

DCM is a <u>generative model</u>
= a quantitative / mechanistic description of how observed data are generated.



- Key features:

 1- Dynamic

 2- Causal

 3- Neuro-physiologically motivated

 4- Operate at hidden neuronal interactions

 5- Bayesian in all aspects

 6- Hypothesis-driven

 7- Inference at multiple levels.

DCM [default] implementation:

Deterministic Stochastic [Daunizeau et al. 2009]

Bilinear Nonlinear [Stephan et al. 2008]

The one-state neuronal The two-state [Marreiros et al. 2008]

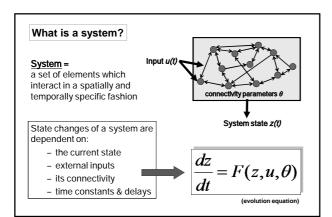


"The central idea behind dynamic causal modelling (DCM) is to treat the brain as a deterministic nonlinear dynamic system that is subject to inputs and produces outputs."

"DCM assumes the responses are driven by designed changes in inputs."

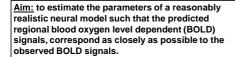
"DCM is used to test the specific hypothesis that motivated the experimental design. It is not an exploratory technique [...]; the results are specific to the tasks and stimuli employed during the experiment."

[Friston et al. 2003 Neuroimage]

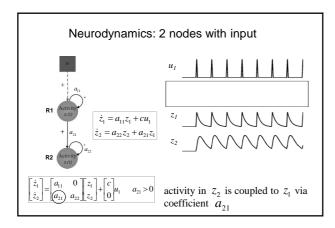


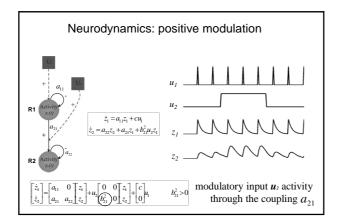
Basic idea of DCM for fMRI

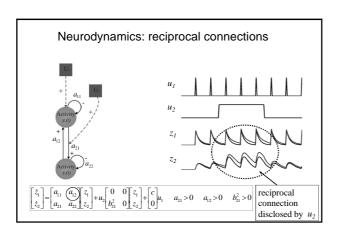
- ◆ Effective connectivity is parameterised in terms of coupling among unobserved brain states (e.g., neuronal activity in different regions). The objective is to estimate these parameters by perturbing the system and measuring the response.
- $\mbox{\Large \star}$ A cognitive system is modelled as a bilinear model of neural population dynamics (z).
- \bullet The modelled neuronal dynamics (z) is transformed into area-specific BOLD signals (y) by a hemodynamic forward model (λ).

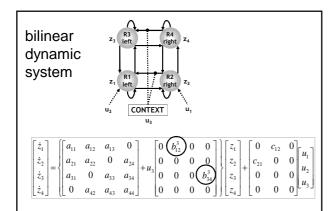


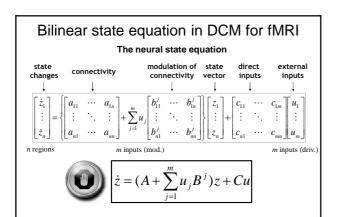


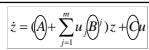






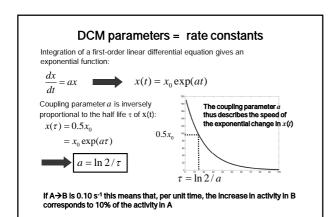


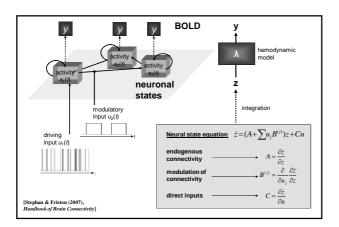


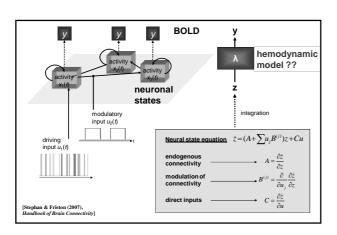


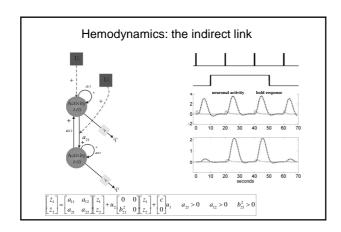
- "C", the direct or driving effects:
- extrinsic influences of inputs on neuronal activity.
- "A", the endogenous coupling or the latent connectivity:
- fixed or intrinsic effective connectivity;
 first order connectivity among the regions in the absence of input;
 average/baseline connectivity in the system (DCM10/DCM8).
- "B", the bilinear term, modulatory effects, or the induced connectivity:
- context-dependent change in connectivity; eq. a second-order interaction between the input and activity in a source region when causing a response in a target region.

