1

ASSIGNMENT 3

C.RAMYA TULASI

Download all python codes from

https://github.com/ka-raja-babu/Matrix-Theory/tree/main/Assignment3/Codes

and latex-tikz codes from

https://github.com/ka-raja-babu/Matrix-Theory/ tree/main/Assignment3

1 Question No 2.56

Construct a tangent to a circle of radius 4 units from a point on concentric circle of radius 6 units.

2 Solution Data from the given question

| | Symbols | Circle1 | Circle2 |
|--------|-----------|--|--|
| Centre | O | $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ | $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ |
| Radius | r_1,r_2 | 4 | 6 |

Let PQ and PR be tangents from point P on circle with radius 6 to the point Q and R on circle with radius 4.

Using the fact that angle between radius and tangent of a circle is 90, From $\triangle OPQ$

$$\cos\theta = \frac{4}{6} \tag{2.0.1}$$

$$\theta = 48.5$$
 (2.0.2)

Angle between PQ and OP = 180-(90+48.5)=41.8

... Angle between OP and OQ is 48.5 and angle between PQ and OP is 41.8

Now,

$$\mathbf{Q} = 4 \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix} = \begin{pmatrix} 2.64 \\ 2.96 \end{pmatrix} \tag{2.0.3}$$

Similarly, from $\triangle OPR$

$$\mathbf{R} = \begin{pmatrix} 2.64 \\ -2.96 \end{pmatrix} \tag{2.0.4}$$

Now, vertices of $\triangle OPQ$ and $\triangle OPR$:

$$\mathbf{O} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{P} = \begin{pmatrix} 6 \\ 0 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 2.64 \\ 2.96 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} 2.64 \\ -2.96 \end{pmatrix}$$
(2.0.5)

Plot of Tangent PQ and PR:

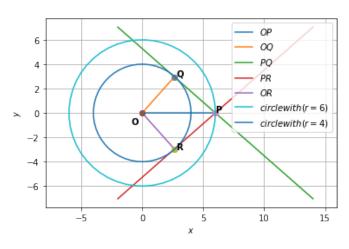


Fig. 2.1: Tangents to a circle of radius 4 units from a point on concentric circle of radius 6 units