

COMP3721 Tutorial 8

November 8, 2017

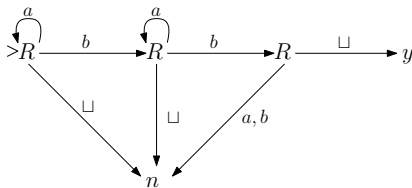
Problem 1

- Q1. Give a Turing machine that decides the regular language a^*ba^*b .

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Solution:



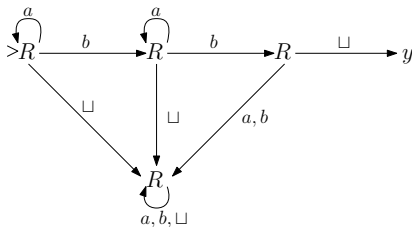
Problem 2

Q2. Give a Turing machine that semi-decides the regular language a^*ba^*b .

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Solution:



Problem 3

- Q3. Prove that a language L is recursive if and only if L and \bar{L} are both recursively enumerable.

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Only-if part: since L is recursive, so is \bar{L} . Since L and \bar{L} are recursive, they are also recursively enumerable.

If part: since L and \bar{L} are recursively enumerable, there are standard Turing machines M_1 and M_2 semi-decide them respectively. Now we use M_1 and M_2 to construct a Turing machine M^* that decides L , which implies that L is recursive.

Conceptually, given a string w , M^* passes w to both of M_1 and M_2 , and run M_1 and M_2 in a parallel manner. If M_1 halts, then M^* halts and accepts w . If M_2 halts, then M^* halts and rejects w . Note that M^* always halts since exactly one of M_1 and M_2 will halt on any given string.