#### template.cpp

```
#include <bits/stdc++.h>
using namespace std;
#define fastio() ios_base::sync_with_stdio(false);cin.tie(
    → NULL); cout.tie(NULL)
#define foreach(iterator,object) for(auto iterator = object.
    → begin(); iterator != object.end(); iterator++)
#define foreach_rev(iterator,object) for(auto iterator =
    → object.rbegin(); iterator != object.rend(); iterator
    \hookrightarrow ++)
typedef long long 11;
typedef long long unsigned int llu;
typedef double dbl;
typedef long double ldbl;
typedef pair <int, int> pii;
typedef pair <11,11> pl;
typedef vector <1l> v1;
typedef vector <vl> vvl;
typedef vector <pl> vpl;
typedef vector <vpl> vvpl;
#define sll static ll
#define sllu static llu
#define pll pl
#define VI vector <int>
#define PQ priority_queue
#define fi first
#define se second
#define sz(x) (int)x.size()
#define lng(x) (int)x.length()
#define bgn(x) x.begin()
#define end(x) x.end()
#define all(x) (x).begin(),(x).end()
#define pb push_back
#define apnd append
#define is even(x) ((x&1)?0:1)
#define elif else if
#define ln "\n"
void solve(ll case number){
#define NUMBER_OF_TESTS
```

```
int main(){
   fastio():
   11 Q = 1;
#ifdef NUMBER_OF_TESTS
   11 T:
    cin >> T;
   for(Q=1: Q<=T: Q++){</pre>
       // cout << "Case #" << Q << ": ":
       solve(Q);
#else
   // while(1)
       solve(Q++);
#endif
   return 0;
alias.sh
alias g='find_.._-maxdepth_1_-regex_".*\.c\(pp\)?"_-exec_bash_
    \hookrightarrow -c_{\sqcup}"g++_{\sqcup}-std=gnu++17_{\sqcup}-g3_{\sqcup}-fdiagnostics-color=always_{\sqcup}-
    \hookrightarrow ou{}.o.tmpu-cu{}u2>&1u|uheadu-nu10"u";";ug++u-ou"$(
    → 2>,,/dev/null,
AhoCorasick.cpp
#include "Trie.cpp"
class AhoCorasick{
private:
   vvl ans;
   Trie trie:
   vl wl;
public:
    AhoCorasick(){}
   AhoCorasick(const vs& dictionary){
       for(string s : dictionary){
           wl.pb(s.size());
       trie = Trie(dictionary);
   const vvl& find_occurrences(string& text){
```

ans.assign(wl.size(), vl());

 $\hookrightarrow$  style

c = text[i]:

for(ll i=0; i<text.size(); i++){</pre>

for(ll 1 : trie.next\_leaves(c)){

// i is used later as an integer, don't change

```
ans[1].pb(i-wl[1]+1);
       }
       return ans;
};
ArticulationBridge.cpp
template<class T> class ArticulationBridge{
#define g (*pg)
public:
    typedef long long 11;
    typedef std::pair<ll,ll> pl;
    typedef std::vector<11> v1;
    typedef std::vector<T> vt;
    typedef std::vector<vt> vvt;
    typedef std::pair<pl,T&> plte;
    typedef std::vector<plte> vplte;
    typedef std::function<ll(const T&)> fetnt;
    static ll def_etn(const T& e){
       return e:
    vl articulations, generated_components;
    vplte bridges, trees, backs; // , forward, cross;
private:
    11 n, pos;
    vvt* pg;
    vl num, low;
    fetnt etn;
    void dfs(ll p, ll u){
       11 \text{ v. c} = 0. \text{ a} = 0:
       num[u] = low[u] = pos++;
       for(T& ed : g[u]){
           v = etn(ed);
           if(!num[v]){
               trees.pb(plte(pl(u,v), ed));
               dfs(u, v):
```

if(num[u] <= low[v]) a++:</pre>

 $\hookrightarrow$  )):

generated\_components[u] = a;

articulations.pb(u);

}else if(v != p){

}

if(a > 0){

}

if(p==-1) a=c-1:

if(num[u] < low[v]) bridges.pb(plte(pl(u,v), ed</pre>

if(num[u] > num[v]) backs.pb(plte(pl(u,v), ed))

if(low[u] > low[v]) low[u] = low[v];

if(low[u] > num[v]) low[u] = num[v];

```
}
                                                                            for(i=1: i<n: i++)</pre>
                                                                                                                                       vvt core:
public:
                                                                                if(P[i].y < P[P0].y || (P[i].y == P[P0].y && P[ private:</pre>
   ArticulationBridge(){}
                                                                                     \hookrightarrow il.x > P[P0].x))
                                                                                    P0 = i:
   ArticulationBridge(const vvt& graph, ll v = -1, fetnt
                                                                                                                                       const vvt* pg;
        → edge_to_node = def_etn){
                                                                             point temp = P[0];
                                                                                                                                       fetnt etn;
                                                                            P[0] = P[P0];
       g = graph;
                                                                                                                                       fsedt sed;
       if(v == -1){
                                                                            P[P0] = temp:
                                                                                                                                       fmet me:
                                                                            // second, sort points by angle w.r.t. pivot PO
           n = g.size();
                                                                                                                                       Tarjan<T> tj;
       }else{
                                                                            pivot = P[0]; // use this global variable as
                                                                                                                                   public:
                                                                                 → reference
                                                                                                                                       static T& def_me(T& sv, const T& nv){
           n = v;
                                                                                // sort(++P.begin(), P.end(), angleCmp); // we
       }
                                                                                                                                          return sv;
       etn = edge_to_node;
                                                                                     → do not sort P[0]
       num.assign(n, 0);
                                                                             sort(++P.begin(), end(P), angleCmp); // we do not
                                                                                                                                       static T& def_sed(T& sv, ll v){
       low.resize(n);
                                                                                 → sort P[0]
                                                                                                                                           return sv = v;
                                                                            // third, the ccw tests
       generated_components.assign(n, 0);
       pos = 1;
                                                                             vpoint& S = convex_hull;
                                                                                                                                       CoreDAG(){}
       for(11 v=0; v<n; v++){</pre>
                                                                                                                                       CoreDAG(
                                                                            S.pb(P[n-1]);
           if(!num[v]) dfs(-1, v);
                                                                            S.pb(P[0]);
                                                                                                                                           const vvt& graph,
       }
                                                                            S.pb(P[1]);
                                                                                                                                          11 v = -1
                                                                                                                                          fetnt edge_to_node = Tarjan<T>::def_etn,
                                                                            i = 2:
#undef g
                                                                                                                                          fsedt set_edge_destination = def_sed,
                                                                             while (i < n){
};
                                                                                // note: N must be >= 3 for this method to work
                                                                                                                                           fmet merge_edges = def_me
                                                                                j = (11)S.size()-1;
                                                                                                                                       ) {
                                                                                if (ccw(S[j-1], S[j], P[i])) S.pb(P[i++]); //
                                                                                                                                           std::vector<mlt> mm;
ConvexHull.cpp
                                                                                     → left turn, accept
                                                                                                                                           typename mlt::iterator mit:
                                                                                else S.pop_back(); // or pop the top of S until
                                                                                                                                           ll i, x, y;

→ we have a left turn

                                                                                                                                           pg = &graph;
class ConvexHull{
                                                                                                                                           me = merge_edges;
public:
                                                                             chs = convex_hull.size();
                                                                                                                                           etn = edge_to_node;
   typedef std::vector<point> vpoint;
                                                                             // return S;
                                                                                                                                           sed = set_edge_destination;
   vpoint convex_hull; // convex_hull[0] == convex_hull[chs
                                                                                                                                          if(v == -1){
        \hookrightarrow -1], points are ccw
                                                                         // return the result
                                                                                                                                              n = g.size();
   11 chs:
                                                                 };
                                                                                                                                          }else{
   static point pivot: // static is required by angleCmp PAY
                                                                                                                                              n = v:

→ ATTENTION TO THIS FOR MORE INSTANCES

                                                                 point ConvexHull::pivot = point(0,0); // use this global
private:

→ variable as reference

                                                                                                                                           tj = Tarjan<T>(graph, v, edge_to_node);
   static bool angleCmp(const point& a, const point& b) {
                                                                                                                                           nssc = tj.nssc;
       if(collinear(pivot, a, b))
                                                                                                                                          vl& ssc = tj.ssc;
           return dist(pivot, a) < dist(pivot, b);</pre>
                                                                 CoreDAG.cop
                                                                                                                                          mm.resize(nssc):
       dbl d1x = a.x - pivot.x, d1y = a.y - pivot.y;
                                                                                                                                          for(i=0; i<n; i++){</pre>
       db1 d2x = b.x - pivot.x, d2y = b.y - pivot.y;
                                                                                                                                              x = ssc[i]:
       return (atan2(d1y, d1x) < atan2(d2y, d2x));</pre>
                                                                 #include "Tarjan.cpp"
                                                                                                                                              for(const T& e : g[i]){
   }
                                                                                                                                                  v = ssc[etn(e)];
public:
                                                                 template<class T> class CoreDAG{
                                                                                                                                                  if(x != v){
   // #undef end
                                                                 #define g (*pg)
                                                                                                                                                  mit = mm[x].find(y);
   ConvexHull(vector<point> P) {
                                                                 public:
                                                                                                                                                      if(mit == mm[x].end()){
           11 i, j, n = (11)P.size();
                                                                     typedef long long 11;
                                                                                                                                                         mm[x][v] = e:
           if(n <= 3) {
                                                                     typedef std::vector<ll> vl;
                                                                                                                                                      }else{
              if (!(P[0] == P[n-1])) P.pb(P[0]);
                                                                     typedef std::vector<vl> vvl;
                                                                                                                                                         me(mit->second. e):
              convex hull = P:
                                                                     typedef std::vector<T> vt:
                                                                                                                                                     }
              chs = convex_hull.size();
                                                                     typedef std::vector<vt> vvt;
                                                                                                                                                  }
              return:
                                                                     typedef typename Tarjan<T>::fetnt fetnt;
                                                                                                                                              }
                                                                     typedef std::function<T&(T&, 11)> fsedt;
```

typedef std::function<T&(T&, const T&)> fmet;

typedef std::map<11,T> mlt;

ll nssc;

core.resize(nssc);

