## **Boolean algebra and logic gates**

A and B can be equal 0 or 1.

 $\bar{A}$  = not A, contradiction of A, A reversed

Statement 1. - Commutative Law

A+B = B+A A\*B = B\*A

**Statement 2.** - Associative Law

(A+B)+C=A+(B+C)

Statement 3.

A\*(B+C) = A\*B+A\*CA+(B\*C) = (A+B)\*(A+C)

Statement 4. - Idempotent Law

A+A=AA\*A=A

Statement 5.

 $A*B+A*\bar{B} = A$ (A+B)\*(A+B) = A

Statement 6. - Absorption Law

A+A\*B = AA\*(A+B) = 1 Statement 7. - Identity Law

0+A=A0\*A=0

Statement 8.

1+A=11\*A=A

Statement 9.

 $\bar{A}+A=1$  $\bar{A}*A=0$ 

Statement 10.

 $A+\bar{A}*B = A+B$  $A*(\bar{A}+B) = A*B$ 

Statement 11. - De Morgan's Law

 $\frac{\overline{A+B}}{A*B} = \overline{A}*\overline{B}$  $\overline{A*B} = \overline{A}+\overline{B}$ 

Y is the result of letting A and B through a given logic gate.

OR			AND				XOR		NOT	
Y = A+B		Y = A*B			Y	$Y = A^*\overline{B} + \overline{A}^*B$			$Y = \overline{A}$	
Α	В	Y	Α	В	Υ	Α	В	Υ	Α	В
0	0	0	0	0	0	0	0	0	0	1
0	1	1	0	1	0	0	1	1	1	0
1	0	1	1	0	0	1	0	1		
1	1	1	1	1	1	1	1	0		
0	$\sum$	<b>&gt;</b> -0	8=		<b>)</b> —0	8		<b>&gt;</b>		
NOR $Y = \overline{A + B}$			NAND Y = <u>A * B</u>			XNOR $Y = A^*B + \overline{A}^*\overline{B}$				
Α.	В	Y	Α.	В	Υ	Α	В	Υ		
0	0	1	0	0	1	0	0	1		
0	1	0	0	1	1	0	1	0		
1	0	0	1	0	1	1	0	0		
1	1	0	1	1	0	1	1	1		
00		<b>&gt;</b> -0	8		<b>)•</b> -0	8		<b>&gt;</b> -0		

Α	В	$\overline{A*B}$	Ā*B
0	0	1	1
0	1	1	0
1	0	1	0
1	1	0	0

