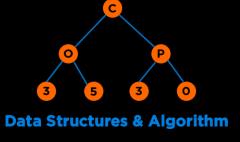
Final Exam Review



Categories of Data Structures

Linear Ordered

Non-linear Ordered

Not Ordered

Lists

Trees

Sets

Stacks

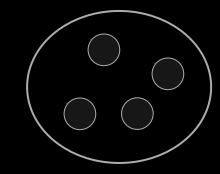
Graphs

Tables/Maps

Queues



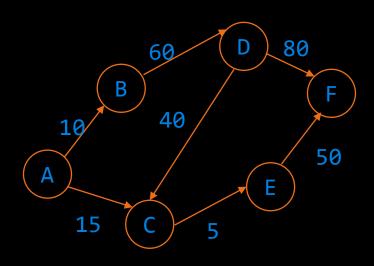




Announcements

- You must take the exam between:
 - 6pm 10pm EST on April 12 [All students except UFOL/UDER]
 - 6pm April 12 to April 14 [UFOL/UDER students]
- The exam will be over Honorlock and you are allowed one double sided handwritten sheet of notes.
- The exam duration is 2 hours. This means you must start by 8 pm EST or else you will lose time.
- Exam 2 Topics and Expectations Guide: <u>Link</u>
- Exam reviews: Exam 2 Resources

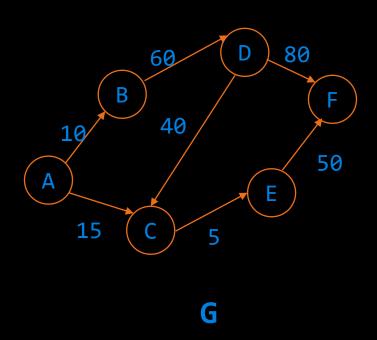
Common Representations



- Edge List
- Adjacency Matrix
- Adjacency List

G

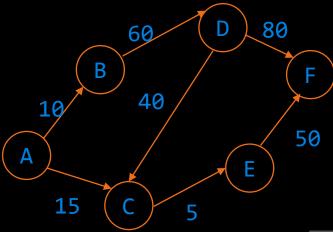
Edge List



Α	В	10
Α	С	15
В	D	60
D	С	40
D	F	80
Е	F	50
С	Е	5

 $G = \{(A,B), (A,C), (B,D), (D,C), (D,F), (E,F), (C,E)\}$

Edge List



G

Α	В	10
Α	С	15
В	D	60
D	С	40
D	F	80
Е	F	50
С	Е	5

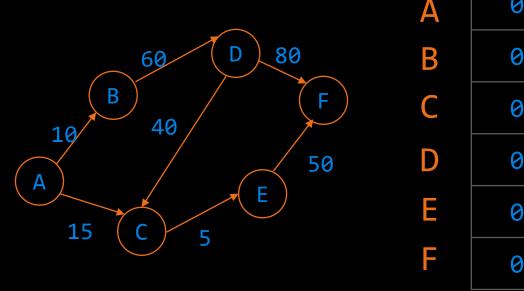
Common Operations:

1. Connectedness

2. Adjacency

Space: O(E)

Adjacency Matrix

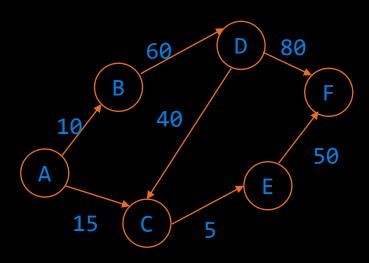


A	В	C	D	E	F
0	10	15	0	0	0
0	0	0	60	0	0
0	0	0	0	5	0
0	0	40	0	0	80
0	0	0	0	0	50
0	0	0	0	0	0

Insertion:

```
G[from][to] = weight; (if there is an edge, "from" -> "to")
G[from][to] = 0; (otherwise)
```

Adjacency Matrix Implementation



Ιr	าрเ	ıt	
7			
Д	В	10	
Д	C	1 5	
В	D	60	
D	C	40	
C	Е	5	
D	F	80	
	Е	ГΩ	

		0	1	2	3	4	5
Мар	0	0	10	15	0	0	0
A 0	1	0	0	0	60	0	0
B 1 C 2	2	0	0	0	0	5	0
D 3	3	0	0	40	0	0	80
E 4	4	0	0	0	0	0	50
F 5	5	0	0	0	0	0	0

