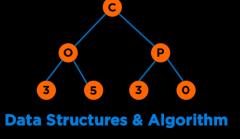
# Algorithm Analysis



#### Agenda

- What is an Algorithm?
- Difference between a Program and an Algorithm
- Multiple Ways of Solving a Problem
- Benefits of Evaluating an Algorithm
- How can we evaluate programs?
  - Approach 1 (Simulation: Timing)
  - Approach 2 (Modeling: Counting)
  - Approach 3 (Asymptotic Behavior: Order of Growth)









## Algorithm

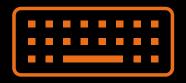


### Algorithm

An algorithm is a step-by-step procedure for solving a problem.

#### Algorithm

An algorithm is a step-by-step procedure for solving a problem.



Input



Output



Definite & Unambiguous



## Algorithm vs Program

	Algorithm	Code or Program
Focus of a professional		
Form		
Dependence on H/W or OS		
Professional's Cognitive State		
Correctness/Performance		

## Algorithm vs Program

	Algorithm	Code or Program
Focus of a professional	Design	Implementation
Form	Pseudocode	Programming Language
Dependence on H/W or OS	No	Yes
Professional's Cognitive State	Thinking	Doing
Correctness/Performance	Analysis	Testing









Problem: Determine if a sorted array contains any duplicates.

-13	-11	12	14	24	24	100	102

Objective: Determine if a sorted array contains any duplicates.

-13	-11	12	14	24	24	100	102

Silly algorithm: Every possible pair

Objective: Determine if a sorted array contains any duplicates.

```
-13 -11 12 14 24 24 100 102
```

Silly algorithm: Every possible pair

Better algorithm: Compare adjacents

Objective: Determine if a sorted array contains any duplicates.

-13	-11	12	14	24	24	100	102

Silly algorithm: Every possible pair

Better algorithm: Compare adjacents



## Are all programs/algorithms equal in terms of performance?

#### Performance

In terms of what?



#### Performance

#### In terms of what?

- Time
- Space



### Why do we care about algorithms?

#### Why do we care about algorithms?

Knowing



Experiencing



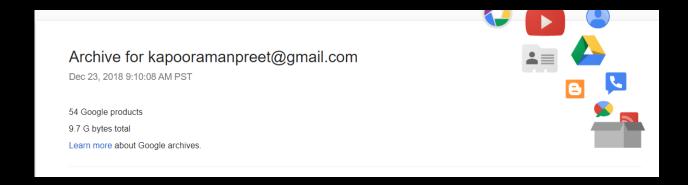
Selling



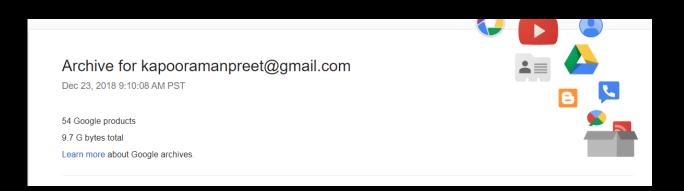
Cost



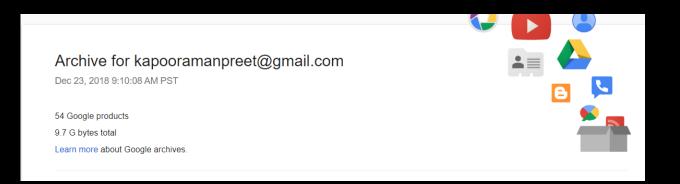




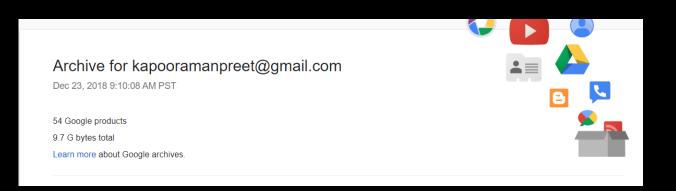
- Google has 2 billion active users
- Conservative estimate ~ 1 GB of data/user
- Total Data (Space):



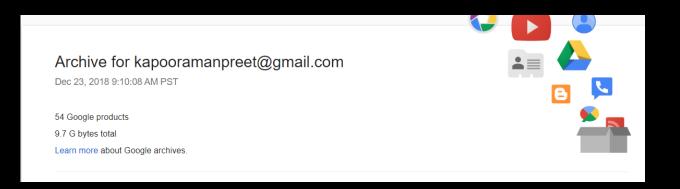
- Google has 2 billion active users
- Conservative estimate ~ 1 GB of data/user
- Total Data (Space): 2 Exabytes
- Total Time:



- Google has 2 billion active users
- Conservative estimate ~ 1 GB of data/user
- Total Data (Space): 2 Exabytes
- Total Time:
  - Operation Speed: 0.5 ns
  - Linear Search
  - Binary Search



- Google has 2 billion active users
- Conservative estimate ~ 1 GB of data/user
- Total Data (Space): 2 Exabytes
- Total Time:
  - Operation Speed: 0.5 ns
  - Linear Search: 11574 days or 31 years
  - Binary Search: 31s



# In short, we care about performance ...

So, how do we measure performance?



