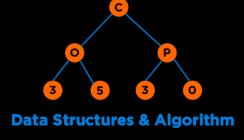
Sets, Maps and Hash Tables



Categories of Data Structures

Linear Ordered

Non-linear Ordered

Not Ordered

Lists

Trees

Sets

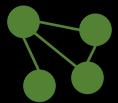
Stacks

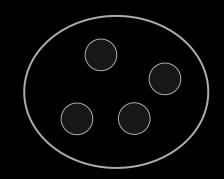
Graphs

Tables/Maps

Queues







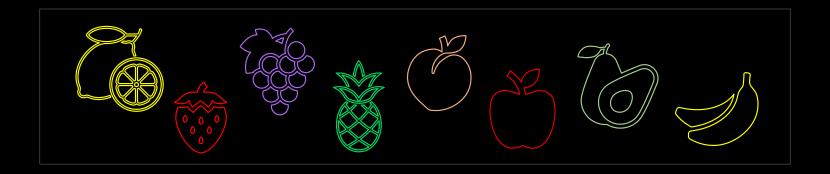


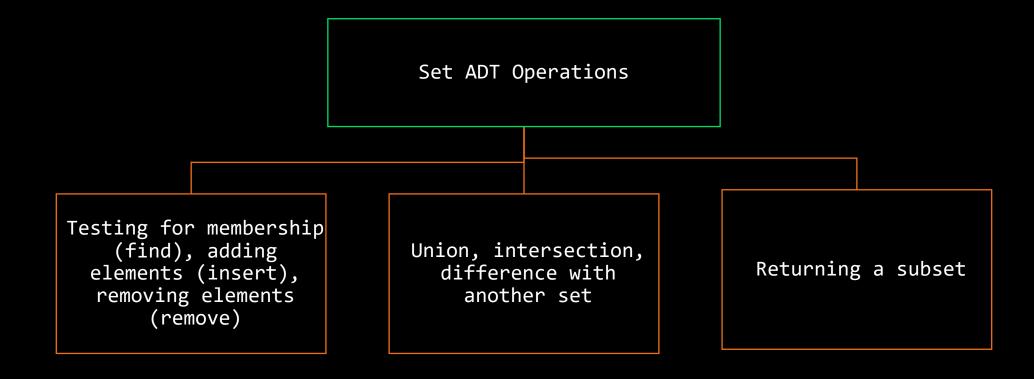


A set is a collection that contains no duplicate elements

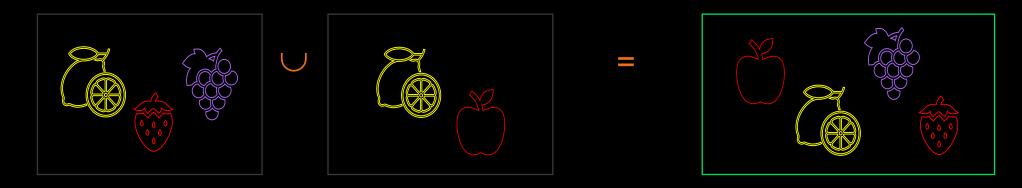
Set objects

- are not indexed
- do not reveal the order of insertion of items
- do enable efficient search and retrieval of information
- do allow removal of elements without moving other elements around

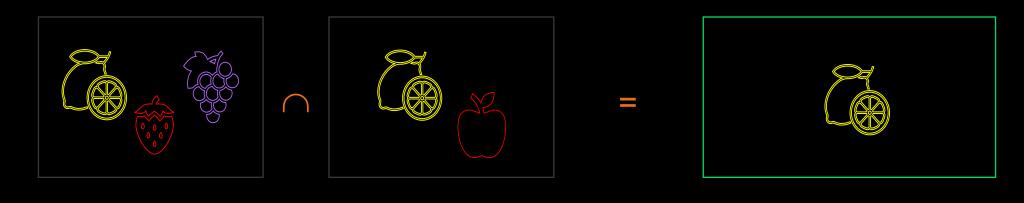




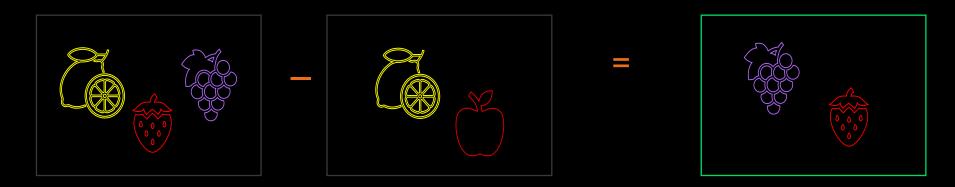
Union of two sets, A \cup B is a set whose elements belong either to A or B or to both A and B.