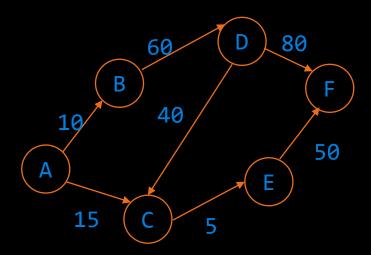
Insertion:

```
G[from][to] = weight; (if there is an edge, "from" -> "to")
G[from][to] = 0; (otherwise)
```

```
#include <iostream>
    #include<map>
    #define VERTICES 6
    using namespace std;
    int main()
06
           int no lines, wt, j=0;
           string from, to;
           int graph [VERTICES][VERTICES] = {0};
10
           map<string, int> mapper;
           cin >> no lines;
11
12
           for(int i = 0; i < no lines; i++)</pre>
13
                 cin >> from >> to >> wt;
14
                 if (mapper.find(from) == mapper.end())
15
                        mapper[from] = j++;
                 if (mapper.find(to) == mapper.end())
                        mapper[to] = j++;
                 graph[mapper[from]][mapper[to]] = wt;
19
20
21
           return 0;
```

https://www.onlinegdb.com/Hy8M0CnsS

Adjacency Matrix



G

Ma	ар
Α	0
В	1
C	2
D	3
Ε	4
F	5

 0
 1
 2
 3
 4
 5

 0
 0
 10
 15
 0
 0
 0

 1
 0
 0
 0
 60
 0
 0

 2
 0
 0
 0
 0
 5
 0

 3
 0
 0
 40
 0
 0
 80

 4
 0
 0
 0
 0
 0
 0

 5
 0
 0
 0
 0
 0
 0

Common Operations:

Connectedness

```
Is A connected to B?
G["A"]["B"] ~ O(1)
```

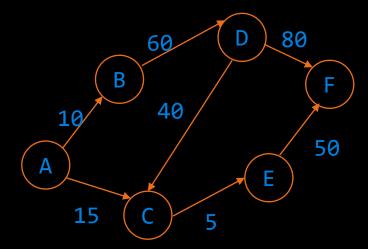
2. Adjacency

What are A's adjacent nodes?
for each element x in G["A"]
 if x ! = 0

~ O(|V|)

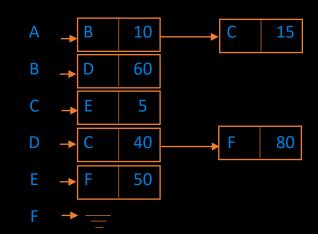
Space: **0(|V| * |V|)**

Adjacency List



G

Sparse Graph:
Edges ~ Vertices



Common Operations:

Connectedness

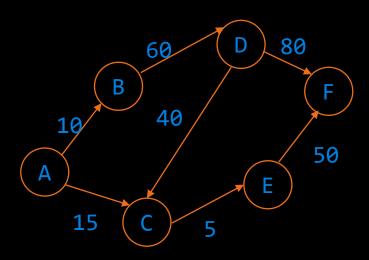
```
Is A connected to B?
for each element x in G["A"]
   if x ! = 'B'
        ~ O(outdegree|V|)
```

2. Adjacency

```
What are A's adjacent nodes?

G["A"] ~ O(outdegree|V|)
```

Adjacency List Implementation

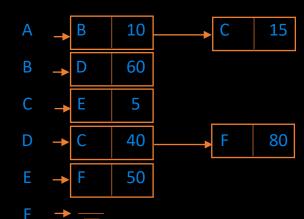


Input

7
A B 10
A C 15
B D 60
D C 40
C E 5
D F 80

E F 50

G



Insertion:

