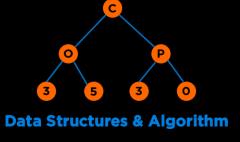
Final Exam Review



Categories of Data Structures

Linear Ordered

Non-linear Ordered

Not Ordered

Lists

Trees

Sets

Stacks

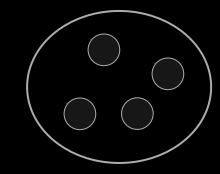
Graphs

Tables/Maps

Queues



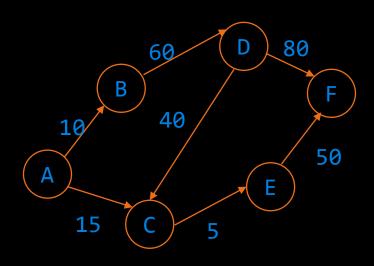




Announcements

- You must take the exam between:
 - 6pm 11:59pm EST on July 26 [All students except UFOL/UDER]
 - 6pm July 26 to 11:59 pm July 26 [UFOL/UDER students]
- The exam will be over Honorlock and you are allowed one double sided handwritten sheet of notes.
- The exam duration is 2 hours. This means you must start by 10 pm EST or else you will lose time.
- Exam 2 Topics and Expectations Guide: Link
- Exam reviews: Exam 2 Resources

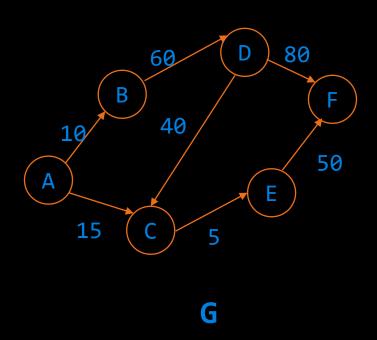
Common Representations



- Edge List
- Adjacency Matrix
- Adjacency List

G

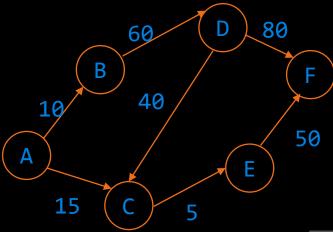
Edge List



Α	В	10
Α	С	15
В	D	60
D	С	40
D	F	80
Е	F	50
С	Е	5

 $G = \{(A,B), (A,C), (B,D), (D,C), (D,F), (E,F), (C,E)\}$

Edge List



G

Α	В	10
Α	С	15
В	D	60
D	С	40
D	F	80
Е	F	50
С	Е	5

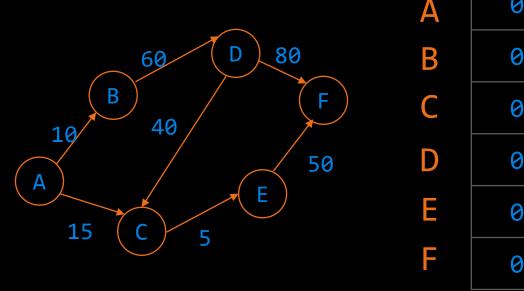
Common Operations:

1. Connectedness

2. Adjacency

Space: O(E)

Adjacency Matrix

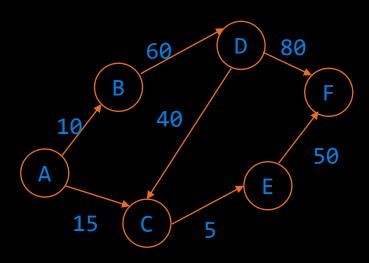


A	В	C	D	E	F
0	10	15	0	0	0
0	0	0	60	0	0
0	0	0	0	5	0
0	0	40	0	0	80
0	0	0	0	0	50
0	0	0	0	0	0

Insertion:

```
G[from][to] = weight; (if there is an edge, "from" -> "to")
G[from][to] = 0; (otherwise)
```