for(i=nssc: i--:){

// first, find PO = point with lowest Y and if tie

 $\hookrightarrow$  : rightmost X

11 PO = 0;

#### DeterminantGaussJordan.cpp

```
#define __GAUSS_JORDAN_EPS 10e-9
template <class T> class GaussJordan{
#define a (*A)
#define b (*B)
public:
   typedef long long 11;
   typedef double dd;
   typedef vector<T> gjvt;
   typedef vector<gjvt> gjvvt;
   static dd def_norm(const T& t){
       if(t<0) return -t;</pre>
       return t;
   11 r:
   T d = 1:
   gjvvt* A;
   gjvvt* B;
private:
   ll n, ma, mb;
   dd eps;
   function <dd(const T&)> norm;
   inline bool is zero(T& x){
       static T zero = (T)(0);
       if(norm(x) \le eps){
           x = zero:
           return true;
       }
       return false;
   void print(){
       ll i, j;
       for(i=0; i<n; i++){</pre>
           for(j=0; j<ma; j++){</pre>
               cout << a[i][j] << '\t';
           }
           cout << "|\t":
           for(j=0; j<mb; j++){</pre>
```

```
cout << b[i][j] << '\t';
        cout << '\n';
   }
    cout << '\n';
}
void swap(gjvt& a0, gjvt& a1, gjvt& b0, gjvt& b1){
    static ll i;
    static T dt:
    for(i=ma; i--;){
       dt = a0[i];
       a0[i] = a1[i]:
       a1[i] = dt;
    for(i=mb; i--;){
       dt = b0[i]:
       b0[i] = b1[i];
       b1[i] = dt:
   }
    d *= -1: // added wrt notebook
    // cout << "Swap\n";
    // print();
T normalize(gjvt& a0, gjvt& b0, ll c){
    static T k:
    k = (T)1/a0[c];
    d *= k; // added wrt notebook
    a0[c] = 1:
    while((++c) \le ma){
        a0[c] *= k;
    for(c=mb; c--;){
       b0[c] *= k;
    // cout << "Normalize\n";</pre>
    // print();
    return k;
void reduce(gjvt& a0, gjvt& a1, gjvt& b0, gjvt& b1, ll c)
     \hookrightarrow {
    static T k;
    if(is_zero(a1[c])){
    }
    k = a1[c]; // k = a1[c]/a0[c]; // a0[c] == 1
    a1[c] = 0;
    // d *= k:
    while((++c)<ma){</pre>
       a1[c] -= a0[c]*k:
    for(c=mb; c--;){
       b1[c] -= b0[c]*k;
    // cout << "Reduce\n";</pre>
    // print();
```

```
}
public:
   GaussJordan(gjvvt& _A, gjvvt& _B, dd _eps =
        → __GAUSS_JORDAN_EPS, function<dd(const T&)> _norm =

    def_norm, 11 ABrows = 0, 11 Acols = 0, 11 Bcols =
        → 0){
       A = & A:
       B = \&_B;
       if(ABrows){
          n = ABrows;
       }else{
          n = a.size():
       if(Acols){
          ma = Acols:
       }else{
          ma = a[0].size();
       if(Bcols){
          mb = Bcols:
       }else{
          mb = b[0].size();
       eps = _eps;
       norm = _norm;
       // print();
   11 solve(){
       // the absolute value of the returned value is the
            → number of columns of A minus the rank of A
       // in case of a linear system, the returned value is:
          // positive if the system has multiple solutions,
               → and it equals the number of "free"
               → variables
          // negative if the system is not solvable
          // zero if the system has exactly one soluton (

→ stored in b[:][0])
       11 c, i, u = 0, p;
       T pa, pt;
       for(r=c=0; r<n && c<ma; r++, c++){
          for(; c<ma; c++){</pre>
              p = r;
              pa = norm(a[p][c]);
              for(i=r+1: i<n: i++){
                  if((pt = norm(a[i][c])) > pa){
                     p = i;
                     pa = pt;
                 }
              if(!is_zero(a[p][c])) break;
          if(c==ma) break;
          if(p!=r){
              swap(a[r], a[p], b[r], b[p]);
```

```
normalize(a[r], b[r], c);
           for(i=0: i<n: i++) if(r!=i){</pre>
               reduce(a[r], a[i], b[r], b[i], c);
       }
       if(ma == r){ // added wrt notebook
           d = (T)1/d:
       }else{
           d = 0:
       }
       if(mb){
           for(i=r: i<n: i++){</pre>
               if(!is_zero(b[i][0])){
               }
           if(u) return u;
       }
       return ma-r;
#undef a
#undef b
};
```

## Dijkstra.cpp

```
template < class T, class W> class Dijkstra{
// T: type of edge
// W: type of weight
#define g (*pg)
public:
   typedef long long 11;
   typedef std::vector<W> vw;
   typedef std::vector<T> vt;
   typedef std::vector<vt> vvt;
   typedef std::pair<W,ll> pwl;
   typedef std::priority_queue<pwl> pqt;
   typedef std::function<ll(const T&)> fetnt;
   typedef std::function<W(const T&)> fetwt;
   static ll def etn(const T& e){
       return e.first;
   }
   static W def_etw(const T& e){
       return e.second;
   }
   vw dist;
   ll reached:
private:
   ll n, s, t;
   const vvt* pg;
   fetnt etn;
   fetwt etw;
public:
   Dijkstra(){}
```

```
Diikstra(
       const vvt& graph,
       11 \text{ source} = 0,
       11 destination = -1,
       11 _v = -1,
       W inf_w = __DIJKSTRA_INF,
       W timeout = DIJKSTRA INF.
       fetnt edge_to_node = def_etn,
       fetwt edge_to_weight = def_etw
   ){
       pqt pq;
       11 u. v:
       W w, tw;
       pg = &graph;
       s = source;
       t = destination:
       if(_v == -1) n = g.size();
       else n = v:
       etn = edge_to_node;
       etw = edge_to_weight;
       reached = 0;
       dist.assign(n, inf_w);
       dist[s] = 0:
       pq.push(pwl(0, s));
       while(!pq.empty()){
           w = -pq.top().first;
           if(w > timeout) break;
           u = pq.top().second;
           pq.pop();
           if(dist[u] < w) continue;</pre>
           reached++:
           if(u == t) break;
           for(const T& ed : g[u]){
              v = etn(ed):
              tw = etw(ed);
              if(dist[v] > dist[u] + tw){
                  dist[v] = dist[u] + tw;
                  pq.push(pwl(-dist[v], v));
              }
          }
       }
   }
#undef g
};
```

# Dinic.cpp

```
typedef long long 11;
   typedef pair<11,11> pl;
   typedef array<11,3> dinic_node;
   typedef pair<pl,T> dinic_edge;
   T total_flow = 0;
   vector<T> rf;
   vector<bool> in S:
   vector<11> min_cut_edges;
private:
   enum{
       visited, deleted, level
   }:
   vector<dinic_node> v;
   vector<dinic_edge> e;
   vector<vector<pl>>> g;
   ll n, m, m2, s, t, i, r;
   T fm:
   static T flow_min(const T& x, const T& y){
       if(x<y) return x;</pre>
       return v:
   void dinic_bfs(){
       queue<11> q;
       11 x, y;
       v[s][visited] = r:
       q.push(s);
       while(!q.empty()){
           x = q.front();
           q.pop();
           if(x == t) continue;
           for(const pl& yy : g[x]){
              y = yy.first;
               if(rf[yy.second] != (T)0 && v[y][visited] < r){</pre>
                  v[y][level] = v[x][level] + 1;
                  v[v][visited] = r;
                  q.push(y);
              }
           }
       }
   T dinic dfs(ll x, T f){
       11 v. z:
       T ret = 0, tmp = 0;
       if(x == t) return f:
       for(const pl& yy : g[x]){
           if(f == (T)0) break;
           y = yy.first;
           z = vv.second;
           if(rf[z]!=(T)0 && v[y][deleted] < r && v[y][level] ==</pre>

    v[x][level]+1){
               tmp = dinic_dfs(y, flow_min(f, rf[z]));
               rf[z] -= tmp;
               rf[(z<m)?(z+m):(z-m)] += tmp;
              f -= tmp;
               ret += tmp:
```

```
}
                                                                      ll min cut(){
                                                                          11 x:
       if(ret != (T)0){
                                                                          vector<ll> q;
           v[x][deleted] = r;
                                                                          11 qb;
       }
                                                                          in_S.assign(n, false);
                                                                          in_S[s] = true;
       return ret;
                                                                          q.push_back(s);
                                                                          for(qb=0; qb<q.size(); qb++){</pre>
   T step(){
                                                                             x = q[qb];
       r++:
       dinic_bfs();
                                                                             for(const pl& yy : g[x]){
                                                                                 if(rf[yy.second]){
       return dinic_dfs(s, fm);
   }
                                                                                     if(!in_S[yy.first]){
public:
                                                                                         in_S[vv.first] = true;
   Dinic(ll _v, ll _e, const vector<dinic_edge>& edges, ll
                                                                                         q.push_back(yy.first);
        → source = 0, ll sink = -1, const T& flow_max =
                                                                                 }

→ __DINIC_FLOW_MAX) {
                                                                             }
       n = v;
                                                                          }
       m = _e;
                                                                          for(11 x : q){
       m2 = m << 1;
       e = edges:
                                                                              for(const pl& yy : g[x]){
                                                                                 if(!in_S[yy.first] && yy.second < m){</pre>
       e.resize(m2);
                                                                                     min_cut_edges.push_back(yy.second);
       for(i=m; i--;){
           e[i+m].__dinic_eu = e[i].__dinic_ev;
                                                                                 }
           e[i+m].__dinic_ev = e[i].__dinic_eu;
                                                                             }
                                                                          }
       s = source;
                                                                          return q.size();
       if(sink == -1){
           t = n-1:
                                                                  };
       }else{
           t = sink;
                                                                  DSU.cpp
       fm = flow_max;
       r = 0:
                                                                  class DSU{
       total_flow = 0;
                                                                  public:
       v.assign(n, \{0,0,0\});
                                                                      typedef long long 11;
       rf.reserve(m2);
                                                                      typedef std::vector<ll> vl;
       g.assign(n, vector<pl>());
                                                                      11 cc;
       for(i=0; i<m; i++){</pre>
                                                                  private:
           rf[i] = e[i].__dinic_ec;
                                                                      11 n;
           g[e[i].__dinic_eu].push_back(pl(e[i].__dinic_ev, i
                                                                      vl id, rk, sz;
                \hookrightarrow ));
                                                                  public:
       }
                                                                      DSU(){}
       for(i=m; i<m2; i++){</pre>
                                                                      DSU(11 n){
           rf[i] = 0:
                                                                          static ll i;
           g[e[i].__dinic_eu].push_back(pl(e[i].__dinic_ev, i
                                                                          cc = n;
                \hookrightarrow ));
                                                                          rk.assign(n, 0);
       }
                                                                          sz.assign(n, 1);
   }
                                                                          id.resize(n):
   void execute(){
                                                                          for(i=n; i--;){
       T ret:
                                                                              id[i] = i;
       do-f
                                                                          }
           ret = step();
           total_flow += ret;
                                                                      ll findSet(ll i){
       }while(ret != (T)0);
                                                                          if(id[i] == i) return i:
                                                                          return id[i] = findSet(id[i]);
```

```
bool isSameSet(ll i, ll i){
       return findSet(i) == findSet(j);
   11 unionSet(ll i, ll j){
       static 11 x, y;
       x = findSet(i):
       v = findSet(j);
       if(x != y){
           cc--;
           if(rk[x] < rk[y]){
              sz[y] += sz[x];
              return id[x] = v;
           }else{
               sz[x] += sz[y];
              if(rk[x] == rk[y]) rk[x]++;
              return id[y] = x;
           }
       }
       return x;
   ll getSize(ll i){
       return sz[findSet(i)];
   }
}:
```

### ExpressionEvaluator.cpp

```
template <class T> class ExpressionEvaluator{
private:
   11 pos = 0:
   11 \text{ errpos} = -1:
   11 errcode = 0;
   ll explen;
   string exp;
   string ops;
   string opars = "([{";
   string cpars = ")]}";
   11 npars[4] = {};
   bool sgn;
   bool chk_par;
   stack<ll> parsht;
   stack<ll> parshp;
   function<T(const string&, size_t*)> stoT;
   static T def_stoT(const string& str, size_t* idx){
       return stod(str, idx);
   static bool is mul(char c){
       return c=='*' || c=='/';
   bool is_op(char c){
       return ops.find(c) != string::npos;
   bool is_cpar(char c){
```