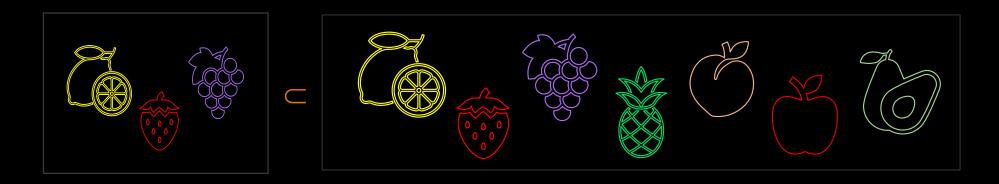
Intersection of sets $A \cap B$ is the set whose elements belong to both A and B.



Difference of sets A - B is the set whose elements belong to A but not to B.



Set A is a subset of set B, A \subset B if every element of set A is also an element of set B.



Lists vs Sets

	Lists	Sets
Order and Access through Element Index	Yes	No
Duplicates	Yes	No
Implementations	Array Based, Linked Lists	Array Based, Tree Based

Sets in C++

	std::set	std::unordered_set
Order in Elements	Yes	No
Initialization	std::set <type> s;</type>	std::unordered_set <type> s;</type>
Common Methods	insert, erase, find, count, size, empty	<pre>insert, erase, find, count, size, empty, bucket_size, load_factor</pre>
Implementations	Binary Search Tree (TreeSet)	Hash Table (Hash Set)
Time Complexity of Common Operations	O(log n) for a Self- Balancing BST, e.g. Red Black Tree	0(1) + 0(k) for hash



Sets in C++ Example

```
// Ordered tree-based set
    set <int> s1;
03
    // insert elements in random order
05
   s1.insert(5);
06 | s1.insert(2);
    s1.insert(4);
   s1.insert(11);
    s1.insert(2); // only one 2 will be added to the set
10
    // printing set
12 set <int> :: iterator itr1;
13 cout << "The set s1 is : ";
    for (itr1 = s1.begin(); itr1 != s1.end(); ++itr1)
15
               cout << " " << *itr1;</pre>
```

```
The set s1 is : 2 4 5 11
```

```
//Unordered Set - Hash-based
    unordered set <int> s2;
03
    // insert elements in random order
    s2.insert(5);
06 | s2.insert(2);
    s2.insert(4);
08 s2.insert(11);
    s2.insert(2); // only one 2 will be added to the set
10
    // printing set
11
    unordered set <int> :: iterator itr2;
13
    cout << "The set s2 is:";</pre>
    for (itr2 = s2.begin(); itr2 != s2.end(); ++itr2)
15
               cout << " " << *itr2;
    cout << endl;</pre>
    cout << "Bucket count: " << s2.bucket_count();</pre>
    cout << "\nLoad Factor: " << s2.load factor();</pre>
   cout << "\nMax Load Factor:" << s2.max load factor();</pre>
```

```
The set s2 is: 11 4 5 2
Bucket count: 7
Load Factor: 0.571429
Max Load Factor: 1
```



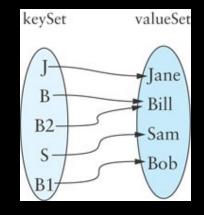
Maps



Maps

A map is a collection of key-value pairs that do not contain duplicate keys.

- Maps are sort of an abstraction over Sets
- The Keys in a map are a Set.
- Values can be non-unique [Many-to-One Relationship, Onto Mapping]
- If you store values along with keys in a Set data structure, you get a Map





Maps

Type of item	Key	Value
University student	Student ID number	Student name, address, major, grade point average
Online store customer	E-mail address	Customer name, address, credit card information, shopping cart
Inventory item	Part ID	Description, quantity, manufacturer, cost, price

Maps in C++

	std::map	std::unordered_map
Order in Elements	Yes	No
Initialization (Internally stored as pairs)	<pre>std::map<type, type=""> m;</type,></pre>	<pre>std::unordered_map <type,< td=""></type,<></pre>
Common Methods	insert, [], erase, find, count, size, empty	<pre>insert, [], erase, find, count, size, empty, bucket_size, load_factor</pre>
Implementations	Binary Search Tree (TreeMap)	Hash Table (Hash Map)



