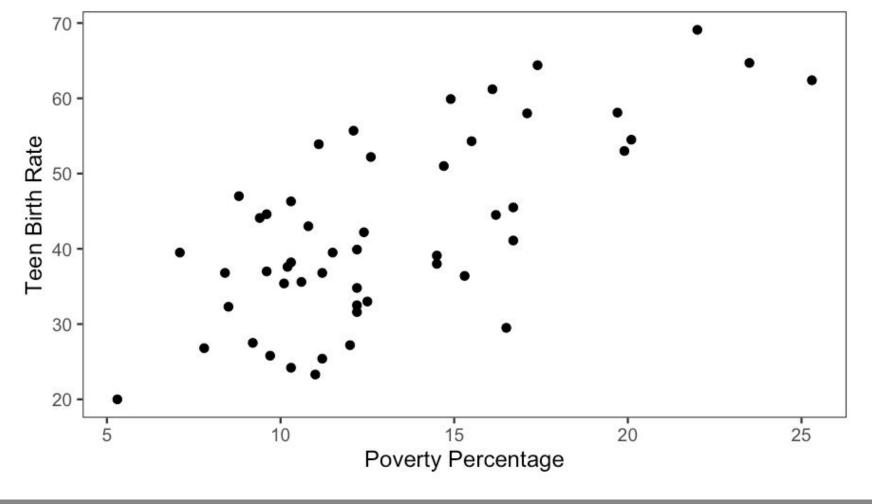
What's your hypothesis?

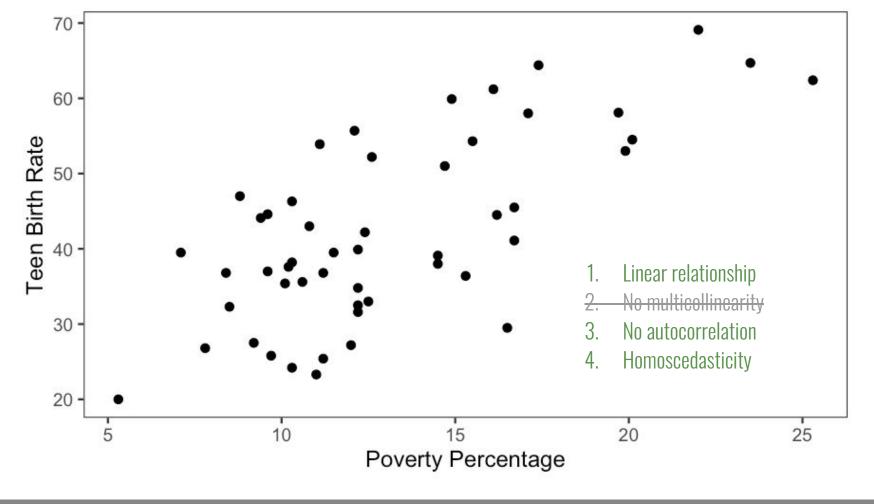


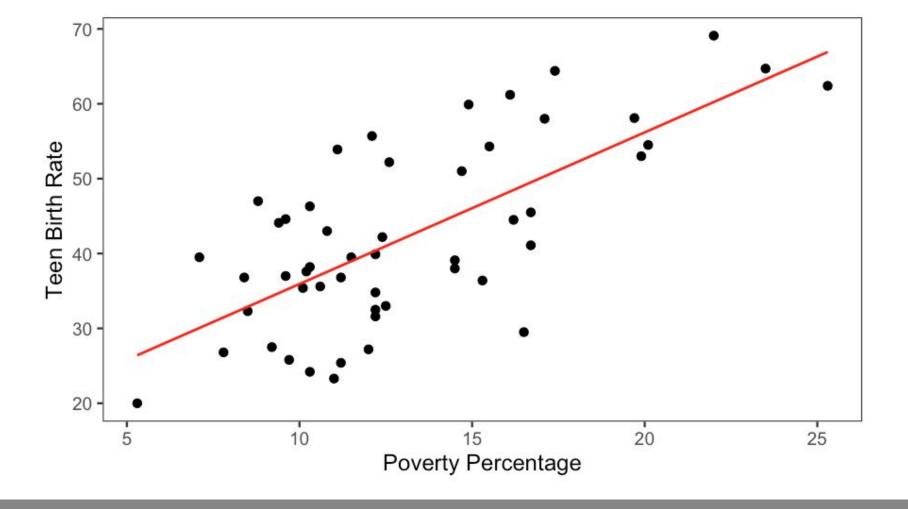
	Location [‡]	PovPct [‡]	Brth15to17	Brth18to19	ViolCrime	TeenBrth
1	Alabama	20.1	31.5	88.7	11.2	54.5
2	Alaska	7.1	18.9	73.7	9.1	39.5
3	Arizona	16.1	35.0	102.5	10.4	61.2
4	Arkansas	14.9	31.6	101.7	10.4	59.9
5	California	16.7	22.6	69.1	11.2	41.1
6	Colorado	8.8	26.2	79.1	5.8	47.0
7	Connecticut	9.7	14.1	45.1	4.6	25.8
8	Delaware	10.3	24.7	77.8	3.5	46.3
9	District_of_Columbia	22.0	44.8	101.5	65.0	69.1
10	Florida	16.2	23.2	78.4	7.3	44.5
11	Georgia	12.1	31.4	92.8	9.5	55.7
12	Hawaii	10.3	17.7	66.4	4.7	38.2
13	Idaho	14.5	18.4	69.1	4.1	39.1
14	Illinois	12.4	23.4	70.5	10.3	42.2
15	Indiana	9.6	22.6	78.5	8.0	44.6
16	Iowa	12.2	16.4	55.4	1.8	32.5
17	Kansas	10.8	21.4	74.2	6.2	43.0