}

```
return cpars.find(c) != string::npos;
}
void divide(T& res, T& v){
   if(v == 0){
       if(res != 0){
           errcode = 2;
       }else if(!errcode){
           errcode = 3;
       res = 0;
   }else{
       res /= v:
   }
11 operate(T& res, T& v, char op){
   if(op == '+'){
       res += v;
   }else if(op == '-'){
       res -= v;
   }else if(op == '*'){
       res *= v;
   }else if(op == '/'){
       divide(res, v);
   }else{
       errpos = pos;
       return 1;
   }
   v = 0:
   return 0;
ll read number(T& n){
   sll i;
   size_t idx;
   for(i=pos; pos<explen && !is_op(exp[pos]); pos++);</pre>
   try{
       n = stoT(exp.substr(i, pos-i), &idx);
   }catch(const invalid_argument& e){
       errpos = i;
       return 1;
   }catch(const out_of_range& e){
       errpos = i;
       return 1;
   if(pos==i || i+idx!=pos){
       errpos = pos;
       return 1;
   }
   pos--;
   return 0;
ll evaluate_r(T& res, bool mul, char op, ll& nel){
   ll par, i, cnel;
   char lop = 0;
   T v = 0;
   if(!mul){
```

```
op = '+';
                                                                             return 1;
   if(sgn){
       res = 0;
                                                                          return 0;
       if(exp[pos] == '-'){
                                                                      }else if(op){
           op = '-';
                                                                          if(read_number(v)){
           pos++;
                                                                              return 1;
           nel = 1:
       }else if(exp[pos] == '+'){
                                                                          lop = op;
                                                                          op = 0;
           pos++;
       }
                                                                      }else{
   }
                                                                          op = exp[pos];
                                                                          if(is_mul(op)){
                                                                             if(!mul){
for(; pos<explen; pos++, nel++){</pre>
   if((par = opars.find(exp[pos])) != string::npos){
                                                                                 pos++;
       if(!op){
                                                                                 if(evaluate_r(v, true, op, nel)){
           errpos = pos;
                                                                                     return 1;
           return 1;
                                                                                 op = exp[pos];
       if(par) for(i=0; i<=par; i++){</pre>
                                                                                 if(is_cpar(op)){
           if(npars[i]){
                                                                                     op = 0;
               errpos = pos;
                                                                                     pos--;
               return 1;
           }
                                                                              if(operate(res, v, lop)){
       npars[par]++;
                                                                                 return 1;
       parsht.push(par);
       parshp.push(pos++);
                                                                         }else{
       v = 0;
                                                                             if(operate(res, v, lop)){
       cnel = 0;
                                                                                 return 1;
       if(evaluate_r(v, false, 0, cnel)){
                                                                             if(mul){
           return 1:
       }
                                                                                 return 0;
       lop = op;
                                                                         }
                                                                      }
   }else if((par = cpars.find(exp[pos])) != string::
        → npos){
       if(op || parsht.empty() || parshp.top() == pos
                                                                  if(operate(res, v, lop)){
            \hookrightarrow -1){
                                                                      return 1;
                                                                  }
           errpos = pos;
           return 1;
                                                                  return 0;
       }
       if(parsht.top() != par){
                                                           public:
           errpos = pos;
                                                              ExpressionEvaluator(const string& expression, bool
           return 1;
                                                                   → signed_numbers = true, bool check_parenthesis =

    false, function<T(const std::string&, size_t*)>
       if(chk_par && nel<2){</pre>
                                                                   → string_to_T = def_stoT, const string& operators =
                                                                   → "+-*/"){
           errpos = pos;
           return 1;
                                                                  exp = expression;
       }
                                                                  explen = exp.size();
       if(!mul){
                                                                  sgn = signed_numbers;
           npars[par]--;
                                                                  chk_par = check_parenthesis;
           parsht.pop();
                                                                  ops = operators + opars + cpars;
           parshp.pop();
                                                                  stoT = string_to_T;
       if(operate(res, v, lop)){
                                                              11 evaluate(T& ans){
```

### extended\_euclidean-catalan.cpp

```
typedef long long 11;
#define mod 100000007
// implemented from https://en.wikipedia.org/wiki/

→ Extended_Euclidean_algorithm#Pseudocode

#define ee_refresh(o,n) tmp=n; n=o-q*n; o=tmp
void extended_euclidean(ll a, ll b){
   ll old r=a, r=b, old s=1, s=0, old t=0, t=1, tmp, q:
   while(r){
      q = old_r / r;
      ee_refresh(old_r, r);
      ee_refresh(old_s, s);
      ee refresh(old t. t):
   // output "Bezout coefficients:", (old_s, old_t)
   // output "greatest common divisor:", old_r
   // output "quotients by the gcd:", (t, s)
// implemented from https://en.wikipedia.org/wiki/
    // #define ee_refresh(o,n) tmp=n; n=o-q*n; o=tmp
11 inv(ll a, ll m){
   ll t = 0, new t = 1, r = m, new r = a, tmp, q;
   while(newr != 0){
      q = r / newr;
      ee_refresh(t, newt);
       ee_refresh(r, newr);
   }
   // if(r > 1)
   // return "a is not invertible";
   if (t < 0)
      t = t + m;
   return t;
```

#### Factorization.cpp

```
template <class T> class Factorization{
public:
    typedef long long 11;
    typedef std::pair<T,ll> pTl;
    typedef std::vector<pTl> vpTl;
    static ll factorize(vpTl& res, T n){
       11 x:
       T r, i;
       res.resize(0):
       if(n == (T)0){
           res.push_back(pTl((T)0, 1));
           return 1:
       }
       if(n<(T)0){
           res.push_back(pTl((T)-1,1));
           n = -n;
       if(n == (T)1){
           res.push_back(pTl((T)1, 1));
           return res.size():
       }
       for(i=(T)2, r=(T)sqrt((double)n); i <= r; i+=((i==(T)
            \hookrightarrow 2)?(T)1:(T)2) ){
           for (x=0 ; n\%i==(T)0 ; n/=i, x++);
               res.push_back(pTl(i, x));
               r = (T)sqrt((double)n);
           }
       }
       if(n!=(T)1){
           res.push_back(pTl(n, 1));
       return res.size():
};
```

# FFTit.cpp

```
template <class T, class F> class FFTit{
```

```
public:
   typedef long long int 11;
   typedef complex<F> cf;
   typedef vector<cf> vcf;
   typedef vector<T> vt;
   static constexpr F pi = acos(-1);
private:
   static T fft_round(const F& f){
       return f+(F)(0.5):
   static void fft_uw(vcf& v, ll n, bool inverse = false){
       #define a (*pa)
       #define b (*pb)
       // assuming n == pow(2,k)
       vcf u, *pa, *pb, *pt;
       u.reserve(v.size());
       pa = &v;
       pb = &u:
       11 n2 = n > 1, c=0, i, j, d, x;
       cf w. dw:
       F t;
       for (d=n2, t=pi*(F)(inverse?-1:1); d; d>>=1, t/=(F)2)
           dw = cf(cos((double)t), sin((double)t));
           for(i=0: i<d: i++){</pre>
               for(j=i, w=cf((F)1), x=i; j<n; j+=(d<<1), w*=</pre>
                    \hookrightarrow dw, x+=d){
                  b[x] = a[j] + w*a[j+d];
                  b[x+n2] = a[i] - w*a[i+d];
           }
           pt = pa;
           pa = pb;
           pb = pt;
           c++;
       if(c&1){
           for(i=n; i--; ){
              v[i] = u[i];
           }
       if(inverse){
           for(i=n; i--;){
              v[i] /= (F)n:
           }
       #undef a
       #undef b
   static ll fft(vcf& res, const vt& p, ll n = -1){
       if(n == -1) n = p.size();
       for(m=1; m<n; m<<=1);</pre>
       res = vcf(p.begin(), p.end());
```

vector<vector<pl>>> g;

```
res.resize(m, (F)0);
       fft uw(res. m. false):
       return m:
   }
   static ll ifft(vt& res, vcf p, function<T(const F&)> ftot
        \hookrightarrow = fft_round, ll n = -1){
       ll m. i:
       if(n == -1) n = p.size();
       for(m=1: m<n: m<<=1):</pre>
       p.resize(m, (F)0);
       fft_uw(p, m, true);
       res.resize(m):
       for(i=m; i--;){
           res[i] = ftot(p[i].real());
       }
       return m;
   static ll multiply(vt& res, const vt& p, const vt& q,
        → function<T(const F&)> ftot = fft_round){
       vcf a. b:
       11 i, n, m = p.size() + q.size();
       for(n=1; n<m; n<<=1);</pre>
       fft(a, p, n);
       fft(b, q, n);
       for(i=0: i<n: i++){</pre>
           a[i] *= b[i];
       ifft(res, a, ftot, n);
       return n;
}:
```

## FordFulkersonDijkstra.cpp

```
#define __ffd_eu first.first
#define ffd ev first.second
#define __ffd_ec second
#define ffd nflow first
#define ffd nvisited second.first
#define __ffd_nparent second.second
template <class T> class FFD{
public:
   typedef long long 11;
   typedef pair<11,11> pl;
   typedef pair<T,pl> ffd_node;
   typedef pair<pl,T> ffd_edge;
   typedef pair<T,ll> ptl;
   T total_flow = 0;
   vector<T> rf:
private:
   11 \text{ n, m, m2, s, t, i, r = 0}
   vector<ffd node> v:
   vector<ffd_edge> e;
```

```
T fm = 0:
   T vis(){
       priority_queue<ptl> q;
      11 x, y;
      T f = 0, tmp = 0;
       v[s]. ffd nvisited = ++r:
       q.push(ptl(fm, s));
       while(!q.empty()){
          f = q.top().first;
          x = q.top().second;
          if(x == t){}
              while(x != s){
                 y = v[x].__ffd_nparent;
                 rf[y] -= f;
                 rf[(y < m)?(y+m):(y-m)] += f;
                 x = e[y].__ffd_eu;
             }
              return f;
          q.pop();
          if(v[x].__ffd_nflow != f) continue;
          for(pl yy : g[x]){
             y = yy.first;
              tmp = min(f,rf[yy.second]);
              if(rf[yy.second]!=(T)0 && ( v[y].__ffd_nvisited
                  v[y].__ffd_nvisited = r;
                 v[y].__ffd_nparent = yy.second;
                 v[v].__ffd_nflow = tmp;
                 q.push(ptl(tmp, y));
             }
          }
       }
       return (T)0;
public:
   FFD(11 _v, 11 _e, const vector<ffd_edge>& edges, 11
        → source = 0, ll sink = -1, const T& flow_max =
        → __FFD_FLOW_MAX) {
       n = v;
       m = e:
       m2 = m << 1;
       e = edges:
       e.resize(m2);
       for(i=m; i--;){
          e[i+m]. ffd eu = e[i]. ffd ev:
          e[i+m].__ffd_ev = e[i].__ffd_eu;
      }
       s = source:
       if(sink == -1){
          t = n-1:
       }else{
          t = sink;
```

```
fm = flow max:
       v.assign(n, ffd_node((T)0, pl(0,0)));
       v[s].__ffd_nflow = fm;
       rf.resize(m2):
       g.assign(n, vector<pl>());
       for(i=0; i<m; i++){</pre>
           rf[i] = e[i].__ffd_ec;
           g[e[i].__ffd_eu].push_back(pl(e[i].__ffd_ev, i));
       for(i=m; i<m2; i++){</pre>
          rf[i] = 0;
           g[e[i].__ffd_eu].push_back(pl(e[i].__ffd_ev, i));
   };
   void execute(){
       T ret:
       while((ret = vis()) != (T)0){
           total flow += ret:
       }
};
Fraction.cpp
char __FRACTION_SEPARATOR = '|';
template <class T> class Fraction{
private:
   static T gcd(T a, T b){
       static T r;
       if(a<0) a = -a;
       if(b<0) b = -b:
       if(!b){
           if(!a){
              return 1;
           return a;
       }
       r = a\%b;
       while(r){
           a = b:
           b = r;
           r = a\%b:
       return b;
   }
public:
   T num, den:
   char sep = FRACTION SEPARATOR:
   FractionT (T numerator = T)0, T denominator = T1,
        → char separator = __FRACTION_SEPARATOR){
       sep = separator;
```