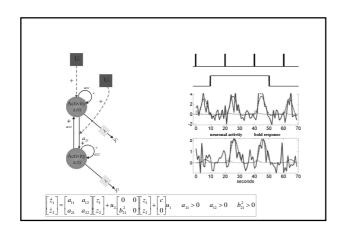
[Units]: rates, [Hz]; Strong connection = an effect that is influenced quickly or with a small time constant.

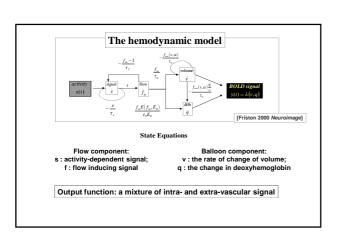


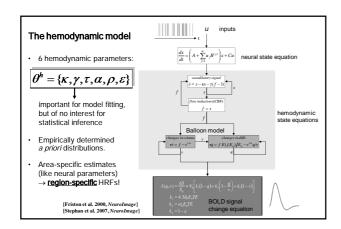


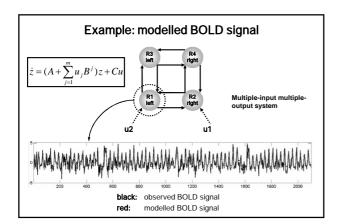




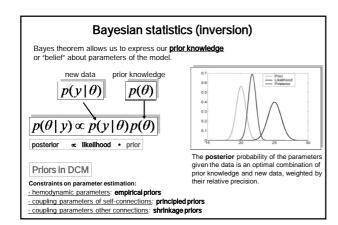






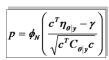


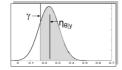
Priors & parameter estimation



Inference about DCM parameters: Bayesian inversion

- Gaussian assumptions about the posterior distributions of the parameters
- Use of the cumulative normal distribution to test the probability that a certain parameter (or contrast of parameters $c^T\,\eta_{\theta|y})$ is above a chosen threshold γ :





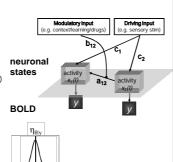
By default, y is chosen as zero ("does the effect exist?").
 Bayesian parameter estimation by means of expectation-maximisation (EM)
 [Friston 2002 Neuroimag

DCM: practical steps

Select areas you want to model

- Extract timeseries of these areas (x(t))
- Specify at neuronal level
 - what drives areas (c)
 - how areas interact (a)
 - what modulates interactions (b)
- State-space model with 2 levels:
 - Hidden neural dynamics
 - Predicted BOLD response
- · Estimate model parameters:

Gaussian a posteriori parameter distributions, characterised by mean $\eta_{\theta|y}$ and covariance $C_{\theta|y}$.



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Attention to motion in the visual system

Stimuli 250 radially moving dots at 4.7 degrees/s

Pre-Scanning

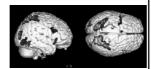
5 x 30s trials with 5 speed changes (reducing to 1%) Task - detect change in radial velocity

Scanning (no speed changes)
6 normal subjects, 4 x 100 scan sessions; each session comprising 10 scans of 4 different conditions

FAFNFAFNS....

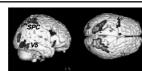
- F fixation point only
 A motion stimuli with attention (detect changes)
- N motion stimuli without attention S no motion





[Büchel & Friston 1997, Cereb. Cortex] [Büchel et al. 1998, Brain]

How we can interpret, mechanistically, the increase in activity of area V5 by attention when motion is physically unchanged.



Choice of areas and time series extraction. → Three ROIs: V1, V5, and SPC.

Definition of driving inputs.

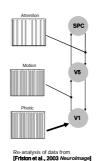
→ All visual stimuli/conditions (photic: A N S)

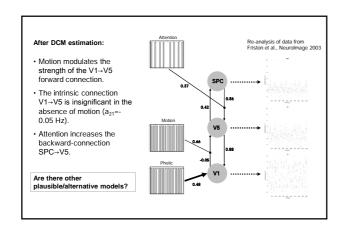
Definition of modulatory inputs.
→ The effects of motion and attention (A N)

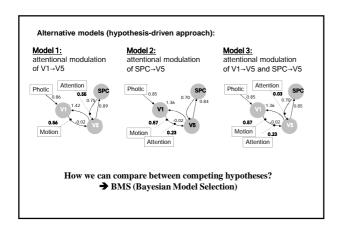
Building the model:

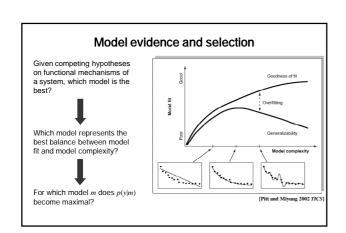
- 1- how to connect regions (intrinsic connections "A");
 2- how the driving inputs enter the system (extrinsic effects "C");
 3- define the context-dependent connections (modulatory effects "B").

