1

ASSIGNMENT-1

C.RAMYA TULASI

Download all python codes from

https://github.com/CRAMYATULASI/ ASSIGNMENT-1/tree/main/ASSIGNMENT %201/CODES

and latex-tikz codes from

https://github.com/CRAMYATULASI/ ASSIGNMENT-1/tree/main/ASSIGNMENT %201

1 QUESTION NO-2.23

Construct $\triangle LMN$ right angled at M such that LN = 5 and MN = 3.

2 SOLUTION

Let

$$\mathbf{L} = \begin{pmatrix} 0 \\ l \end{pmatrix}, \mathbf{M} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{N} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$$
 (2.0.1)

Now.

$$\|\mathbf{N} - \mathbf{M}\|^2 = \|\mathbf{N}\|^2 = 3^2 = 9$$
 (2.0.2)

$$\|\mathbf{L} - \mathbf{M}\|^2 = \|\mathbf{L}\|^2 = l^2$$
 (2.0.3)

We know,

$$||\mathbf{L} - \mathbf{N}||^2 = (\mathbf{L} - \mathbf{N})^T (\mathbf{L} - \mathbf{N})$$

$$= \mathbf{L}^T \mathbf{L} + \mathbf{N}^T \mathbf{N} - \mathbf{L}^T \mathbf{N} - \mathbf{L}^T \mathbf{L}$$
(2.0.5)

$$= ||\mathbf{L}||^2 + ||\mathbf{L}||^2 - 2\mathbf{L}^T \mathbf{N}$$
 (2.0.6)

$$= ||\mathbf{L}||^2 + ||\mathbf{N}||^2 - 2.0 \tag{2.0.7}$$

$$= l^2 + 3^2 \tag{2.0.8}$$

$$= l^2 + 9 (2.0.9)$$

But we know LN=5

$$SO, ||\mathbf{L} - \mathbf{N}||^2 = 5^2 = 25$$
 (2.0.10)

$$l^2 + 9 = 25 \tag{2.0.11}$$

$$l^2 = 25 - 9 \tag{2.0.12}$$

$$l^2 = 16 (2.0.13)$$

$$l = \pm 4$$
 (2.0.14)

As we consider $\triangle LMN$ in first quadrant we consider l=4

Therefore,
$$l = 4$$
 (2.0.15)

Now, Vertices of given $\triangle LMN$ can be written as,

$$\mathbf{L} = \begin{pmatrix} 0 \\ l \end{pmatrix} = \begin{pmatrix} 0 \\ 4 \end{pmatrix}, \mathbf{M} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{N} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$$
 (2.0.16)

Now, $\triangle LMN$ can be plotted using vertices LM, MN and LN.

