चौधरी PHOTOSTAT

"I don't love studying. I hate studying. I like learning. Learning is beautiful."



"An investment in knowledge pays the best interest."

Hi, My Name is

Mathematical Science for CSIR NET Dips Academy

Unit-I:
1- Complex Number System

2- Functions of complex Variables (w=f(z))

3. Limit, Continuity, Differentiability [L,C,D)

of w=f(z).

4. Analyticity and its proporties

5. Singularities

Unit-II:
Complex Integration:
1- Fundamental of complem integration

(curve of Definition of complex integration)

2. Theorems on complex integration

3-C.I.F., C.I.F.D., C.I.F.H.D.

(cauchy Integral Formula), [Cauchy Integral formula

for Défivative!, (cauchy Integral Formula for Higher Desivative)

4 - tioville Liouville's Theorem and its application

Unit - III :Levies and Expansions:,-

1 - Power series *

2 - Taylor seales

3 - Laurent 1s expension or, Laurent's series

4- Application of Laurentis and Taglosis expansion (a) Zeros of analytic funct ⁿ (b) Entension of Lioville's theorem (c) Singularities re-visited (d) Residue at Z=a: Res[f(z),a]
Unil-IV Special Types of Functins 1. Meromorphic functin / Retional functin
2. Argument Theorem / Argument Fun (+1) 3. Rouchels Theorem *
Uni-l-V Conformel mepping 1. Fundamental of Conformality 2. Bilines / Modrous Transformation 4. Linear Fractional Transformation 3. Maximum / Minimum Modulus Principle 3. Schwarz's lummer and its application.

Complex Number System

Dale 06/11/2019

 $++ \qquad \chi_{+1} = 0$ $\chi_{L-1} = 0$

 $M^2-2=0$ J_1

 $2^2+1 \qquad \qquad \dot{z}=\sqrt{-1}$

Then, we have,

called the complex number system

It For every complex no. Z=x+i'y

there is unique (x,y) = TP2, denoting the

position of Z.

1/2

i.e, at every pt. of the cartesian plane into

It When in the Earlespan plane

He When act any point in the Cartesian plane we obtain a complex normber, the plane is called Complex-plane or Agand-plane or,

PLR, オノ~ Z=ルインナ 00, 7- planc.

#

2= 8 (0) 0, 1 4 = 8 sin 0

thin Z = K+i'y has equivalent from (7,0) called poler from of Z= K+iy.

(8,0) C TD2

Mode: - Z=O+io hes no-boler form. (:: x=0)

N' # Principal Argument of Z (Arg 2):-

ArgZ = Principal Argument $= \theta \in (-\pi, \pi]$

Let Z= Niy + D; X = D

f d = tan -1/2 =7 $0 \leq d \leq \frac{\pi}{3}$

$$\begin{array}{c|c}
0 = \frac{\pi}{2} \\
0 = -\pi
\end{array}$$

$$0 = -\pi$$

$$0 = -\pi$$

$$Z = -1 + 4i$$

$$-1 + and = |\frac{4}{-1}| = yd = -1 + an - 1(4)$$

$$-180' - 76'$$

$$= 104'$$

$$arg Z = \{Arg Z + 2nx : n \in \mathcal{I}\}$$

$|Z| = Absolute value of Z$

$$= \int \frac{\chi^2 + \chi^2}{\chi^2} = \chi$$

$$= \int \frac{\chi^2 + \chi^2}{\chi^2} = \chi$$

$$\int \frac{\chi^2}{\chi^2} = \chi^2 = \chi^2$$

$$\int \frac{\chi^2}{\chi^2} = \chi^2$$

Mode: log(Z,Z) may not be logZ, +logZL. id a, b e ¢ at may have more than one values. Principal value of ab = ebloga = pb. LP. V. of logal eg: Find principal value of (1+i)t P. V. of (1+i) = eilog(1+i) = eillog52 + i至) = e-7 + ilojs = e-4. e ilogs = e 7 cos (log sel + i e 7 sinlogs :. Re[P.V. of (1+i)] = e-4. co, log 52. Eip.v. of ii = eilogi = e iliz =logi. =log1+ix = 6-3 = - 7/2

S. John

Mote!-

e.1'

$$log Z_1 + log Z_2 = log x_1 x_2 + i \left(\frac{1}{2}x - \frac{x}{2} \right)$$

$$log Z_1 + log Z_2 = log x_1 x_2 + i \left(\frac{1}{2}x - \frac{x}{2} \right)$$

Mote!

$$e^{Z} = e^{\kappa \cdot iy}$$

$$= e^{\kappa} \cdot e^{iy}$$

$$= e^{\kappa} \cdot cojy + ie^{\kappa} siny$$

$$Re e^{Z} = e^{\kappa} cojy$$

$$Im e^{Z} = e^{\kappa} siny$$

Inder: -

- 1. Vector 5 paces and Sub-Spaces (Fundamental)
- 2. Spanning (Generation) of Vector-Spaces
- 3. Bases and Dimensions:
- 4. More on Subspaces

 * Direct Sum

 * Juotient Spaces
- 5. Homo-morphism / Linear Transformation
- 6. Linear Algebra (i.e., Linear Operator- and Algebra)
- 7. Matrin of Linea Transformation
- 8. Basic Properties of Madrices
- 9. System of Linear Equations
- 10. Eigen Values and Eigen Vectors of a L.D.
- 11. Diagonalisation of Matrices
- 12. Joseln Canonical Form
- 13. Juadratic Form
- 14. Inner Product 5 paces
- 15. Linear Functionals
- 16. Appendix

• . • C € - .