Maps in C++ Example

```
01
    //Unordered Map - Hash-based
02
    unordered map<char,int> table unordered;
03
    // insert elements in random order
04
05
    table unordered['b']=30;
06
    table_unordered['a']=10;
    table_unordered['c']=50;
07
    table unordered['a']=40;
98
09
10
    // printing set
11
    for(auto member: table_unordered)
12
          cout << member.first << " " << member.second <<"\n";</pre>
13
    cout << "Load Factor: " << table unordered.load factor();</pre>
14
```

```
a 40b 30c 50
```

```
c 50
b 30
a 40
Load Factor: 0.428571
```



Questions



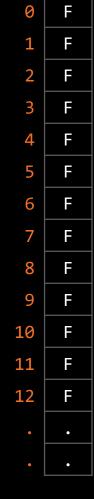
Hash Tables



Problems with Tree Based Maps and Sets

- If the datatypes are comparable such as integers or characters, tree-based maps and sets makes sense. What if the data itself is incomparable?
- Common operations such as insert() or search() are O(log n). Can we do better than this?

- Let's say we want to insert 11, 2 and 5 into a set
- Initially all values are false



- Let's say we want to insert 11, 2 and 5 into a set
- Initially all values are false
- When we insert an item, we set the value at index to true



```
class ArraySet
02
03
        private:
04
             bool set[100] = {0};
        public:
05
            void insert(int value);
06
07
             bool search(int value);
08
    };
09
    void ArraySet::insert(int value)
11
12
        set[value] = 1;
13
14
    bool ArraySet::search(int value)
16
17
        return set[value];
18
```

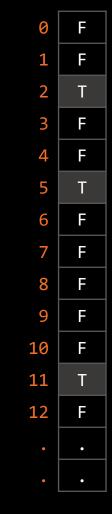
```
19 int main()
20 {
21    ArraySet testSet;
22    testSet.insert(5);
23    std::cout << std::boolalpha << testSet.search(15) <<"\n";
24    std::cout << std::boolalpha << testSet.search(5);
25    return 0;
26 }</pre>
```

10

11

12

- Let's say we want to insert 11, 2 and 5 into a set
- Initially all values are false
- When we insert an item, we set the value at index to true
- Common operations
 - Insert:
 - Find:



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- Common operations
 - Insert: O(1)
 - Find: O(1)



- Let's say we want to insert 11, 2 and 5 into a set
- Initially all values are false
- When we insert an item, we set the value at index to true
- Common operations
 - Insert: O(1)
 - Find: O(1)
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- Problems with this: wastes memory and other datatypes?
- What if we want to store: "cat" or "dog"?
 - Idea: Convert "cat" or "dog" into a number
 - Approach: Use the first letter 'c' = 3, 'd' = 4

11 12

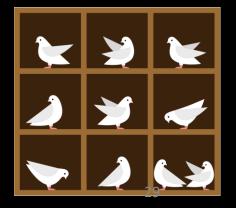
- Problems with this: wastes memory and other datatypes?
- What if we want to store: "cat" or "dog"?
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 - Problem: What happens with "cap"?



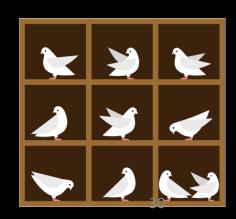
- What if we want to store: "cat" or "dog"?
 - Idea: Convert "cat" or "dog" into a number
 - Approach: Use the first letter 'c' = 3, 'd' = 4
 - Problem: What happens with "cap"? "Collision"
- To fix this use all digits by multiplying each by a power of 27
 - Index of "cat" is $(3 \times 27^2) + (1 \times 27^1) + (20 \times 27^0) = 2234$.