#### Questions to ask when evaluating programs

- Time: How much time does this take?
- Space: How much space does this consume?
- Data: Are there any patterns in our data?



Code #1

```
01 auto t1 = Clock::now();
02 for(int i=0; i<1000; i++);
03 auto t2 = Clock::now();
04 Print t2-t1</pre>
```

#### Code #2

```
01 auto t1 = Clock::now();
02 for(int i=0; i<1000000; i++);
03 auto t2 = Clock::now();
04 Print t2-t1</pre>
```

#### Code #1

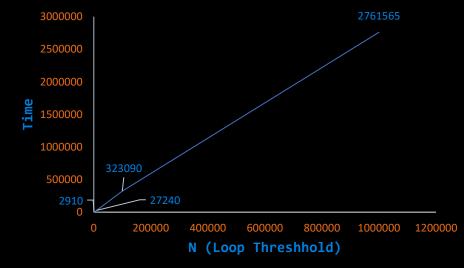
```
01 auto t1 = Clock::now();
02 for(int i=0; i<1000; i++);
03 auto t2 = Clock::now();
04 Print t2-t1</pre>
```

#### Code #2

```
01 auto t1 = Clock::now();
02 for(int i=0; i<1000000; i++);
03 auto t2 = Clock::now();
04 Print t2-t1</pre>
```

#### Output

```
Delta t2-t1 (1000): 2910 nanoseconds
Delta t2-t1 (10000): 27240 nanoseconds
Delta t2-t1 (100000): 323090 nanoseconds
Delta t2-t1 (1000000): 2761565 nanoseconds
```



Pros	Cons

Pros	Cons
Easy to measure	Results vary across machines
Easy to interpret	Compiler dependent
	Results vary across implementations
	Not predictable for small inputs
	No clear relationship between input and time



**Count the number of operations** 

#### Count the number of operations

Operation	Symbolic count
<pre>int sum=0;</pre>	
int i=0;	
i <n;< td=""><td></td></n;<>	
i++	
sum += i;	
print sum	
T(n)	

#### Count the number of operations

Operation	Symbolic count
<pre>int sum=0;</pre>	1
int i=0;	1
i <n;< td=""><td>0n = n+1</td></n;<>	0n = n+1
i++	n
sum += i;	n
print sum	1
T(n)	3n+4

Pros	Cons

Pros	Cons
Independent of computer	All operations are equal
Input dependence is captured in model (Scaling)	Tedious to compute
	Results vary across implementations
	Doesn't tell you actual time

#### Count the number of operations

01	int sum=0;
02	for(int i=0; i <n; i++)<="" td=""></n;>
03	sum += i;
04	print sum

Operation	Symbolic count
<pre>int sum=0;</pre>	1
int i=0;	1
i <n;< td=""><td>0n = n+1</td></n;<>	0n = n+1
i++	n
sum += i;	n
print sum	1
T(n)	3n+4

#### **Tedious to compute:**

Different variables, so many operations, so many equations!



#### **Approach 2 (Modeling: Counting)**

#### Count the number of operations

01	int sum=0;			
02	for(int i=0; i <n; i++)<="" td=""></n;>			
03	sum += i;			
04	print sum			

<b>Operation</b>	Symbolic count
int sum=0;	1
int i=0;	1
i <n;< td=""><td>0n = n+1</td></n;<>	0n = n+1
i++	n
sum += i;	n
print sum	1
T(n)	3n+4

#### **Tedious to compute:**

Different variables, so many operations, so many equations!



Can we eliminate the complexity or get rid of extraneous variables?

## Approach 3 (Asymptotic Behavior: Order of Growth)



### Which variables should we eliminate?

<b>Operation</b>	Symbolic count
<pre>int sum=0;</pre>	1
int i=0;	1
i <n;< td=""><td>0n = n+1</td></n;<>	0n = n+1
i++	n
sum += i;	n
print sum	1
T(n)	3n+4

## nputs: n

#### **Growth of Functions**

Time, y = T(n)

	1	log n	n	n log n	n²	n³	<b>2</b> <sup>n</sup>	n!
1								
10								
100								
1000								
10000								
100000								
1000000								
1000000								
10000000								

## nputs: n

#### **Growth of Functions**

#### Time, y = T(n)

	1	log n	n	n log n	n²	n³	<b>2</b> <sup>n</sup>	n!
1	1							
10	1							
100	1							
1000	1							
10000	1							
100000	1							
1000000	1							
10000000	1							
10000000	1							

## nputs: n

#### **Growth of Functions**

#### Time, y = T(n)

	1	log n	n	n log n	n²	n³	<b>2</b> <sup>n</sup>	n!
1	1	0						
10	1	3						
100	1	7						
1000	1	10						
10000	1	13						
100000	1	17						
1000000	1	20						
1000000	1	23						
10000000	1	27						

