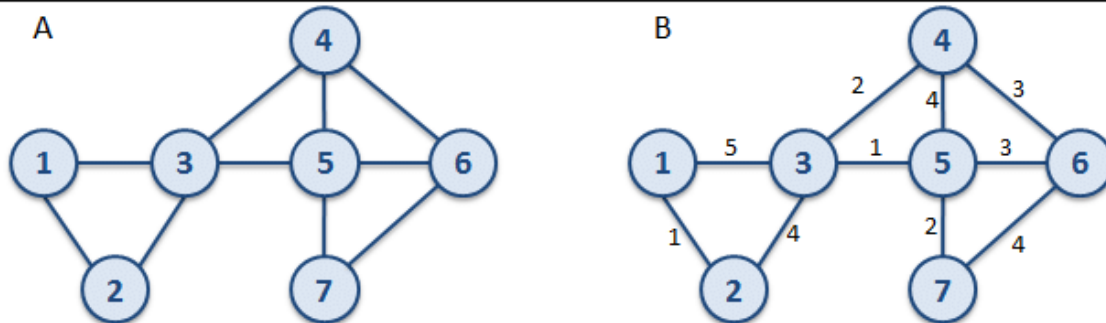


### TAD Graph

Graph =  $\{V = \{v_1, v_2, \dots, v_n\}, E = \{e_1 = (v_{i1}, v_{j1}, w_1), e_2 = (v_{i2}, v_{j2}, w_2), e_m = (v_{im}, v_{jm}, w_m)\}, \text{directed, weighted}\}$



{inv:

1.  $\forall e_k \in E, v_{ik} \in V \wedge v_{jk} \in V, w_k > 0$
2.  $\text{directed} = \text{false} \Rightarrow (\forall (a, b) \in E \exists (b, a) \in E, a, b \in V)$
3.  $\text{weighted} = \text{false} \Rightarrow \forall e_k \in E, w_k = 1$

}

### Primitive Operations

- Graph  $\langle \rangle \rightarrow \langle \text{Graph} \rangle$  Constructor
- addVertex  $\langle \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Modifier
- addEdge  $\langle \text{Vertex}, \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Modifier
- addEdge  $\langle \text{Vertex}, \text{Vertex}, \text{double} \rangle \rightarrow \langle \text{Graph} \rangle$  Modifier
- removeVertex  $\langle \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Modifier
- removeEdge  $\langle \text{Vertex}, \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Modifier
- getNumberOfVertices  $\langle \rangle \rightarrow \langle \text{Integer} \rangle$  Analyzer
- getNumberOfEdges  $\langle \rangle \rightarrow \langle \text{Integer} \rangle$  Analyzer
- areAdjacent  $\langle \text{Vertex}, \text{Vertex} \rangle \rightarrow \langle \text{boolean} \rangle$  Analyzer
- searchInGraph  $\langle T \rangle \rightarrow \langle \text{boolean} \rangle$  Analyzer
- getVertex  $\langle \text{Graph} \rangle \rightarrow \text{List} \langle \text{Vertex} \rangle$  Analyzer
- isDirected  $\langle \rangle \rightarrow \langle \text{boolean} \rangle$  Analyzer
- isWeighted  $\langle \rangle \rightarrow \langle \text{boolean} \rangle$  Analyzer
- bfs  $\langle \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Analyzer
- dfs  $\langle \rangle \rightarrow \langle \text{Graph} \rangle$  Analyzer
- dijkstra  $\langle \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Analyzer
- floyd-warshall  $\langle \rangle \rightarrow \langle \text{Double}[][] \rangle$  Analyzer
- prim  $\langle \text{Vertex} \rangle \rightarrow \langle \text{Graph} \rangle$  Analyzer
- kruskal  $\langle \rangle \rightarrow \langle \text{Graph} \rangle$  Analyzer

