1

ASSIGNMENT-2

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Download all python codes from

https://github.com/CRAMYATULASI/ ASSIGNMENT_2/tree/main/ASSIGNMENT2/ CODES

and latex-tikz codes from

https://github.com/CRAMYATULASI/ ASSIGNMENT_2/tree/main/ASSIGNMENT2

1 QUESTION NO-2.34

Draw GOLD such that OL = 7.5, GL = 6, GD = 6, LD = 5 and OD = 10.

2 SOLUTION

Given,

$$OL = 7.5, GL = 6, GD = 6, LD = 5, OD = 10.$$
 (2.0.1)

Now,

$$OL = ||\mathbf{O} - \mathbf{L}|| = 7.5$$
 (2.0.2)

$$GL = ||\mathbf{G} - \mathbf{L}|| = 6$$
 (2.0.3)

$$GD = \|\mathbf{G} - \mathbf{D}\| = 6$$
 (2.0.4)

$$LD = ||\mathbf{L} - \mathbf{D}|| = 5 \tag{2.0.5}$$

$$OD = \|\mathbf{O} - \mathbf{D}\| = 10$$
 (2.0.6)

- 1) We know,a quadrilateral is a polygon with 4 sides if we have four points they will not form a quadrilateral if any three points are collinear.
- 2) Now, let us use the above fact and consider two triangles on same base if any three points are collinear it cannot be a triangle and then given sides cannot form a quadrilateral if any three sides are collinear. $\triangle LDO$ and $\triangle LDG$ are two triangles of given quadrilateral which are on same base LD Now, we check if any three sides are collinear in two triangles. Let us consider $\triangle LDO$ -

$$\|\mathbf{O} - \mathbf{L}\| + \|\mathbf{O} - \mathbf{D}\| = 17.5 > \|\mathbf{L} - \mathbf{D}\|$$
 (2.0.7)

$$\|\mathbf{O} - \mathbf{D}\| + \|\mathbf{L} - \mathbf{D}\| = 15 > \|\mathbf{O} - \mathbf{L}\|$$
 (2.0.8)

$$\|\mathbf{O} - \mathbf{L}\| + \|\mathbf{L} - \mathbf{D}\| = 12.5 > \|\mathbf{O} - \mathbf{D}\|$$
 (2.0.9)

Triangle inequality is satisfied.

 \therefore $\triangle LDO$ can be constructed. Similarly, Now we consider $\triangle LDG$

$$\|\mathbf{L} - \mathbf{D}\| + \|\mathbf{G} - \mathbf{L}\| = 11 > \|\mathbf{G} - \mathbf{D}\|$$
 (2.0.10)

$$\|\mathbf{G} - \mathbf{L}\| + \|\mathbf{G} - \mathbf{D}\| = 12 > \|\mathbf{L} - \mathbf{D}\| \quad (2.0.11)$$

$$\|\mathbf{L} - \mathbf{D}\| + \|\mathbf{G} - \mathbf{D}\| = 11 > \|\mathbf{G} - \mathbf{L}\|$$
 (2.0.12)

Triangle inequality is satisfied.

- $\therefore \triangle LDG$ can be constructed.
- ∴ Given sides form a quadrilateral.

Vertices of quadrilateral GOLD:

Now from $\triangle LDO$, the sides of $\triangle LDO$ are known Which means vertices O,L and D can be obtained using example 1.2.3

Similarly, the vertices of $\triangle LDG$ can be obtained using example 1.2.3

.: Vertices of given Quadrilateral GOLD can be written as.

$$\mathbf{L} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{D} = \begin{pmatrix} 5 \\ 0 \end{pmatrix}, \mathbf{O} = \begin{pmatrix} -1.875 \\ 7.26 \end{pmatrix}, \mathbf{G} = \begin{pmatrix} 2.5 \\ 5.5 \end{pmatrix}$$
(2.0.13)

Plot of the Quadrilateral GOLD:

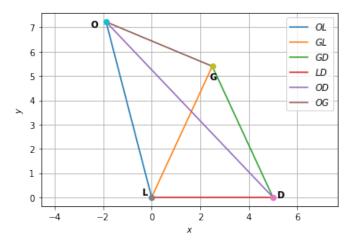


Fig. 2.1: Quadrilateral GOLD