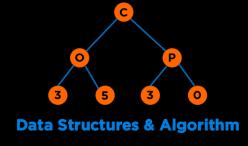
# Lists, Stacks and Queues



## **Categories of Data Structures**

**Linear Ordered** 

**Non-linear Ordered** 

**Not Ordered** 

Lists

**Trees** 

Sets

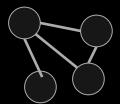
**Stacks** 

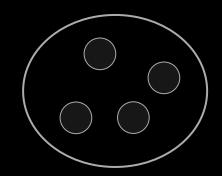
**Graphs** 

Tables/Maps

Queues







### Agenda

- Data Structures
- Abstract Data Types
- Lists
  - Array Implementation
  - Linked List Implementation and its types
  - Lists in C++
- Stacks
  - Array Based and Linked List Based
  - Stacks in C++
  - Use Cases
- Queues
  - Array Based and Linked List Based
  - Queue in C++
  - Use cases



# Data Structures

#### **Data Structures**

#### A data structure is a way to store and organize data

- Mathematical or Logical models (Abstract Data Types)
  - List: Store, Read, Modify
- Implementation (Concrete)
  - Arrays, Linked List, Vector, ArrayList, List

# Abstract Data Types

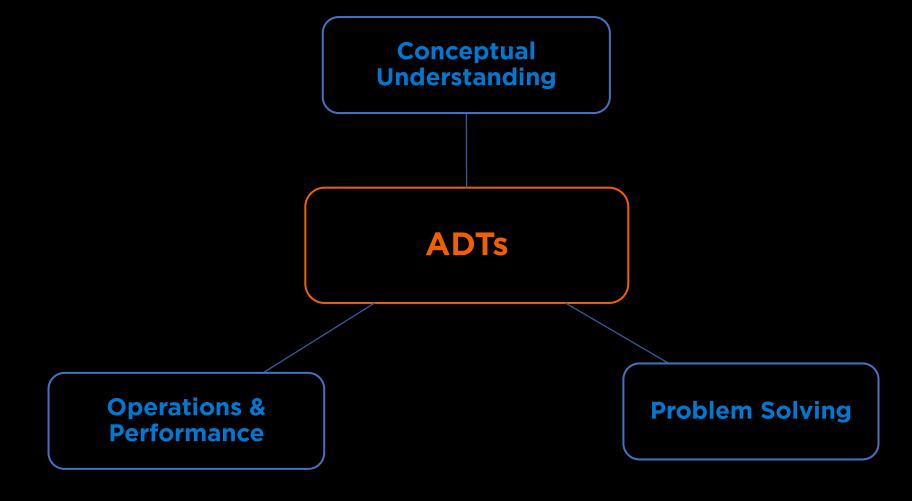


### **Abstract Data Types**

- Class of objects whose logical behavior is defined by a set of values and a set of operations
  - Define data (properties) and operations (behavior)
  - Don't care about implementation



# Abstract Data Types (ADTs)



# Lists



#### List

- Ordered Collection of Data (Ordered = Position)
- Elements have some position
- Linear Structure
- Can have some size or grow/shrink
- No limit on nature of elements

## **List - Characteristics**

Data

Operations

#### **List - Characteristics**

#### Data

- Items
- Number of Items (Size)
- Capacity

#### Operations

- Read/Write an element
- Add or remove an element
- Find an element
- Count
- Traverse the list (Printing)



Characteristics		
Operations		
Performance		
Benefits		
Drawbacks		

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Contiguous Indices</li> <li>Elements are stored contiguously in memory</li> <li>Allows Random Access</li> </ul>		
Operations			
Performance			
Benefits			
Drawbacks			

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Contiguous Indices</li> <li>Elements are stored contiguously in memory</li> <li>Allows Random Access</li> </ul>		
Operations	<ul><li>Adding - Beginning, Middle, End</li><li>Removal - Beginning, Middle, End</li></ul>		
Performance		Add	Remove
	Beginning		
	End		
	Middle		
Benefits			
Drawbacks			

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Contiguous Indices</li> <li>Elements are stored contiguously in memory</li> <li>Allows Random Access</li> </ul>		
Operations	<ul> <li>Adding - Beginning, Middle, End</li> <li>Removal - Beginning, Middle, End</li> </ul>		
Performance		Add	Remove
	Beginning	0(n)	O(n)
	End	0(1)	0(1)
	Middle	0(n)	0(n)
Benefits			
Drawbacks			

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Contiguous Indices</li> <li>Elements are stored contiguously in memory</li> <li>Allows Random Access</li> </ul>		
Operations	<ul><li>Adding - Beginning, Middle, End</li><li>Removal - Beginning, Middle, End</li></ul>		
Performance		Add	Remove
	Beginning	0(n)	0(n)
	End	0(1)	0(1)
	Middle	0(n)	0(n)
Benefits	■ Constant Access Time, arr[i] = arr + (i*sizeOf(type))		
Drawbacks			