Adjacency Matrix Implementation



Input				
7				
Д	В	10		
Д	C	1 5		
В	D	60		
D	C	40		
C	Е	5		
D	F	80		
	Е	ГΩ		

		0	1	2	3	4	5
Map 0	0	0	10	15	0	0	0
A 0	1	0	0	0	60	0	0
B 1 C 2	2	0	0	0	0	5	0
D 3	3	0	0	40	0	0	80
E 4	4	0	0	0	0	0	50
F 5	5	0	0	0	0	0	0

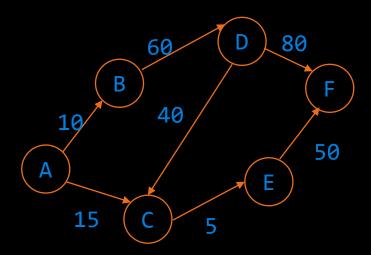
Insertion:

```
G[from][to] = weight; (if there is an edge, "from" -> "to")
G[from][to] = 0; (otherwise)
```

```
#include <iostream>
    #include<map>
    #define VERTICES 6
    using namespace std;
    int main()
06
           int no lines, wt, j=0;
           string from, to;
           int graph [VERTICES][VERTICES] = {0};
10
           map<string, int> mapper;
           cin >> no lines;
11
12
           for(int i = 0; i < no lines; i++)</pre>
13
                 cin >> from >> to >> wt;
14
                 if (mapper.find(from) == mapper.end())
15
                        mapper[from] = j++;
                 if (mapper.find(to) == mapper.end())
                        mapper[to] = j++;
                 graph[mapper[from]][mapper[to]] = wt;
19
20
21
           return 0;
```

https://www.onlinegdb.com/Hy8M0CnsS

Adjacency Matrix



G

Ma	ар
Α	0
В	1
C	2
D	3
Е	4
F	5

 0
 1
 2
 3
 4
 5

 0
 0
 10
 15
 0
 0
 0

 1
 0
 0
 0
 60
 0
 0

 2
 0
 0
 0
 0
 5
 0

 3
 0
 0
 40
 0
 0
 80

 4
 0
 0
 0
 0
 0
 0

 5
 0
 0
 0
 0
 0
 0

Common Operations:

Connectedness

```
Is A connected to B?
G["A"]["B"] ~ O(1)
```

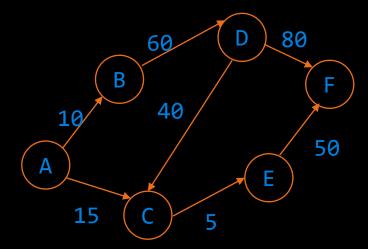
2. Adjacency

What are A's adjacent nodes?
for each element x in G["A"]
 if x ! = 0

~ O(|V|)

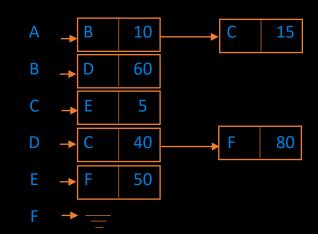
Space: **0(|V| * |V|)**

Adjacency List



G

Sparse Graph:
Edges ~ Vertices



Common Operations:

Connectedness

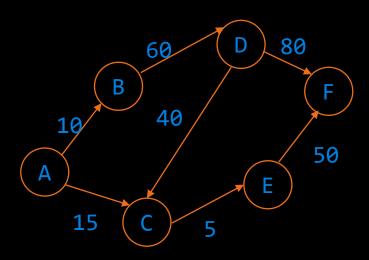
```
Is A connected to B?
for each element x in G["A"]
   if x ! = 'B'
        ~ O(outdegree|V|)
```

2. Adjacency

```
What are A's adjacent nodes?

G["A"] ~ O(outdegree|V|)
```

Adjacency List Implementation

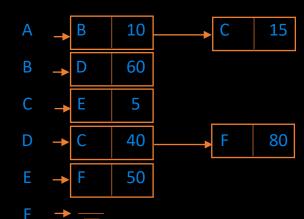


Input

7
A B 10
A C 15
B D 60
D C 40
C E 5
D F 80

E F 50

G



Insertion:

If to or from vertex not present add vertex Otherwise add edge at the end of the list

```
#include <iostream>
    #include<map>
    #include<vector>
    #include<iterator>
    using namespace std;
07
    int main()
           int no lines;
           string from, to, wt;
           map<string, vector<pair<string,int>>> graph;
11
           cin >> no_lines;
12
           for(int i = 0; i < no lines; i++)</pre>
13
14
15
                 cin >> from >> to >> wt;
                 graph[from].push back(make pair(to, stoi(wt)));
16
17
                 if (graph.find(to)==graph.end())
18
                        graph[to] = {};
19
20
```

https://onlinegdb.com/HkJq9iFaI

Graph Implementation

	Edge List	Adjacency Matrix	Adjacency List
Time Complexity: Connectedness	O(E)	0(1)	O(outdegree(V))
Time Complexity: Adjacency	O(E)	0(V)	O(outdegree(V))
Space Complexity	O(E)	0(V*V)	O(V+E)



Alt Text for the Graph on Next Slide

Vertex: Neighbors of Vertex (Edges pointing from a vertex to the neighbor)

A: B, E, F

B: A, C, F, H

C: B, D, F, G, H, I

D: C, E, F, G

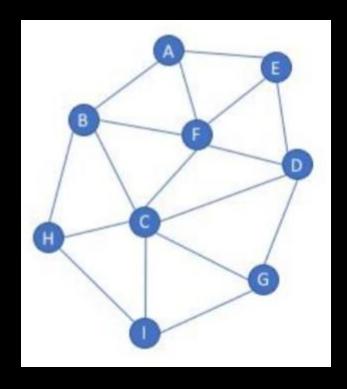
E: A, D, F

F: A, B, C, D, E

G: C, D, I

H: B, C, I

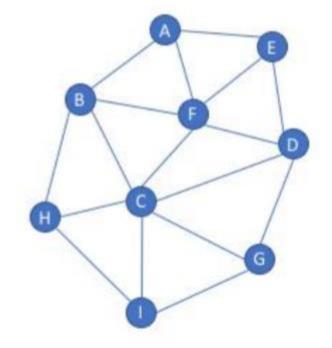
I: C, G, H





Graph - BFS

- Which of the following are valid breadth first search traversals for this graph?
- a) AFBEDCHGI
- b) ICHGBFDAE
- c) DCFEGHIBA
- d) EAFDBHCIG
- e) FAEDCBGIH





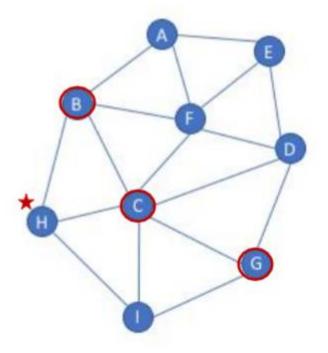
Graph - BFS

- Which of the following are valid breadth first search traversals for this graph?
- a) AFBEDCHGI
- b) ICHGBFDAE
- c) DCFEGHIBA
- d) EAFDBHCIG
- e) FAEDCBGIH

All the options except for d

Why not d?







Alt Text for the Graph on Next Slide

Vertex: Neighbors of Vertex (Edges pointing from a vertex to the neighbor)