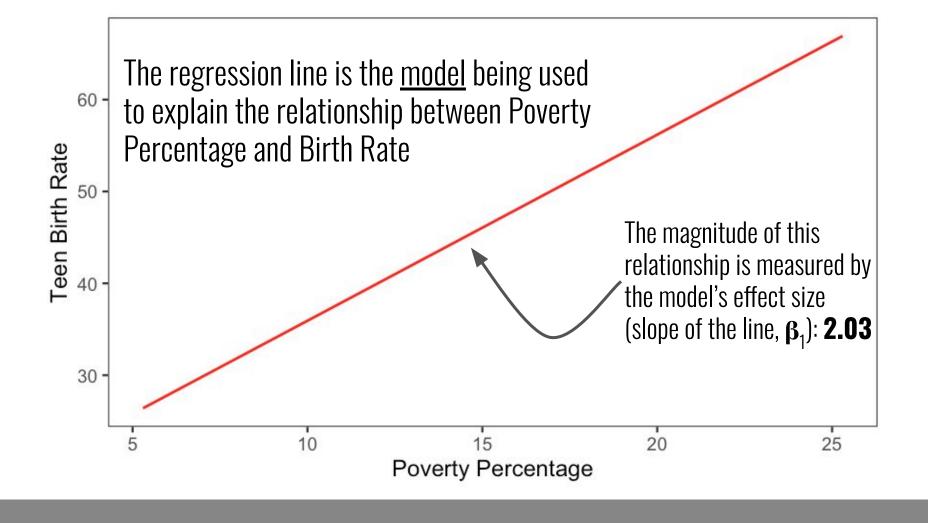
EDA: distributions

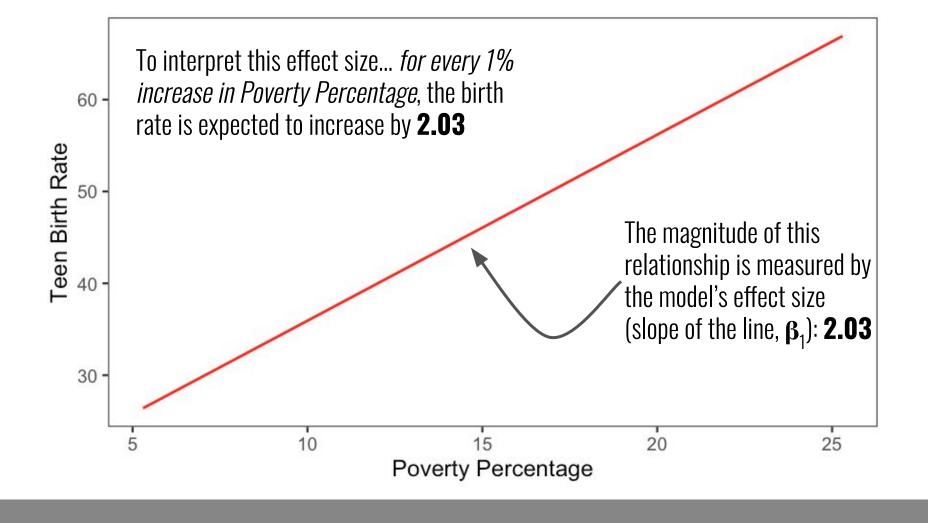


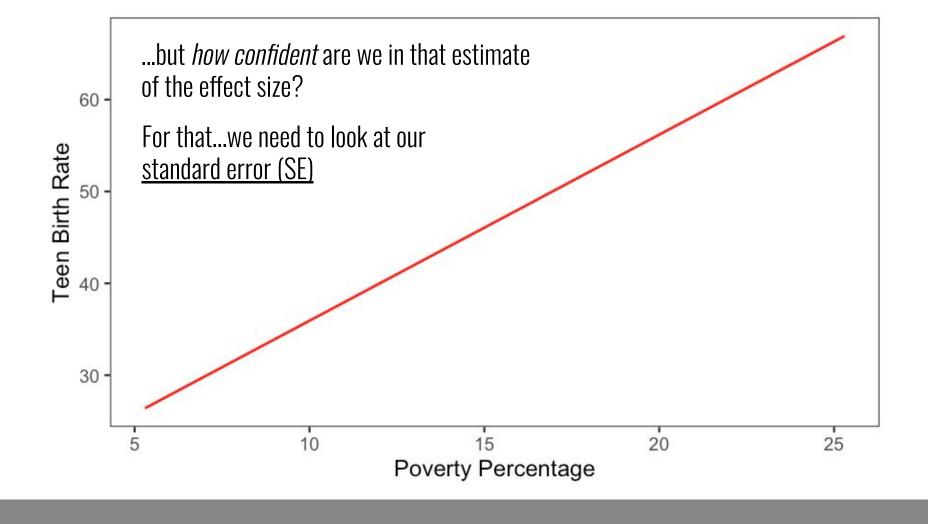