T g = gcd(numerator, denominator);

num = numerator/g:

den = denominator/g;

```
if(den < 0){
       num = -num:
       den = -den:
   }
Fraction<T>(const string& str, size_t* idx = NULL, char
    → separator = FRACTION SEPARATOR){
   Tn, d;
   size_t p, q;
   n = stoll(str, &p);
   if(str[p] == separator){
       d = stoll(str.substr(p+1), &q);
       *this = Fraction<T>(n, d, separator);
       p += q+1;
   }else{
       *this = Fraction<T>(n, (T)1, separator);
   if(idx != NULL){
       *idx = p;
string to_string() const{
   stringstream ss;
   ss << num;
   if(den != 1){
       ss << sep << den;
   return ss.str();
Fraction<T> operator+(const Fraction<T>& x) const{
   T n.d:
   if(den && x.den){
       d = den*x.den / gcd(den, x.den);
       n = d/den*num + d/x.den*x.num:
       return Fraction<T>(n,d,sep);
   }
   return Fraction<T>((T)1, (T)0, sep);
Fraction<T> operator-(const Fraction<T>& x) const{
   Fraction<T> b;
   b.num = -x.num:
   b.den = x.den:
   return (*this)+b;
Fraction<T> operator*(const Fraction<T>& x) const{
   Fraction<T> b;
   Tg:
   g = gcd(num, x.den);
   b.num = num / g;
   b.den = x.den / g;
   g = gcd(den, x.num);
   b.num *= x.num / g;
   b.den *= den / g;
   return b;
}
```

```
Fraction<T> operator/(Fraction<T> x) const{
   T t = x.num:
   x.num = x.den:
   x.den = t;
   if(x.den<0){
       x.num = -x.num;
       x.den = -x.den:
   return (*this)*x:
bool operator==(const Fraction<T>& x) const{
   return num == x.num && den == x.den:
bool operator<(const Fraction<T>& x) const{
   T = num, b = den, c = x.num, d = x.den, g;
   g = gcd(a, c);
   a /= g;
   c /= g;
   g = gcd(b, d);
   b /= g;
   d /= g;
   return a*d < b*c;</pre>
bool operator>(const Fraction<T>& x) const{
   return x<(*this);</pre>
bool operator<=(const Fraction<T>& x) const{
   return (*this)==x || (*this)<x;</pre>
bool operator>=(const Fraction<T>& x) const{
   return (*this)==x || (*this)>x:
bool operator!=(const Fraction<T>& x) const{
   return !((*this)==x);
void operator+=(const Fraction<T>& x){
    (*this) = (*this) + x;
void operator==(const Fraction<T>& x){
    (*this) = (*this)-x;
void operator*=(const Fraction<T>& x){
    (*this) = (*this)*x;
void operator/=(const Fraction<T>& x){
    (*this) = (*this)/x;
int operator<=>(const Fraction<T>& x) const{
   if((*this)==x){
       return 0:
   }else if((*this)<x){</pre>
       return -1;
   }else{
       return 1:
```

```
*/
};
template <class T> Fraction<T> stofrac(const string& str,
     → size_t* idx, char separator){
       return Fraction<T>(str, idx, separator);
template <class T> string to_string(const Fraction<T>& x){
       return x.to_string();
template <class T> istream& operator>>(istream& is, Fraction<
     \hookrightarrow T>& x){
       string s;
       is >> s:
       x = Fraction<T>(s, NULL, x.sep);
   return is:
template <class T> ostream& operator<<(ostream& os, const
     → Fraction<T>& x){
       os << x.to_string();
       return os;
}
```

#### GaussJordan.cpp

```
#define __GAUSS_JORDAN_EPS 10e-9
template <class T> class GaussJordan{
#define a (*A)
#define b (*B)
public:
   typedef long long 11;
   typedef double dd;
   typedef vector<T> gjvt;
   typedef vector<gjvt> gjvvt;
   static dd def_norm(const T& t){
       if(t<0) return -t;</pre>
       return t;
   11 r:
   T d = 1;
   gjvvt* A;
   givvt* B;
private:
   ll n, ma, mb;
   dd eps;
   function <dd(const T&)> norm:
   inline bool is zero(T& x){
       static T zero = (T)(0);
       if(norm(x) <= eps){</pre>
           x = zero;
           return true;
       return false;
```

```
}
                                                                 }
                                                                                                                                          for(i=0; i<n; i++) if(r!=i){</pre>
void print(){
                                                             public:
                                                                                                                                             reduce(a[r], a[i], b[r], b[i], c);
   11 i, j;
                                                                 GaussJordan(gjvvt& _A, gjvvt& _B, dd _eps =
                                                                                                                                      }
   for(i=0; i<n; i++){</pre>

→ __GAUSS_JORDAN_EPS, function<dd(const T&)> _norm =
       for(j=0; j<ma; j++){</pre>

    def_norm, 11 ABrows = 0, 11 Acols = 0, 11 Bcols =
                                                                                                                                      d = (T)1/d;
           cout << a[i][i] << '\t';
                                                                      \hookrightarrow 0){
                                                                                                                                      if(mb){
                                                                     A = & A:
                                                                                                                                          for(i=r: i<n: i++){</pre>
       cout << "|\t";
                                                                     B = \&_B;
                                                                                                                                             if(!is_zero(b[i][0])){
       for(j=0; j<mb; j++){</pre>
                                                                     if(ABrows){
                                                                                                                                                 u--;
           cout << b[i][j] << '\t';
                                                                        n = ABrows;
                                                                                                                                          }
       }
                                                                     }else{
       cout << '\n';
                                                                        n = a.size():
                                                                                                                                          if(u) return u;
   }
                                                                     if(Acols){
   cout << '\n';
                                                                                                                                      return ma-r;
                                                                        ma = Acols;
void swap(gjvt& a0, gjvt& a1, gjvt& b0, gjvt& b1){
                                                                     }else{
                                                                                                                               #undef a
                                                                        ma = a[0].size();
                                                                                                                               #undef b
   static ll i;
   static T dt:
                                                                    }
                                                                                                                               };
   for(i=ma; i--;){
                                                                     if(Bcols){
       dt = a0[i]:
                                                                        mb = Bcols:
       a0[i] = a1[i];
                                                                     }else{
                                                                                                                               geometry.cpp
       a1[i] = dt;
                                                                        mb = b[0].size();
   }
                                                                                                                               #define EPS (dbl)1e-9
   for(i=mb; i--;){
                                                                     eps = _eps;
                                                                                                                               #define PI (dbl)(acos(-1.0))
       dt = b0[i]:
                                                                     norm = _norm;
       b0[i] = b1[i];
       b1[i] = dt;
                                                                 11 solve(){
                                                                                                                               }
                                                                     // the absolute value of the returned value is the
                                                                                                                               ////// OGGETTI GEOMETRICI //////
                                                                          → number of columns of A minus the rank of A
                                                                                                                               T normalize(gjvt& a0, gjvt& b0, l1 c){
                                                                     // in case of a linear system, the returned value is:
   static T k:
                                                                        // positive if the system has multiple solutions,
   k = (T)1/a0[c];
                                                                             \hookrightarrow and it equals the number of "free"
                                                                                                                               /* punti, note:
                                                                             → variables
   a0[c] = 1;
                                                                                                                                   - punti inizializzati di default a (0,0)
   while((++c)<ma){</pre>
                                                                        // negative if the system is not solvable
                                                                                                                                   - per inizializzare si puo' usare normalmente p.x = tmpx;
                                                                        // zero if the system has exactly one soluton (
       a0[c] *= k;
                                                                                                                                       \hookrightarrow p.y = tmpy o
   }

    stored in b[:][0])

                                                                                                                                      anche p(tmpx,tmpy);
   for(c=mb; c--;){
                                                                    11 c, i, u = 0, p;
                                                                                                                                  - overload del bool op. < per sort
       b0[c] *= k;
                                                                     T pa, pt;
                                                                                                                                   - overload del bool op. == per controlli di uguaglianza,
   }
                                                                     for(r=c=0 ; r<n && c<ma ; r++, c++){</pre>
                                                                                                                                       → per usare !=
                                                                        for(; c<ma; c++){</pre>
   return k;
                                                                                                                                      usare !(p1 == p2)
                                                                            p = r;
void reduce(gjvt& a0, gjvt& a1, gjvt& b0, gjvt& b1, ll c)
                                                                            pa = norm(a[p][c]);
                                                                                                                               struct point {
                                                                            for(i=r+1; i<n; i++){</pre>
                                                                                                                                  dbl x,y;
   static T k;
                                                                                if((pt = norm(a[i][c])) > pa){
                                                                                                                                  point() {
   if(is_zero(a1[c])){
                                                                                   p = i;
                                                                                                                                      x=y=0.0;
       return;
                                                                                   pa = pt;
                                                                                }
                                                                                                                                  point(dbl qx,dbl qy) : x(qx),y(qy) {}
                                                                            }
   k = a1[c]; // k = a1[c]/a0[c]; // a0[c] == 1
   a1[c] = 0;
                                                                            if(!is_zero(a[p][c])) break;
                                                                                                                                  bool operator < (point other) const {</pre>
   while((++c)<ma){</pre>
                                                                                                                                      if(fabs(x - other.x) > EPS)
       a1[c] -= a0[c]*k;
                                                                        if(c==ma) break;
                                                                                                                                          return (x < other.x);</pre>
   }
                                                                                                                                      return (y < other.y);</pre>
   for(c=mb; c--;){
                                                                            swap(a[r], a[p], b[r], b[p]);
                                                                                                                                  }
       b1[c] = b0[c]*k;
   }
                                                                        normalize(a[r], b[r], c);
                                                                                                                                  bool operator == (point other) const {
```

```
return (fabs(x - other.x) < EPS && (fabs(y - other.y)</pre>
                                                               point rotate(point p,dbl theta) {
                                                                   dbl rad = theta * M_PI / 180.0; //se l'angolo e' gia' in
            \hookrightarrow < EPS) ):
   }

→ rad cancellare questa linea

                                                                                                                                // crea vettore da a -> b
};
                                                                   return point( (p.x * cos(rad) - p.y * sin(rad) ),(p.x *
                                                                                                                                vec to_vec(point a,point b) {
                                                                        \hookrightarrow sin(rad) + p.y * cos(rad) ));
                                                                                                                                   return vec(b.x - a.x, b.y - a.y);
                                                                                                                               }
// retta: a,b,c coefficienti equazione implicita
struct line {
   dbl a.b.c:
                                                               // retta passante per due punti
                                                                                                                               // scalare * vettore (?)
                                                               line line_2points(point p1,point p2) {
                                                                                                                               vec scale(vec v,dbl s) {
                                                                                                                                   return vec(v.x * s, v.v * s);
                                                                   dbl p,q,r;
// vettore
                                                                   if(fabs(p1.x - p2.x) < EPS) {
struct vec {
                                                                       p = 1.0; q = 0.0; r = -p1.x;
                                                                                                                               // traslazione di un punto p con vettore v
   dbl x.v:
                                                                                                                               point translate(point p,vec v) {
   vec(dbl _x, dbl _y) : x(_x),y(_y) {}
                                                                      p = -(dbl)(p1.y - p2.y) / (p1.x - p2.x);
                                                                                                                                   return point(p.x + v.x, p.y + v.y);
                                                                       q = 1.0;
                                                                      r = -(dbl)(p * p1.x) - p1.y;
/* !!! IMPORTANTE !!!: rappresentare i poligoni come vector

→ di punti, con

                                                                   line tmp = \{p,q,r\};
                                                                                                                               // prodotto scalare
                                                                                                                               dbl dot(vec a, vec b) {
                     con primo punto che si ripete anche
                                                                   return tmp;

→ come ultimo. E.g.:

                                                                                                                                   return (a.x * b.x + a.y * b.y);
   vector <point> polygon;
   polygon.pb(p1);
                                                               // controlla se due rette sono parallele
   polygon.pb(p2);
                                                               bool are_parallel(line 11, line 12) {
                                                                                                                               // quadrato del vettore
   polygon.pb(p3);
                                                                   return (fabs(11.a-12.a) < EPS) && (fabs(11.b-12.b) < EPS)
                                                                                                                               dbl norm_sq(vec a) {
                                                                                                                                   return (a.x * a.x + a.y * a.y);
   polygon.pb(p4);
                                                                                                                               }
   polygon.pb(pn); // p1,p2,...,pn sono i punti dei
       → vertici del poligono
                                                                // controlla se due rette sono uguagli
                                                                                                                               // distanza punto - retta passante per a e b
   polygon.pb(polygon[0]);
                                                               bool are same(line 11. line 12) {
                                                                                                                               dbl dist_to_line(point p, point a, point b, point &c) {
                                                                   return are_parallel(11 ,12) && (fabs(11.c - 12.c) < EPS);
                                                                                                                                   vec ap = to_vec(a,p); vec ab = to_vec(a,b);
                                                                                                                                   dbl u = dot(ap,ab) / norm_sq(ab);
c = translate(a,scale(ab,u));
/////// FUNZIONI UTILI ////////
                                                                                                                                   return dist(p,c);
// trovare punto di intersezione
                                                                                                                               }
                                                               point find_intersection(line 11, line 12) {
                                                                   point p;
// distanza euclidea tra punti
                                                                   p.x = (12.b * 11.c - 11.b * 12.c) / (12.a * 11.b - 11.a * 11.b)
                                                                                                                               // distanza punto - segmento ab
dbl dist(point p1,point p2) {
                                                                        \hookrightarrow 12.b):
                                                                                                                                dbl dist_to_segment(point p, point a, point b, point &c) {
   return sqrt( (p1.x - p2.x) * (p1.x - p2.x) + (p1.y - p2.y)
                                                                   if(fabs(11.b) > EPS) p.y = -(11.a * p.x + 11.c);
                                                                                                                                   vec ap = to_vec(a,p); vec ab = to_vec(a,b);
        \hookrightarrow ) * (p1.y - p2.y) );
                                                                   else p.y = -(12.a * p.x + 12.c);
                                                                                                                                   dbl u = dot(ap,ab) / norm_sq(ab);
                                                                                                                                   if(u < 0.0) {
                                                                   return p;
                                                                                                                                       c = point(a.x,a.y);
// distanza di Manhattan tra punti
                                                                                                                                       return dist(p,a);
dbl manh_dist(point p1,point p2) {
                                                                                                                                   7
   return ( fabs(p1.x - p2.x) + fabs(p1.y - p2.y) );
                                                                // controlla se un punto e' in una retta
                                                                                                                                   if(u > 1.0) {
                                                               bool is_point_in_line(point p,line 1) {
                                                                                                                                       c = point(b.x,b.y);
                                                                   if((1.a * p.x + 1.b * p.y + 1.c) < EPS) return true;</pre>
                                                                                                                                       return dist(p,b);
                                                                   return false;
// rotazione punti ccw. wrt (0.0)
```

```
return dist_to_line(p,a,b,c);
// ritorna angolo aob in radianti
double angle(point a, point o, point b) {
   vec oa = to_vec(o,a), ob = to_vec(o,b);
   return acos(dot(oa,ob) / sqrt(norm_sq(oa) * norm_sq(ob)))
        \hookrightarrow :
// prodotto vettoriale
dbl cross(vec a, vec b) {
   return (a.x * b.y - a.y * b.x);
// controlla se un punto e' a sinistra di un segmento(?) non
    → so come spiegarlo
bool ccw(point p, point q, point r) {
   return (cross(to_vec(p,q),to_vec(p,r)) > 0);
// controlla se tre punti si trovano sulla stessa retta
bool collinear(point p, point q, point r) {
   return (fabs(cross(to_vec(p,q),to_vec(p,r))) < EPS);</pre>
// controlla se un punto e' interno, sulla od esterno ad una
    // centro c e raggio r, ritorna O se interno, 1 se sulla
    // per pi greco usare PI, definito sopra
int inside_circle(point p, point c, dbl r) {
   dbl dx = p.x - c.x, dy = p.y - c.y;
   dbl Euc = dx * dx + dy * dy, rSq = r * r;
   if(Euc < rSq) return 0;</pre>
   if(fabs(Euc - rSq) < EPS) return 1;</pre>
   return 2:
// perimetro triangolo
dbl triangle_perimeter(dbl ab, dbl bc, dbl ac) {
   return (ab + bc + ac);
// area triangolo a partire dai lati, per partire dai punti
    → usare dist()
dbl triangle_area(dbl ab, dbl bc, dbl ac) {
   dbl s = triangle_perimeter(ab,bc,ac) / 2;
```

```
return sgrt(s * (s - ab) * (s - bc) * (s - ac)):
// raggio circonferenza inscritta
dbl r_incircle(dbl ab, dbl bc, dbl ac) {
   return triangle area(ab.bc.ac) / (0.5 *

    triangle_perimeter(ab,bc,ac));
// controlla (e trova) l'esistenza della circonferenza

→ inscritta?

// i triangoli non sono sempre inscrivibili?
// cp3 non e' molto chiaro a riguardo, onestamente non

→ toccherei troppo

// l'implementazione, comunque passati p1, p2, p3, ctr, r in
    // e in r il raggio e ritorna 1 se esiste(?)
int in_circle(point p1, point p2, point p3, point &ctr, dbl &
    \hookrightarrow r) {
   r = r_{incircle(dist(p1,p2),dist(p2,p3),dist(p3,p1))};
   if (fabs(r) < EPS) return 0:</pre>
   line 11, 12:
   dbl ratio = dist(p1, p2) / dist(p1, p3);
   point p = translate(p2, scale(to_vec(p2, p3), ratio / (1
        \hookrightarrow + ratio))):
   11 = line_2points(p1, p);
   ratio = dist(p2, p1) / dist(p2, p3);
   p = translate(p1, scale(to_vec(p1, p3), ratio / (1 +
        → ratio)));
   12 = line_2points(p2, p);
   ctr = find_intersection(11, 12);
   return 1:
// trova raggio circonferenza circoscritta al triangolo,
    → passare dist() lati
dbl r circumcircle(double ab, double bc, double ca) {
   return ab * bc * ca / (4.0 * triangle_area(ab, bc, ca));
// perimetro di un poligono
dbl perimeter(const vector <point> &P) {
   dbl result = 0.0:
   for(int i=0;i<sz(P)-1;i++) result += dist(P[i],P[i+1]);</pre>
   return result:
```

```
// area di un poligono
dbl area(const vector <point> &P) {
   dbl result=0.0,x1,x2,y1,y2;
   result = P[0].y*P.back().x - P[0].x*P.back().y; // bug
        → fix wrt notebook
   for(int i=0:i<sz(P)-1:i++) {</pre>
       x1 = P[i].x: x2 = P[i+1].x:
       v1 = P[i].v; v2 = P[i+1].v;
       result += (x1 * y2 - x2 * y1);
   return fabs(result) / 2.0:
// controlla se un poligono e' convesso, potrebbe dare
    → problemi con lati collineari
bool is convex(const vector <point> &P) {
   int s = sz(P):
   if(s <= 3) return false:</pre>
   bool is_left = ccw(P[0],P[1],P[2]);
   for(int i=1:i<s-1:i++)</pre>
       if((ccw(P[i], P[i+1], P[(i+2) == s ? 1 : i+2]) !=
            return true;
// controlla se un punto pt e' in un poligono P
bool in_polygon(point pt, const vector <point> &P) {
   if(!sz(P)) return false;
   dbl sum = 0:
   for(int i=0;i<sz(P)-1;i++) {</pre>
       if(ccw(pt,P[i],P[i+1])) sum += angle(P[i],pt,P[i+1]);
       else sum -= angle(P[i],pt,P[i+1]);
   return (fabs(fabs(sum) - 2*PI) < EPS);</pre>
// punto di intersezione tra linea e segmento
point line_intersect_seg(point p, point q, point A, point B)
    \hookrightarrow {
   dbl a = B.v - A.v:
   dbl b = A.x - B.x:
   dbl c = B.x * A.y - A.x - B.y;
   dbl u = fabs(a * p.x + b * p.y + c);
   dbl v = fabs(a * q.x + b * q.y + c);
   return point((p.x * v + q.x * u) / (u+v), (p.y * v + q.y
        \hookrightarrow * u) / (u+v));
```