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Contiguous Indices</li> <li>Elements are stored contiguously in memory</li> <li>Allows Random Access</li> </ul>		
<b>Operations</b>	<ul><li>Adding - Beginning, Middle, End</li><li>Removal - Beginning, Middle, End</li></ul>		
Performance		Add	Remove
	Beginning	0(n)	0(n)
	End	0(1)	0(1)
	Middle	0(n)	0(n)
Benefits	<pre>Constant Access Time, arr[i] = arr + (i*sizeOf(type))</pre>		
Drawbacks	Expensive for adding/removing elements from front		

```
class Node
{
    public:
        Node *next;
        int data;
};
```

```
int main ()
  Node* obj = new Node;
  obj -> data = 10;
  obj -> next = nullptr;
  obj -> next = new Node;
  obj -> next -> data = 20;
  obj -> next -> next = nullptr;
  obj -> next -> next = new Node;
  obj -> next -> next -> data = 30;
  obj -> next -> next -> next = nullptr;
 return 0;
```

```
class Node
{
    public:
        Node *next;
        int data;
};
```

```
int main ()
 Node* obj = new Node;
 obj -> data = 10;
  obj -> next = nullptr;
 obj -> next = new Node;
 obj -> next -> data = 20;
 obj -> next -> next = nullptr;
 obj -> next -> next = new Node;
  obj -> next -> next -> data = 30;
  obj -> next -> next -> next = nullptr;
 return 0;
```

**Problem:** 



```
class Node
                                         int main ()
    public:
                                             Node* obj = new Node(10, nullptr);
        Node *next;
                                             obj = new Node(20, obj);
                                             obj = new Node(30, obj);
        int data;
        Node(int d, Node* n);
                                             cout << "Size = "<< obj -> size();
                                             return 0;
    private:
        int size();
};
Node::Node(int d, Node* n)
   this -> data = d;
    this -> next = n;
int Node::size()
   if(this == nullptr)
        return 0;
    else
        return 1 + (this->next)->size();
```

```
public:
        Node *next;
        int data;
        Node(int d, Node* n);
   private:
        int size();
};
Node::Node(int d, Node* n)
   this -> data = d;
    this -> next = n;
int Node::size()
   if(this == nullptr)
        return 0;
    else
        return 1 + (this->next)->size();
```

class Node

```
int main ()
{
    Node* obj = new Node(10, nullptr);
    obj = new Node(20, obj);
    obj = new Node(30, obj);
    cout << "Size = "<< obj -> size();
    return 0;
}
```

#### **Problem:**

**Too much details** 



#### **Encapsulate Node: Better Design**

```
class List
struct Node
                                     public:
 int data;
 Node *next;
                                        int size;
                                        Node* head;
};
                                        Node* tail;
or
                                     public:
                                        List();
class Node
                                        void push_front(int);
    public:
        Node *next;
        int data;
};
```

#### **Encapsulate Node: Better Design**

```
struct Node
{
   int data;
   Node *next;
};

or

class Node
{
   public:
        Node *next;
        int data;
};
```

```
class List
     public:
        int size;
        Node* head;
        Node* tail;
     public:
        List();
        void push front(int);
};
List::List()
    size = 0;
    head = new Node;
    tail = new Node;
    head -> next = tail;
```

```
void List::push front(int x)
    Node* temp = new Node;
    temp -> data = x;
    temp -> next = head->next;
    head -> next = temp;
    size++;
int main()
    List obj;
    obj.push_front(15);
    obj.push front(20);
    obj.push_front(15);
    return 0;
```



#### Do not expose internal details to the client

```
int main()
{
    List myList;
    myList.push_front(15);
    myList.push_front(20);
    myList.push_front(15);
    return 0;
}
```

Characteristics		
Operations		
Performance		
Benefits		
Drawbacks		



Characteristics	<ul> <li>Consists of Nodes         <ul> <li>□ Data</li> <li>□ Pointer to Next Node</li> </ul> </li> <li>Stores Similar Elements</li> <li>■ Elements are linked in memory but stored non-contiguously</li> <li>■ Does not allow Random Access</li> </ul>
Operations	
Performance	
Benefits	
Drawbacks	2



Characteristics	<ul> <li>Consists of Nodes         <ul> <li>□ Data</li> <li>□ Pointer to Next Node</li> </ul> </li> <li>Stores Similar Elements</li> <li>Elements are linked in memory but stored non-contiguously</li> <li>□ Does not allow Random Access</li> </ul>
Operations	<ul> <li>Adding (Add) - PushFront(Key), PushBack(Key)</li> <li>Removal (Remove) - PopFront, PopBack</li> <li>Access (Get) - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>
Performance	
Benefits	
Drawbacks	



Characteristics	<ul> <li>Consists of Nodes</li> <li>Data</li> <li>Pointer to Next Node</li> <li>Stores Similar Elements</li> <li>Elements are linked in memory but stored non-contiguously</li> <li>Does not allow Random Access</li> </ul>		
Operations	<ul> <li>Adding (Add) - PushFront(Key), PushBack(Key)</li> <li>Removal (Remove) - PopFront, PopBack</li> <li>Access (Get) - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>		
Performance	PushFront	PushBack	AddBefore
	PopFront	PopBack	AddAfter
	TopFront	TopBack	
	Find	Erase	Empty
Benefits			
Drawbacks			