If to or from vertex not present add vertex Otherwise add edge at the end of the list

```
#include <iostream>
    #include<map>
    #include<vector>
    #include<iterator>
    using namespace std;
07
    int main()
           int no lines;
           string from, to, wt;
           map<string, vector<pair<string,int>>> graph;
11
           cin >> no_lines;
12
           for(int i = 0; i < no lines; i++)</pre>
13
14
15
                 cin >> from >> to >> wt;
                 graph[from].push back(make pair(to, stoi(wt)));
16
17
                 if (graph.find(to)==graph.end())
18
                        graph[to] = {};
19
20
```

https://onlinegdb.com/HkJq9iFaI

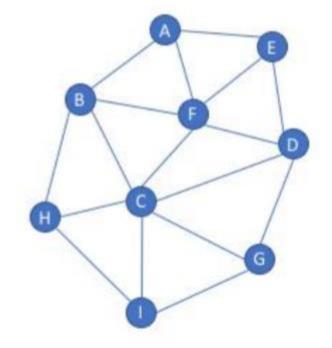
Graph Implementation

	Edge List	Adjacency Matrix	Adjacency List
Time Complexity: Connectedness	O(E)	0(1)	O(outdegree(V))
Time Complexity: Adjacency	O(E)	0(V)	O(outdegree(V))
Space Complexity	O(E)	0(V*V)	O(V+E)



Graph - BFS

- Which of the following are valid breadth first search traversals for this graph?
- a) AFBEDCHGI
- b) ICHGBFDAE
- c) DCFEGHIBA
- d) EAFDBHCIG
- e) FAEDCBGIH





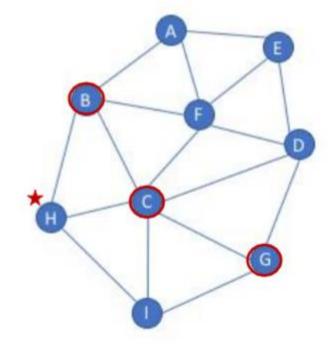
Graph - BFS

- Which of the following are valid breadth first search traversals for this graph?
- AFBEDCHGI
- ICHGBFDAE
- DCFEGHIBA
- EAFDBHCIG
- FAEDCBGIH

All the options except for d

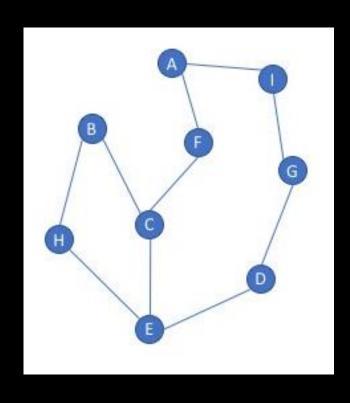
Why not d?







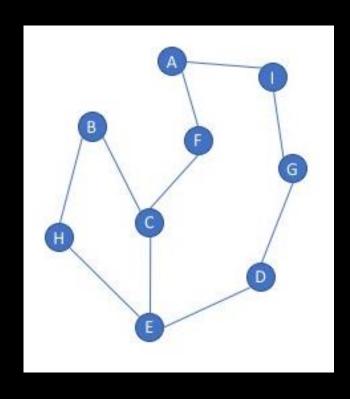
Valid DFS: Which DFS are valid?



- HECBDGIAF
- CEHBDGIAF
- AFCEHBIGD
- DECBHFAIG



Valid DFS: Which DFS are valid?



- HECBDGIAF
- CEHBDGIAF
- AFCEHBIGD
- DECBHFAIG



BFS Pseudocode

- Write pseudocode/code for implementing the Breadth First Search Algorithm of a graph, G that takes a source vertex S as input. (8).
- Also, state the Big O complexity of the traversal in the worst case (2).



```
string source = "A";
    std::set<string> visited;
03
    std::queue<string> q;
04
    visited.insert(source);
05
    q.push(source);
06
07
    cout<<"BFS: ";</pre>
08
09
    while(!q.empty())
10
          string u = q.front();
11
12
          cout << u;
13
          q.pop();
14
          vector<string> neighbors = graph[u];
15
          for(string v: neighbors)
16
17
18
19
                      visited.insert(v);
20
                      q.push(v);
21
22
23
```

```
string source = "A";
    std::set<string> visited;
    std::stack<string> s;
04
    visited.insert(source);
    s.push(source);
07
    cout<<"DFS: ";</pre>
08
    while(!q.empty())
10
          string u = s.top();
11
12
          cout << u;
13
          s.pop();
          vector<string> neighbors = graph[u];
14
15
          for(string v: neighbors)
16
17
                if(visited.count(v)==0)
18
                       visited.insert(v);
19
20
                      s.push(v);
21
22
23
```