- To fix this use all digits by multiplying each by a power of 27
 - Index of "cat" is $(3 \times 27^2) + (1 \times 27^1) + (20 \times 27^0) = 2234$.
- As long as base >=26, we will get a unique number and no collisions. If it is less than 26, we are guaranteed for collisions due to pigeonhole principle



- To fix this use all digits by multiplying each by a power of 27
 - Index of "cat" is $(3 \times 27^2) + (1 \times 27^1) + (20 \times 27^0) = 2234$.
- As long as base >=26, we will get a unique number and no collisions. If it is less than 26, we are guaranteed for collisions due to pigeonhole principle
 - If base = 2, index of "ac" is $(1 \times 2^1) + (3 \times 2^0) = 5$
 - If base = 2, index of "e" is (5 x 2°) = 5
 - If base = 27, index of "ac" is (1 x 27¹) + (3 x 27°) = 30
 - If base = 27, index of "e" is (5 x 27°) = 5



How to deal with Strings - ASCII and Unicode?

- Increase the base for other characters as 26 characters is too restrictive
 - ASCII: 128 characters
 - Unicode: 143,859 characters



How to deal with Strings - ASCII and Unicode?

- Increase the base for other characters as 26 characters is too restrictive
 - ASCII: 128 characters
 - Unicode: 143,859 characters
- Fixed the problem of storing other datatypes
- Problem: ?



How to deal with Strings - ASCII and Unicode?

- Increase the base for other characters as 26 characters is too restrictive
 - ASCII: 128 characters
 - Unicode: 143,859 characters
- Fixed the problem of storing other datatypes
- Problem: How do we store large values? Overflows, lead to collisions again. And we are now wasting even more space.

Crux of the Problem

Approach

Data -> Hash Function -> Hash Code

Hash code values for different data map to same index in array even after increasing a lot of space in table:

"cat" -> transform2("cat") -> 34

→ 1. poor hash functions

"cat" -> transform127("cat") -> 48534

- 2. limitations of language
- "cat" -> transform143859("cat") -> 62,086,379,522

-> 1956837378

Collisions are Inevitable due to overflows!



Crux of the Problem

Problem

- Wastes memory if we have hash tables that are large
- Has collisions based on language limitations or poor hash functions

Solution

- allow collisions
- use collision resolution strategies
- use small table sizes initially and increase it as per need when performance is affected



Hash Tables

Approach

- Data -> Hash Function -> Hash Code -> Reduce -> Index
- Insert the data (D) at the index in the table and if there is some other data at the index which is not D, then there is a collision and use a collision resolution mechanism

Hash Function

- A function that converts a data object to a hash code.
- Properties
 - Input: Object x
 - Output: An integer representation of x
 - If x is equal to y, H(x) = H(y)
 - If x is not equal to y, it would be great if H(x) is not equal to H(y)

Hash Function Examples

A function, H() that converts a data object, x to a hash code.

```
    H(x): { return 0; }
    H(x): { return Sum of all ASCII values; }
    H(x): { return Powers of 31 with ASCII; }
    H(x): { return Random Number; }
    H(x): { return Current Time; }
```

Hash Function Examples

A function, H() that converts a data object, x to a hash code.

```
    Poor - H(x): { return O; }
    Ok - H(x): { return Sum of all ASCII values; }
    Good - H(x): { return Powers of 31 with ASCII; }
    Invalid - H(x): { return Random Number; }
    Invalid - H(x): { return Current Time; }
```

Hash Function Examples

- A function, H() that converts a data object, x to a hash code.
 - H(x): { return Powers of 31 with ASCII; }
 - Primes are usually used over composites
 - Smaller primes are preferred for faster calculations

Hash Functions

Should evenly distribute the data

Should be easy to compute



Collision Resolution

- Buckets and Load Factor
- Separate Chaining
 - Open Hashing
 - Fixed
 - Resizable
- Open Addressing
 - Closed Hashing
 - Linear Probing
 - Quadratic Probing



Collision Resolution: Terms

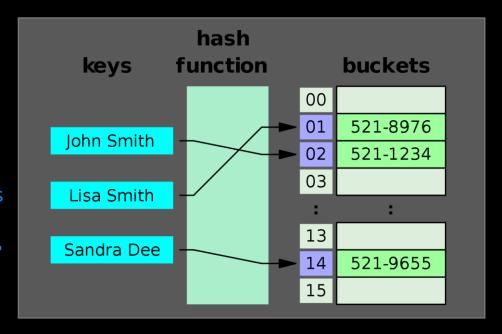
Buckets

Total slots in the Hash Table structure

Load Factor

$$\text{Load Factor}(\alpha) = \frac{\text{Total number of entries}}{\text{Number of buckets}}$$

