

# COMP3721 Tutorial 9

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## 1 Undecidability

Q1. Prove that the following problems are undecidable.

- (a) Given a Turing machine  $M$ , a state  $q$ , and a string  $w$ , does  $M$  ever reach state  $q$  when started with input  $w$  from its initial state?
- (b) To determine, given a Turing machine  $M$  and a symbol  $\sigma$ , does  $M$  ever write the symbol  $\sigma$  when started on the empty tape?
- (c) Given a Turing machine  $M$  and an input string  $w$ , does  $M$  use a finite amount of tape squares on input  $w$ ?