

1 List of symbols

(1 indicates a dimensionless quantity and – indicates not applicable).

Symbol	Variable name	Units	Description
$\arctan2(y, x)$	–	–	The four quadrant inverse tangent which returns values in the interval $[-\pi, \pi]$, inclusive.
c	<code>c</code>	ms^{-1}	Sound speed in water.
$D(v)$	<code>filter_v[n] ['D']</code>	1	Integer filter decimation factor.
$DFT_{N_{DFT}}(x)$		–	The discrete Fourier transform of length N_{DFT} of x .
f		Hz	Frequency.
f_c		Hz	Frequency at centre of linear upswing chirp pulse. Equivalent to $f_{start} + \frac{ f_{stop} - f_{start} }{2}$.
f_n	<code>f_n</code>	Hz	Nominal operating frequency of a transducer.
f_s	<code>f_s</code>	Hz	Analogue to digital sampling frequency.
$f_{s,dec}$	<code>f_s_dec</code>	Hz	Decimated sampling frequency.
f_{start}	<code>f_1</code>	Hz	Start frequency of linear upswing chirp pulse.
f_{stop}	<code>f_2</code>	Hz	Stop frequency of linear upswing chirp pulse.
$g(\theta, \phi, f)$	<code>g_theta_phi_m</code>	1	Transducer gain as a function of echo arrival angle in the beam and frequency.
$g_0(f)$	<code>g_0_m</code>	1	Transducer gain along the main acoustic axis, i.e. $g(\theta, \phi, f)$ where $\theta = \phi = 0$.
$h_{bp}(i, v)$	<code>filter_v[n] ['h_fl_i']</code>	1	Complex valued receiving filter coefficients.
i		1	Generic integer index.
$\Im(x)$		–	The imaginary part of x .
j			The square root of -1 .
m	<code>m</code>	1	Sample index in frequency domain.

N_u	N_u	1	Total number of transducer sectors/transceiver channels that are used to receive and process the acoustic signal.
N_v		1	Total number of filter stages.
N_w		1	Number of samples used in the sliding Hanning window.
n	n	1	Sample index in time domain.
$P_{rx,e,t}(f)$		W	FT of the received electric power in a matched load for the signal from a single target at frequency f .
$P_{rx,e,t}(m)$	$P_{rx_e_t_m}$	W	DFT of the received electric power in a matched load for the signal from a single target.
$P_{rx,e,v}(f)$		W	FT of the received electric power in a matched load for the signal from a volume at frequency f .
$P_{rx,e,v}(m)$	$P_{rx_e_v_m}$	Wm^2	DFT of the received electric power in a matched load for the signal from a volume.
$p_{rx,e}(n)$	$p_{rx_e_n}$	W	Received electric power in a matched load.
$p_{tx,e}$	p_{tx_e}	W	Transmitted electric power.
$p_{tx,auto}(n)$	p_{tx_auto}	1	Square of the absolute value of the matched filter autocorrelation function.
$\Re(x)$		–	The real part of x .
r		m	Distance from transducer.
r_0		m	Reference distance.
r_c		m	Distance from the transducer to the centre of the range volume covered by t_w .
$r_c(n)$		m	$range_c$ at sample number n .
$r(n)$	r_n	m	Distance from transducer.
$S_p(n)$	Sp_n	dB re 1 m ²	Point scattering strength.
S_v		dB re 1 m ⁻¹	Volume backscattering strength.
$S_v(f)$		dB re 1 m ⁻¹	Volume backscattering strength at frequency f .
$S_v(n)$	Sv_n	dB re 1 m ⁻¹	Volume backscattering strength at sample index n .

TS		dB re 1 m ²	Target strength.
TS(f)		dB re 1 m ²	Target strength at frequency f .
TS(m)	TS_m	dB re 1 m ²	Target strength at frequency index m .
t		s	Time.
t_w	t_w	s	Duration of sliding window for calculating volume backscattering strength.
u		1	Receiver channel number and transducer sector number.
$u(i)$		1	The Heaviside step function.
V		m ³	Volume occupied by scattering targets.
v		1	Filter stage.
w		1	The Hann window function.
$w(i)$	w_i	1	The Hann window function for index i , defined by $w(i) = 0.5(1 + \cos(2\pi i/N_w))$, $-N_w/2 \leq i \leq N_w/2$.
$\tilde{w}(i)$	w_tilde_i	1	Normalised Hann window.
x^*		–	The complex conjugate of x .
$\ x\ _2$		–	The l^2 -norm of x , also known as the Euclidean norm.
$Y_{\text{mf,auto}}(m)$	Y_mf_auto_m	1	Discrete Fourier transform (DFT) of the autocorrelation function for the matched filter.
$Y_{\text{mf,auto,red}}(m)$	Y_mf_auto_m_red	1	DFT of the reduced autocorrelation function for the matched filter.
$Y_{\text{pc,t}}(m)$	Y_pc_t_m	V	DFT of the pulse compressed signal from a single target.
$\tilde{Y}_{\text{pc,t}}(m)$	Y_tilde_pc_t_m	Vm	DFT of the pulse compressed signal from a single target normalized by the DFT of the reduced autocorrelation function for the matched filter.
$Y_{\text{pc,v}}(m)$	Y_pc_v_m	Vm	DFT of the pulse compressed signal from a volume. Compensated for spreading loss.