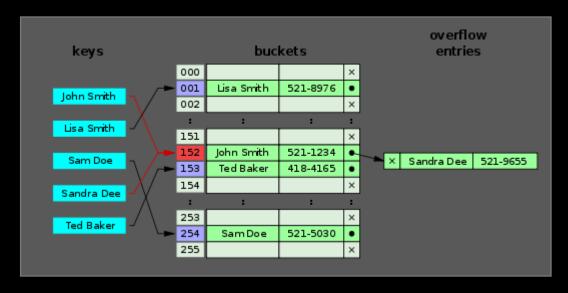
If load factor increases a certain threshold, then move to a larger table using rehashed values



https://en.wikipedia.org/wiki/Hash table

Collision Resolution: Separate Chaining

Key Idea: buckets store a linked list; collisions are appended to the list

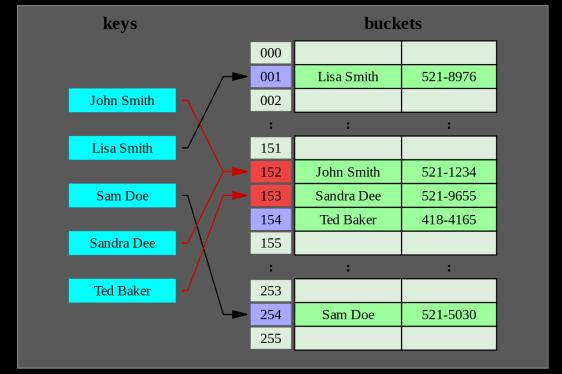


https://en.wikipedia.org/wiki/Hash table



Collision Resolution: Open Addressing (Linear Probing)

Key Idea: all entries in a bucket; collisions are added to empty spots

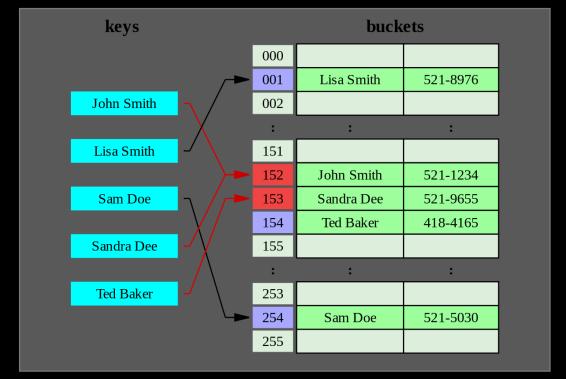


Move the probe by 1 unit



Collision Resolution: Open Addressing (Quadratic Probing)

Key Idea: all entries in a bucket; collisions are added to empty spots



Move the probe by 1, 4, 9, 16 ... units



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE
```



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE
```

Insert a.

- 0

- 3
- 4

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE
```

```
Insert a. H(a) = 97

Index = H(a) \% 5 = 2
```

- 0
- 1
- 2
- 3
- 4



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
Insert a. H(a) = 97
             Index = H(a) \% 5 = 2
```

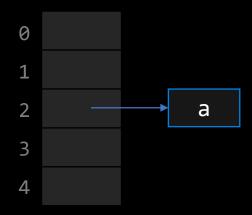


```
Load Factor = 0.2
Maximum Load Factor = 0.8
```



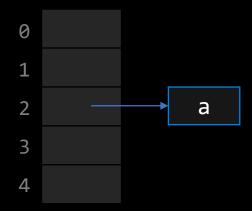
```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE
```

Insert ac.



```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

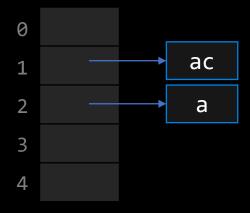
```
Insert ac. H(ac) = 97 + 99 = 196
             Index = H(ac) \% 5 = 1
```



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
Insert ac. H(ac) = 97 + 99 = 196
             Index = H(ac) \% 5 = 1
```

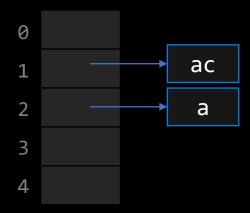


```
Load Factor = 0.4
Maximum Load Factor = 0.8
```



H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

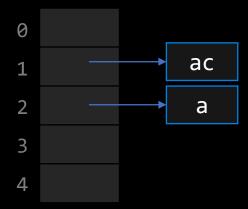
Insert f.