#### **Growth of Functions**

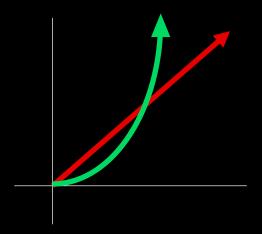
#### Time, y = T(n)

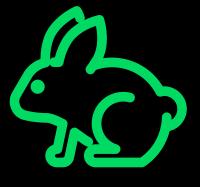
		1	log n	n	n log n	n²	n³	<b>2</b> <sup>n</sup>	n!
	1	1	0	1	0	1	1	2	1
	10	1	3	10	30	100	1000	1024	3628800
	100	1	7	100	700	10000	1000000	1.26765E+30	9.3326E+157
	1000	1	10	1000	10000	1000000	1000000000	1.0715E+301	#NUM!
	10000	1	13	10000	130000	10000000	1E+12	#NUM!	#NUM!
•	100000	1	17	100000	170000	1000000000	1E+15	#NUM!	#NUM!
	1000000	1	20	1000000	2000000	1E+12	1E+18	#NUM!	#NUM!
	1000000	1	23	1000000	23000000	1E+14	1E+21	#NUM!	#NUM!
1	0000000	1	27	10000000	270000000	1E+16	1E+24	#NUM!	#NUM!

#### Order of Growth gets Faster or Functions rise faster

# Eliminate functions that grow slower

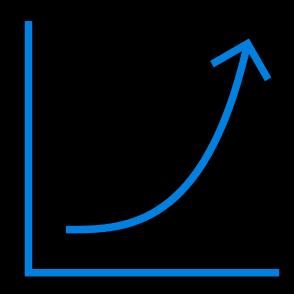






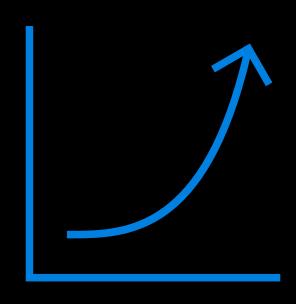


## Approach 3 (Asymptotic Behavior: Order of Growth)

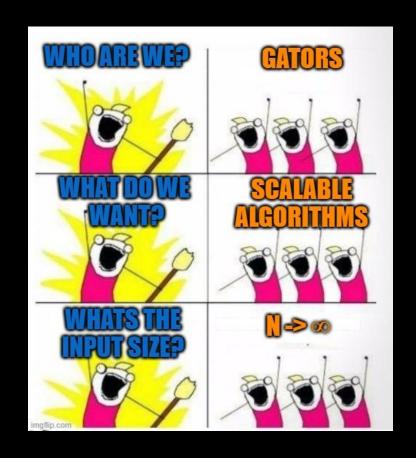


**Very Large N** 

## Approach 3 (Asymptotic Behavior: Order of Growth)



**Very Large N** 





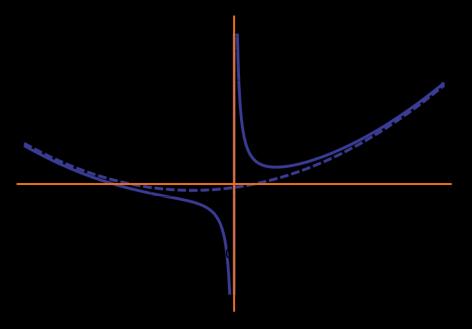
#### Notations for Algorithm Complexity

#### Time - Number of Operations:

- Big-O: Upper Bound
- Big- $\Omega$ : Lower Bound
- Big-⊕: Upper + Lower Bound

#### **Asymptotic Bounding**

- Line that approaches a curve but never meets
- Analysis of tail behavior
- N -> Infinity



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#### Big O (Visualize)

 $T(n) \in O(f(n))$ 

- If there exists two positive constants,  $n_0$  and c, such that  $T(n) \le c.f(n)$  for all  $n \ge n_0$
- f(n) is an upper bound on performance
- T(n) will grow no faster than constant times f(n)
- Use tighter upper bound

#### Big $\Omega$

#### $T(n) \in \Omega(g(n))$

- If there exists two positive constants,  $n_0$  and c, such that  $T(n) \ge c.g(n)$  for all  $n \ge n_0$
- g(n) is a lower bound on growth rate of T(n)
- T(n) will grow no slower than constant times g(n)
- Use tighter lower bound



#### Big ⊕

$$T(n) \in \Theta(g(n))$$

- If T(n) = O(g(n)) and  $T(n) = \Omega(g(n))$
- $c_1.g(n) \le T(n) \le c_2.g(n)$  for all  $n \ge n_0$
- g(n) is a tight upper and lower bound on the growth rate of T(n)

#### Big $\Theta$ vs Big O vs Big $\Omega$

	Informal meaning:	Family	Family Members, T(n)
Big Theta ⊕(f(N))	Order of growth is f(N).	⊕(N²)	N <sup>2</sup> /12 2N <sup>2</sup> N <sup>2</sup> + 11N
Big O O(f(N))	Order of growth is less than or equal to f(N).	O(N <sup>2</sup> )	N <sup>2</sup> /2 N <sup>2</sup> + 1 Ig(N)
Big $\Omega$ $\Omega$ (f(N))			