Vector Speces and Sub-Spaces!.

External Composition

Let f: AXB --- C

adopt * for fle, 1 = a*b Ha, b) = AXB

i.e, if fleib) = C

Me mai de

ax6= c

* is called an external composition. (NW ARB

if A=B=C => * is Binary Operation

or, internel composition.

13 = R[x] - 10}

A = 9

٦

,

C= MUlol

define f: AXB ---> C

f(d, p(x)) = deg (d. p(x))

..... f: 7xy* --- y*

f (d, a) = ed

d * a = ad

```
Vector Space!
    Let (V, +) be an abelian group L+ is a notation
for the binery operation on V)
    e.g. V= ] I, (12], (34), (12)(34)]
       (V, +)
      (12) + U2) = I
  f(F,+,·) be a field.
   define FXV --- V
     an externel composition,
         deF, XeV
        d \cdot X = f(d \cdot X) \in V
   then V forms vector space over F.
  if (i) \d, B EF, X EV
       (d+ p). X = d. X + p. X
   (ii) HdeF, X, YEV
   d.(X+Y)= d.X+d.Y
  - (iii) Hair GF, XEV
       (d \cdot \beta) \cdot X = d \cdot (\beta \cdot X)
   (iv) 1 EF, XEV, 1 is unity of F
```

1.1.X = X.

II The elements of V are called vectors and that of Fare scalars, we may also think in this way, the elements of V are objects and that of Fare multiples.

II The identity of (V, +) will be referred as zero vector and denoted by \overline{O} .

And $D \in F$ is called D' scalar.

It Scalars are always just kept on the left of vectors.

(i) O.X = D + X EV, DEF

(ii) c.D = D + CEF; -1 is the additive

(iii) (-11.X = -X, -1 EF; -1 is the additive

inverse of remity.

 $\begin{aligned} & (V, +) = (\mathbb{P}^+, \cdot) \\ & (F, +, \cdot) = (\mathbb{R}, +, \cdot) \\ & (F, +, \cdot) = (\mathbb{R} \times +, \cdot)$

V is a vector space over R.

Let VI+1 de an abelian. (+ is the notation for the B.D. on V) & (F, +, .) de a field. if f: #XV --- V 3.d. f (d, x) = d. X then V forms V.S. over F. 4 (i) (d+ p). X = d. X + p. X (ii) $q \cdot (X + A) = q \cdot X + q \cdot A$ Hid, BEF (iii) (d.b). X = d.(p.X) b X, Y EV (iv) 1. X = X $\underbrace{e.g.}^{+}(V,+)=(\mathbb{R}^{+},\cdot)$ F-R J: FXV -- $t[q,X] = X_q$ Here, (pt,) is an abelian of pis a field (i) (d+B).X = Xd+B... 'd. X + B. Y = X d. XB = X d. B :. (d+)).X = d.X+ 3.X d. (x+ y) = (x+ y)d $= (X \cdot Y)^{d} = X^{d} \cdot Y^{d}$

W.

C

[iii] (d. p) X = X dap : d. [B.X] = d. XB = (X +)7 = X px = X dp (iv) 1. X = X = X Let (R,+,.) be a ring then if $V=R \Rightarrow (V, +)$ is an Abelian group. Let F < R 5. d. F is a field. define f: FXV - V as $f(d, X) = d \cdot X$ wher ', 1 is that of (p,+,.) f is well defined as d, X & R. as \ d, | B \ F | X, Y \ E V => d, B, X, Y \ P and (P, +,.) is sing => (i) ~ (d+B).x=d.x+B.x (ii) d. (x+Y) = d.x+d.Y (iii) = d. p.) x = d. p.x) if the unity of F & 12 are same, then same I.X = X + X G R. K=>. Whe additive of of any ring R forms V.S. over its subring (which is field) if unity of R A subring an same and the endernal combosition is the multiplication of (R,+1.)".

9

3

 $P = \begin{cases} \{a, b\}, c, d \in R\} \end{cases}$ $\begin{cases} \{P_1 + P_1, b\} \text{ is a sing } \end{cases}$ $\Rightarrow V = \{P_1 + P_2, b\} \text{ is an abelian } \{P_2, b\} \end{cases}$ $F = \begin{cases} \{a, a\}, c, d \in R\} \end{cases}$ $F = \begin{cases} \{a, a\}, c, d \in R\} \end{cases}$

(F, +, ·) is a field and FCR

(F, +, ·) is a field and FCR

if (.) of (R, +, ·) is taken the external

composit V doesn't form V.S. over F.

C

C

C

as
$$1 = \begin{bmatrix} x & x_1 \\ x & x_2 \end{bmatrix} \in F \quad x = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \in V$$

$$1 = \begin{bmatrix} x & x_1 \\ x & y_2 \end{bmatrix} \neq X$$

Jai Maa Saraswati	
Jet: - A collection of well defined dis	-1;
By well de	\int_{Γ}
we mean, there is no confusion or ambigui	4
By well de we mean, there is no confusion or ambiguit regarding the inclusion or the exclusion of the object.	>
of A isn i.e, A =n.	
PLA] = gn.	
Proof: - Let Al=n, -then	
No. of subseds of A having no element = no	0
· · · · · · · · · · · · · · · · · · ·	• (
	, ,
No. of subsets of A having nelement = "	(
We have,	
nc6+nc1++ncn=/P(A)/	
By Binomial theorem,	
· (1+x) n = n co + nc, x + + n cn x n - 1)	
On comparing Of III.	
Wegen N=1	
·. /PLA) / = (H1)n = gn.	