A: F, I

B: C, H

C: B, E, F

D: E, G

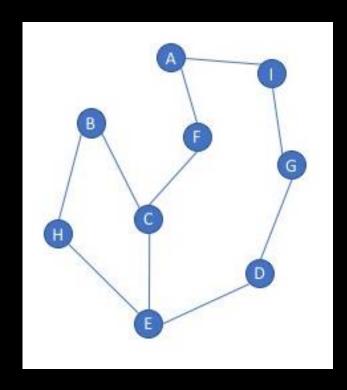
E: C, D, H

F: A, C

G: D, I

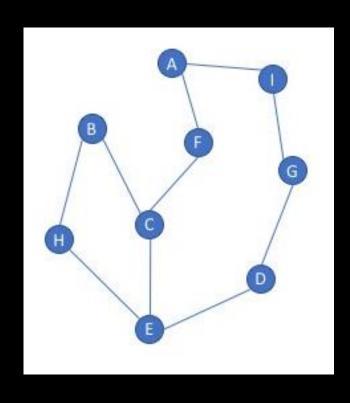
H: B, E

I: A, G





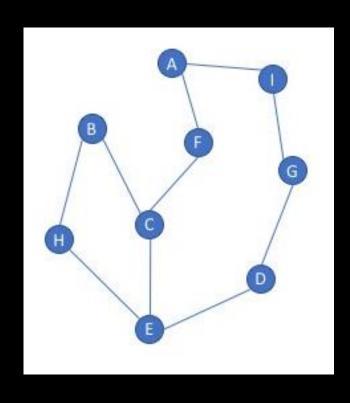
Valid DFS: Which DFS are valid?



- HECBDGIAF
- CEHBDGIAF
- AFCEHBIGD
- DECBHFAIG



Valid DFS: Which DFS are valid?



- HECBDGIAF
- CEHBDGIAF
- AFCEHBIGD
- DECBHFAIG



Applied Traversal

A connected component of a graph is a collection of vertices in which any two vertices in a component have a path between them. Given an unweighted and undirected graph represented as an adjacency list, write a function using pseudocode or C++ code which will return the number of vertices in the largest component of the graph. You do not need to write main method for reading and creating a graph. Assume that the graph is passed into your function which has the following signature:

```
unsigned int largest component(unordered map<int, vector<int>>& adjListGraph){
        // code here
Example input:
1: 4
2: 0, 6
3: 0
4: 1, 5
5: 4
Example output: 4
Explanation: There are three connected components: (0,2,3,6); (1,4,5); and (7). Of these, the largest has 4
vertices.
Also, state the Big O complexity of the solution in the worst case.
```



Applied Traversal

```
#include <unordered map>
#include <vector>
#include <unordered_set>
using namespace std;
unsigned int dfs(int node, unordered_map<int, vector<int>>& adjListGraph, unordered_set<int>& visited) {
   visited.insert(node);
   unsigned int size = 1; // Start with the current node
   for (int neighbor : adjListGraph[node]) {
       if (visited.find(neighbor) == visited.end()) {
           size += dfs(neighbor, adjListGraph, visited);
    return size;
unsigned int largest_component(unordered_map<int, vector<int>>& adjListGraph) {
   unordered set<int> visited;
   unsigned int maxComponentSize = 0;
   for (const auto entry : adjListGraph) {
       int node = entry.first;
       if (visited.find(node) == visited.end()) {
           unsigned int componentSize = dfs(node, adjListGraph, visited);
            if (componentSize > maxComponentSize) {
               maxComponentSize = componentSize;
   return maxComponentSize;
```



```
string source = "A";
    std::set<string> visited;
03
    std::queue<string> q;
04
    visited.insert(source);
05
    q.push(source);
06
07
    cout<<"BFS: ";</pre>
08
09
    while(!q.empty())
10
          string u = q.front();
11
12
          cout << u;
13
          q.pop();
14
          vector<string> neighbors = graph[u];
15
          for(string v: neighbors)
16
17
18
19
                      visited.insert(v);
20
                      q.push(v);
21
22
23
```

```
string source = "A";
    std::set<string> visited;
    std::stack<string> s;
04
    visited.insert(source);
    s.push(source);
07
    cout<<"DFS: ";</pre>
08
    while(!q.empty())
10
          string u = s.top();
11
12
          cout << u;
13
          s.pop();
          vector<string> neighbors = graph[u];
14
15
          for(string v: neighbors)
16
17
                if(visited.count(v)==0)
18
                       visited.insert(v);
19
20
                      s.push(v);
21
22
23
```



BFS Pseudocode

- Write pseudocode/code for implementing the Breadth First Search Algorithm of a graph, G that takes a source vertex S as input. (8).
- Also, state the Big O complexity of the traversal in the worst case (2).