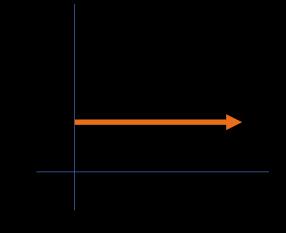


#### Constant Growth Rate, O(1)

If processing time is independent of the number of inputs n, the algorithm grows at a constant rate

```
01 int sum(int n)
02 {
03    int sum = 0;
04    sum += n;
05    return sum;
06 }
07
```

n	y = f(c)
1	3
10	3
100	3
1000	3
10000	3
100000	3
1000000	3
1000000	3
10000000	3







#### **Linear Growth Rate**

If processing time increases in proportion to the number of inputs n, the algorithm grows at a linear rate

```
01 int sum(int n)
02 {
03     int sum = 0;
04     for (int i=0; i<n; i++)
05         sum += i+1;
06     return sum;
07 }</pre>
```

n	y = f(n)
1	1
10	10
100	100
1000	1000
10000	10000
100000	100000
1000000	1000000
1000000	10000000
10000000	10000000



$$T(n) = 3n + 4$$
,  $T(n) \in O(n)$ , c=4,  $n_0 > 4$ 

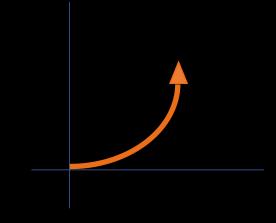


#### **Quadratic Growth Rate**

If processing time increases in proportion to the square of input size n, the algorithm grows at a quadratic rate

```
bool find(int n[][], int t)
01
02
      int i, j;
03
04
      for(i=0; i < n.size; i++)
05
        for(j=0; j < n.size; j++)
            if (x[i][j] == t)
06
07
               return true;
80
        return false;
09
```

n	$y = f(n^2)$
1	1
10	100
100	10000
1000	1000000
10000	10000000
100000	1000000000
100000	1E+12
10000000	1E+14
10000000	1E+16



$$T(n) = n^2 + 3n + 5$$
,  $T(n) \in O(n^2)$ ,  $c=?$ ,  $n_0>?$ 

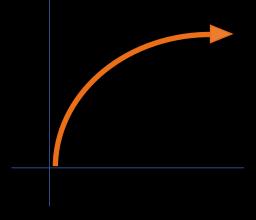


#### **Logarithmic Growth Rate**

If processing time increases in proportion to the log n, the algorithm grows at a logarithmic rate

```
01 int sum(int n)
02 {
03     int sum = 0;
04     for (int i=1; i<=n; i*=2)
05         sum += i;
06     return sum;
07 }</pre>
```

n	$y = f(\log_2 n)$
1	0
10	3
100	7
1000	10
10000	13
100000	17
1000000	20
1000000	23
10000000	27



#### **Different Growth Rates**

#### Time

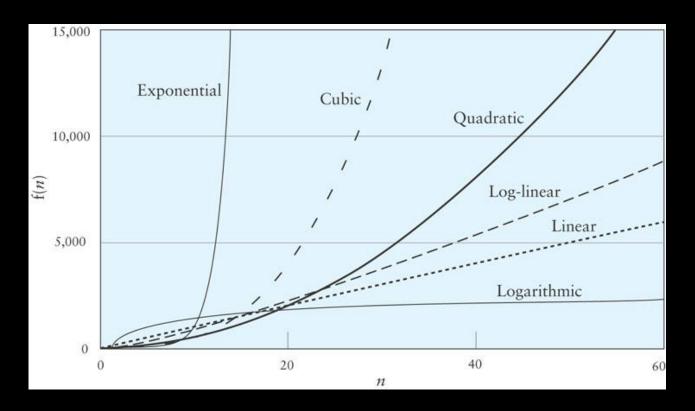
S	
ᆂ	
$oldsymbol{\Omega}$	

	O(1)	O(log n)	O(n)	O(n log n)	O(n²)	O(n³)	O(2 <sup>n</sup> )	O(n!)
1	1	0	1	0	1	1	2	1
10	1	3	10	10	100	1000	1024	3628800
100	1	7	100	200	10000	1000000	1.26765E+30	9.3326E+157
1000	1	10	1000	3000	100000	1000000000	1.0715E+301	#NUM!
10000	1	13	10000	40000	10000000	1E+12	#NUM!	#NUM!
100000	1	17	100000	500000	1000000000	1E+15	#NUM!	#NUM!
1000000	1	20	1000000	600000	1E+12	1E+18	#NUM!	#NUM!
10000000	1	23	1000000	7000000	1E+14	1E+21	#NUM!	#NUM!
10000000	1	27	10000000	800000000	1E+16	1E+24	#NUM!	#NUM!