- Visual inputs drive V1.
- · Activity then spreads to hierarchically arranged visual
- Motion modulates the strength of the V1→V5 forward connection.
- Attention modualtes the strength of the SPC→V5 backward connection.









Bayesian model selection (BMS)

Bayes' rule:

$$p(\theta \mid y,m) = \frac{p(y \mid \theta,m)p(\theta \mid m)}{p(y \mid m)}$$

Model evidence:

$$p(y|m) = \int p(y|\theta,m) \cdot p(\theta|m) d\theta$$

Model evidence: probability of generating data y from parameters θ that are randomly sampled from the prior p(m).

Maximum likelihood: probability of the data y for the specific parameter vector θ

- accounts for both accuracy and complexity of the model
- allows for inference about structure (generalisability) of the model
- integral usually not analytically solvable, approximations necessary

Approximations to the model evidence in DCM

monotonic function

$$\longrightarrow$$

Maximizing log model evidence = Maximizing model evidence

Log model evidence = balance between fit and complexity

$$\log p(y | m) = accuracy(m) - complexity(m)$$
$$= \log p(y | \theta, m) - complexity(m)$$

The negative variotional free energy (F) approximation [Penny et al. 2014, NeuroImage] [Penny et al. 2010, PLoS Comp Biol]

Under Gaussian assumptions about the posterior (Laplace approximation), the negative free energy \emph{F} is a lower bound on the log model evidence:

$$\Rightarrow F = \log p(y \mid m) - KL[q(\theta), p(\theta \mid y, m)]$$

The complexity term in F

The negative free energy ${\it F}$ accounts for parameter interdependencies.

$$\mathit{KL}\big[q(\theta),p(\theta\,|\,m)\big]$$

$$= \frac{1}{2} |C_{\theta}| - \frac{1}{2} |C_{\theta|y}| + \frac{1}{2} (\mu_{\theta|y} - \mu_{\theta})^{T} C_{\theta}^{-1} (\mu_{\theta|y} - \mu_{\theta})$$

- The complexity term of F is higher
 - the more independent the prior parameters (\uparrow effective DFs)
 - the more dependent the posterior parameters
 - the more the posterior mean deviates from the prior mean
- NB: DCM8/DCM10/DCM12 only uses F for model selection !

Bayes factors

To compare two models, we can just compare their log evidences.

But: the log evidence is just some number – not very intuitive!

A more intuitive interpretation of model comparisons is made possible by Bayes factors:

positive value, [0; ∞[

$$BF_{12} = \frac{p(y | m_1)}{p(y | m_2)}$$

Kass & Raftery classification: [Kass & Raftery 1995, J. Am. Stat. Assoc.]

| BF ₁₂ | $p(m_1 y)$ | Evidence |
|------------------|------------|-------------|
| 1 to 3 | 50-75% | weak |
| 3 to 20 | 75-95% | positive |
| 20 to 150 | 95-99% | strong |
| ≥ 150 | ≥99% | Very strong |

Bayesian Model Selection in group studies.

Fixed effects BMS at group level

Group Bayes factor (GBF) for 1...K subjects:

$$GBF_{ij} = \prod_{k} BF_{ij}^{(k)} \qquad BF_{ij} = \frac{p(y \mid m_i)}{p(y \mid m_j)}$$

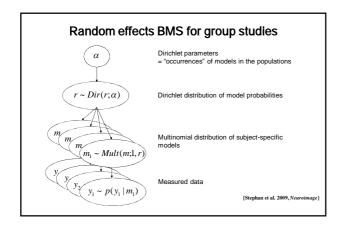
Average Bayes factor (ABF):

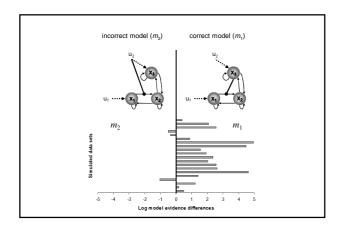
$$ABF_{ij} = \sqrt[K]{\prod_{k} BF_{ij}^{(k)}}$$

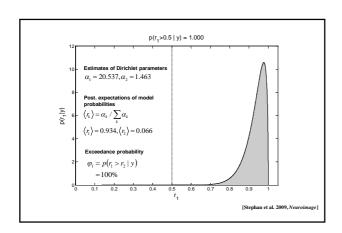
- Problems:

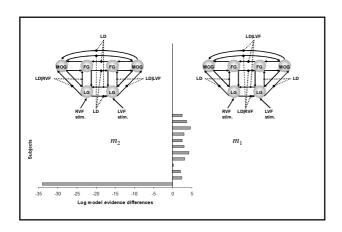
 ▶ blind with regard to group heterogeneity;

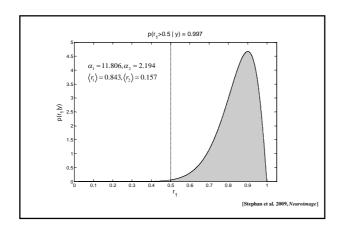
 ▶ sensitive to outliers.