Indmeffed: Let A = { x1, x2, ---, xn } 9. Let A be the sed during containing (2n+1) elements, then the number of subsects of A having (a) 2n-1 (C) 2n+1 => d+d = 22n+1 Any-(d)

```
Carlesian Product: -
            Let A & B be any Ino non-empty
52+S
  define AXB= [(a,b): QEA, LEB)
Then, AXB is defined as Cartesian product of
A & B.
91 either A or B is empty, then
       AXB = \phi.
Proberdies:
 1) 9+ |A|=m, |B|=h
    Hen AXB = mxn = mn
 ii) (AUB) X C = (AXC) U(BXC)
 iii) (Anb) XC = (Axc) n(Bxc).
 iv) (AXB) (CXD) = (Anc) X(BAD).
y, 9f A and B have 99 elements in common
then the no of elements common to AXB and
 BXA is
(i) 100 (ii) 299 (iii) 992 (iv)101.
JOSh: -(AXB) N(BXA) = (ANB) X(BNA)
                     = 99 X 99
                      = 992
```

3

J

J

j

9

J

J

I

1

J

Ĵ

Ć

7

7

Relation: -Let A and B be any two seds any subsed of AXB is defined as relation from AtoB. It Two relations are said to be different distinct if and only if they correspond to different subsets. if |A|= m and |B| = n Then, No. of ocladions from AtoB = 2mn = graix (B). i.e. Relation Types of rel's on the sed A: 1) Identity relation: Led A be any sed and SCAXA is destinced as identity relation if every elemente of A is related to itself only. i.e, I = } (e, a) : * a ∈ A } e.g. I,= {(1,11,(1,11, (2,2),(2,3))} Iz= { (1,11, (2,2) } ×

Note: - Identity relation is always unique.

I3 = { (1,11, (2,2),(3,3)}

C

C

C

C

C

2) Reflexive veln: Let A be any sed and SEAXX then 5 is said to be rullexive rell if ICS. e.j. 5= { (1,11, (1,2), (1,2) } X J 5=1(1,11,(2,2),(3,3),(1,2)} 5= { (1,11, (2,21, (3,3)} 3 7 3 ## 91 /A1 = n, Hen Fotal noi of reflexive rely on A = gn2-n No. of choices for elements of the type P8001-(ai, ai) = 1 (a:,a; 1= 2 where i + j i. No of seflexive seln = 1 x1x -- x1 x2 x2x -- xx nt-n diny $= g^{n^2-n}$ 3) groeflerive reln: Let Abe and set and SCAXA then S is said to be irreflerive rely if Ins= .

A = {1,2,3} 5= {(1,11, (1,21,(2,3)) X 5 = {(1,2), (3,2)} ## 94 /A1= n, Then Total noi of isreflexive vel's = 2n2n Proof: -NIO of choices for the elements of the tape (ai, ai)=1 (ai, es)=2 .. No of irreflexive relas = 1x1x - - x1 x2x2x - - - x2 nt-n diany n Times = 2 n2-n. 4) Symmedric reln:-Let Abe a rel and SEAXA then S is said to be symmetric rell in (a, b) = 5 => (b, 2) = 5 i.e, if and then bra.

C

C

C

C

C

C

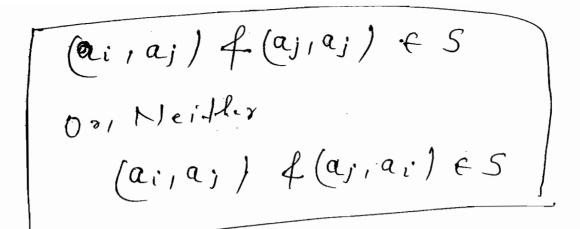
C

Ej:- A = { 1, x, 3 } S= ! (1,11, (2,2), (2,3) }

5= { (1,1) , (2,3), (3,2) } ## 9 f /Al= n, then Total no of symmedric ochis = gn[n+1) Proof: -1 10' of choices for the elements of type (i,ai)= 2 of the paix 1) (ai, ai) + (ai, ai) = 2 where i + j i. 1000 of symmedric relys = 3 XIX - - XI X XXIX - - XI n2-n dimey ndimy - 2" x 2" 12 = 2 ht n2-h $= \chi \frac{n^2 - 1}{2}$ $= 2 \frac{n(n+1)}{2}$ = 2 = 7