Characteristics	<ul> <li>Consists of Nodes</li> <li>Data</li> <li>Pointer to Next Node</li> <li>Stores Similar Element</li> <li>Elements are linked in Does not allow Random</li> </ul>	nts In memory but stored r	non-contiguously
Operations	<ul> <li>Adding (Add) - PushFront(Key), PushBack(Key)</li> <li>Removal (Remove) - PopFront, PopBack</li> <li>Access (Get) - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>		
Performance	PushFront - O(1)	PushBack - O(n)	AddBefore - O(n)
	PopFront - O(1)	PopBack - O(n)	AddAfter - O(1)
	TopFront - O(1)	TopBack - O(n)	
	Find - O(n)	Erase - O(n)	Empty - 0(1)
Benefits			
Drawbacks			



Characteristics	<ul> <li>Consists of Nodes</li> <li>Data</li> <li>Pointer to Next Node</li> <li>Stores Similar Element</li> <li>Elements are linked in Does not allow Random</li> </ul>	nts In memory but stored r	non-contiguously
Operations	<ul> <li>Adding (Add) - PushFront(Key), PushBack(Key)</li> <li>Removal (Remove) - PopFront, PopBack</li> <li>Access (Get) - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>		
Performance	PushFront - 0(1)	PushBack - O(n)	AddBefore - O(n)
	PopFront - 0(1)	PopBack - O(n)	AddAfter - O(1)
	TopFront - 0(1)	TopBack - O(n)	
	Find - O(n)	Erase - O(n)	Empty - 0(1)
Benefits	<ul><li>Adding/Removing in front is faster, O(1)</li></ul>		
Drawbacks			



Characteristics	<ul> <li>Consists of Nodes         <ul> <li>Data</li> <li>Pointer to Next Node</li> </ul> </li> <li>Stores Similar Elements</li> <li>Elements are linked in memory but stored non-contiguously</li> <li>Does not allow Random Access</li> </ul>		
Operations	<ul> <li>Adding (Add) - PushFront(Key), PushBack(Key)</li> <li>Removal (Remove) - PopFront, PopBack</li> <li>Access (Get) - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>		
Performance	PushFront - 0(1)	PushBack - O(n)	AddBefore - O(n)
	PopFront - 0(1)	PopBack - O(n)	AddAfter - O(1)
	TopFront - 0(1)	TopBack - O(n)	
	Find - O(n)	Erase - O(n)	Empty - 0(1)
Benefits	<ul><li>Adding/Removing in front is faster, O(1)</li></ul>		
Drawbacks	<ul><li>Expensive for random access, O(n)</li><li>TopBack, PushBack, PopBack and AddBefore are expensive</li></ul>		



# List: Single Linked List with Tail

Characteristics	<ul> <li>Consists of Nodes and has a Tail         <ul> <li>Data</li> <li>Pointer to Next Node</li> </ul> </li> <li>Stores Similar Elements</li> <li>Elements are linked in memory but stored non-contiguously</li> <li>Does not allow Random Access</li> </ul>		
Operations	<ul> <li>Adding - PushFront(Key), PushBack(Key)</li> <li>Removal - PopFront, PopBack</li> <li>Access - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>		
Performance	PushFront - 0(1)	PushBack - 0(1)	AddBefore - O(n)
	PopFront - 0(1)	PopBack - O(n)	AddAfter - O(1)
	TopFront - 0(1)	TopBack - O(1)	
	Find - O(n)	Erase - O(n)	Empty - O(1)
Benefits	Solves the issue of pushing back and getting last element		
Drawbacks	■ Expensive for PopBack and AddBefore		



# **List: Doubly Linked List with Tail**

Characteristics	<ul> <li>Consists of Nodes         <ul> <li>Data</li> <li>Pointer to Next and Previous Node</li> </ul> </li> <li>Stores Similar Elements</li> <li>Elements are linked in memory but stored non-contiguously</li> <li>Does not allow Random Access</li> </ul>		
Operations	<ul> <li>Adding - PushFront(Key), PushBack(Key)</li> <li>Removal - PopFront, PopBack</li> <li>Access - TopFront, TopBack</li> <li>Find(Key), Erase(Key), Empty()</li> <li>AddBefore(Node, Key), AddAfter(Node, Key)</li> </ul>		
Performance	PushFront - 0(1)	PushBack - 0(1)	AddBefore - 0(1)
	PopFront - 0(1)	PopBack - O(1)	AddAfter - O(1)
	TopFront - 0(1)	TopBack - 0(1)	
	Find - O(n)	Erase - O(n)	Empty - O(1)
Benefits	■ Solves the issue of PopBack and AddBefore		
Drawbacks	■ Extra memory		