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

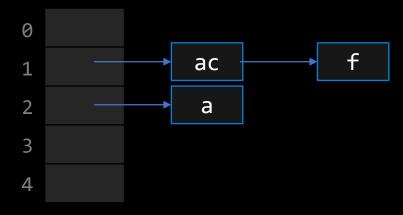
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

Insert f. H(f) = 101Index = H(f) % 5 = 1



```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
Insert f. H(f) = 101
             Index = H(f) \% 5 = 1
```

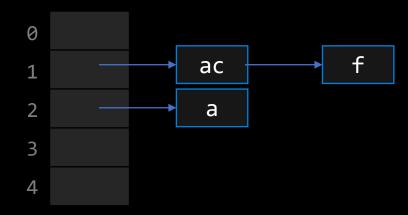


Load Factor = 0.6 Maximum Load Factor = 0.8



H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

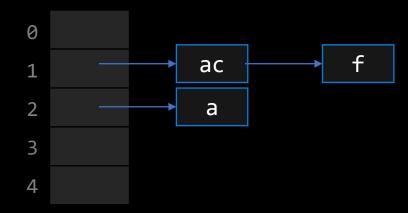
Search f.



H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

Search f.
$$H(f) = 101$$

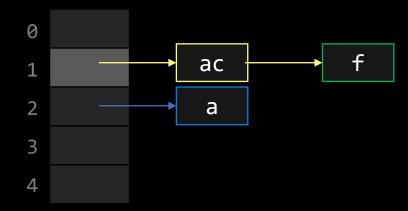
Index = $H(f) \% 5 = 1$



H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

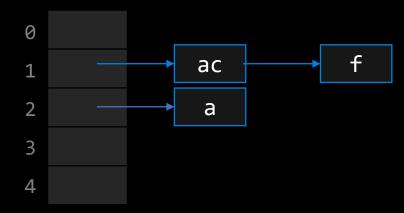
Search f.
$$H(f) = 101$$

Index = $H(f) \% 5 = 1$



H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

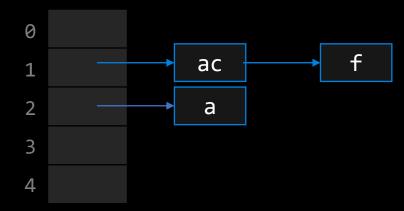
Insert cat.



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

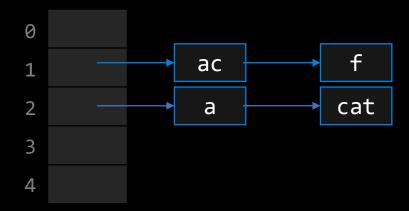
```
Insert cat. H(cat) = 99 + 97 + 116 = 312
             Index = H(cat) % 5 = 2
```



```
Data -> Hash Function -> Hash Code -> Reduce -> Index
```

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
Insert cat. H(cat) = 99 + 97 + 116 = 312
             Index = H(cat) % 5 = 2
```

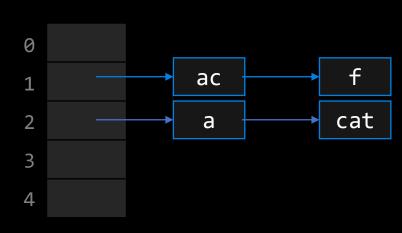


```
Load Factor = 0.8
Maximum Load Factor = 0.8
```



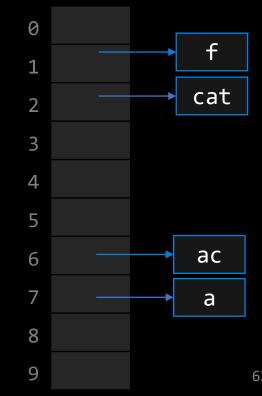
H(key) = Sum of key's ASCII characters

R(Hashcode) = Hashcode % TABLE_SIZE



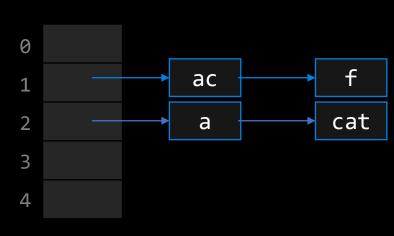
Rehashing

H(ac) = 196, Index = 196 % 10 = 6
H(f) = 101, Index = 101 % 10 = 1
H(a) = 97, Index = 97 % 10 = 7
H(cat) = 312, Index = 312 % 10 = 2





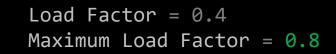
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE

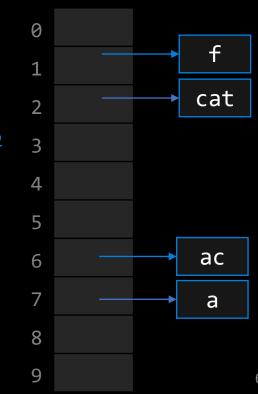


Load Factor = 0.8 Maximum Load Factor = 0.8

H(ac) = 196, Index = 196 % 10 = 6H(f) = 101, Index = 101 % 10 = 1 H(a) = 97, Index = 97 % 10 = 7 H(cat) = 312, Index = 312 % 10 = 2

Rehashing







H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE_SIZE

Open addressing/Closed Hashing: Index is not determined by hash code, i.e., index is open

01234

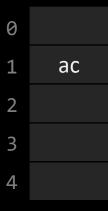