V

3



5) Asymetric ocletions: -

16/07/2019

C

C

C

C

Let Abe any sed and SEAXA,

Then S is said to be asymmetric relation if

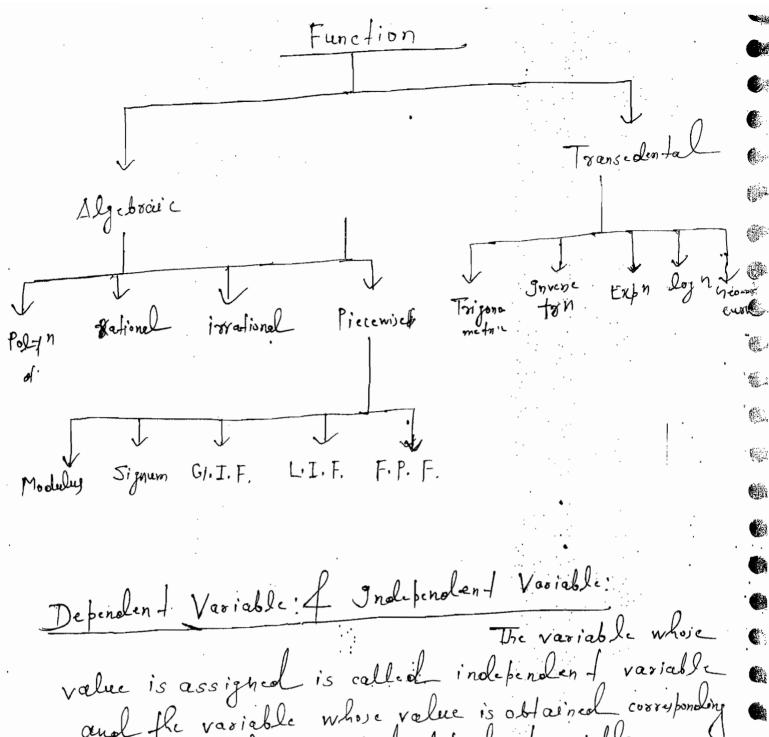
(a,b) CS => (1,2) GS

Mode: - 9 f veln is asymmetric then it is to iverflexive.

i.e, Asymmerloic => 9 reflexive Rel's

Ej:- $A = \{1,2,3\}$ $5 = \{(1,11,(2,3))\}$ $5 = \{(2,3),(3,2)\}$

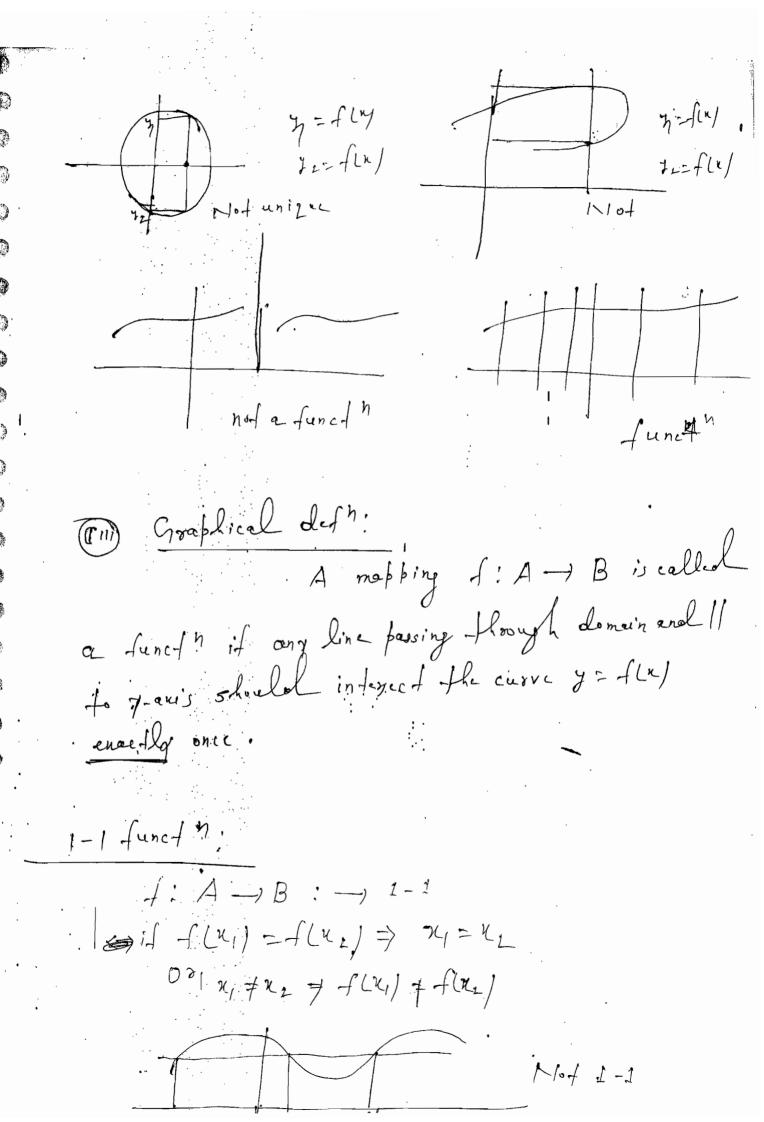
5 = /(2,3//



value is assigned is called indépendent variable and fle variable whose value is obtained corresponding to assigned value is called dépendent variable.

Function: DEVERG element in domain having a unique image in codemoun.

YREA: Junique YEB such Hod J=f(n).