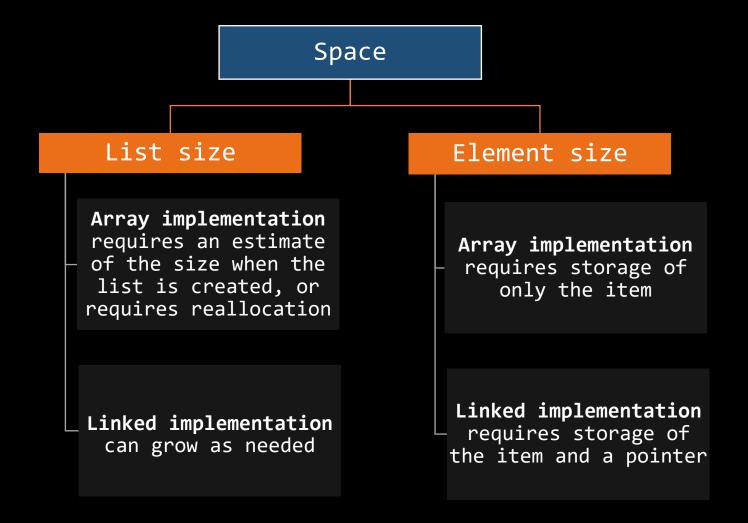


## List - Example: Circular Linked List

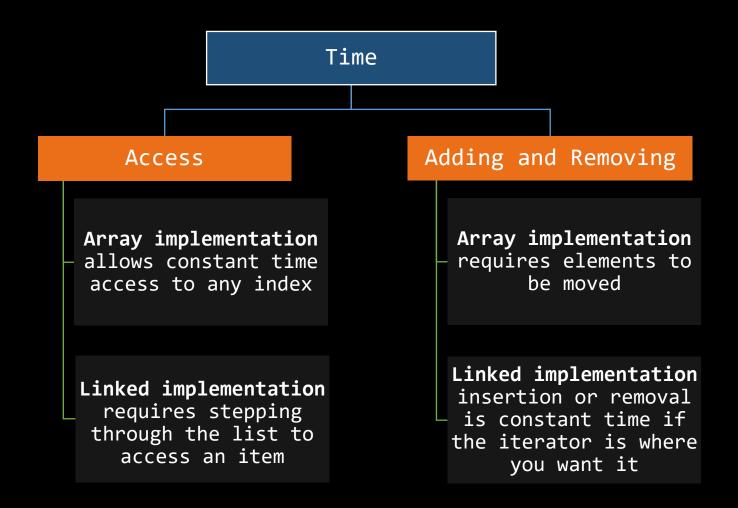
Single Circular

Doubly Circular

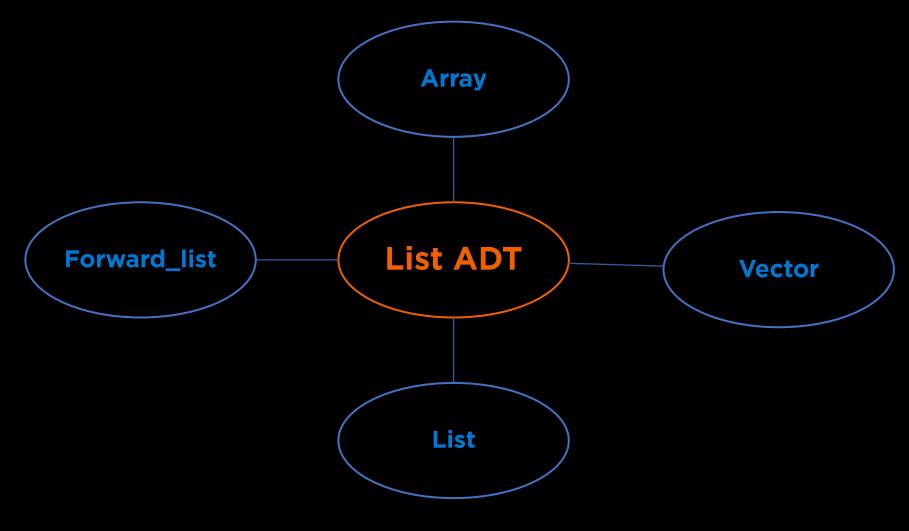
# Array vs Linked List: Space



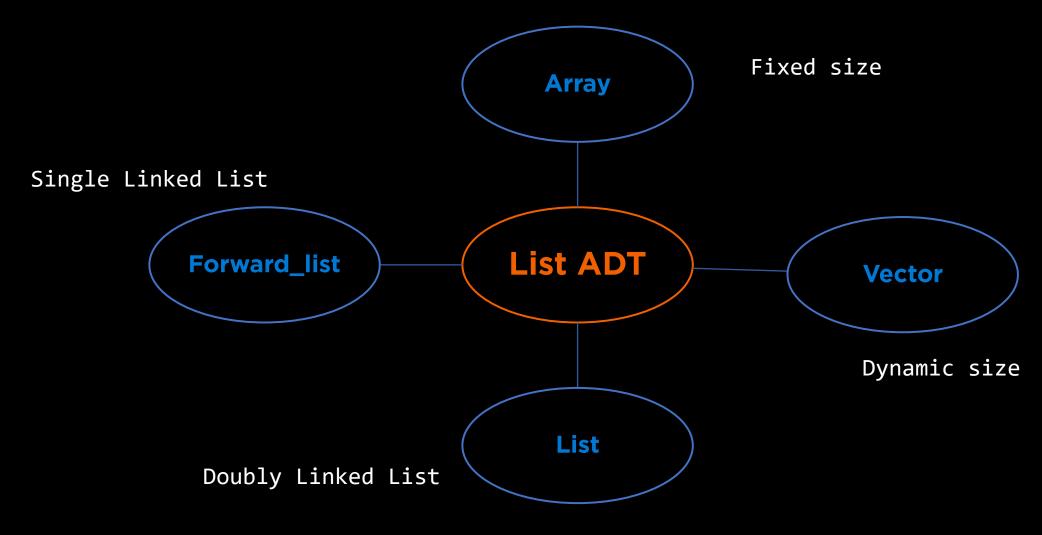
# **Array vs Linked List: Time**



### **Lists in C++ Standard Template Library**



### Lists in C++ Standard Template Library



### Lists in C++ STL: List

#### List containers are implemented as doubly-linked lists

Function	Operation
Constructor(n, val)	Constructs a container with n elements. Each element is a copy of val (if provided).
<pre>void push_front (val)</pre>	Inserts a new element at the beginning of the list, right before its current first element.

```
std::list<int> mylist (4,100); [100, 100, 100, 100]
mylist.push_front (200); [200, 100, 100, 100]
```



### Lists in C++ STL: List

#### **Printing a List**

```
01 list<int> mylist (4,100);  // [100, 100, 100, 100]
02 mylist.push_front (200);  // [200, 100, 100, 100, 100]
03 for(list<int>::iterator it = mylist.begin(); it != mylist.end(); ++it)
04 cout << ' ' << *it;</pre>
```

Prints: 200 100 100 100 100

#### All containers have Iterators!



### **Iterators**

- Variables to keep track of where we are in a data set
- Iterator Class
  - Operators to advance to next data (++)
  - Dereference Operator (\*) to access data
  - Operators to compare two iterators (!=)
  - Assignment operator (=)
- Container or the main data structure you are implementing Class
  - begin() methods
  - end() methods



### Iterators

	category			properties	valid expressions
all categories			copy-constructible, copy-assignable and destructible	X b(a); b = a;	
			Can be incremented	++a a++	
			Input	Supports equality/inequality comparisons	a == b a != b
				Can be dereferenced as an <i>rvalue</i>	*a a->m
		Forward C	Output	Can be dereferenced as an <i>Ivalue</i> (only for <i>mutable iterator types</i> )	*a = t *a++ = t
Random Access	Bidirectional			default-constructible	X a; X()
				Multi-pass: neither dereferencing nor incrementing affects dereferenceability	{ b=a; *a++; *b; }
				Can be decremented	a a *a
				Supports arithmetic operators + and -	a + n n + a a - n a - b
				Supports inequality comparisons (<, >, <= and >=) between iterators	a < b a > b a <= b a >= b
				Supports compound assignment operations += and -=	a += n a -= n