#### HeavyLightDecomposition.cpp

Aggiungere...

## Hungarian.cpp

```
// the following code is copied from https://www.topcoder.com
    ← /community/competitive-programming/tutorials/
    → assignment-problem-and-hungarian-algorithm/ and
    \hookrightarrow modified
class HungarianMaxMatch{
public:
   typedef long long 11;
   typedef vector<ll> v1;
   typedef vector<vl> vvl;
   #define int 11
   #define N 500 //max number of vertices in one part
   // #define INF 100000000 //just infinity
   #define INF 100000000000 //just infinity
   int cost[N][N]; //cost matrix
   int n, max_match; //n workers and n jobs
   int lx[N], ly[N]; //labels of X and Y parts
   int xy[N]; //xy[x] - vertex that is matched with x,
   int yx[N]; //yx[y] - vertex that is matched with y
   bool S[N], T[N]; //sets S and T in algorithm
   int slack[N]; //as in the algorithm description
   int slackx[N]; //slackx[y] such a vertex, that
```

```
// l(slackx[y]) + l(y) - w(slackx[y],y) = slack[y]
int prev[N]; //array for memorizing alternating paths
int ww; //weight of the optimal matching
void init_labels()
   memset(lx, 0, sizeof(lx));
   memset(ly, 0, sizeof(ly));
   for (int x = 0; x < n; x++)
   for (int y = 0; y < n; y++)
   lx[x] = max(lx[x], cost[x][y]);
void augment() //main function of the algorithm
   if (max_match == n) return; //check wether matching is
        → already perfect
   int x, y, root; //just counters and root vertex
   int q[N], wr, rd; //q - queue for bfs, wr,rd - write
        \hookrightarrow and read
   //pos in queue
   wr = rd = 0;
   memset(S, false, sizeof(S)); //init set S
   memset(T, false, sizeof(T)); //init set T
   memset(prev, -1, sizeof(prev)); //init set prev - for

    → the alternating tree

   for (x = 0; x < n; x++) //finding root of the tree
   if (xy[x] == -1)
   {
   q[wr++] = root = x;
   prev[x] = -2;
   S[x] = true;
   break;
   for (y = 0; y < n; y++) //initializing slack array
   slack[v] = lx[root] + lv[v] - cost[root][v];
   slackx[y] = root;
   }
   //second part of augment() function
   while (true) //main cycle
       while (rd < wr) //building tree with bfs cycle
       x = q[rd++]; //current vertex from X part
       for (y = 0; y < n; y++) //iterate through all

    ⇔ edges in equality graph

       if (cost[x][y] == lx[x] + ly[y] && !T[y])
       if (yx[y] == -1) break; //an exposed vertex in Y
            → found, so
       //augmenting path exists!
       T[y] = true; //else just add y to T,
       q[wr++] = yx[y]; //add vertex yx[y], which is
```

```
→ matched
   //with y, to the queue
   add_to_tree(yx[y], x); //add edges (x,y) and (y,yx
        \hookrightarrow [v]) to the tree
   if (y < n) break; //augmenting path found!</pre>
   if (y < n) break; //augmenting path found!</pre>
   update_labels(); //augmenting path not found, so
        → improve labeling
   wr = rd = 0;
   for (y = 0; y < n; y++)
   //in this cycle we add edges that were added to
        \hookrightarrow the equality graph as a
   //result of improving the labeling, we add edge (
        → slackx[y], y) to the tree if
   //and only if !T[y] && slack[y] == 0, also with

    → this edge we add another one

   //(y, yx[y]) or augment the matching, if y was
        → exposed
   if (!T[y] && slack[y] == 0)
   if (yx[y] == -1) //exposed vertex in Y found -

→ augmenting path exists!

   x = slackx[y];
   break;
   }
   else
   T[y] = true; //else just add y to T,
   if (!S[yx[y]])
   q[wr++] = yx[y]; //add vertex yx[y], which is
        → matched with
   //y, to the queue
   add_to_tree(yx[y], slackx[y]); //and add edges (x,
        \hookrightarrow y) and (y,
   //yx[y]) to the tree
   }
   }
   if (y < n) break; //augmenting path found!</pre>
if (y < n) //we found augmenting path!
   max_match++; //increment matching
   //in this cycle we inverse edges along augmenting
   for (int cx = x, cy = y, ty; cx != -2; cx = prev[
        \hookrightarrow cx], cy = ty)
   ty = xy[cx];
   yx[cy] = cx;
   xy[cx] = cy;
```

```
}
       augment(); //recall function, go to step 1 of the
            → algorithm
}//end of augment() function
void update_labels()
{
   int x, y, delta;
   delta = INF; //init delta as infinity
   for (y = 0; y < n; y++) //calculate delta using slack
   if (!T[v])
   delta = min(delta, slack[y]);
   for (x = 0; x < n; x++) //update X labels
   if (S[x]) lx[x] -= delta;
   for (y = 0; y < n; y++) //update Y labels
   if (T[y]) ly[y] += delta;
   for (y = 0; y < n; y++) //update slack array
   if (!T[v])
   slack[v] -= delta;
}
void add_to_tree(int x, int prevx)
//x - current vertex, prevx - vertex from X before x in

    → the alternating path,

//so we add edges (prevx, xy[x]), (xy[x], x)
   S[x] = true; //add x to S
   prev[x] = prevx; //we need this when augmenting
   for (int y = 0; y < n; y++) //update slacks, because</pre>
        \hookrightarrow we add new vertex to S
   if (lx[x] + ly[y] - cost[x][y] < slack[y])
   slack[v] = lx[x] + lv[v] - cost[x][v];
   slackx[y] = x;
   }
int hungarian()
{
   max_match = 0; //number of vertices in current
        → matching
   memset(xy, -1, sizeof(xy));
   memset(yx, -1, sizeof(yx));
   init_labels(); //step 0
   augment(); //steps 1-3
   for (int x = 0; x < n; x++) //forming answer there
   ww += cost[x][xy[x]];
   return ww;
HungarianMaxMatch(vvl& cost_matrix, ll rows, ll columns){
   11 i,j;
   n = max(rows, columns):
```

