### COMP3721 Tutorial 8

CSE, HKUST

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(1) Knowing that  $M = (K, \Sigma, \delta, s, H)$ , give the mathematical definition of the following Turing machine.



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$$M$$
  $a \neq \square$   $M$ 

### Solution:

 $M' = (K', \Sigma, \delta', s, \{h'\})$  where

- $K' = K \cup \{h'\}$

(2) Explain what this machine does on the input  $\triangleright \underline{\sqcup} w$ .

$$>R^{a \neq \sqcup} R^{b \neq \sqcup} R \sqcup aR \sqcup b$$

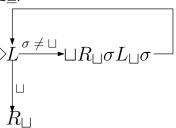
(2) Explain what this machine does on the input ⊳<u>\</u>w.

$$>R^{\frac{a \neq \sqcup}{}}R^{\frac{b \neq \sqcup}{}}R \sqcup aR \sqcup b$$

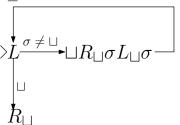
#### Solution:

If  $|w| \ge 2$ , then this machine copies the first two symbols of w, and paste them to the end of w.

(3) Trace the operation of the following Turing machine when started on  $\triangleright \sqcup aabb \sqcup$ .



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The output is ⊳⊔aabbbbaa<u>⊔</u>