#### Order of Growth gets Faster, Complexity increases

Constant < Logarithmic < Linear < Loglinear < Polynomial < Exponential < Factorial

#### **Different Growth Rates**



http://bigocheatsheet.com/

## Tips for Asymptotic Analysis (Big O)

#### Tip #1: Addition (Independence)

#### Tip #1: Addition (Independence)

$$T(n, m) = O(n+m)$$

#### **Tip #2: Drop Constant Multipliers**

```
01 void func1(int n)
02 {
03    for (int i=0; i<n; i++)
04         cout<<i;
05
06    for (int j=0; j<n; j++)
07         cout<<j;
08 }
09</pre>
```

#### Tip #2: Drop Constant Multipliers

```
01 void func1(int n)
02 {
03     for (int i=0; i<n; i++)
04          cout<<i;
05
06     for (int j=0; j<n; j++)
07          cout<<j;
08 }
09</pre>
```

$$T(n) = O(n+n) = O(2n)$$
 ~  $O(n)$ 

#### Tip #3: Different Input Variables

#### Tip #3: Different Input Variables

$$T(n, l) = O(n+l)$$

Describe what the variable is, Always! Example: O(s) where s is the size or length of a string



## Tip #4a: Drop Lower Order Terms with Similar Growth Rates

## Tip #4a: Drop Lower Order Terms with Similar Growth Rates

```
01 void func1(int n, int m)
02 {
03    for (int i=0; i<n; i++)
04         cout<<i;
05
06    for (int j=1; j<=n; j*=2)
07         cout<<j;
08 }
09</pre>
```

```
T(n) = O(n + log_2 n)
~ O(n)^*
```

\*Both variables are n and grow at the same rate.

## Tip #4b: Drop Lower Order Terms with Similar Growth Rates

## Tip #4b: Drop Lower Order Terms with Similar Growth Rates

```
01 void func1(int n, int m)
02 {
03    for (int i=0; i<n; i++)
04         cout<<i;
05
06    for (int j=1; j<=m; j*=2)
07         cout<<j;
08 }
09</pre>
```

```
T(n, m) = O(n + log_2 m)
~ O(n)^*
```

\*Assuming n and m are growing at the same rate.

If you are **given** in the question that n and m are growing at the same rate or if you **assume** they are growing at the same rate, then simplifying is fine



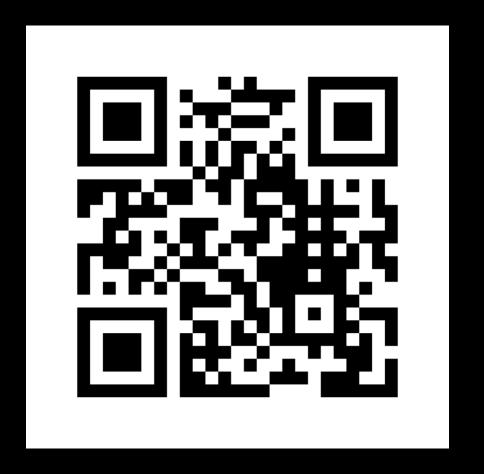
## Tip #4c: Do not drop Lower Order Terms with different Growth Rates

```
T(n, m) = O(n + \log_2 m)^*
```

\*Assuming no relationship is given between n and m.

#### Mentimeter

**Menti.com 9381 5899** 



#### Mentimeter

```
An algorithm's total run time is given by the expression, T(n, p) = 10n + p. What is the representation of this program's execution time in Big 0?
```

$$O(n+p)$$



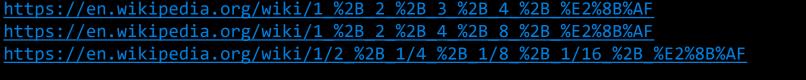
```
for (int i = 100; i > -1; i--)
  for (int j = i; j > 1; j/=2)
      print("viola")
```

0(1)



## Logarithmic growth

for(i = n; 
$$i >= 1$$
;  $i /= 2$ )





```
for(int i = n; i > 0; i /= 2)
    for(int j = 1; j < i; j++)
        sum += 1;</pre>
```



```
// This is A
for(int i=1; i<n; i*=2);
// This is B
for(int i=1; i<n; i*=3);</pre>
```

They both take same time in terms of Big O

```
// This is A
for(int i=1; i<n; i*=2);
// This is B
for(int i=1; i<n; i*=3);</pre>
```

B will be faster in terms of execution time/simulation

# **Enter Data**

<b>Best Case</b>	Average Case	<b>Worst Case</b>
Lowest cost	Average cost for all n	Highest cost

#### **Enter Data**

<b>Best Case</b>	Average Case	<b>Worst Case</b>
Lowest cost	Average cost for all n	<b>Highest cost</b>

- Average/Best/Worst case measure actual costs at a specific input instance.
- You can define a specific order of instance but cannot propose variability in input size.
  - In general, calculating best case time complexity under the assumption that the data structure has a small size, example: when an array has size 1 or the tree is empty should be avoided. The complexity is calculated without thinking about the size of input. But it is perfectly fine to think about the properties of input or data structure such as data is sorted, height will always be proportional to log n for a balanced tree, etc.
  - Asymptotic analysis assumes n is very large. Whether it be big O, theta, or omega, it always refers to the case of very large n. The best / average / worst cases arise in different structural cases, exclusive of size.
- **Growth Rate measures change in costs.**