#### Hungarian-double.cpp

};

```
// the following code is copied from https://www.topcoder.com
    → /community/competitive-programming/tutorials/
    → assignment-problem-and-hungarian-algorithm/ and
    → modified
class HungarianMaxMatch{
public:
    typedef long long 11;
    typedef double ct;
    typedef vector<ct> vc;
   typedef vector<vc> vvc;
    #define int ll
    #define N 500 //max number of vertices in one part
    // #define INF 100000000 //just infinity
    #define INF 100000000000 //just infinity
    ct cost[N][N]; //cost matrix
    int n, max_match; //n workers and n jobs
    ct lx[N], ly[N]; //labels of X and Y parts
   int xy[N]; //xy[x] - vertex that is matched with x,
    int yx[N]; //yx[y] - vertex that is matched with y
   bool S[N], T[N]; //sets S and T in algorithm
    ct slack[N]; //as in the algorithm description
   int slackx[N]; //slackx[v] such a vertex, that
   // l(slackx[y]) + l(y) - w(slackx[y],y) = slack[y]
    int prev[N]; //array for memorizing alternating paths
   ct ww; //weight of the optimal matching
   void init_labels()
       memset(lx, 0, sizeof(lx));
       memset(ly, 0, sizeof(ly));
       for (int x = 0; x < n; x++)
       for (int y = 0; y < n; y++)
       lx[x] = max(lx[x], cost[x][y]);
```

```
void augment() //main function of the algorithm
   if (max_match == n) return; //check wether matching is
        → already perfect
   int x, y, root; //just counters and root vertex
   int q[N], wr, rd; //q - queue for bfs, wr,rd - write
         → and read
   //pos in queue
   wr = rd = 0:
   memset(S, false, sizeof(S)); //init set S
   memset(T, false, sizeof(T)); //init set T
   memset(prev, -1, sizeof(prev)); //init set prev - for
        \hookrightarrow the alternating tree
   for (x = 0; x < n; x++) //finding root of the tree
   if (xy[x] == -1)
   {
       q[wr++] = root = x;
       prev[x] = -2;
       S[x] = true;
       break:
   for (y = 0; y < n; y++) //initializing slack array</pre>
       slack[y] = lx[root] + ly[y] - cost[root][y];
       slackx[v] = root:
   //second part of augment() function
   while (true) //main cycle
       while (rd < wr) //building tree with bfs cycle</pre>
       x = q[rd++]; //current vertex from X part
       for (y = 0; y < n; y++) //iterate through all

    ⇔ edges in equality graph

       if (cost[x][y] == lx[x] + ly[y] && !T[y])
       if (yx[y] == -1) break; //an exposed vertex in Y
            \hookrightarrow found, so
       //augmenting path exists!
       T[y] = true; //else just add y to T,
       q[wr++] = yx[y]; //add vertex yx[y], which is
            → matched
       //with y, to the queue
       add_to_tree(yx[y], x); //add edges (x,y) and (y,yx
            \hookrightarrow [y]) to the tree
       if (y < n) break; //augmenting path found!
       if (y < n) break; //augmenting path found!</pre>
       update_labels(); //augmenting path not found, so
            → improve labeling
       wr = rd = 0;
       for (y = 0; y < n; y++)
       //in this cycle we add edges that were added to
```

```
    → the equality graph as a

       //result of improving the labeling, we add edge (
            \hookrightarrow slackx[v], v) to the tree if
       //and only if !T[y] && slack[y] == 0, also with

    → this edge we add another one

       //(y, yx[y]) or augment the matching, if y was
             → exposed
       if (!T[v] && slack[v] == 0)
       if (yx[y] == -1) //exposed vertex in Y found -
             → augmenting path exists!
       x = slackx[v];
       break:
       else
       T[y] = true; //else just add y to T,
       if (!S[yx[y]])
       q[wr++] = yx[y]; //add vertex yx[y], which is
            \hookrightarrow matched with
       //y, to the queue
       add_to_tree(yx[y], slackx[y]); //and add edges (x,
            \hookrightarrow v) and (v.
        //yx[y]) to the tree
       if (y < n) break; //augmenting path found!
   if (y < n) //we found augmenting path!</pre>
       max_match++; //increment matching
       //in this cycle we inverse edges along augmenting
       for (int cx = x, cy = y, ty; cx != -2; cx = prev[
            \hookrightarrow cx], cy = ty)
       ty = xy[cx];
       yx[cy] = cx;
       xy[cx] = cv;
       augment(); //recall function, go to step 1 of the
            → algorithm
}//end of augment() function
void update_labels()
   int x, y;
   ct delta;
   delta = INF; //init delta as infinity
   for (v = 0; v < n; v++) //calculate delta using slack
```

```
if (!T[v])
   delta = min(delta, slack[v]):
   for (x = 0; x < n; x++) //update X labels
   if (S[x]) lx[x] = delta;
   for (y = 0; y < n; y++) //update Y labels
   if (T[v]) lv[v] += delta;
   for (y = 0; y < n; y++) //update slack array
   if (!T[v])
   slack[v] -= delta:
void add to tree(int x, int prevx)
//x - current vertex, prevx - vertex from X before x in
     \hookrightarrow the alternating path,
//so we add edges (prevx, xy[x]), (xy[x], x)
   S[x] = true; //add x to S
   prev[x] = prevx; //we need this when augmenting
   for (int y = 0; y < n; y++) //update slacks, because
        \hookrightarrow we add new vertex to S
   if (lx[x] + ly[y] - cost[x][y] < slack[y])
   slack[y] = lx[x] + ly[y] - cost[x][y];
   slackx[y] = x;
}
int hungarian()
   max match = 0: //number of vertices in current
        → matching
   memset(xy, -1, sizeof(xy));
   memset(yx, -1, sizeof(yx));
   init_labels(); //step 0
   augment(); //steps 1-3
   for (int x = 0; x < n; x++) //forming answer there
   ww += cost[x][xv[x]];
   return ww;
HungarianMaxMatch(vvc& cost_matrix, ll rows, ll columns){
   11 i.i:
   n = max(rows, columns);
   for(i=columns: i-->rows:)
       for(j=columns; j--;)
           cost[i][j] = 0;
   for(i=rows: i--:){
       for(j=rows; j-->columns;)
           cost[i][j] = 0;
       for(j=columns; j--;)
           cost[i][j] = cost_matrix[i][j];
   hungarian();
#undef int
```

```
#undef N
#undef INF
}:
```

## IndexMap.cpp

```
#include<bits/stdc++.h>
using namespace std:
typedef long long 11;
typedef 11 K;
typedef 11 V;
#define succ(x)((x)+1)
#define prec(x)((x)-1)
const K dummyk = -1;
11 \ \text{accmod} = 0:
K tofind = dummyk;
11 \text{ kfound} = 0;
K imgk, imok;
vector<K> imh, imhi, imhf;
11 \text{ imkpos} = 0;
typedef pair<pair<11,11>,V> IMV;
typedef map<K,IMV,bool(*)(K, K)> mymap;
mymap indexmap;
bool imcmp (K lhs, K rhs) {
   if(accmod == 0){
       return lhs < rhs:
   if(accmod == 1){
       11 tk = lhs ^ rhs ^ imok;
       if(imh[imh.size()-1] != tk) imh.push_back(tk);
       if(kfound && tk!=tofind){
           imgk = tk;
           kfound = 0:
           tofind = dummvk:
       }else if(lhs == tofind || rhs == tofind){
           kfound = 1:
       return ((lhs==imok)?imgk:lhs) < ((rhs==imok)?imgk:rhs)</pre>
   11 tk = lhs ^ rhs ^ dummyk;
   if(imh[imh.size()-1] == tk){
       accmod = 0;
       imkpos += indexmap.find(tk)->second.first.first + 1;
       accmod = 2;
   ll sl:
   imh.push_back(tk);
```

```
accmod = 0:
    sl = indexmap.find(tk)->second.first.first;
    if(sl == imkpos){
       kfound = tk;
        return false;
    }
    accmod = 2:
    if(sl < imkpos){</pre>
       imkpos -= sl + 1:
       return rhs == dummyk;
    }
    return lhs == dummvk:
bool(*ptcmp)(K,K) = imcmp;
mymap imtmpm(ptcmp);
mymap::iterator node, nodec;
bool testc(K k, K kc){
    for(K x : imh){
       if(x == k) return true;
       if(x == kc) return false:
    }
    return false:
}
11 updwc(K k, K kc){
    imgk = imok = k;
    node = indexmap.find(k);
    // child
    imgk = imok = kc;
    tofind = k:
    kfound = 0:
    imh.clear();
    imh.push_back(dummyk);
    nodec = indexmap.find(imgk);
    imok = imgk;
    tofind = dummyk;
    kfound = 0;
    imh.clear():
    imh.push_back(dummyk);
    nodec = indexmap.find(imgk);
    tofind = dummvk:
    kfound = 0;
    if(nodec!=indexmap.end() && testc(k, nodec->first)){
        return nodec->second.first.second:
    }
    return 0:
}
void updw(K k){
    node->second.first.first = updwc(k, prec(k));
    node->second.first.second = 1 + node->second.first.first
        \hookrightarrow + updwc(k, succ(k));
```

```
}
void insert(K k, V v){
    accmod = 1;
    imh.clear();
   imh.push_back(dummyk);
   imgk = imok = k:
    indexmap[k] = IMV(\{\{0,0\},v\});
   imhi = imh:
    imh.clear():
   imh.push_back(dummyk);
    imgk = imok = k:
    indexmap.find(k);
    imhf = imh;
    set<K> hs(imhf.begin(), imhf.end());
    for(ll i=imhi.size(); --i; ) if(!hs.count(imhi[i])){
       updw(imhi[i]);
   for(ll i=imhf.size(); --i; ){
       updw(imhf[i]):
   }
    accmod = 0;
K iloc(ll pos){
   11 r;
    accmod = 2;
    imkpos = pos;
    imh.clear();
   imh.push_back(dummyk);
   indexmap.find(dummvk):
    accmod = 0:
    r = kfound:
   kfound = 0:
    return r;
V get(K k){
    return indexmap.find(k)->second.second;
int test(const vector<K>& vk. const vector<K>& v){
   for(K kk : vk){
       insert(kk, kk):
       iloc(kk);
       // for(K k : vk){
       // node = indexmap.find(k):
       // cout << node->first << ', ' << node->second.first.
            → first << ' ' << node->second.first.second <<</pre>
            → '\n':
       // if(k == kk) break:
       // cout << '\n';
   K kk:
```

```
for(ll i=0; i<indexmap.size(); i++){</pre>
        kk = iloc(i):
        if(kk != v[i] || get(kk) != v[i]) return 0;
    }
    return 1;
}
int main(){
    indexmap = imtmpm:
    vector<K> v, vk({1,2,3,5,7,8,9,11,13});//,14,15});
    cerr << vk.size() << '\n';</pre>
    v = vk:
    sort(v.begin(), v.end());
    do{
        indexmap.clear();
        if(!test(vk. v)){
            for(ll x : vk) cout << x << ',';</pre>
            cout << '\n':
        }
        // break;
    }while(next_permutation(vk.begin(), vk.end()));
    return 0;
}
KMP.cpp
int n,i,Q,T,m,j,k,x,y,b[maxn];
string t,p;
void preprocessing(){
    int i=0,j=-1;b[0]=-1;
    while(i<m){</pre>
        while(j>=0 && p[i]!=p[j])j=b[j];
        i++; j++;
        b[i]=j;
    }
void search(){
    int i=0, j=0;
    while(i<n){</pre>
        while(j>=0 && t[i]!=p[j])j=b[j];
        i++; j++;
        if(j==m){
            cout << "P_{\sqcup} found_{\sqcup} at_{\sqcup} index_{\sqcup \sqcup} "<< i-j << ln;
}
Kruskal.cpp
```

