

# ASSIGNMENT 6

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Download all python codes from

<https://github.com/CRAMYATULASI/ASSIGNMENT6/tree/main/ASSIGNMENT6/CODES>

Latex-tikz codes from

<https://github.com/CRAMYATULASI/ASSIGNMENT6/tree/main/ASSIGNMENT6>

## 1 QUESTION No 2.42

Find the point at which the tangent to the curve  $y = \sqrt{4x-3} - 1$  has its slope  $\frac{2}{3}$ .

## 2 SOLUTION

Given curve,

$$y = \sqrt{4x-3} - 1 \quad (2.0.1)$$

$$\Rightarrow (y+1)^2 = 4x-3 \quad (2.0.2)$$

$$\Rightarrow y^2 - 4x + 2y + 4 = 0 \quad (2.0.3)$$

From above equation,

$$\mathbf{V} = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, \mathbf{u} = \begin{pmatrix} -2 \\ 1 \end{pmatrix}, f = 4 \quad (2.0.4)$$

$$|\mathbf{V}| = 0 \quad (2.0.5)$$

$\therefore$  Given curve (2.0.1) is parabola.

In standard form,

$$\mathbf{P} = \mathbf{I} \Rightarrow p_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad (2.0.6)$$

Given slope of tangents is  $\frac{2}{3}$  then direction vectors and normal vectors are,

$$m = \begin{pmatrix} 1 \\ \frac{2}{3} \end{pmatrix} \Rightarrow \begin{pmatrix} 3 \\ 2 \end{pmatrix}, n = \begin{pmatrix} 2 \\ -3 \end{pmatrix} \quad (2.0.7)$$

$$\kappa = \frac{p_1^T \mathbf{u}}{p_1^T n} \Rightarrow -1 \quad (2.0.8)$$

$\therefore$  Point of contact for tangent of parabola is,

$$\begin{pmatrix} \mathbf{u} + \kappa n^T \\ \mathbf{V} \end{pmatrix} \mathbf{q} = \begin{pmatrix} f \\ \kappa n - \mathbf{u} \end{pmatrix} \quad (2.0.9)$$

$$\Rightarrow \begin{pmatrix} -4 & -4 \\ 0 & 0 \\ 0 & 1 \end{pmatrix} \mathbf{q} = \begin{pmatrix} -4 \\ 0 \\ 2 \end{pmatrix} \quad (2.0.10)$$

$$\Rightarrow \mathbf{q} = \begin{pmatrix} 3 \\ 2 \end{pmatrix} \quad (2.0.11)$$

$\therefore$  Point of contact for tangent of given curve is

$$\mathbf{q} = \begin{pmatrix} 3 \\ 2 \end{pmatrix} \quad (2.0.12)$$

Plot of Tangent to the given curve -

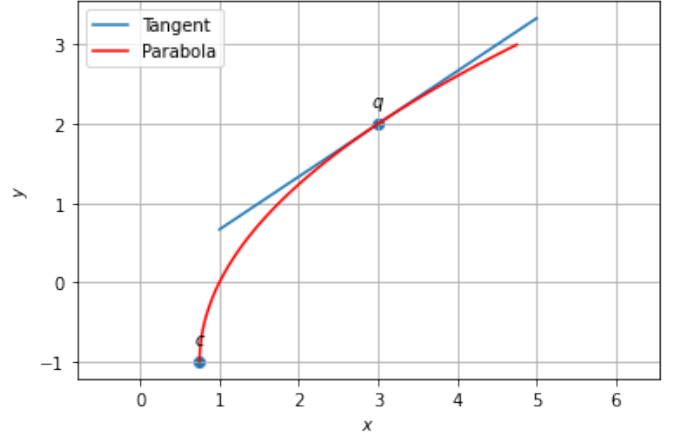


Fig. 2.1: Tangent to Parabola.