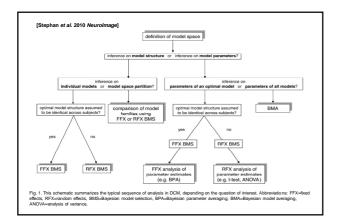








| Levels of inference: Group/p | opulation level |
|--|---|
| Family level System/model level Parameter/connection level | |
| [Seghier et al. 2010, Front Syst Neurosci] | |
| ♣ Family level: | [Penny et al. 2010, PLoS Comp Biol] |
| - Useful when no clear winning model // m | |
| Models assigned to subsets (families) →Inference: a class/type of models that | |
| System level: - Useful when a clear winning model can | |
| →Interence: the best combination of ir | nputs+connections that explains the data. |
| ◆ Connection level: - Useful when connectivity parameters are →Inference: Bayesian parameters average. | |





BMS has nothing to say about the "true" models. find the most plausible (useful) model, form a set of alternatives, given data. Best model = best balance between accuracy and complexity.

DCM model space: Compatibility // Size // Plausibility.

BMS cannot be applied to models fitted to different data!(Only models with the same ROIs can be compared using BMS).

It is helpful to constrain your DCM model space.

number of ROIs limited to 8 in SPM8 (GUI).

(e.g., 6 ROIs, fully connected, 1 Billion alternative modulations!).

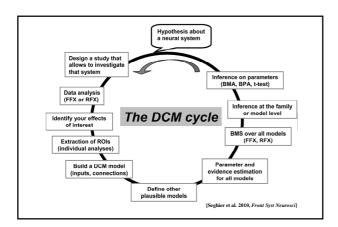
- # Define sets of models that are plausible, in a systematic way, given prior knowledge about the system (e.g. anatomical, TMS, previous studies).
 - \rightarrow Bad models may affect your BMS results (DCM space = a "relative" space)!

Which DCM version? DCM5 || DCM8 || DCM10 || DCM12.

- Keep the same DCM version for your project (over models, families, and subjects).

- Indicate the DCM version in your papers.

| Extensions in DCM for fMRI (SPM12): | | | | | |
|-------------------------------------|--------------------------------------|---|--|--|--|
| F | Bayesian Model Selection BMS | [Penny et al. 2004 Neuroimage]. | | | |
| ŀ | Slice specific sampling | [Kiebel et al. 2007 Neuroimage]. | | | |
| ŀ | Refined hemodynamic model | [Stephan et al. 2007 Neuroimage]. | | | |
| ŀ | The two-state DCM | [Marreiros et al. 2008 Neuroimage]. | | | |
| ŀ | The non-linear DCM | [Stephan et al. 2008 Neuroimage]. | | | |
| ŀ | Random-effects BMS | [Stephan et al. 2009 Neuroimage]. | | | |
| ŀ | Stochastic DCM | [Daunizeau et al. 2009 Physica D]. | | | |
| ŀ | Anatomical-based priors for DCM | [Stephan et al. 2009 Neuroimage]. | | | |
| ŀ | Family level inference BMS | [Penny et al. 2010 PLoS Comp Biol]. | | | |
| ŀ | Bayesian model averaging BMA | [Penny et al. 2010 PLoS Comp Biol]. | | | |
| ŀ | Network discovery | [Friston et al. 2011 Neuroimage]. | | | |
| ŀ | Stochastic DCM (random fluctuations) | [Li et al. 2011 Neuroimage]. | | | |
| Ŀ | Network discovery for large DCMs | [Seghier & Friston et al. 2013 Neuroimage]. | | | |
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| Reviews: | |
|----------|--|
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| | |

Stephan et al. (2010). Ten simple rules for DCM. Neurolmage.

Daunizeau et al. (2010). DCM: a critical review of the biophysical and statistical foundations. NeuroImage.

Seghier et al. (2010). Identifying abnormal connectivity in patients using dynamic causal modeling of fMRI responses : Front Syst Neurosci.

Friston (2011). Functional and effective connectivity: A review. Brain Connectivity.

Practical examples: (DCM-fMRI at the FIL)

- Inter-hemispheric interactions and laterality for words and pictures: Seghier et al. (2011) Cerebral Cortex.

- Prediction error and putamen: den Ouden et al. (2010) J Neurosci.

- Top-down effects on form perception: Cardin et al. (2011) Cerebral Cortex.

- Multilingual vs. Monlingual monitoring of speech production: Parker-Jones et al. (2013) *J Neurosci*.