#include "DSU.cpp"

```
if(e == -1){
                                                                                                                                              build(rc(p), ravg(l,r), r)
template<class T> class Kruskal{
                                                                             e = edges.size():
                                                                                                                                          ):
#define e (*pe)
                                                                                                                                       }
public:
                                                                                                                                       void update(ll p, ll v, ll l, ll r){
                                                                         ten.assign(_e, 1);
   typedef long long 11;
                                                                         *this = Kruskal(0, edges, v, ten, cc, sorted, _e);
                                                                                                                                           if(v != LZD){
   typedef std::vector<ll> vl;
                                                                                                                                               st[p] = lz2st(st[p], v, width(l,r));
   typedef std::pair<ll,ll> pl;
                                                                     Kruskal(vptel& sorted_edges, ll v, const vb& enabled, ll
                                                                                                                                               updateson(lc(p), v):
                                                                          \hookrightarrow cc = 1, ll _e = -1){
   typedef std::pair<T,pl> ptel;
                                                                                                                                              updateson(rc(p), v);
   typedef std::vector<ptel> vptel;
                                                                         *this = Kruskal(0, sorted edges, v, enabled, cc, true.
                                                                                                                                              lz[p] = LZD:
   typedef std::vector<bool> vb;
                                                                              \hookrightarrow _e);
                                                                                                                                           }
                                                                                                                                       }
   vb used;
   vl tree_edges;
                                                                     ll get tree(ll v){
                                                                                                                                       11 rqr(ll p, ll l, ll r){
                                                                         return dsu.findSet(v);
                                                                                                                                           update(p, lz[p], l, r);
   T cost;
                                                                                                                                           if(i>r || 1>j) return 0;
   ll ncc;
                                                                     bool is_same_tree(ll u, ll v){
                                                                                                                                           if(i<=l && r<=j) return st[p];</pre>
private:
   bool all_en = false;
                                                                         return dsu.isSameSet(u,v);
                                                                                                                                           return stadd(
                                                                     }
                                                                                                                                              rqr(lc(p), l, lavg(l,r)),
   11 n.m:
                                                                 #undef e
                                                                                                                                              rqr(rc(p), ravg(l,r), r)
   vb en:
                                                                 };
                                                                                                                                           );
   vptel* pe;
   DSU dsu:
   Kruskal(char dummy_pvt, vptel& edges, 11 v, const vb&
                                                                                                                                       11 rur(11 p, 11 1, 11 r){

→ enabled, ll cc = 1, bool sorted = false, ll _e =
                                                                 LazySegmentTree.cpp
                                                                                                                                           update(p, lz[p], l, r);
                                                                                                                                           if(i>r || 1>j) return st[p];
        \hookrightarrow -1){
      11 i;
                                                                                                                                           if(i<=1 && r<=j){</pre>
                                                                 class ST{
       pe = &edges;
                                                                                                                                               update(p, v, l, r);
                                                                 public:
                                                                                                                                              return st[p];
       n = v;
                                                                     typedef long long 11;
       if(_e == -1){
                                                                     typedef std::vector<ll> vl:
          m = e.size():
                                                                                                                                           return st[p] = stadd(
                                                                 private:
       }else{
                                                                                                                                              rur(lc(p), l, lavg(l,r)),
                                                                     // functions for range sum query with incremental range
                                                                                                                                              rur(rc(p), ravg(1,r), r)
          m = _e;
                                                                          → updates (increment all elements between 3 and 7 by
                                                                                                                                           ):
                                                                                                                                       }
       if(!sorted){
                                                                     // these must be adapted to the actual problem
                                                                                                                                   public:
           sort(e.begin(), e.end());
                                                                     #define stadd(left.right) ((left)+(right))
       }
                                                                                                                                       ST(const vl& a, ll lazv default value=0){
                                                                     // stadd is used to add results of subrange queries in st
                                                                                                                                           // LZD value is used to determine whether there is
       en = enabled;
                                                                     #define lzadd(st_old,up_val) ((st_old)+(up_val))
       cost = 0:
                                                                                                                                                → already a value that shuld be updated (lazily)
                                                                     // lzadd is used to add a new lazy value (in lz) where an
       used.assign(m, false);
                                                                                                                                           // each query and update the lazy value is checked,
                                                                          → old one is already present
                                                                                                                                                \hookrightarrow and if it is LZD no updates occur
       dsu = DSU(n):
                                                                     #define lz2st(st_old, lz_val, rng_width) ((st_old)+(
       for(i=0; i<m && cc!=dsu.cc; i++){</pre>
                                                                                                                                           a = \&_a;
                                                                          → lz_val)*(rng_width))
           if(en[i] && !dsu.isSameSet(e[i].second.first, e[i
                                                                                                                                           LZD = lazy_default_value;
                                                                     // lz2st is used to update st with lazy value in lz,
               → ].second.second)){
                                                                                                                                           n = _a.size();
                                                                          → rngwidth is the width of the range being updated
              dsu.unionSet(e[i].second.first, e[i].second.
                                                                                                                                           st.resize(n<<2):
                                                                     // then lz_val is automatically cleared
                   → second);
                                                                                                                                           lz.assign(n<<3, LZD);</pre>
                                                                     #define lc(x) ((x)<<1)
              used[i] = true:
                                                                                                                                           build(1, 0, n-1):
                                                                     #define rc(x) (lc(x)+1)
              tree_edges.push_back(i);
                                                                     #define lavg(x,y) (((x)+(y))>>1)
              cost += e[i].first;
                                                                                                                                       11 rq(11 1, 11 r){
                                                                     #define ravg(x,y) (lavg(x,y)+1)
          }
                                                                                                                                           i = 1:
                                                                     #define width(1,r) ((r)-(1)+1)
      }
                                                                                                                                           j = r;
                                                                     #define updateson(ps,v) lz[ps]=lzadd(lz[ps],v)
       ncc = dsu.cc:
                                                                                                                                           return rqr(1, 0, n-1);
                                                                     ll n, i, j, v, LZD;
                                                                     const vl* a;
public:
                                                                                                                                       void ru(ll 1, ll r, ll newval){
                                                                     vl st. lz:
   Kruskal(){}
                                                                                                                                           v = newval:
                                                                     11 build(11 p, 11 1, 11 r){
   Kruskal(vptel& edges, ll v, ll cc = 1, bool sorted =
                                                                                                                                           i = 1;
                                                                         if(1 == r) return st[p] = (*a)[1];
        \hookrightarrow false, ll _e = -1){
                                                                                                                                           j = r;
                                                                         return st[p] = stadd(
       vb ten:
                                                                                                                                           rur(1, 0, n-1):
                                                                            build(lc(p), l, lavg(l,r)),
```

```
}
                                                                  LCA(const vvt& tree, ll vertex = 0, ll dimension = -1,
                                                                       → fetnt edge to node = def etn){
   #undef updateson
   #undef width
                                                                     pt = &tree:
                                                                     if(dimension == -1){}
   #undef ravg
   #undef lavg
                                                                         n = tree.size();
   #undef rc
                                                                     }else{
   #undef lc
                                                                         n = dimension:
};
                                                                     }
                                                                     etn = edge_to_node;
                                                                     e.resize(n<<1):
                                                                     1.resize(n<<1);
LCA.cpp
                                                                     h.assign(n, -1);
                                                                     p.resize(n);
#include "LazySegTree.cpp"
                                                                     p[vertex] = vertex;
                                                                     es = 0:
template<class T> class LCA{
                                                                     dfs(vertex, 0):
#define t (*pt)
                                                                     st = LazySegTree<pl>(1, pl(-1,(11)1e18), lmin);
public:
   typedef long long 11;
                                                                  11 lca(ll u, ll v){
   typedef std::vector<ll> vl;
                                                                     if(h[u] < h[v])
   typedef std::pair<ll,ll> pl;
                                                                         return e[st.range_query(h[u], h[v]).first];
   typedef std::vector<pl> vpl;
   typedef std::vector<T> vt;
                                                                     return e[st.range_query(h[v], h[u]).first];
   typedef std::vector<vt> vvt;
   typedef std::function<ll(const T&)> fetnt;
                                                                  11 depth(ll u){
   static inline 11 def etn(const T& e){
                                                                     return l[h[u]].second;
       return e;
   }
                                                                  ll distance(ll u. ll v){
private:
                                                                     ll a = lca(u,v);
   LazySegTree<pl> st;
                                                                     return depth(u) + depth(v) - (depth(a)<<1);</pre>
   const vvt* pt;
   ll n, es;
                                                                  11 parent(11 v, 11 d){
   vl e, h, p;
                                                                     while (d--) v = p[v];
   vpl 1;
                                                                     return v:
   fetnt etn;
   static pl& lmin(pl& r, const pl& a, const pl& b){
                                                                  ll parent(ll v){
       if(a.second < b.second) return r = a;</pre>
                                                                     return p[v];
       return r = b;
   }
                                                                  11 low_midpoint(ll u, ll v){
   void dfs(ll v, ll d){
                                                                     static ll a, d0, d1;
      11 u:
                                                                     a = lca(u, v):
      h[v] = es:
                                                                     d0 = distance(a, u):
      l[es] = pl(es,d);
                                                                     d1 = distance(a, v);
      e[es++] = v:
                                                                     if(d0 < d1) return parent(v, (d0+d1)>>1);
      for(const T& ed : t[v]){
                                                                     return parent(u, (d0+d1)>>1);
          u = etn(ed):
          if(h[u] == -1){
                                                              #undef t
              p[u] = v;
                                                              };
              dfs(u, d+1);
             l[es] = pl(es,d);
              e[es++] = v;
                                                              MinCostMaxFlow.cpp
          }
      }
   }
                                                              public:
                                                              #define mcmf eu first.first
```

LCA(){}

#define \_\_mcmf\_ev first.second

```
#define __mcmf_ec second.second
#define mcmf ecost second.first
#define __mcmf_ncost first.first
#define __mcmf_nflow first.second
#define __mcmf_nvisited second.first
#define __mcmf_nparent second.second
template <class W,class T> class MinCostMaxFlow{
public:
   typedef long long 11;
   typedef pair<11,11> pl;
   typedef pair<W,T> pwt;
   typedef pair<pwt,pl> mcmf_node;
   typedef pair<pl,pwt> mcmf_edge;
   typedef pair<T,ll> ptl;
   typedef pair<pwt,ll> pwtl;
   T total_flow = 0;
   W total cost = 0:
   vector<T> rf;
private:
   11 \text{ n, m, m2, s, t, i, r = 0}
   vector<mcmf_node> v;
   vector<mcmf_edge> e;
   vector<vector<pl>>> g;
   T fm = 0:
   T vis(){
       priority_queue<pwtl> q;
       11 x, y;
       T f = 0, tf = 0;
       W c, tc;
       v[s]. mcmf nvisited = ++r:
       v[s].__mcmf_ncost = 0;
       v[s].__mcmf_nflow = fm-total_flow;
       q.push(pwtl(pwt(0,fm-total_flow), s));
       while(!q.empty()){
           c = -q.top().first.first;
           f = q.top().first.second;
           x = q.top().second;
           q.pop();
           if(v[x].__mcmf_ncost != c || v[x].__mcmf_nflow !=
               \hookrightarrow f) continue:
           for(pl yy : g[x]){
              y = yy.first;
              tc = c + e[yy.second].__mcmf_ecost;
              tf = min(f,rf[yy.second]);
              if(
                  rf[yy.second]!=(T)0 && (
                      v[y].__mcmf_nvisited<r ||
                      v[v]. mcmf ncost>tc ||
                      (v[y].\_mcmf\_ncost==tc \&\& v[y].
                           -- __mcmf_nflow<tf)</pre>
                  )
              ){
                  v[y].__mcmf_nvisited = r;
                  v[y].__mcmf_nparent = yy.second;
```

```
v[y].__mcmf_nflow = tf;
                  v[v]. mcmf ncost = tc:
                  q.push(pwtl(pwt(-tc, tf), y));
          }
      }
       if(v[t].__mcmf_nvisited == r){
          f = v[t].__mcmf_nflow;
           total cost += v[t]. mcmf ncost * f:
           for(x=t; x!=s; x=e[y].__mcmf_eu){
              v = v[x].__mcmf_nparent;
              rf[v] -= f:
              rf[(y < m)?(y+m):(y-m)] += f;
          return f;
       }
       return (T)0;
   }
public:
   MinCostMaxFlow(
      11 _v,
       11 _e,
       const vector<mcmf_edge>& edges,
      11 \text{ source} = 0,
       11 \sin k = -1.
       const T& flow_max = __MCMF_FLOW_MAX
   ){
       n = v;
       m = _e;
       m2 = m << 1;
       e = edges;
       e.resize(m2);
       for(i=m: i--:){
           e[i+m]. mcmf eu = e[i]. mcmf ev:
           e[i+m].__mcmf_ev = e[i].__mcmf_eu;
           e[i+m]. mcmf ecost = -e[i]. mcmf ecost:
      }
       s = source:
       if(sink == -1){
           t = n-1;
       }else{
           t = sink:
       fm = flow_max;
       v.assign(n, mcmf_node(pwt((W)1e12, (T)0), pl(0,0)));
       v[s]._mcmf_ncost = 0;
       v[s]. mcmf nflow = fm:
       rf.resize(m2);
       g.assign(n, vector<pl>());
       for(i=0: i<m: i++){</pre>
          rf[i] = e[i].__mcmf_ec;
           g[e[i].__mcmf_eu].push_back(pl(e[i].__mcmf_ev, i))
       for(i=m: i<m2: i++){</pre>
```