				Supports offset dereference operator ([])	a[n]

#### **Iterators: Forward**

```
1.  // Forward Lists - support forward iterators: https://www.cplusplus.com/reference/forward_list/forward_list/
2.
3.  std::forward_list<int> flist_container {1, 2, 3, 4, 5};
4.
5.  for(auto it = flist_container.begin(); it != flist_container.end(); it++)
6.  {
7.    std::cout << *it << std::endl;
8.    std::cout << *(--it); //This line will throw an error as iterator does not support going backward
9.    std::cout << *(it + 2); //This line will throw an error as iterator does not support random access
10.    break;
11. }</pre>
```

#### **Iterators: Bidirectional**

```
1.  // Lists - support bidirectional iterators: https://www.cplusplus.com/reference/list/list/
2.  std::list<int> list_container {1, 2, 3, 4, 5};
3.
4.  for(auto it = list_container.begin(); it != list_container.end(); it++)
5.  {
6.    std::cout << *it << " ";
7.    std::cout << *(--it) << std::endl; //This line is undefined behavior
8.    //std::cout << *(it + 2); //This line will throw an error as iterator does not support random access break;
10. }</pre>
```

#### **Iterators: Random Access**

```
// Vectors - support random access iterators: https://cplusplus.com/reference/vector/vector/
2.
      std::vector<int> vector_container {1, 2, 3, 4, 5};
3.
4.
5.
      for(auto it = vector_container.begin(); it != vector_container.end(); it++)
6.
          std::cout << *it << " ";</pre>
          std::cout << *(--it) << " "; //This line is undefined behavior</pre>
8.
          std::cout << *(it + 2);</pre>
9.
10.
          break;
11.
12.
```

### Merge Two Sorted Linked Lists of Integers

### Merge Two Sorted Linked Lists of Integers

```
given ListA, ListB both sorted
create mergedList
place iterA at the head of list A, iterB at the head of list B
itemA is item iterA is pointing to and itemB is item iterB is pointing to
while iterA is not at end of ListA and iterB is not at end of ListB
         if itemA == itemB
                  make a copy of itemA and add it to mergedList
                  move iterA and iterB forward
         else if itemA < itemB
                  make a copy of itemA and add it to mergedList
                   move iterA forward
         else
                  make a copy of itemB and add it to mergedList
                  move iterB forward
```

Pseudocode:

### Merge Two Sorted Linked Lists of Integers

```
given ListA, ListB both sorted
create mergedList
place iterA at the head of list A, iterB at the head of list B
itemA is item iterA is pointing to and itemB is item iterB is pointing to
while iterA is not at end of ListA and iterB is not at end of ListB
         if itemA == itemB
                  make a copy of itemA and add it to mergedList
                  move iterA and iterB forward
         else if itemA < itemB
                  make a copy of itemA and add it to mergedList
                   move iterA forward
         else
                  make a copy of itemB and add it to mergedList
                  move iterB forward
while iterA is not at end of list
         make a copy of itemA and add it to mergedList
         move iterA forward
while iterB is not at end of list
         make a copy of itemB and add it to mergedList
         move iterB forward
```

Pseudocode:

### Merge Two Sorted Linked Lists of Integers (Union)

```
int arr1[] = {16,22,77,129};
     int arr2[] = {1,2,7,29,77,155,166};
03
     //Creating Lists from Arrays
     list<int> list1 (arr1, (arr1 + (sizeof(arr1) / sizeof(int))) );
     list<int> list2 (arr2, (arr2 + (sizeof(arr2) / sizeof(int))) );
07
     //Final Merged Sorted List
     list<int> list3;
10
     list<int>::iterator l1 = list1.begin();
12
     list<int>::iterator 12 = list2.begin();
13
     while(l1 != list1.end() && l2 != list2.end())
15
16
         if((*11) < (*12))
17
18
             list3.push_back(*11);
19
             11++;
20
21
         else
22
         if((*12) < (*11))
23
24
             list3.push_back(*12);
25
             12++;
26
27
         else
28
29
             list3.push back(*11);
30
             11++;
31
             12++;
32
33
```

```
34
35 while(l1 != list1.end())
36 {
37     list3.push_back(*l1);
38     l1++;
39  }
40
41 while(l2 != list2.end())
42 {
43     list3.push_back(*l2);
44     l2++;
45 }
46
```



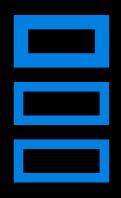
### Recommended Resources

- http://www.cplusplus.com/reference/stl/
- Linked List Questions on Stepik
- https://stackoverflow.com/questions/5384358/how-does-a-sentinel-node-offerbenefits-over-null
- OpenDSA Ch-9.1-9.7
- **Templated Singly Linked List:** <a href="https://cathyatseneca.gitbooks.io/data-structures-and-algorithms/lists/list\_declaration.html">https://cathyatseneca.gitbooks.io/data-structures-and-algorithms/lists/list\_declaration.html</a>
- https://www.cplusplus.com/reference/iterator/
- https://www.geeksforgeeks.org/input-iterators-in-cpp/
- https://onlinegdb.com/Nk9XgDjG-

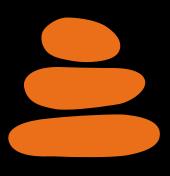
# Stacks

### Stack

Last in First Out (LIFO)







### **Stack ADT**

#### Data

- o **Items**
- Number of Items
- o Top

#### Operations

o push(item): inserts an element

o pop(): removes and returns the last inserted element

o peek(): returns the last inserted element without removing it

o size(): returns the number of elements stored

o isEmpty(): indicates whether no elements are stored

Characteristics	
Operations	
Performance	
Benefits	
Drawbacks	

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Access through top index</li> </ul>
Operations	
Performance	
Benefits	
Drawbacks	

Characteristics	<ul><li>Fixed Size</li><li>Stores Similar Elements</li><li>Access through top index</li></ul>
Operations	<pre>push(item) pop() peek() size() isEmpty()</pre>
Performance	
Benefits	
Drawbacks	

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Access through top index</li> </ul>
Operations	<pre>push(item) pop() peek() size() isEmpty()</pre>
Performance	<pre>push(item) pop() peek() size() isEmpty()</pre>
Benefits	
Drawbacks	

Characteristics	<ul><li>Fixed Size</li><li>Stores Similar Elements</li><li>Access through top index</li></ul>
Operations	<ul> <li>push(item)</li> <li>pop()</li> <li>peek()</li> <li>size()</li> <li>isEmpty()</li> </ul>
Performance	<ul> <li>push(item) - O(1)</li> <li>pop() - O(1)</li> <li>peek() - O(1)</li> <li>size() - O(1)</li> <li>isEmpty() - O(1)</li> </ul>
Benefits	
Drawbacks	

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Access through top index</li> </ul>
Operations	<pre>push(item) pop() peek() size() isEmpty()</pre>
Performance	<pre>push(item) - 0(1) pop() - 0(1) peek() - 0(1) size() - 0(1) isEmpty() - 0(1)</pre>
Benefits	■ Constant time to add and remove elements
Drawbacks	

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Operations	<pre>push(item) pop() peek() size() isEmpty()</pre>
Performance	<pre>push(item) - 0(1) pop() - 0(1) peek() - 0(1) size() - 0(1) isEmpty() - 0(1)</pre>
Benefits	■ Constant time to add and remove elements
Drawbacks	■ Fixed size and no random access