Graph Algorithm Mix n Match

- Finds the shortest paths in a weighted graph
- Find the minimum cost connected network
- Scheduling algorithm, list steps in a process
- Finds the shortest path in an unweighted graph

Prim's or Kruskals

BFS

DFS

Topological Sort Dijkstra's Algorithm



Graph Algorithm Mix n Match

Finds the shortest paths in a weighted graph
 Find the minimum cost connected network
 Scheduling algorithm, list steps in a process
 Finds the shortest path in an unweighted graph
 DFS
 Topological Sort
 Dijkstra's Algorithm



Alt Text for the Graph on Next Slide

Vertex: Neighbors of Vertex (Edges pointing from a vertex to the neighbor)

A: -

B: C, E

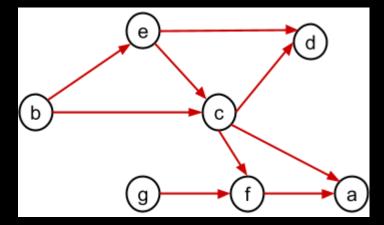
C: A, D, F

D: -

E: C, D

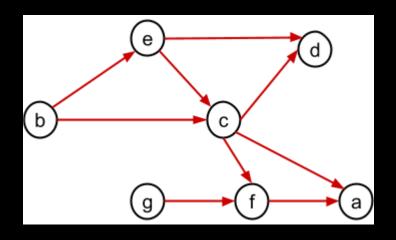
F: A

G: F





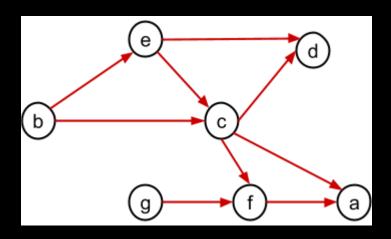
Which of the choices below represent a valid topological sort ordering of this graph?



- b, e, c, g, f, a, d
- b, a, c, g, f, e, d
- b, g, f, c, e, a, d
- b, e, c, g, a, f, d
- b, g, e, c, d, f, a
- b, f, c, g, a, e, d



Which of the choices below represent a valid topological sort ordering of this graph?



- b, e, c, g, f, a, d
- b, a, c, g, f, e, d
- b, g, f, c, e, a, d
- b, e, c, g, a, f, d
- b, g, e, c, d, f, a
- b, f, c, g, a, e, d



What does this code do?

```
#include <set>
#include <stack>
using namespace std;
bool doSomething(const Graph& graph, int src, int dest)
    set<int> visited;
    stack<int> s;
    visited.insert(src);
    s.push(src);
    while(!s.empty())
        int u = s.top();
        s.pop();
        for(auto v: graph.adjList[u])
            if(v == dest)
                return true;
            if ((visited.find(v) == visited.end())) {
                visited.insert(v);
                s.push(v);
    return false;
```



What does this code do?

```
#include <set>
#include <stack>
using namespace std;
bool doSomething(const Graph& graph, int src, int dest)
    set<int> visited;
    stack<int> s;
    visited.insert(src);
    s.push(src);
    while(!s.empty())
        int u = s.top();
        s.pop();
        for(auto v: graph.adjList[u])
            if(v == dest)
                return true;
            if ((visited.find(v) == visited.end())) {
                visited.insert(v);
                s.push(v);
   return false;
```

Returns whether a given vertex is reachable from another vertex using DFS



Scenario

A county government maintains a network of roads. The county government has tabulated the cost of maintaining each road. They need to minimize the cost of road maintenance but ensure that all places in the county are accessible.

Which graph algorithm that we discussed in class could they use to solve this problem? What are the vertices, what are the edges, what are the edge values?



Scenario

A county government maintains a network of roads. The county government has tabulated the cost of maintaining each road. They need to minimize the cost of road maintenance but ensure that all places in the county are accessible.

Which graph algorithm that we discussed in class could they use to solve this problem? What are the vertices, what are the edges, what are the edge values?