Graph Algorithm Mix n Match

- Finds the shortest paths in a weighted graph
- Find the minimum cost connected network
- Scheduling algorithm, list steps in a process
- Finds the shortest path in an unweighted graph

Prim's or Kruskals

BFS

DFS

Topological Sort Dijkstra's Algorithm

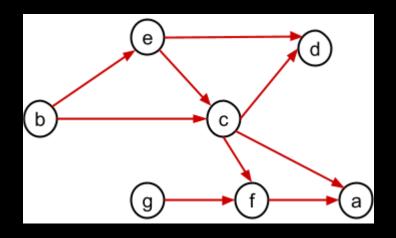


Graph Algorithm Mix n Match

Finds the shortest paths in a weighted graph
 Find the minimum cost connected network
 Scheduling algorithm, list steps in a process
 Finds the shortest path in an unweighted graph
 DFS
 Topological Sort
 Dijkstra's Algorithm



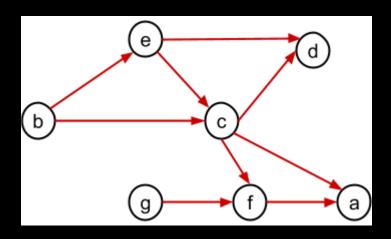
Which of the choices below represent a valid topological sort ordering of this graph?



- b, e, c, g, f, a, d
- b, a, c, g, f, e, d
- b, g, f, c, e, a, d
- b, e, c, g, a, f, d
- b, g, e, c, d, f, a
- b, f, c, g, a, e, d



Which of the choices below represent a valid topological sort ordering of this graph?



- b, e, c, g, f, a, d
- b, a, c, g, f, e, d
- b, g, f, c, e, a, d
- b, e, c, g, a, f, d
- b, g, e, c, d, f, a
- b, f, c, g, a, e, d



What does this code do?

```
#include <set>
#include <stack>
using namespace std;
bool doSomething(const Graph& graph, int src, int dest)
    set<int> visited;
    stack<int> s;
    visited.insert(src);
    s.push(src);
    while(!s.empty())
        int u = s.top();
        s.pop();
        for(auto v: graph.adjList[u])
            if(v == dest)
                return true;
            if ((visited.find(v) == visited.end())) {
                visited.insert(v);
                s.push(v);
    return false;
```



What does this code do?

```
#include <set>
#include <stack>
using namespace std;
bool doSomething(const Graph& graph, int src, int dest)
    set<int> visited;
    stack<int> s;
    visited.insert(src);
    s.push(src);
    while(!s.empty())
        int u = s.top();
        s.pop();
        for(auto v: graph.adjList[u])
            if(v == dest)
                return true;
            if ((visited.find(v) == visited.end())) {
                visited.insert(v);
                s.push(v);
   return false;
```

Returns whether a given vertex is reachable from another vertex using DFS



Scenario

A county government maintains a network of roads. The county government has tabulated the cost of maintaining each road. They need to minimize the cost of road maintenance but ensure that all places in the county are accessible.

Which graph algorithm that we discussed in class could they use to solve this problem? What are the vertices, what are the edges, what are the edge values?



Scenario

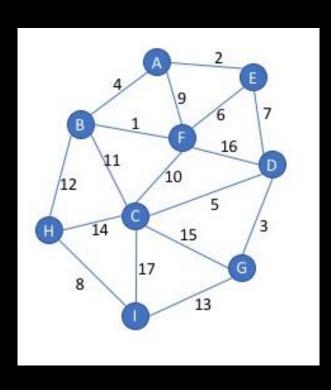
A county government maintains a network of roads. The county government has tabulated the cost of maintaining each road. They need to minimize the cost of road maintenance but ensure that all places in the county are accessible.

Which graph algorithm that we discussed in class could they use to solve this problem? What are the vertices, what are the edges, what are the edge values?