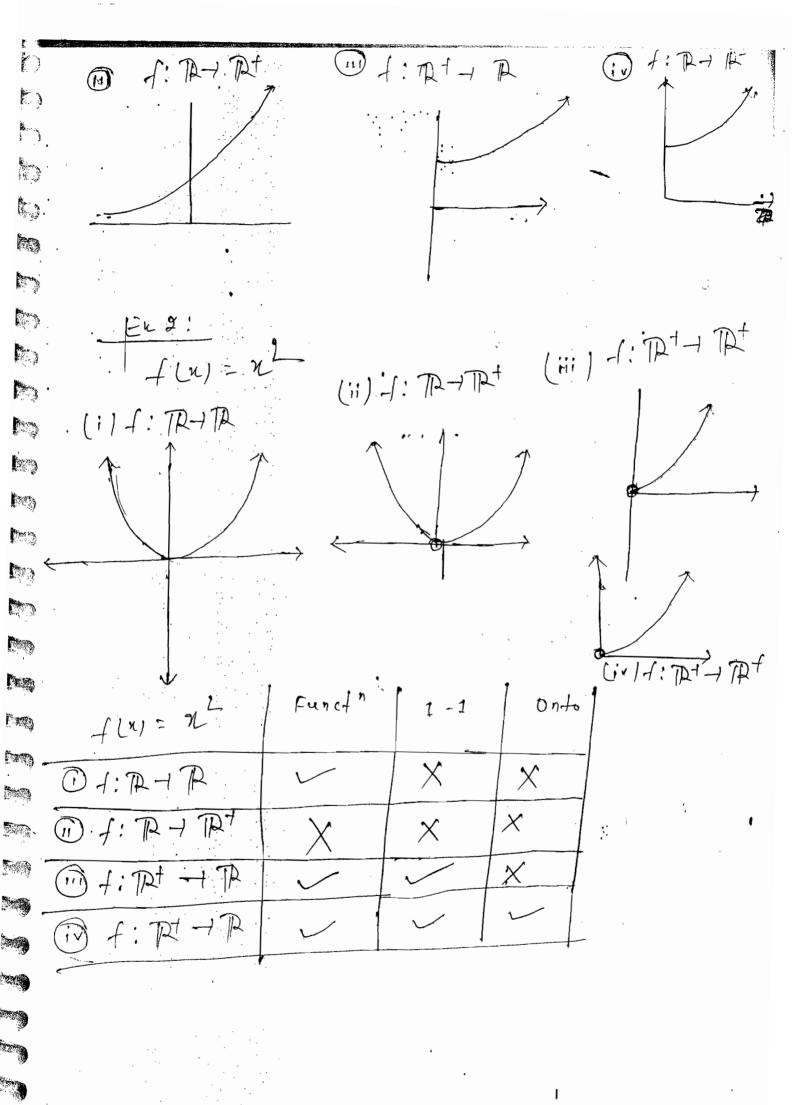


Since flui) = flui) = flus / + 7 2, = 2 = 23 'A functor of A -) B is called 1-1, if I and line passing through co-domain and II to u-aus should intersect the curve y-flux at most once. Onto funct n:

Range - Codomain

A functo f: A-1 B is called and if any line passing through co-domain and 11-4-anis should should intersect the curve y-flx) at least once.

, M	fun cold	1 1-1	Drito
En:- Ilul-en	A UN CATA		X
TO I DIR			
0 1. 1			
(i) f: R-) R+			31
(m) 1: R+ + R:			X
(v) f: R-1 -1 R-1			
(V) + R	<u> </u>		 -
1 R	1.	1	
soln:		One our	
300			
			→ K
()			,
			•
	· K	if ont)
	. 1 >	10-t	- 1



/9 1 [mil de] J = f(x) [min] 24 x 1 x 1 Any = Je-7 = des fonce d/w y fg_ = 4-7 = slope of L. - Slobe of Lwhen P-) y do = (Super of fangend al puint 9) Graffical term Algebraic des rate of chang - did

0

Differential Equation:

Angreyn between dependent variables indépendent varjable and contain fotel desirative et. D.V. of w.r.t. independent variable is called D.T.

(1) y = fin dy dy = sink dy + 2 = sink du + fuy = er dis + diz = 0 ! Simple P.D.t.

107, = f(x) 72 = g(x)

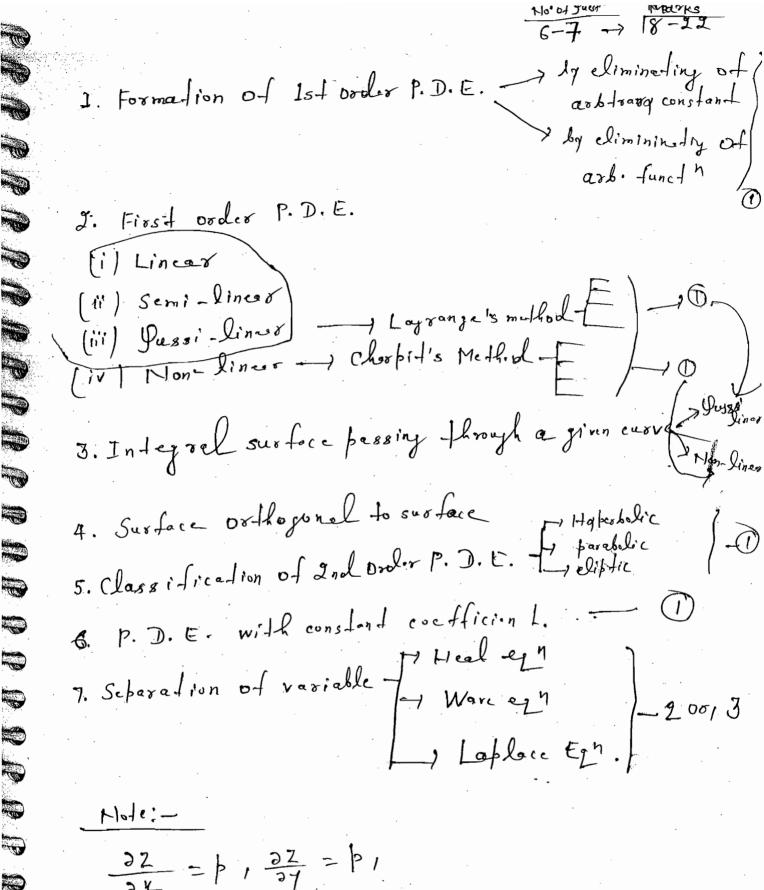
107=f(x18) 32 + 32 =D 32 + 32 = sin(248)