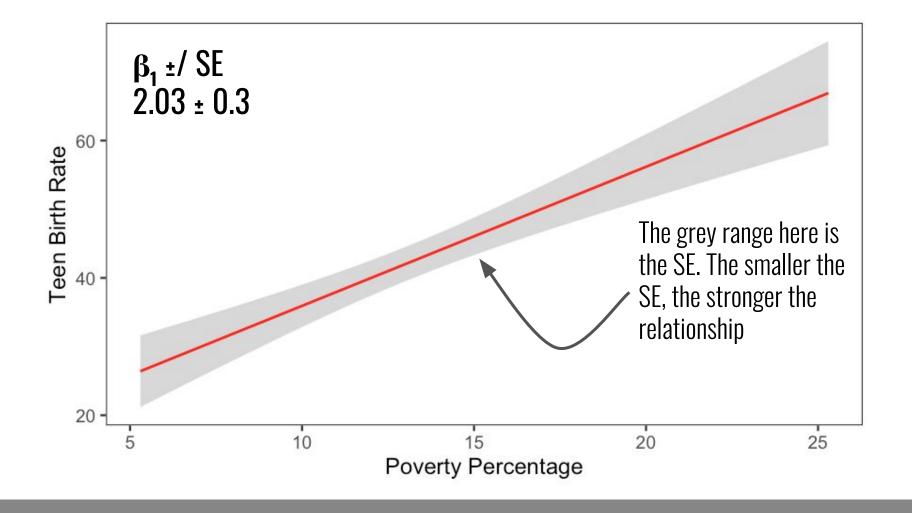




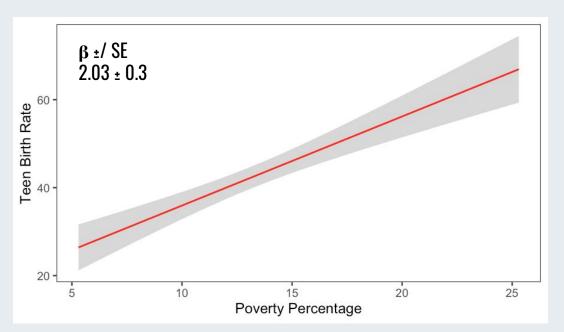






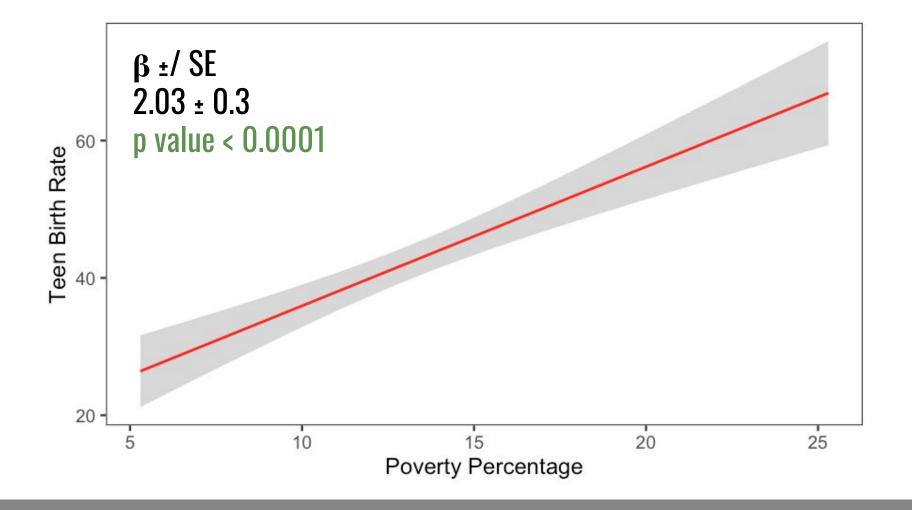