## Recommended Readings

- https://dev.to/sherryummen/asymptotic-notations-b-oot-big-o-bigomega-big-theta-49e7
- Chapter 8.10 OpenDSA: Common Misunderstanding
- https://cs.stackexchange.com/questions/23068/how-do-o-and-%CE%A9-relate-to-worst-and-best-case
- https://qr.ae/pNyFxo
- https://cs.stackexchange.com/questions/23593/is-there-a-systembehind-the-magic-of-algorithm-analysis
- https://stackoverflow.com/questions/25593619/why-small-thetaasymtotic-notation-doesnt-exists/54542603

#### Useful series

1 + 2 + 3 + 4 + 
$$\cdots$$
 + n = n.(n+1)/2  
1 + 2 + 4 + 8 +  $\cdots$  + 2<sup>k</sup> = 2<sup>k+1</sup> - 1  
n + n/2 + n/4 + n/8 +  $\cdots$  + 1 = 2n - 1

https://en.wikipedia.org/wiki/1 %2B 2 %2B 3 %2B 4 %2B %E2%8B%AF https://en.wikipedia.org/wiki/1 %2B 2 %2B 4 %2B 8 %2B %E2%8B%AF https://en.wikipedia.org/wiki/1/2 %2B 1/4 %2B 1/8 %2B 1/16 %2B %E2%8B%AF



#### **Linear Search**

```
#include <iostream>
      #include <string>
2.
      std::string linearSearch(const std::string arr[], int size, std::string t)
4.
5.
          for(int i = 0; i < size; i++)
6.
               if(arr[i].compare(t) == 0)
7.
8.
                   return std::string("found at index = ") + std::to_string(i);
9.
10.
          return std::string("not found");
11.
12.
      int main()
13.
14.
          std::string arr[] = {"hello", "world", "cop3530", "cop3502"};
          std::string target = "curious";
15.
16.
          int size = sizeof(arr) / sizeof(arr[0]);
          std::cout << (linearSearch(arr, size, target));</pre>
17.
18.
          return 0;
19.
```

```
#include <iostream>
        #include <string>
        std::string linearSearch(const std::string arr[], int size, std::string t)
4.
             for(int i = 0; i < size; i++)
                if(arr[i].compare(t) == 0)
                     return std::string("found at index = ") + std::to string(i);
8.
             return std::string("not found");
10.
11.
12.
        int main()
13.
14.
             std::string arr[] = {"hello", "world", "cop3530", "cop3502", ...};
            std::string target = "curious";
15.
            int size = sizeof(arr) / sizeof(arr[0]);
16.
             std::cout << (linearSearch(arr, size, target));</pre>
17.
18.
            return 0;
19.
```

```
#include <iostream>
        #include <string>
        std::string linearSearch(const std::string arr[], int size, std::string t)
4.
            for(int i = 0; i < size; i++)
                if(arr[i].compare(t) == 0)
                    return std::string("found at index = ") + std::to string(i);
8.
            return std::string("not found");
10.
11.
12.
        int main()
13.
                                                                                             Size of array = size
            std::string arr[] = {"hello", "world", "cop3530", "cop3502", ...};
14.
                                                                                             Max size of any string = s
            std::string target = "curious"; -
15.
            int size = sizeof(arr) / sizeof(arr[0]);
16.
            std::cout << (linearSearch(arr, size, target));</pre>
17.
                                                                                          → Size of target = t
18.
            return 0;
19.
                                                                                             constant
```

```
#include <iostream>
        #include <string>
        std::string linearSearch(const std::string arr[], int size, std::string t)
4.
                                                                                         → linear and dependent on size
            for(int i = 0; i < size; i++)
                                                                                         → linear and dependent on t
               if(arr[i].compare(t) == 0)
                   return std::string("found at index = ") + std::to string(i);
                                                                                          constant
8.
            return std::string("not found");_
10.
                                                                                         → constant
11.
12.
        int main()
13.
                                                                                         Size of array = size
           std::string arr[] = {"hello", "world", "cop3530", "cop3502", ...};
14.
                                                                                         Max size of any string = s
            std::string target = "curious"; -
15.
            int size = sizeof(arr) / sizeof(arr[0]);
16.
            std::cout << (linearSearch(arr, size, target));</pre>
17.
                                                                                      → Size of target = t
18.
            return 0;
19.
                                                                                       constant
```

```
#include <iostream>
        #include <string>
                                                                                                    (size * t) + c
        std::string linearSearch(const std::string arr[], int size, std::string t)
4.
            for(int i = 0; i < size; i++)
                                                                                          → linear and dependent on size
6.
                                                                                         \rightarrow linear and dependent on t
               if(arr[i].compare(t) == 0)
                   return std::string("found at index = ") + std::to string(i);
                                                                                           constant
8.
            return std::string("not found");_
10.
                                                                                          → constant
11.
12.
        int main()
13.
                                                                                          Size of array = size
            std::string arr[] = {"hello", "world", "cop3530", "cop3502", ...}; -
14.
                                                                                          Max size of any string = s
            std::string target = "curious"; -
15.
            int size = sizeof(arr) / sizeof(arr[0]);
16.
            std::cout << (linearSearch(arr, size, target));</pre>
17.
                                                                                       → Size of target = t
18.
            return 0;
19.
                                                                                       constant
                                                                                        → (size * t) + c
```

O (size\*t), where size is size of array and t is size of target string

#### Clarification:

This program will yield an equation,

```
T(size, t) = (size * t) + 5c
```

This function T(size, t) will be an element of O(size.t), O(size.t.t), O(size.size.t), ... and several other functions.