### Nim game e riconducibili

Considera n pile di oggetti. A e B giocano togliendo quanti oggetti vogliono da una di queste pile. Chi toglie l'ultimo oggetto rimanente perde, l'altro vince.

Chiamiamo vincente uno stato del gioco in cui la xor-sum (d'ora in poi chiamata s) del numero di oggetti nelle pile è pari a zero,  $a_i, 1 \le i \le n$  è il numero di elementi nella i-esima pila:

- stato vincente:  $a_1 \oplus a_2 \oplus ... \oplus a_n \neq 0$
- stato perdente:  $a_1 \oplus a_2 \oplus ... \oplus a_n = 0$

Ciò è valido anche nel caso del Nim Game modificato in cui si possono aggiungere elementi. **Importante:** il gioco deve continuare ad essere aciclico.

#### Teorema di Sprague-Grundy e Grundy's values

Considera uno stato v di un gioco Nim-like e  $v_i$  tutti i possibili stati del gioco raggiungibili da v  $(i \in 1, 2, ..., k, k \le 0)$ . A questo stato possiamo associare un Nim-game equivalente con una pila di altezza x. x } è chiamato Grundu's value associato allo stato v.

x può essere calcolato ricorsivamente:

```
x = mex\{x_1, ..., x_k\}
```

dove:  $x_i$  è il Grundy's value associato allo stato  $v_i$ ; la funzione mex identifica il  $minimum\ excludant$ .

Per visualizzare il gioco può essere utilizzato un albero, le cui foglie sono gli stati perdenti e avranno Grundy's value uguale a 0.

```
/* considerare come *base* il seguente codice.
  * state_t: tipo della variabile dello stato
  * der_states: vector con stati derivati dallo stato corrente
  */

map <state_t, int> dp;
map <state_t, vector <state_t> > der_states

int grundy_value(state_t state) {
    if(dp[state]) {
        return dp[state];
    }
}
```

```
set <int> x;
for(auto i:der_states[state]) {
     x.insert(grundy_value(i, der_states[state]));
}
dp[state] = mex(x);
return dp[state];
```

### node\_split.cpp

```
typedef long long 11;
typedef std::pair<ll,ll> pl;
#define plT std::pair<pl,T>
#define vplt std::vector<plT>
#define ic(x) ((x)<<1)
#define og(x) (ic(x)^1)
template < class T > void node_split(vplt& new_edges, const vplt
     → & edges, ll v, const std::vector<T>& node_cap, ll&
     → source. ll& sink){
   new_edges.resize(0);
   for(ll i=v; i--;){
       new_edges.push_back(plT(pl(ic(i),og(i)),node_cap[i]));
   for(const plT& x : edges){
       new edges.push back(plT(pl(og(x.first.first), ic(x.

→ first.second)). x.second)):
   source = og(source);
   sink = ic(sink);
#undef og
#undef ic
#undef vplt
#undef plT
```

## Rabin\_karp.cpp

```
Tarjan.cpp
   vector<long long> h(T + 1, 0);
                                                                                                                                              }else{
   for (int i = 0; i < T; i++)</pre>
                                                                                                                                                  n = v;
                                                                   template < class T> class Tarian {
       h[i+1] = (h[i] + (t[i] - 'a' + 1) * p_pow[i]) % m;
                                                                   #define G (*pg)
   long long h_s = 0;
                                                                   public:
   for (int i = 0; i < S; i++)</pre>
                                                                       typedef long long 11;
       h_s = (h_s + (s[i] - 'a' + 1) * p_pow[i]) \% m;
                                                                                                                                              lk.resize(n):
                                                                       typedef std::vector<ll> vl;
   vector<int> occurences;
                                                                                                                                              ssc.resize(n);
                                                                       typedef std::vector<vl> vvl;
   for (int i = 0: i + S - 1 < T: i++) {
                                                                                                                                              sscs.resize(0):
                                                                       typedef std::vector<bool> vb;
       long long cur_h = (h[i+S] + m - h[i]) % m;
                                                                                                                                              vis = 0:
                                                                       typedef std::stack<ll> sl;
       if (cur_h == h_s * p_pow[i] % m)
                                                                                                                                              nssc = 0;
                                                                       typedef std::vector<T> vt;
           occurences.push_back(i);
                                                                       typedef std::vector<vt> vvt;
   }
                                                                                                                                                  dfs(i);
                                                                       typedef std::function<ll(const T&)> fetnt;
                                                                                                                                              }
   return occurences;
                                                                       vl ssc;
                                                                                                                                          vvl& get_sscs(){
                                                                       static ll def_etn(const T& edge){
                                                                          return edge;
Suffix_array.cpp
                                                                      }
                                                                   private:
                                                                       vvl sscs;
                                                                                                                                                  }
int n,i,Q,T,j,k,t,x,y;
                                                                      ll n, vis;
                                                                                                                                              }
int ra[maxn],sa[maxn],tmpra[maxn],tmpsa[maxn],c[maxn];
                                                                       vl id. lk:
                                                                                                                                              return sscs;
string s;
                                                                       vb os:
                                                                       sl s;
                                                                                                                                      #undef G
void counting(int k){
                                                                       const vvt* pg;
                                                                                                                                      };
   int i,sum,maxi=max(300,n);
                                                                       fetnt etn;
   for(i=0:i<maxn:i++)c[i]=0:</pre>
                                                                       void dfs(ll v){
   for(i=0;i<n;i++)c[i+k<n ? ra[i+k]:0]++;</pre>
                                                                          static 11 t;
                                                                                                                                      Trie.cpp
   for(i=sum=0;i<maxi;i++){</pre>
                                                                          11 u;
       int t=c[i]:
                                                                          id[v] = vis:
       c[i]=sum;
                                                                          lk[v] = vis++;
       sum+=t;
                                                                          s.push(v):
                                                                                                                                      typedef vector<11> v1;
                                                                          os[v] = true:
                                                                                                                                      typedef vector<vl> vvl:
   for(i=0;i<n;i++){</pre>
                                                                          for(const T& e : G[v]){
       tmpsa[c[sa[i]+k <n ? ra[sa[i]+k]:0]++]=sa[i];</pre>
                                                                              u = etn(e):
   }
                                                                              if(id[u] == -1) dfs(u);
                                                                                                                                      class Trie{
   for(i=0;i<n;i++)sa[i]=tmpsa[i];</pre>
                                                                              if(os[u] && lk[v]>lk[u]) lk[v] = lk[u];
                                                                                                                                      private:
                                                                          }
                                                                                                                                          11 states:
                                                                          if(id[v] == lk[v]){
                                                                                                                                          11 state;
void build(){
                                                                              do{
                                                                                                                                          vvl trie:
   int i.k.r:
                                                                                  t = s.top();
                                                                                                                                          vl fail:
   for(i=0;i<n;i++)ra[i]=s[i],sa[i]=i;</pre>
                                                                                                                                          vvl leaves;
                                                                                  s.pop();
   for(k=1:k<n:k<<=1){
                                                                                  os[t] = false:
                                                                                                                                      public:
       counting(k):
                                                                                  ssc[t] = nssc;
                                                                                                                                          Trie(){}
       counting(0);
                                                                              }while(t != v);
       tmpra[sa[0]]=r=0;
                                                                                                                                              ll tstate:
                                                                              nssc++;
       for(i=1;i<n;i++){</pre>
                                                                          }
                                                                                                                                              state = 0;
           tmpra[sa[i]] = (ra[sa[i]] == ra[sa[i-1]] && ra[sa[i] +
                                                                      }
                                                                                                                                              queue<11> fq;
                \hookrightarrow k] == ra[sa[i-1]+k] )? r:++r;
                                                                   public:
                                                                                                                                              states = 1:
       for(i=0:i<n:i++)ra[i]=tmpra[i]:</pre>
                                                                       Tarjan(const vvt& graph, ll v = -1, fetnt edge_to_node =
       if(ra[sa[n-1]]==n-1)break;
                                                                            → def_etn){
                                                                          pg = &graph;
```

etn = edge\_to\_node;
if(v == -1){

```
n = G.size():
       id.assign(n, -1);
       os.assign(n, false);
       for(ll i=0: i<n: i++) if(id[i] == -1){
       if(!sscs.size()){
          sscs.resize(nssc):
          for(ll i=0; i<n; i++){</pre>
              sscs[ssc[i]].push back(i):
#define __TRIE_AB_SIZE 256
typedef vector<string> vs;
   Trie(const vs& dictionary){
       trie.push_back(vl());
       trie[0].assign(__TRIE_AB_SIZE, 0);
       leaves.push_back(vl());
       for(ll s=0; s<dictionary.size(); s++){</pre>
           // s is used later as an integer, don't change
               → style
```

```
for(auto c : dictionary[s]){
       if( !(tstate = trie[state][c]) ){
           tstate = trie[state][c] = states++;
           trie.push_back(vl());
           trie[tstate].assign(__TRIE_AB_SIZE, 0);
           leaves.push_back(v1());
       state = tstate;
   leaves[state].push_back(s);
   state = 0;
}
// find fails
fail.resize(states);
for(11 c=0; c<__TRIE_AB_SIZE; c++){</pre>
   if(trie[0][c]){
       fail[trie[0][c]] = 0;
       fq.push(trie[0][c]);
   }
}
while(!fq.empty()){
    state = fq.front();
```

```
fq.pop();
      for(11 c=0; c<__TRIE_AB_SIZE; c++) if(trie[state][</pre>
           tstate = fail[state];
          while(tstate && !trie[tstate][c]){
              tstate = fail[tstate];
          if(trie[tstate][c]){
             fail[trie[state][c]] = trie[tstate][c];
             for(ll 1 : leaves[trie[tstate][c]]){
                 leaves[trie[state][c]].push_back(1);
             }
          }else{
             fail[trie[state][c]] = 0;
          fq.push(trie[state][c]);
   }
   state = 0; // reset_state();
void reset_state(){
                                                           };
   state = 0;
```

```
}
11 get_initial_state(){
   return 0;
}
const vl& get_leaves(ll state){
   return leaves[state];
11 next_state(ll state, char c){
   while(state && !trie[state][c]){
       state = fail[state];
   }
   if(trie[state][c]){
       return trie[state][c];
   }
   return state;
}
const vl& next_leaves(char c){
   // return get_leaves( state = next_state(state, c) );
   return leaves[ state = next_state(state, c) ];
```