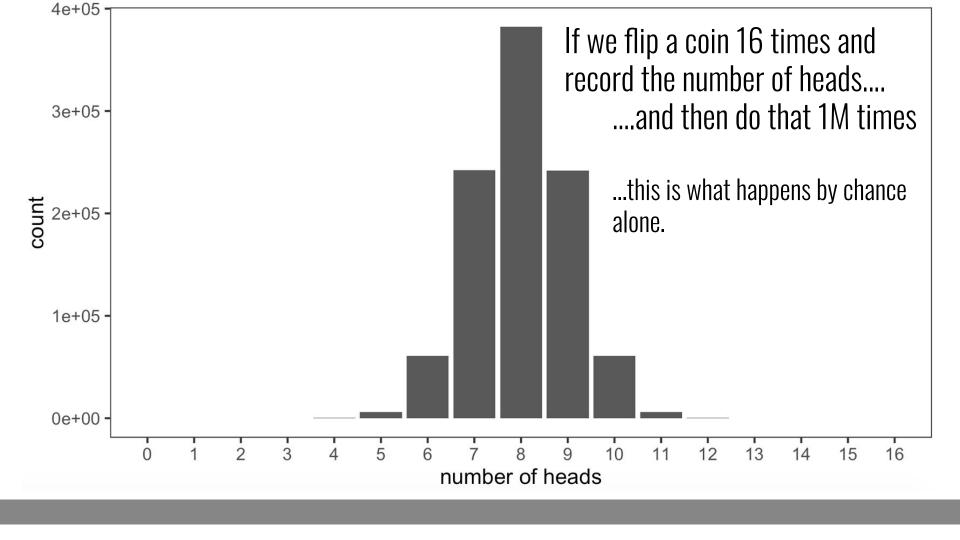


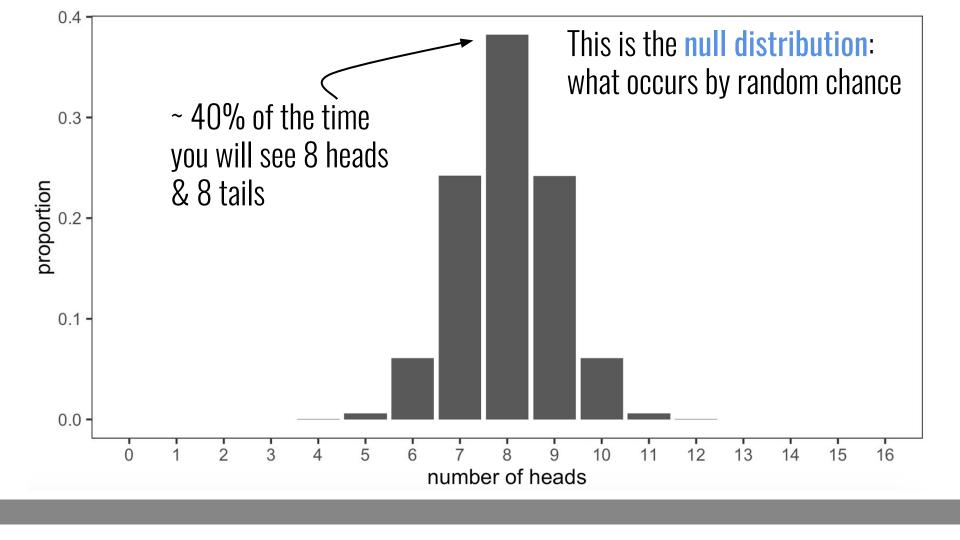
If there were a stronger effect of Poverty on Birth rate, what would β_1 be?