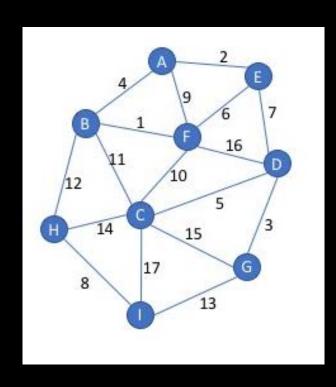
- Prim's or Kruskals algorithm for minimum spanning tree.
- Roads are edges.
- Ends of roads are vertices.
- Edge weights are cost for maintaining roads.



MST using Prims starting from "I"



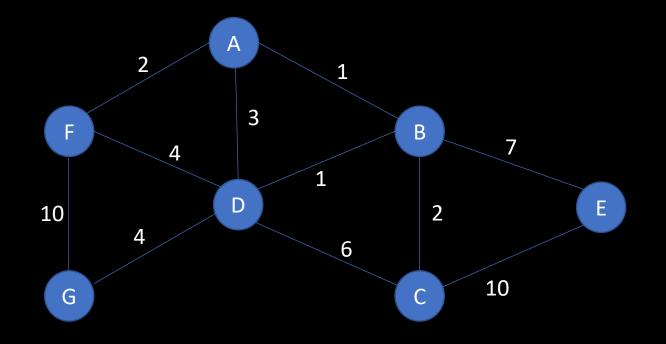
MST using Prims starting from "I"