When we talk about Big O, we want a measure to describe the upper bound. For the sake of the course, we seek the tightest upper bound.



#### Clarification:

This program will yield an equation,

```
T(size, t) = (size * t) + 5c
```

This function T(size, t) will be an element of  $\Omega(\text{size.t})$ ,  $\Omega(\text{size})$ ,  $\Omega(\text{t})$ ,  $\Omega(1)$  ... and several other functions.

When we talk about Big  $\Omega$ , we want a measure to describe the lower bound. For the sake of the course, we seek the tightest lower bound.



#### Clarification:

This program will yield an equation,

```
T(size, t) = (size * t) + 5c
```

In this program, the time complexity of the code is

- 0(size.t)
- $\Omega(\text{size.t})$
- $\Theta(\text{size.t})$



# **Binary Search**

## **Binary Search**

```
int binarySearch(int arr[], int size, int target)
1.
2.
3.
           int start = 0, mid, end = size-1;
           while(start <= end)</pre>
               mid = (start + end)/2;
               if(arr[mid] == target)
                   return mid;
8.
               else if(target > arr[mid])
9.
                    start = mid + 1;
10.
11.
               else
                   end = mid - 1;
12.
13.
14.
           return -1;
15.
```

#### **Peak Finding**

#### o Input:

- You are given an array of numbers
- The data is randomly sorted

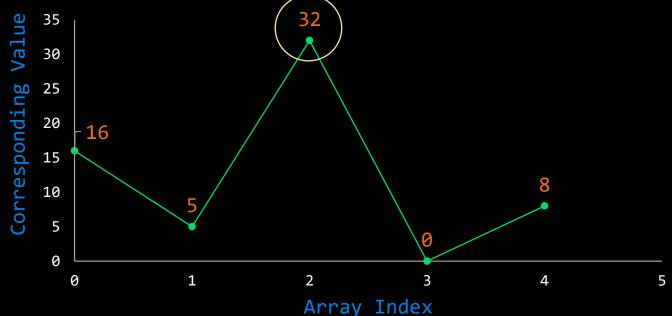
#### Output:

- A Peak value
- Peak is a number such that it is greater than or equal to both of its adjacent elements
- In case of the boundary values, a peak must be greater or equal to the one adjacent element.

 16
 5
 32
 0
 8



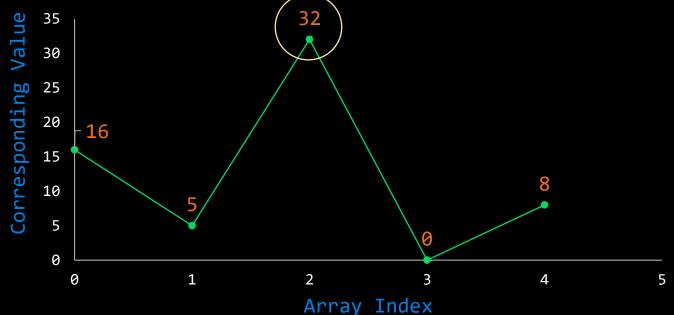
2D Representation of the Problem



Case 1: Central Element larger than both adjacent elements:



2D Representation of the Problem

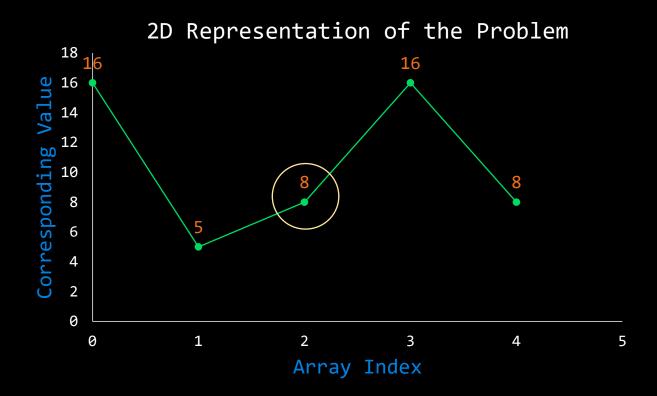


Case 1: Central Element larger than

both adjacent elements: Peak

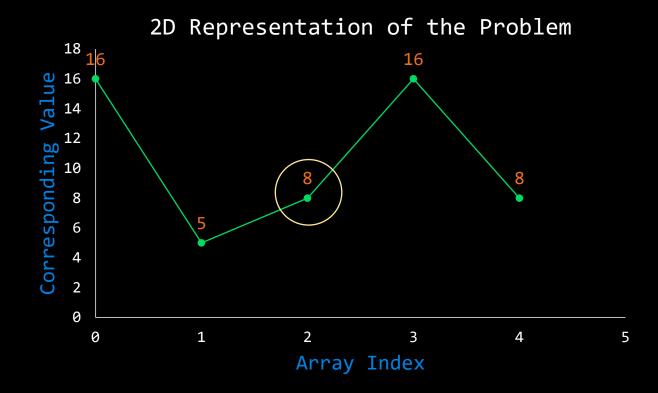
16	5	8	16	8

	16	5	8	16	8
--	----	---	---	----	---



Case 2: Central Element larger than left element and smaller than right element:

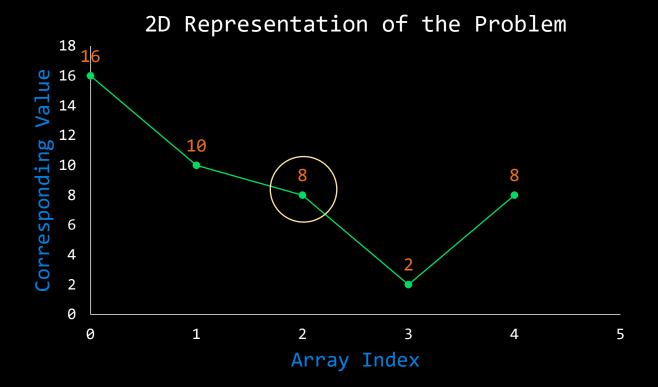
16	5	8	16	8
	l			



Case 2: Central Element larger than left element and smaller than right element: Keep going right

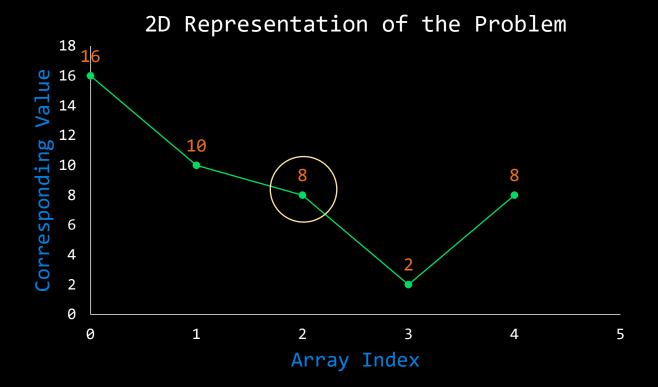
16	10	8	2	8
10	10	O	_	O

16	10	8	2	8



Case 3: Central Element larger than right element and smaller than left element:

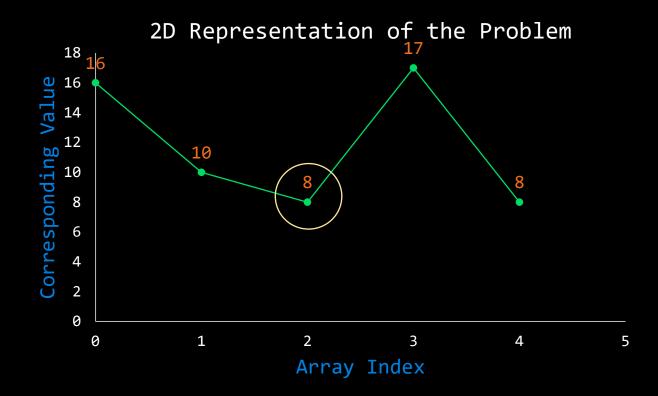
16	10	8	2	8
			_	



Case 3: Central Element larger than right element and smaller than left element: Keep going left

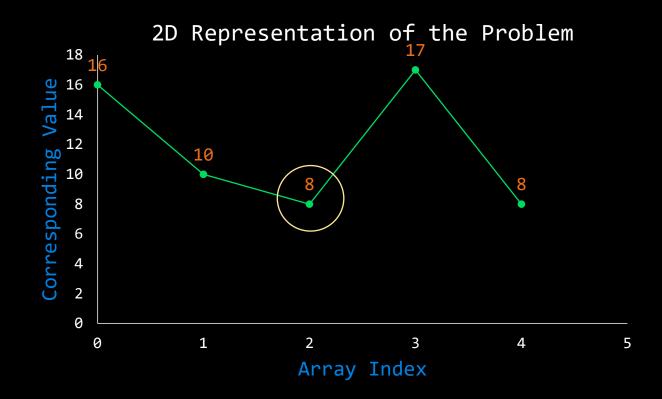
16	10	8	17	8
----	----	---	----	---

16	10	8	17	8



Case 4: Central Element smaller than both adjacent elements:

16	10	8	17	8



Case 4: Central Element smaller than both adjacent elements: Pick any side and keep going

## **Peak Finding**

16   10   8   17   8
----------------------

#### **Time Complexity:**

O(log n) using the divide and conquer approach over O(n) using brute force algorithms

# Questions