- Prim's or Kruskals algorithm for minimum spanning tree.
- Roads are edges.
- Ends of roads are vertices.
- Edge weights are cost for maintaining roads.



Alt Text for the Graph on Next Slide

Vertex: <Neighbors of Vertex (Edges pointing from a vertex to the neighbor), edge weight>

A: <B, 4>, <E, 2>, <F, 9>

B: <A, 4>, <C, 11>, <F, 1>, <H, 12>

C: <B, 11>, <D, 7>, <F, 10>, <G, 15>, <H, 14>, <I, 17>

D: <C, 5>, <E, 7>, <F, 16>, <G, 3>

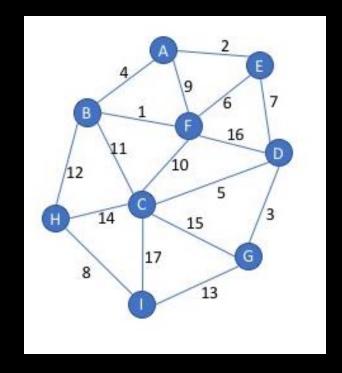
E: <A, 2>, <D, 7>, <F, 6>

F: <A, 9>, <B, 1>, <C, 10>, <D, 16>, <E, 6>

G: <C, 15>, <D, 3>, <I, 13>

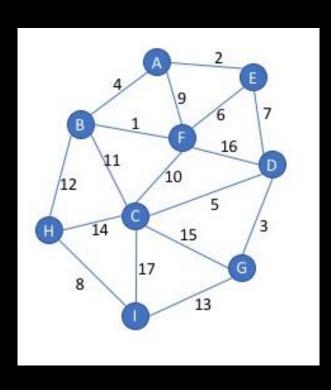
H: <B, 12>, <C, 14>, <I, 8>

I: <C, 17>, <G, 13>, <H, 8>

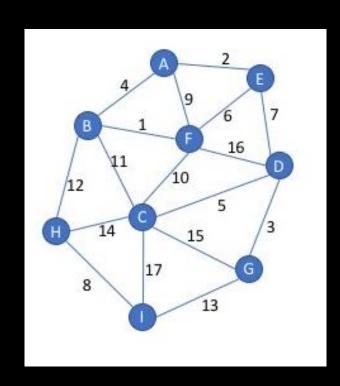




MST using Prims starting from "I"



MST using Prims starting from "I"



IHBFAEDGC



Alt Text for the Graph on Next Slide

Vertex: <Neighbors of Vertex (Edges pointing from a vertex to the neighbor), edge weight>