(N) 21 = f(x,8) Zz= g(x,y). 327 - 2272 - D 371 -1 372 = exy System of P.D.E.

Ordinary differential egn,

unique indépendent variable and total desivative of D.V. word. I.V. is called D.D.E.

7 = f(n) J = f Lx/ 72 = g(r) · dr -17 = siny dy tyl -sine det + fly y = e4 der 7 dr D. Simple O.D.E System of O.D.E. Perfiel Diffion diel ezn. Ang D. E. contoin partial derivative is called partial D. E. Classification of D.E. O.D.E. P.D.E. \$ D.4.5 Simple O.D.E Jostom of Simple O.D. E. P.D.E.

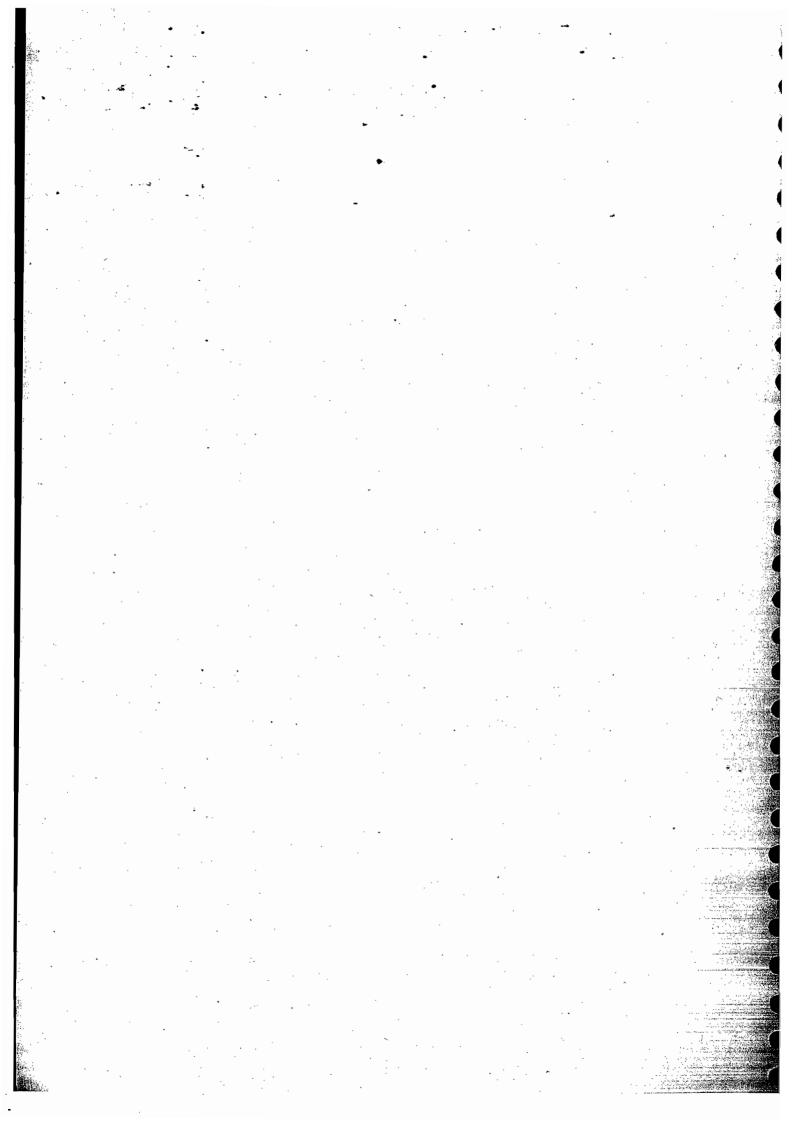


$$\frac{\partial z}{\partial x} = \beta, \frac{\partial z}{\partial y} = \beta,$$

$$\frac{\partial z}{\partial x^{2}} = \delta, \frac{\partial^{2}z}{\partial y^{2}} = \delta,$$

$$\frac{\partial^{2}z}{\partial x^{2}} = \delta, \frac{\partial^{2}z}{\partial y^{2}} = \delta,$$

$$\frac{\partial^{2}z}{\partial x^{2}} = \delta, \frac{\partial^{2}z}{\partial y^{2}} = \delta,$$



Def. Partial Differential Equation. An eg' which contains partial derivative of dependent variable w.s.t. two or more than two indepens -nd variable, is called P.D.E. Hole: -NO. of D. V. = 1 No. of I.V. ≥2 1 32 - 27 = NHY Classification of 1st order P.D.E. A 1st order P.D.E. is said to be linear, if 1. Lincer: it is linear in p12 fZ and of the form PLX, 4/2+ 9 [x,4/2 = R(x,4)2+ S(x,4). のれりナダクニルタマナル3 y3 1 P+2 = KyZ (11) x2p+ y22=1 Ogf SLx14 = D, then it is called homgh linear 1 9f 5 [xiy] = 0, then it is called non-homgh linear P.D.E. P.D.E.