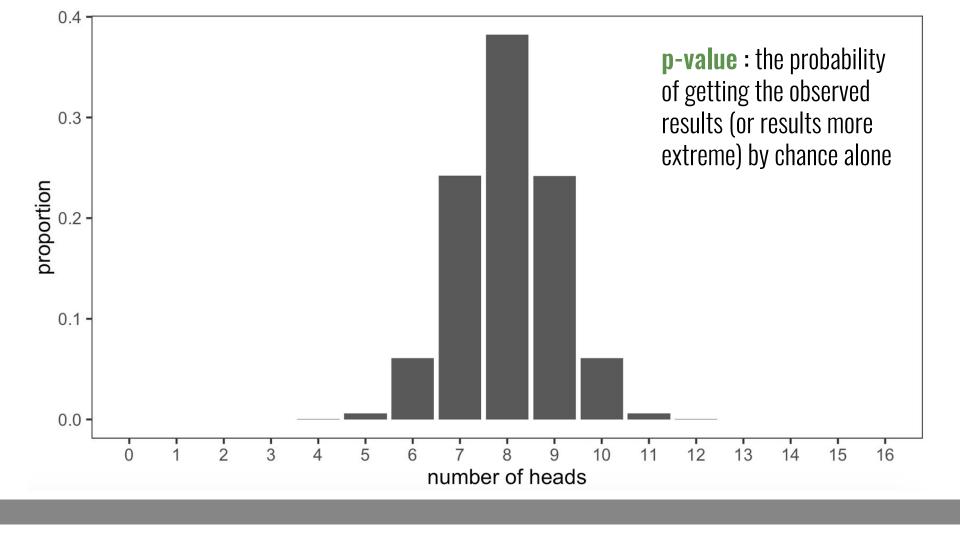
A B < 2.03 > 2.03

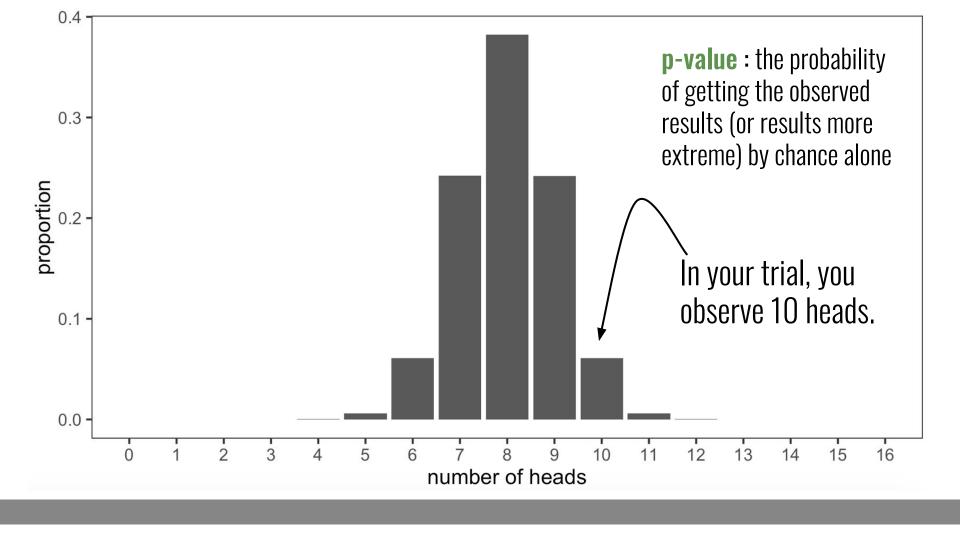


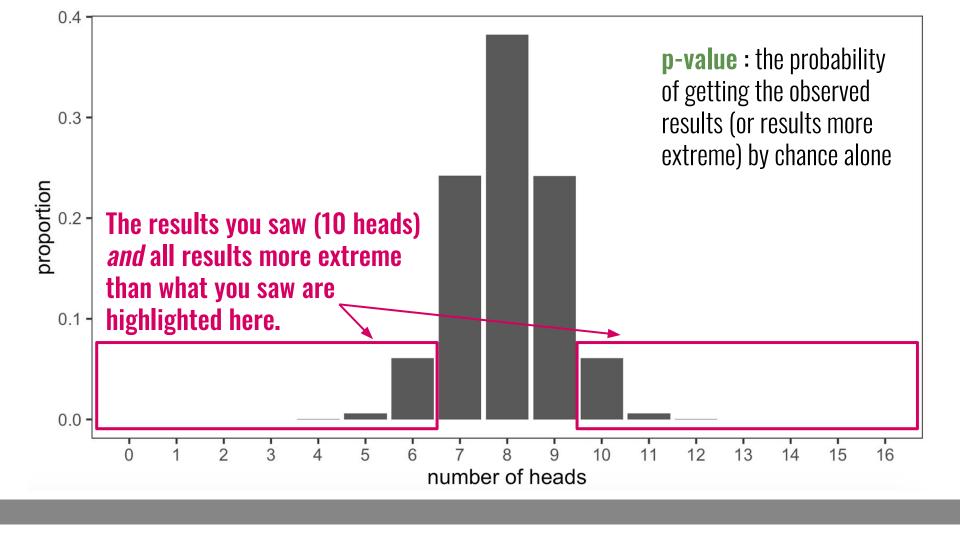
p-value: the probability of getting the observed results (or results more extreme) by chance alone