```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
H(ac) = 196, Index = 196 \% 5 = 1
```

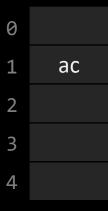
```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
H(ac) = 196, Index = 196 \% 5 = 1
```



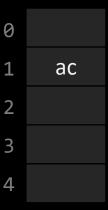
```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
H(ac) = 196, Index = 196 \% 5 = 1
```



```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
H(ac) = 196, Index = 196 \% 5 = 1
H(f) = 101, Index = 101 % 5 = 1
```



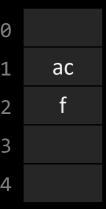
```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

Insert:

0 ac

```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
H(ac) = 196, Index = 196 \% 5 = 1
H(f) = 101, Index = 101 % 5 = 1
H(a) = 97, Index = 97 % 5 = 2
```



```
H(key) = Sum of key's ASCII characters | R(Hashcode) = Hashcode % TABLE SIZE
```

```
H(ac) = 196, Index = 196 \% 5 = 1
H(f) = 101, Index = 101 % 5 = 1
H(a) = 97, Index = 97 % 5 = 2
```



```
H(key) = Sum of key's character ASCII
```

R(Hashcode) = Hashcode % TABLE_SIZE

```
H(ac) = 196, Index = 196 % 5 = 1
H(f) = 101, Index = 101 % 5 = 1
H(a) = 97, Index = 97 % 5 = 2
H(cat) = 312, Index = 312 % 5 = 2
```

```
ac ac f a a
```

Hash Table Example: Open addressing with Linear Probing

```
H(key) = Sum of key's character ASCII
```

R(Hashcode) = Hashcode % TABLE_SIZE

```
H(ac) = 196, Index = 196 % 5 = 1
H(f) = 101, Index = 101 % 5 = 1
H(a) = 97, Index = 97 % 5 = 2
H(cat) = 312, Index = 312 % 5 = 2
```

```
ac ac f a cat
```

Hash Table Example: Open addressing with Linear Probing

```
H(key) = Sum of key's character ASCII
```

R(Hashcode) = Hashcode % TABLE_SIZE

Search ab:

```
H(ab) = 195, Index = 196 % 5 = 0
```

0 ac ac f a a 4 cat

Hash Table Example: Open addressing with Linear Probing

H(key) = Sum of key's character ASCII

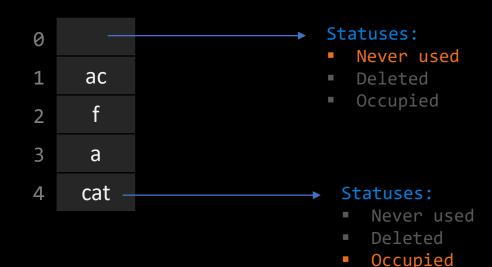
R(Hashcode) = Hashcode % TABLE_SIZE

Search ab:

$$H(ab) = 195$$
, Index = 196 % 5 = 0

Look at bucket 0; if never occupied, then stop and return false;

If occupied, repeat till a bucket is available that is never used, or element is found.





Hash Table Example: Open addressing with Quadratic Probing

R(Hashcode) = Hashcode % TABLE_SIZE

Same as linear probing but indexes are moved quadratically e.g., 1, 4, 9, 16, 25 ... to avoid clusters in the hash table.