$\tilde{Y}_{pc,v}(m)$	<code>Y_tilde_pc_v_m</code>	V	DFT of the pulse compressed signal from a single volume normalized by the DFT of the reduced autocorrelation function for the matched filter. Compensated for spreading loss.
$y_{mf}(n)$	<code>y_mf_n</code>	1	Matched filter. Signal used for pulse compression.
$y_{mf,auto}(n)$	<code>y_mf_auto_n</code>	1	Autocorrelation function for the matched filter.
$y_{mf,auto,red}(n)$	<code>y_mf_auto_red_n</code>	1	Reduced autocorrelation function for the matched filter.
$y_{pc}(n)$	<code>y_pc_n</code>	V	Pulse compressed signal averaged over all transducer sectors.
$y_{pc}(n, u)$	<code>y_pc_nu</code>	V	Pulse compressed signal from channel u .
$y_{pc,aft}(n)$	<code>y_pc_aft_n</code>	V	Pulse compressed signal from the aft transducer half.
$y_{pc,fore}(n)$	<code>y_pc_fore_n</code>	V	Pulse compressed signal from the forward transducer half.
$y_{pc,port}(n)$	<code>y_pc_port_n</code>	V	Pulse compressed signal from the port transducer half.
$y_{pc,s}(n)$	<code>y_pc_s_n</code>	Vm	Pulse compressed signal compensated for spherical spreading.
$y_{pc,star}(n)$	<code>y_pc_star_n</code>	V	Pulse compressed signal from the starboard transducer half.
$y_{pc,t}(n)$	<code>y_pc_t_n</code>	V	Pulse compressed signal from a single target.
$y_{rx}(n, u)$	<code>y_rx_nu</code>	V	Received digitised, bandpass filtered, decimated complex signal after the final filter stage, $y_{rx}(n, u) = y_{rx}(n, u, N_V)$.
$y_{rx}(n, u, v)$		V	Received digitised, bandpass filtered, decimated complex signal.
$y_{rx,a}(t)$		Pa	Analogue acoustic signal received by the transducer.
$y_{rx,e}(t, u)$		V	Analogue electric signal received by each transceiver channel u .
$y_{rx,org}(n, u)$		V	Received digitised signal before the bandpass filtering and decimation stages, $y_{rx,org}(n, u) = y_{rx}(n, u, 0)$.

$y_{\text{tx}}(n)$	y_tx_n	V	Ideal transmitted signal generated from transmit signal properties.
$\tilde{y}_{\text{tx}}(n)$	y_tilde_tx_n	1	Ideal normalized transmitted signal generated from transmit signal properties.
$\tilde{y}_{\text{tx}}(n, v)$	y_tilde_tx_nv	1	Ideal normalized transmitted signal generated from transmit signal properties after application of filter stage v .
$y_{\text{tx},\text{a}}(t)$		Pa	Analogue acoustic transmit signal.
$y_{\text{tx},\text{e}}(t)$		V	Analogue electric transmit signal.
$y_{\theta}(n)$	y_theta_n	rad	Electrical angle along the minor axis of the transducer (alongship when ship-mounted).
$y_{\phi}(n)$	y_phi_n	rad	Electrical angle along the major axis of the transducer (athwartship when ship-mounted).
$z_{\text{rx},\text{e}}$	z_rx_e	Ω	Receiver electric impedance.
$z_{\text{td},\text{e}}$	z_td_e	Ω	Transducer sector electric impedance.
$\alpha(f)$	alpha_m	dB m^{-1}	Absorption coefficient at frequency f .
γ_{θ}	gamma_theta	1	Conversion factor between phase difference in signals from the fore and aft transducer halves and the physical arrival angle of an echo.
γ_{ϕ}	gamma_phi	1	Conversion factor between phase difference in signals from the port and starboard transducer halves and the physical arrival angle of an echo.
θ	theta_n	rad	Angle coordinates along the minor axis of the transducer (alongship when ship-mounted).
λ		m	Acoustic wavelength.
λ_m	lambda_m	m	Acoustic wavelength at frequency index m
σ_{bs}		m^2	Backscattering cross-section.
τ	tau	s	Nominal transmit pulse duration.
τ_{eff}	tau_eff	s	Effective transmit pulse duration.

ϕ	phi	rad	Angle coordinates along the major axis of the transducer (athwartship when ship-mounted).
$\psi(f)$	psi_m	sr	Two-way equivalent beam angle at frequency f .