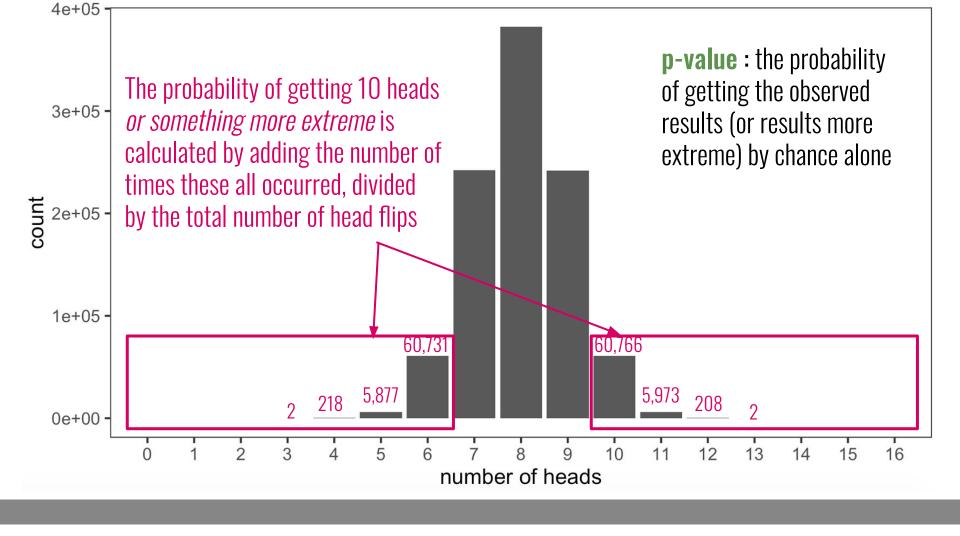


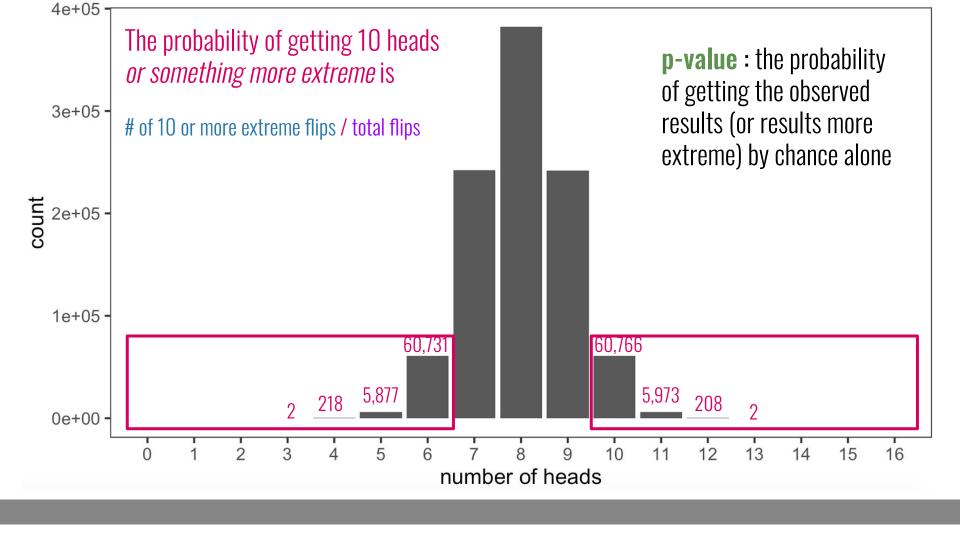


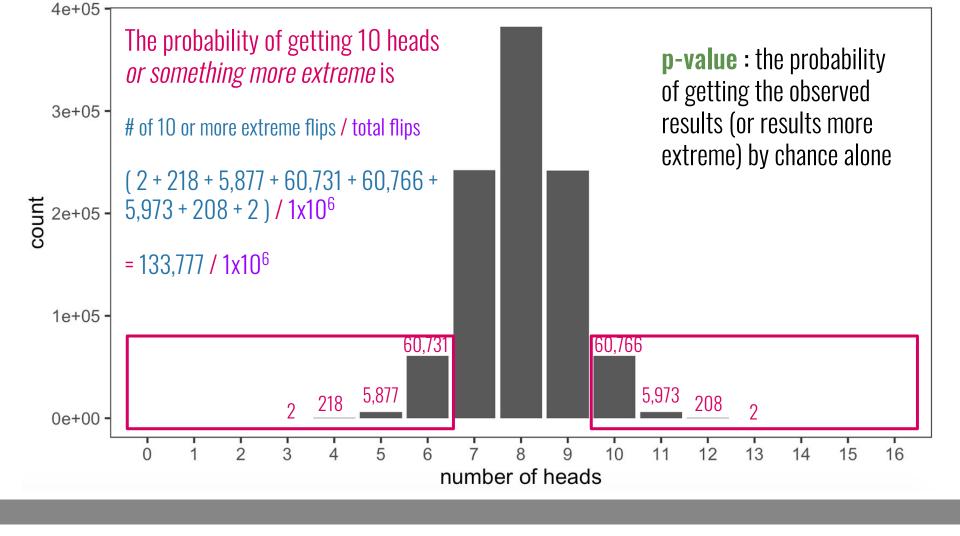


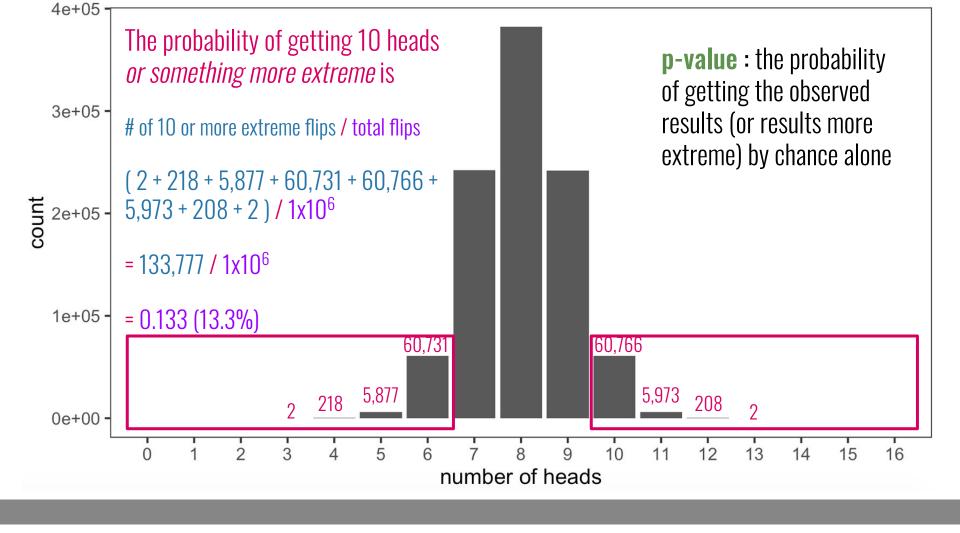


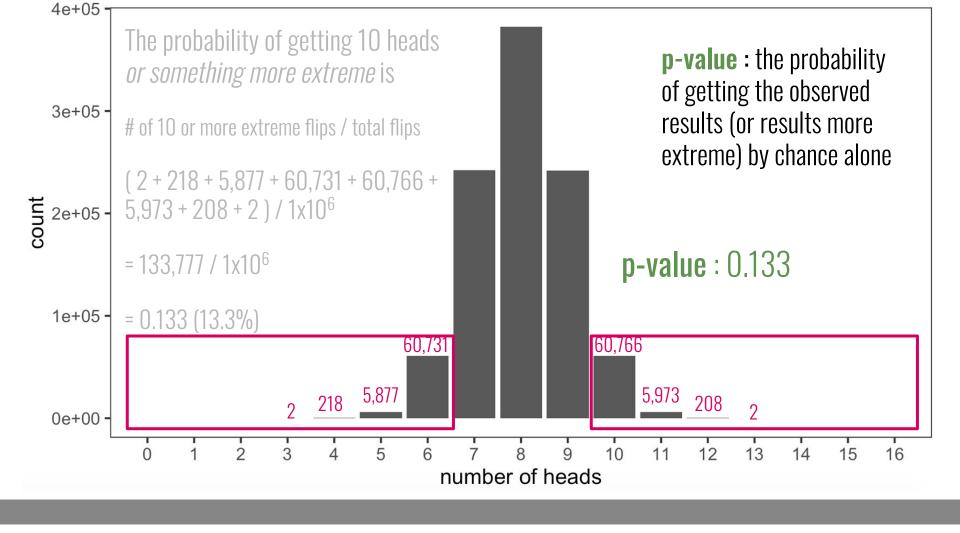


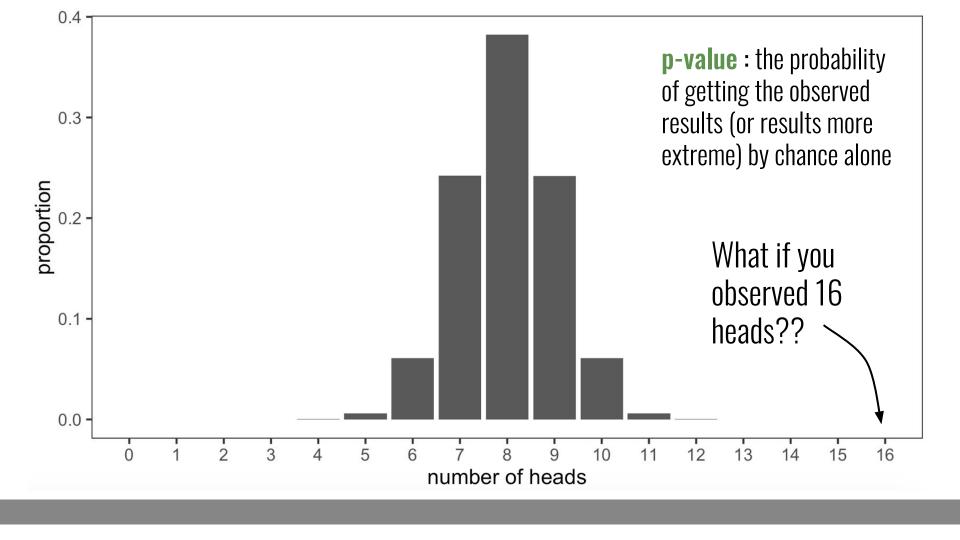


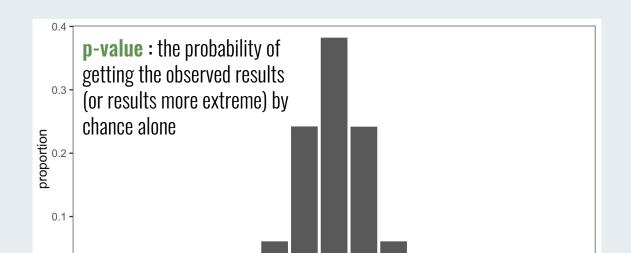














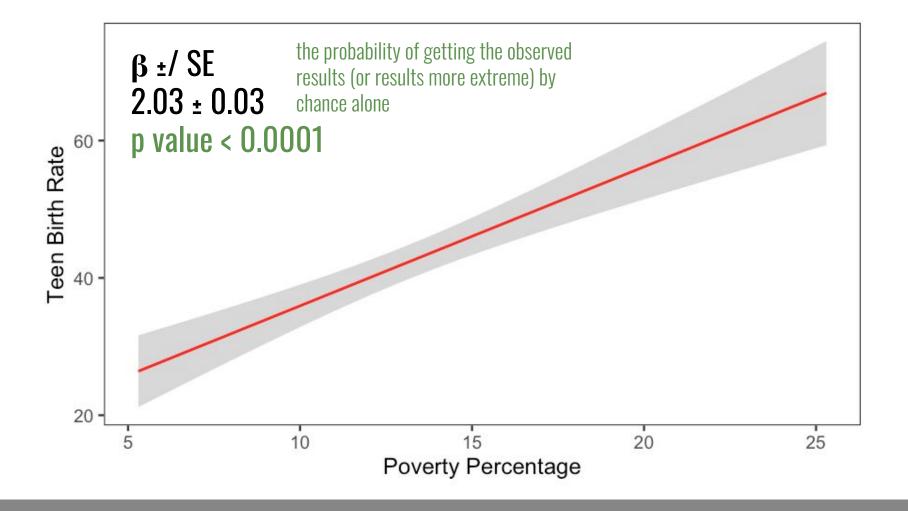
What would be the p-value of you flipping 16 heads?

number of heads

12



0.0 -



Takes into account the effect size (β_1) and the SE

p-value: the probability of getting the observed results (or results more extreme) by chance alone

Confounding





Shoe Size !! Literacy



Big shoes Literate Adult

Shoe Size Literacy

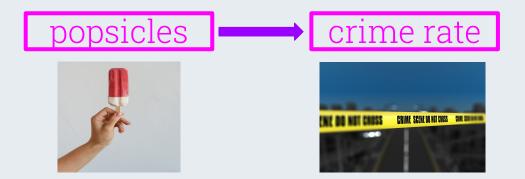
Variable1