Hash Table Example: Open addressing with Quadratic Probing

R(Hashcode) = Hashcode % TABLE_SIZE

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Hash Table Example: Open addressing with Quadratic Probing

```
H(key) = Sum of key's character ASCII R(Hashcode) = Hashcode % TABLE_SIZE
```

Same as linear probing but indexes are moved quadratically e.g., 1, 4, 9, 16, 25 ... to avoid clusters in the hash table.

```
H(ac) = 196, Index = 196 % 5 = 1
H(f) = 101, Index = 101 % 5 = 1
H(k) = 106, Index = 106 % 5 = 1
Move 1 (conflict 2 - f),
Move 4 (conflict 1 - ac),
Move 9 (open 0 - k).
```

```
0 k
1 ac
2 f
3
```



Hash Table Performance

- Time complexities of Search/Insert/Delete are O(1) on average
- Time complexities of Search/Insert/Delete are O(n) in the worst case

Hash Tables and Map vs Set

```
class Set
01
02
03
        private:
04
            string arraySet[100];
05
        public:
            void insert(int value);
06
07
            bool search(int value);
08
    };
09
    void ArraySet::insert(int value)
11
12
        //find the hash of the value
13
        //reduce the hash to get an index
        //check if value is not at index
14
15
                //insert value at index
16
        //otherwise, use collision resolution strategy
17
18
    bool ArraySet::search(int value)
19
20
21
        //find the hash of the value
22
        //reduce the hash to get an index
23
        //check if value is not at index
24
                //return false
25
        //otherwise, search based on collision resolution strategy
26
```

Remember C++ Unordered Maps and Sets are backed by Hash Tables

Sets and Maps in C++ Example

```
//Unordered Set - Hash-based
    unordered set <int> s2;
03
    // insert elements in random order
   s2.insert(5);
   s2.insert(2);
   s2.insert(4);
08 s2.insert(11);
    s2.insert(2); // only one 2 will be added to the set
10
    // printing set
11
12 unordered set <int> :: iterator itr2;
   cout << "The set s2 is:";</pre>
    for (itr2 = s2.begin(); itr2 != s2.end(); ++itr2)
14
15
               cout << " " << *itr2;
16 cout << endl;
   cout << "Bucket count: " << s2.bucket_count();</pre>
   cout << "\nLoad Factor: " << s2.load factor();</pre>
   cout << "\nMax Load Factor:" << s2.max load factor();</pre>
```

```
//Unordered Map - Hash-based
    unordered map<char,int> table unordered;
03
    // insert elements in random order
    table unordered['b']=30;
    table unordered['a']=10;
    table unordered['c']=50;
    table unordered['a']=40;
09
10
    // printing set
    for(auto member: table unordered)
11
          cout << member.first << " " << member.second <<"\n";</pre>
12
13
    cout << "Load Factor: " << table unordered.load factor();</pre>
```

```
c 50
b 30
a 40
Load Factor: 0.428571
```

The set s2 is: 11 4 5 2
Bucket count: 7
Load Factor: 0.571429
Max Load Factor: 1

https://onlinegdb.com/SkHykUnlP



Questions



Mentimeter

Menti.com 4481 0013



Mentimeter

Menti.com 2056 3140



10.1.2 Two Sum Problem

N-sum is a common problem where you are given an array and asked to see if there are N numbers that add up to a target. For this stepik module, you'll be asked to complete Two-Sum. This means you'll be given an array of integers and you have to determine if there are 2 values that sum to a desired target. The method signature is pair<int, int> two_sum(vector<int> arr, int target), which returns a pair of the indices whose values sum to the desired target. If no such 2 value exists, return the pair {-1,-1}. Make sure that the smaller index is first.

Example: arr = [3, 5, 11, 12, 15] target = 17 Output = {1,3}

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the smaller index is first.

```
Example:

arr = [3, 5, 11, 12, 15]

target = 17

Output = {1,3}
```

```
pair<int, int> two sum(vector<int>& arr, int target)
02
        unordered map<int, int> map;
03
        pair<int, int> result(-1, -1);
04
05
        for (int i = 0; i < arr.size(); i++)
06
            int diff = target - arr[i];
07
            if(map.count(diff))
                                         //check if complement is present in the set
98
09
                result.first = map[diff];
10
                result.second = i;
11
12
                break;
13
14
            map[arr[i]] = i;
                                         //add the element to the set otherwise
15
        return result;
16
17
```