2. Semi linearing. D. E. is said to be semi linear A 1st order P. D. E. is said to be semi linear if it is linear in p f 2 but not necessary in Z and of the form

of the form

Plant p + y lant = Plant 2.

1) 22 p + y 22 = 22 y 22 -> Semi liner

J. Guessi lines:

A 1st order P.D.E. is said to be Guessi

Dinear, if it is linear in Pf p p f q and of the

from

P[x,y,z] p + y [x,y,z] = p[x,y,z]

P[x,y,z] p + y [x,y,z] = p[x,y,z]

1 1-12=xy2

(1) (y-z) p+(z-x) 2 = x-y

(m) y2 p +(x-2) 2 = 22

1. PLX17/ > + 9 LX17/9 = RLX17/2 - Scm1-linear

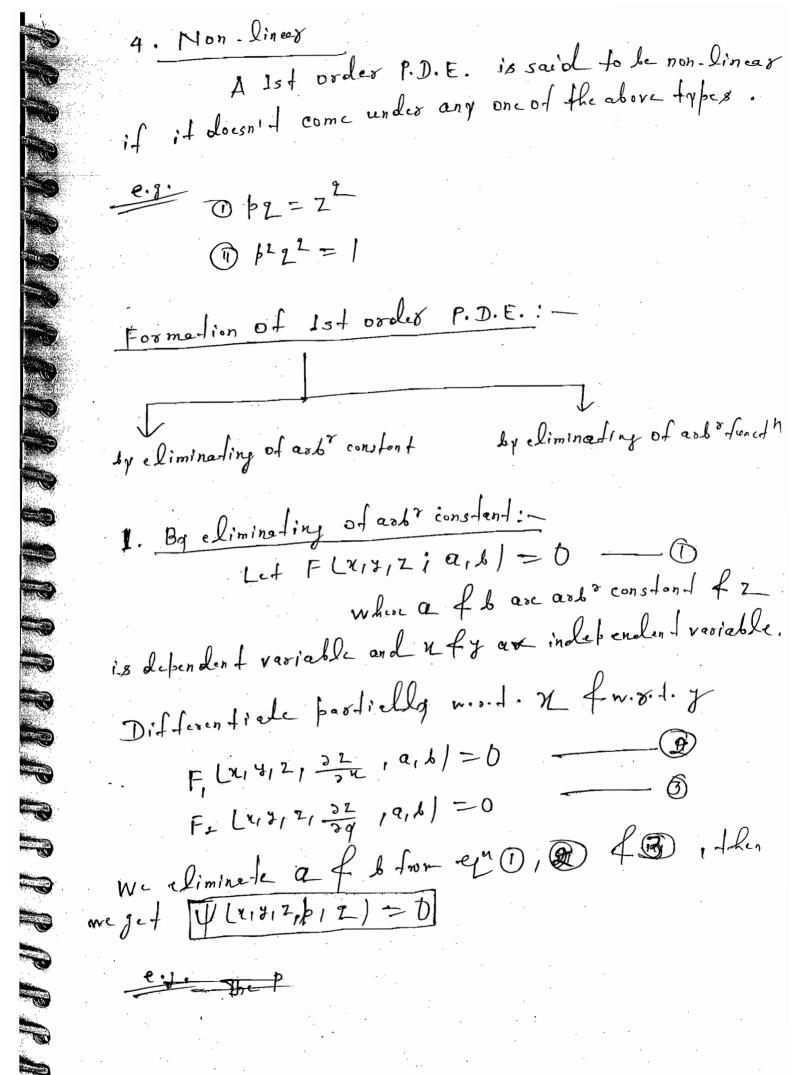
2. PLX17/ > + 9 LX17/2 = PCX17/2/ ______ Scm1-linear

2. PLX17/ > + 9 LX17/2 = PCX17/2/ ______ Scm1-linear

3. PLXIM P+ 9 [X/1/2] 2 = R(X/1/2)

Note:

Linear C Semi-linear C Gussi linear.



The P. D. E. representing the set of all sphere of unit radices with centre in the ny-plane is [ii] y/2-x-2=0 [i] H p2+ 22 = 0 (iv) N.b. T. (ii) 72 (1+ 122)=1 (n-a)+(J-b)+ 22=1 & trap = 0 g(n-a) + 22p = D y 2-2=-2p Hod1 4-1 = - 29 ·. 2-12-42-9-42--1 y 22 (p2 + 22 + 1) = 1 Eg: The P.D. E. for 22 [14 a3] = 8[x+ey+1] is (ii/272= p421 (i1.Z= b2+22 (iv/Z=b)+23 (iii) 272 = p3 + 23 22 (1+ a3) = 8 [x1 a y + b]3 - 0 g (1+ 03) Zp = 29121 07 +6) 2 (1-1 23/2 2 = 24 Q (x+2)+1) 2 - (11) :, 34 1 (19 4 4) [34 D] 14 19 4 4) [$\frac{9}{2} = \frac{9}{4} = \frac{9}$