A: <B, 1>, <D, 3>, <F, 2>

B: <A, 1>, <C, 2>, <D, 1>, <E, 7>

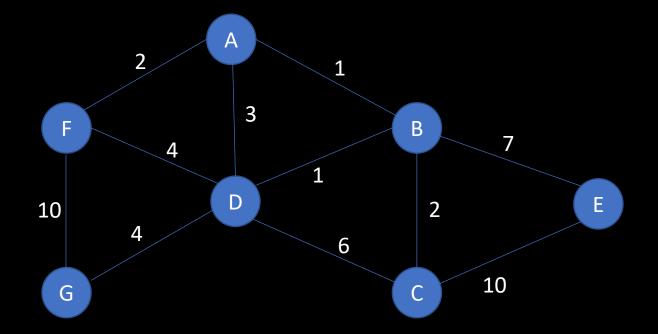
C: <B, 2>, <D, 6>, <E, 10>

D: <A, 3>, <B, 1>, <C, 6>, <F, 4>, <G, 4>

E: <B, 7>, <C, 10>

F: <A, 2>, <D, 4>, <G, 10>

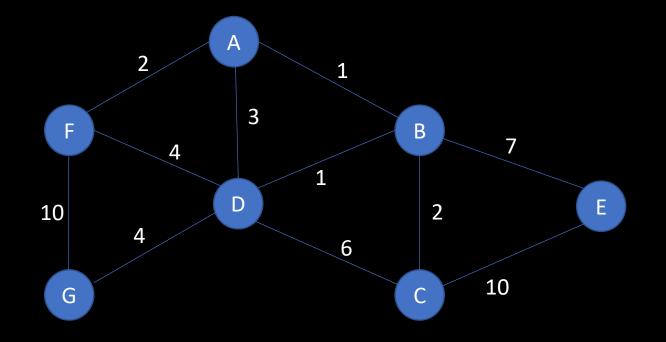
G: <D, 4>, <F, 10>





Dijkstra with A as source

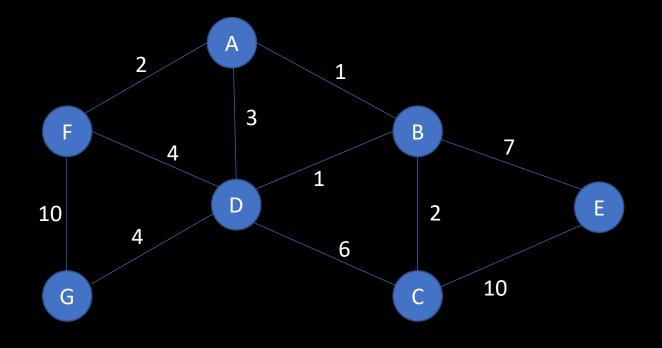
V	D(v)	P(v)
Α		
В		
С		
D		
Е		
F		
G		





Dijkstra with A as source

V	D(v)	P(v)
Α	0	NA
В	1	А
С	3	В
D	2	В
Е	8	В
F	2	А
G	6	D





Alt Text for the Graph on Next Slide

Vertex: <Neighbors of Vertex (Edges pointing from a vertex to the neighbor), edge weight>

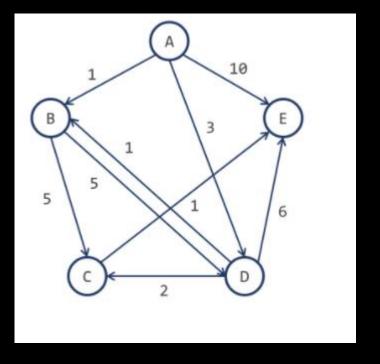
A: <B, 1>, <D, 3>, <E, 10>

B: <C, 5>, <D, 5>

C: <E, 1>

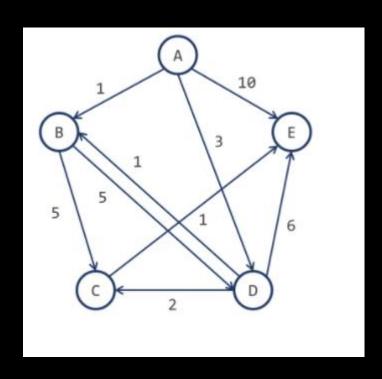
D: <B, 1>, <C, 2>, <E, 6>

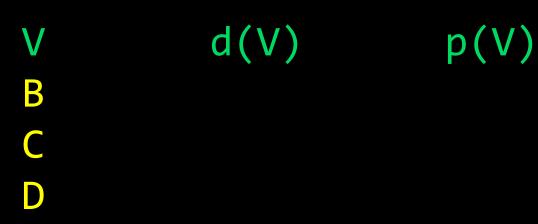
E: -





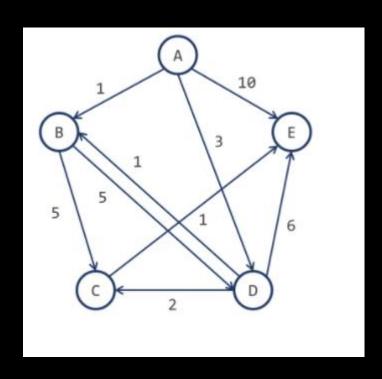
Dijkstra with A as source







Dijkstra with A as source



V	d(V)	p(V)
B	1	A
C	5	D
D	3	A
E	6	C



Questions