IHBFAEDGC

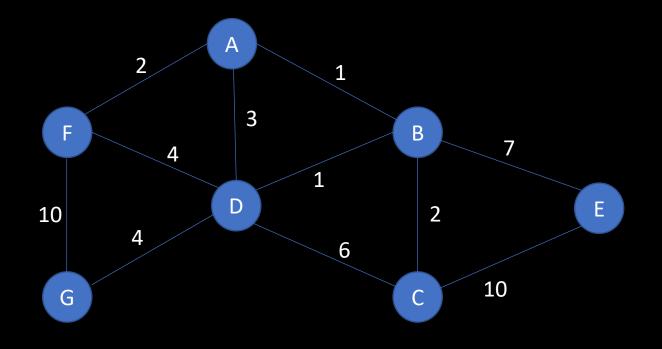


V	D(v)	P(v)
Α		
В		
С		
D		
Е		
F		
G		

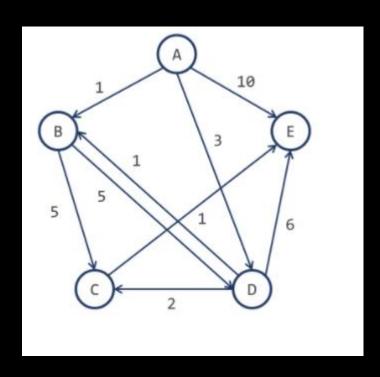


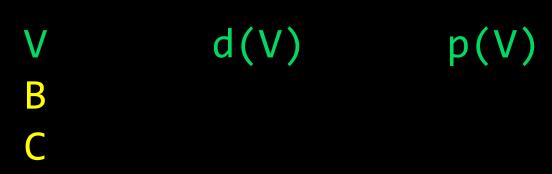


V	D(v)	P(v)
А	0	NA
В	1	А
С	3	В
D	2	В
Е	8	В
F	2	А
G	6	D

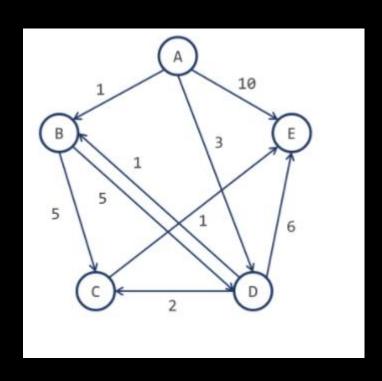












V	d(V)	p(V)
B	1	A
C	5	D
D	3	A
E	6	C



Algorithmic Paradigms

Algorithmic Paradigms

	Properties	Examples
Brute Force	 Generate and Test an Exhaustive Set of all possible combinations Can be computationally very expensive Guarantees optimal solution 	 Finding divisors of a number, n by checking if all numbers from 1n divides n without remainder Finding duplicates using all combinations Bubble/Selection Sort
Divide and Conquer	 Break the problem into subcomponents typically using recursion Solve the basic component Combine the solutions to sub-problems 	Quick SortMerge SortBinary SearchPeak Finding
Dynamic Programming	 Optimal substructure: solution to a large problem can be obtained by solution to a smaller optimal problems Overlapping sub-problems: space of sub-problems must be small, that is, any recursive algorithm solving the problem should solve the same sub-problems over and over, rather than generating new sub-problems. Guarantees optimal solution 	Fibonacci SequenceAssembly SchedulingKnapsack
Greedy Algorithms	 Local optimal solutions at each stage Does not guarantee optimal solution 	Prim's AlgorithmDijkstra's AlgorithmKruskal's Algorithm

Bin Packing

If we have packets that each require 7 units, 8 units, 2 units and 3 units of space, how many minimum bins are required to store all the four packets if each bin can take at most 10 units of space using the following Greedy strategies

First Fit: scan the bins and place the new item in the first bin that is large enough.

Best Fit: scan the bins and place the new item in the bin that finds the spot that creates the smallest empty space



Given this file, generate a Huffman Tree and identify the codes of each character.

care racecar era

- 1. Create a table with symbols and their frequencies
- 2. Construct a set of trees with root nodes that contain each of the individual symbols and their weight (frequency).
- Place the set of trees into a min priority queue.
- 4. while the priority queue has more than one item

 Remove the two trees with the smallest weights.

 Combine them into a new binary tree in which the weight of the tree root is the sum of the weights of its children.

 Insert the newly created tree back into the priority queue.
- 5. Traverse the resulting tree to obtain binary codes for characters

1. Create a table with symbols and their frequencies

care racecar era

Character	Frequency
a	4
r	4
С	3
е	3
()	2

- 2. Construct a set of trees with root nodes that contain each of the individual symbols and their weight (frequency).
- 3. Place the set of trees into a min priority queue.

Character	Frequency
a	4
r	4
С	3
е	3
ر ،	2



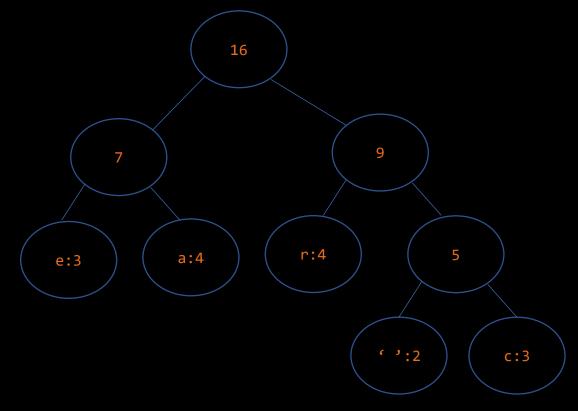
4. while the priority queue has more than one item

Remove the two trees with the smallest weights.

Combine them into a new binary tree in which the weight of the tree root is the sum of the weights of its children.

Insert the newly created tree back into the priority queue.

Character	Frequency
а	4
r	4
С	3
е	3
<i>c</i> >	2





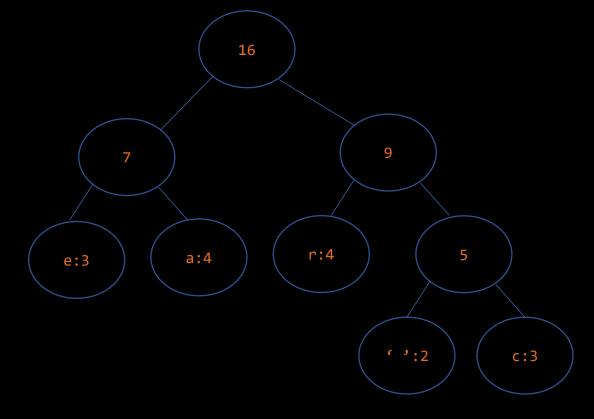
4. while the priority queue has more than one item

Remove the two trees with the smallest weights.

Combine them into a new binary tree in which the weight of the tree root is the sum of the weights of its children.

Insert the newly created tree back into the priority queue.

Character	Frequency	Huffman Code
а	4	01
r	4	10
С	3	111
е	3	00
()	2	110





Questions