$$\frac{2}{2} = \frac{1}{3} (x + ay + 1)$$

$$\frac{7}{2} = \frac{1}{3} (x + ay + 1)$$

$$\frac{7}{2} = \frac{3}{3} \frac{1}{2}$$

$$\frac{7}{2} + \frac{2^{3}}{p^{3}} = \frac{3}{2} \frac{7}{2}$$

$$\frac{7}{2} + \frac{2^{3}}{p^{3}} = \frac{3}{2} \frac{7}{2}$$

$$\frac{7}{2} + \frac{7}{2} = \frac{27}{p^{3}}$$

$$\frac{7}{2} + \frac{7}{2} = \frac{27}{p^{3}}$$

$$\frac{7}{2} + \frac{7}{2} = \frac{7}{2} = \frac{7}{2}$$

$$\frac{7}{2} + \frac{7}{2} = \frac{7}{2}$$

JMS

Unil-I

Chapter-1 - Sets of Jts Fundamentals Chapter-1 Point Set topology of Th

Unit- X

1 - Seguence ort Real number

2 - Siries of Real Number

Unid-3

3

3

1 - Fundamentals of functions

2 - Limits and Continuity

3 - Differentiability

4 - Application of Derivative

Unid-4

+ - Sequence of Function

2 - Jevies of Function

Unit-5

1 - Ricmann Integrability

2- Function of Bounded Variation

Unit-6

1. Function of Several Variables

8 C e 8 G .

-3

3

3

7

3

A well destined collection of distinct objects is called sets.

Mole: - D By well desined, we mean there is no ambiguity or confusion regarding inclusion or exclusion of object.

(i) Empty collection is well defined so it is a sert called void sert or null sert or empty sert and denoted by 11 or \$\phi\$.

eligible to collection for any set.

(iv) Grenerally, seeds are denoted by capital lefters and objects included in the sed, elements are denoted by small lefters a, b, c, x, y, z etc and if a is an object included in the set X, a belongs to X and worker

* Axiom of Regularity (ADR):

to itself i.e, if X is a set then X & X.

-> Dodinary and Endre Ordinary Seds: -

a sert sirt. XEX, X is called extra ordinary sert. A set is called ordinary it it doesn't contain itself as an element.

X = {d is. an object: d is not a teacup} X is a set => X is not a teacup.

=> Russel's Paradon:

X = { A : A is an ordinary sed}
= collection of all the ordinary seds

gf X is ased

gf X is ordinary => X EX

=> X is extra ordinary

C

C

C

C

C

X is extra-ordinary $\Rightarrow X \in X$ $\Rightarrow X$ is ordinary

i.e, X is not a set

i. Therefore is no sed of all the ordinary

X= | A is ascd: A \ A |

= The collection of all the sets

9f X is a sed => X ₹ X

 $\Rightarrow X \in X$

Subsed: -Led A & B are sets, in REA => REB, flen we say A is a subsed of B denoted by ACB. ZZEAS. J. Z ≠ B Mote: To Embody sent is a subsent of every sent. (i) Every set is a subsect of itself. -W => O AUB = { n: REA WAREB} (AnB= } x: XEAN KEB } (1) A-B= } X: X∈A, X & B } (i) A & B = (A-B) U (B-A) = (AUB) - (ANB). O AC = U-A (AUB) = ACABC (VII) (ANB) = ACUBC Viii) A=B (ACB & BCA. * Power sed: -Let Abcased

Let A be a sent

P(A) = {X: X CA}

= The set of all subsets of A.

Led A= la, l, c) P(A)=) \$, {a}, [4], [c], [e, b], [e, c], [e, c], Ç (a, L, c) } C It For any sed A, PLAT + . Proof: - Define PLA) = { X : X CA } Carlesian product: -Let A & B are sets. Define AXB = { (a, b): a ∈ A, b ∈ B} C · where (a, b) is called ordered pair. **C**; C NIHIC: - O A, XA= X-- XAn= #Ai= |a1,a2,--,and C **S** 1:2:0Ai{ n-tupply for some i. Functions: -Let A &B # \$. Then a rule by

which every clement is assigned to some unique element of B is destined as a function from A to B and destined by $f:A \rightarrow B$

if f: A - B Hen, A is called domain (1) B is called co-domain (II) 91 x & A is assigned to y & B, we write ****** g = f(x) And y is called the image of n f n-presinge of 7. 0 (iv) I(A) = } f(n): xeA } CB called the range of of. **E** V Dne-one frenction [Injection]: f(a) = f(b) (=> a=b (vi) Surjection (onto) JLA1 = B. (vii) Bijection- Dre-one and onto. Note: - IN = 11,2,3, -.., n, n+1, -- } J(n)= 11,2,3,--,n). Jimiler sets: -Two non-empty sets are said to be similer if I a bifection between them. The words like equivalent, equinumerous, equipotentiel arcalso result in the place of similar.

DIF A & B 70, we say B has more potential than the of A if onto Sunction from A to B can't be defined.

of got one-one function can't be desined then we say A has more potential than B.

Finite Set: -

A non-empty set is said to be finite if it is similar to 5n.

of A is n, denoted by cood LA) = /AI=n.

Note: - OBy extension of definite set, empty set is also considered as finite set and its cardinality is D.

INTO = \0, 1, 2, 3, --- \
= The sent of all the finite cardinals.

Dre intersection of two power sets can't be disjoint.