## Operations

Graph (boolean directed, boolean weighted, int n)
Create a new graph that may or may not be directed or weighted.
{pre: }
{post: Graph = {V={}, E={}, directed, weighted }

addVertex (Vertex v)
Insert a vertex in the graph.
{pre: $v \notin g.V$ }
{post: $v \in g.V$ }

addEdge (Vertex v1, Vertex v2)
Add an edge of weight 1 that goes from v1 to v2. If the graph is not directed, it also adds it from v2 to v1.
{pre: $v1, v2 \in g.V$ }
{post: edge = (v1, v2, 1) $\in$ g.E. If g.directed = false, edge = (v2, v1, 1) $\in$ g.E }

addEdge (Vertex v1, Vertex v2, double weight)
Add an edge of weight 1 that goes from v1 to v2. If the graph is not directed, it also adds it from v2 to v1.
{pre: v1, v2 ∈ g.V, g.weight = true, w > 0}
{post: edge = (v1, v2, weight) ∈ g.E. If g.directed = false, edge = (v2, v1, weight) ∈ g.E }

removeVertex (Vertex v)
Eliminate v from the graph
{pre: v ∈ g.V }
{post: v ∉ g.V. All vertices that are incidents with v ∉ g.E }

removeEdge (Vertex v1, Vertex v2)
Eliminate the edge that goes from v1 to v2 in the graph
{pre: v1, v2 ∈ g.V, (v1,v2,w) ∈ g.E }
{post: edge= (v1,v2,w) ∉ g.E. If g.directed = false, e' = (v2,v1, w) ∉ g.E }

getNumVertex ()
Returns the number of vertices in the graph
{pre: }
{post: number of vertices}

getNumEdges ()
Returns the number of edges in the graph.
{pre: }
{post: number of edges}

searchInGraph (T value)
Returns if there is a vertex with the given value in the graph.
{pre: }
{post: true if $\exists x \in g.V : \text{value}$

idDirected ()
Returns if the graph is directed
{pre: }
{post: true if is directed, false otherwise}

isWeighted()

Returns if the graph is weighted.

{pre:}

{post: true if is directed, false otherwise}

areAdjacent (Vertex v1, Vertex v2)

Returns if there is an edge from x to y

{pre:  $v1, v2 \in g.V$  }

{post: true if  $(v1, v2, w) \in g.E.$  }

dijkstra (Vertex v)

Carry out the Dijkstra algorithm, taking v as the initial vertex

{pre:  $v \in g.V, g$  }

{post:  $\forall v \in g.V$ , adds attributes v.pred and v.d, corresponding respectively to the predecessor and the distance added by Dijkstra's algorithm}

bfs(Vertex v)

Performs the Breadth First Search algorithm, adjusting information for the vertices of the graph.

{pre v  $\in$  g.V, g:}

{post:  $\forall v \in$  g.V, adds attributes v.pred and v.d, which correspond to those added by the Breadth First Search algorithm}

dfs ()

Performs the Depth First Search algorithm, adjusting information for the vertices of the graph

{pre: }

{post:  
 $\forall v \in$  g.V, adds attributes v.pred, v.d and v.f, which correspond to those added by the Depth First Search algorithm}

floyd-warshall ()

Perform the Floyd-Warshall algorithm on graph.

{pre: }

{post: Returns the dist matrix, where position [i, j] represents the minimum distance to go from vertex  $v_i$  to  $v_j$  }

kruskal ()

Perform Kruskal's algorithm on the graph.

{pre: }

{post:  
{e1, e2,..., en}, where  $e_i \in g.E$  are the edges that belong to the MST formed by Kruskal }

prime (Vertex v)

Perform Prim's algorithm taking r as the root of the tree, adjusting information for the vertices of the graph.

{pre:  $v \in g.V$ , g is not directed }

{post:  $\forall v \in g.V$ , adds attributes v.pred and v.d, which correspond respectively to the predecessor and the key added by Prim's algorithm }