Variable2

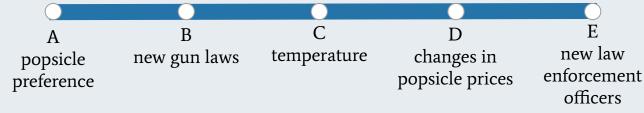
Confounder

Confounding

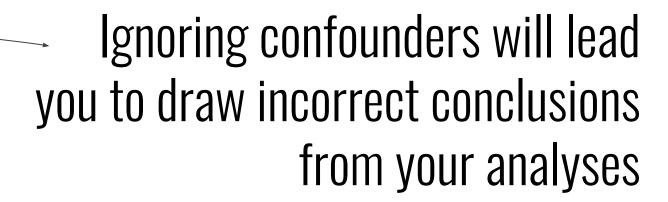




Your analysis sees an increase in crime rate whenever popsicle sales increase. What could confound this analysis?



We'll discuss additional approaches of how to account for confounding in your analysis in the next lecture.



Spine Surgery Results

Sample: 400 patients with index vertebral fractures

Vertebroplasty	Conservative care	Relative risk (95% confidence interval)
30/200 (15%)	15/200 (7.5%)	2.0 (1.1–3.6)
	1	Eeklooks like vertebroplasty
		was way worse for patients!
subsequen	t fractures	

But wait...at time of initial fracture...

	Vertebroplasty N = 200	Conservative care N = 200
Age, y, mean ± SD	78.2 ± 4.1	79.0 ± 5.2
Weight, kg, mean ± SD	54.4 ± 2.3	53.9 ± 2.1
Smoking status, No. (%)	110 (55)	16 (8)

Age and weight are similar between groups. **Smoking Status** differs vastly.

So...let's stratify those results real quick

Smoke			No smoke			
Conservative	RR (95% confidence	Vertebroplasty	Conservative	RR (95% confidence		
	interval)			interval)		
3/16 (19%)	1.1 (0.4, 3.3)	7/90 (8%)	12/184(7%)	1.2 (0.5, 2.9)		
			Conservative RR (95% confidence Vertebroplasty interval)	Conservative RR (95% confidence interval) Vertebroplasty Conservative		

Risk of re-fracture is now similar within group

Confounding



What are possible confounders for our analysis of the effect of poverty on teen birth rate?

A B
I have some Not sure ideas