Characteristics	
Operations	
Performance	
Benefits	
Drawbacks	



Characteristics	<ul> <li>Flexible Size</li> <li>Stores Similar Elements</li> <li>Access through top pointer</li> </ul>
Operations	
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Benefits	<ul><li>Constant time to add and remove elements; Variable size</li></ul>
Drawbacks	■ More memory

### Stack in C++ STL

<b>Operations</b>	C++ STL
<pre>push(item)</pre>	<pre>push(g) - Adds the element 'g' at the top of the stack</pre>
<pre>pop()</pre>	<pre>pop() - Deletes the topmost element of the stack</pre>
<pre>peek()</pre>	■ top() - Returns a reference to the topmost element of the stack
■ size()	<pre>size() - Returns the size of the stack</pre>
<pre>isEmpty()</pre>	<ul><li>empty() - Returns whether the stack is empty</li></ul>

## Stack in C++ STL: Check Palindrome

### Stack in C++ STL: Check Palindrome

```
bool checkPalindrome(string s)
02
03
        stack<char> stk;
         int midIndex = s.length()/2;
                                                                                      Base case to return true if
05
                                                                                      string has one letter or is
        if(s.length() < 2)
                                                                                      an empty string
07
            return true;
08
                                                                                      Pushes first half of string
        for(int i = 0; i < s.length()/2; i++)
                                                                                      characters on stack
             stk.push(s.at(i));
10
11
         if(s.length() % 2 != 0)
12
                                                                                      Ignores central element if
            midIndex += 1;
13
                                                                                      the size of string is odd
14
         for(int i = midIndex; i < s.length(); i++)</pre>
15
16
                                                                                      Compare each element in the
            if(stk.top() != s.at(i))
                                                                                      second half of the string
17
                                                                                      with elements pushed in the
                return false;
                                                                                      stack
            stk.pop();
19
20
21
        return true;
22
                                                                         https://onlinegdb.com/Hy2vC3D\
```

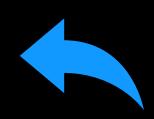
### **Stack Use Cases**

#### Real World

- Plates
- Books
- Pringle Chips







#### Computers

- Function Call Stack
- Evaluate Expressions
- Backtracking
- Balanced Parenthesis
- Undo (CTRL + Z)
- Back button



```
main()
  int i=5;
  foo(i);
     foo(int j)
        int k = j+1;
        bar(k);
           bar(int m)
```

```
main()
  int i=5;
  foo(i);
     foo(int j)
        int k = j+1;
        bar(k);
           bar(int m)
```





```
main()
  int i=5;
  foo(i);
     foo(int j)
        int k = j+1;
        bar(k);
           bar(int m)
```



```
main
PC = 2
i = 5
```



```
main()
  int i=5;
  foo(i);
     foo(int j)
        int k = j+1;
        bar(k);
          bar(int m)
```



#### bar

```
PC = 1
m = 6
```

#### foo

#### main

$$PC = 2$$

$$i = 5$$



#### Stack Use Cases: Balanced Parenthesis

#### Algorithm for method isBalanced

- 1. Create an empty stack of characters
- 2. Assume that the expression is balanced (balanced is true).
- 3. Set index to 0
- 4. while balanced is true and index < the expression's length
  - 5. Get the next character in the data string
  - 6. if the next character is an opening parenthesis
    - 7. Push it onto the stack.
  - 8. else if the next character is a closing parenthesis
    - 9. Pop the top of the stack
    - 10. if stack was empty or its top does not match the closing parenthesis 11. Set balanced to **false**
  - 12. Increment index
- 13. Return true if balanced is true and the stack is empty



### Stack Use Cases: Expression Evaluation

- Dijkstra's two-stack algorithm
  - Value: push on the value stack
  - Operator: push on the operator stack
  - Left parenthesis, (: ignore
  - Right parenthesis, ): pop operator and two values; push the result of applying that operator to the values on the value stack

### Stack Use Cases: Expression Evaluation

#### Postfix Expression: Removes Parenthesis

Postfix Expression	Infix Expression	Value	
4 7 *	4 * 7	28	
4 7 2 + *	4 * (7 + 2)	36	
4 7 * 20 -	(4 * 7) - 20	8	
3 4 7 * 2 / +	3 + ((4 * 7) / 2)	17	

### **Stack Use Cases: Postfix Evaluation**

```
1. create an empty stack of integers
 2. while there are more tokens
     get the next token
     if the first character of the token is a digit
         push the token on the stack
5.
      else if the token is an operator
         pop the right operand off the stack
7.
         pop the left operand off the stack
8.
         evaluate the operation
9.
         push the result onto the stack
10.
11. pop the stack and return the result
```



### Mentimeter

Menti.com

9733 1736





# Queues

### Queue

First in First Out (FIFO)













### **Queue ADT**

#### Data

- o **Items**
- Number of Items
- Front and Back

#### Operations

o enqueue(item): inserts an element to the back of the queue

o dequeue(): removes the element from the front

o size(): returns the number of elements stored

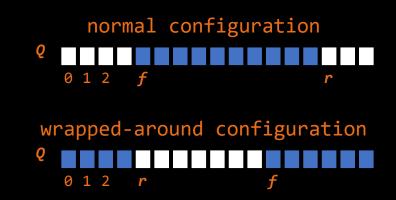
o isEmpty(): indicates whether no elements are stored

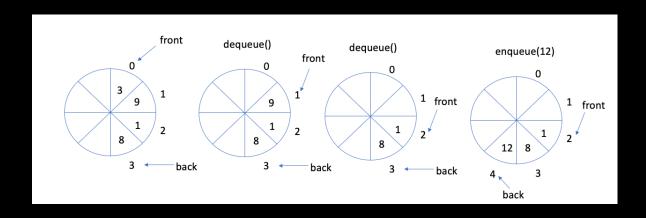
## Queue Implementation - Array

Characteristics	<ul> <li>Fixed Size</li> <li>Stores Similar Elements</li> <li>Access through front index</li> </ul>
Operations	<ul><li>enqueue(item)</li><li>dequeue()</li><li>size()</li><li>isEmpty()</li></ul>
Performance	<ul> <li>enqueue(item) - O(1)</li> <li>dequeue() - O(1)</li> <li>size() - O(1)</li> <li>isEmpty() - O(1)</li> </ul>
Benefits	■ Constant time to add and remove elements
Drawbacks	<ul><li>Limited space</li><li>Rightward drift problem</li></ul>

### Queue Implementation - Circular Array

```
Use an array of size {\it N} in a circular fashion Two variables keep track of the front and rear {\it f} index of the front element {\it r} index immediately past the rear element Array location {\it r} is kept empty
```





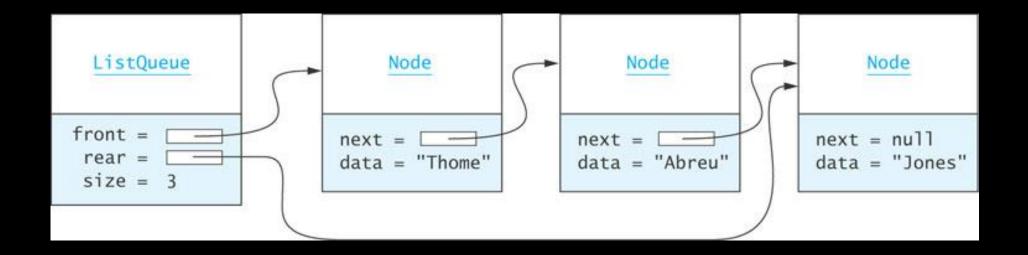
https://stepik.org/lesson/354738/step/1?unit=338782



## Queue Implementation - Circular Array

Characteristics	<ul><li>Fixed Size</li><li>Stores Similar Elements</li><li>Access through front index</li></ul>
Operations	<ul><li>enqueue(item)</li><li>dequeue()</li><li>size()</li><li>isEmpty()</li></ul>
Performance	<ul> <li>enqueue(item) - 0(1)</li> <li>dequeue() - 0(1)</li> <li>size() - 0(1)</li> <li>isEmpty() - 0(1)</li> </ul>
Benefits	■ Constant time to add and remove elements
Drawbacks	■ Limited space

## Queue Implementation - Linked List



## **Queue Implementation - Linked List**

Characteristics	<ul> <li>Flexible Size</li> <li>Stores Similar Elements</li> <li>Access through front pointer</li> </ul>
Operations	<ul><li>enqueue(item)</li><li>dequeue()</li><li>size()</li><li>isEmpty()</li></ul>
Performance	<ul> <li>enqueue(item) - O(1)</li> <li>dequeue() - O(1)</li> <li>size() - O(1)</li> <li>isEmpty() - O(1)</li> </ul>
Benefits	■ Constant time to add and remove elements; Variable size
Drawbacks	■ More memory

### **Queue in C++ STL**

<b>Operations</b>	C++ STL
<ul><li>enqueue(item)</li><li>dequeue()</li><li>size()</li><li>isEmpty()</li></ul>	<ul> <li>push(g) - Adds the element 'g' at the end of the queue</li> <li>pop() - Deletes the first element of the queue</li> <li>size() - Returns the size of the queue</li> <li>empty() - Returns whether the queue is empty</li> <li>front() - Returns a reference to the first element of the queue</li> <li>back() - Returns a reference to the last element of the queue</li> </ul>

### **Queue Use Cases**

- Real World
  - Buying Tickets
  - Drive thru at fast food chains
  - Appointments



- Print Queue
- Task Scheduling by OS
- Packet Forwarding by Routers



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Printer Document View Help			7	-		-
Document Name	Status	Owner	Pages	Size	Submitted	F
Microsoft Word - Queues_Paul_100	7.doc	Paul Wolfgang	52	9.75 MB	1:53:18 PM 10/7/2003	
Microsoft Word - Stacks.doc		Paul Wolfgang	46	9.05 MB	1:53:57 PM 10/7/2003	
Microsoft Word - Trees2.doc		Paul Wolfgang	54	38.4 MB	1:54:41 PM 10/7/2003	
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### **Recommended Resources**

- http://www.cplusplus.com/reference/stl/
- Stacks and Queue Questions on Stepik
- OpenDSA Ch-9.8-9.14