

## Homework 2

**Question 1.** Please read chapter 2 of Chartrand et al. and write a couple sentences about a topic/example/concept that you found difficult or interesting and why?

I like how the book put the concepts of the different types of number in terms of sets such as  $\mathbb{N} \subset \mathbb{Z}$ . This made some concepts easier to understand.

**Question 2.** How many elements are in  $\mathcal{P}(A)$  if  $A = \{n \in \mathbb{Z} : |n| \leq 5\}$ ?

11 integers

$2^{11}$  elements

**Question 3.** Let  $A = \{0, \{0\}, \{0, \{0\}\}\}$ .

(a) Determine which of the following are elements of  $A$  :  $0, \{0\}, \{\{0\}\}$ .

$0, \{0\}$

(b) Determine  $|A|$

3

(c) Determine which of the following are subsets of  $A$  :  $0, \{0\}, \{\{0\}\}$ .

$\{0\}, \{\{0\}\}$

For (d)-(i), determine the indicated sets.

(d)  $\{0\} \cap A$ .

$\{0\}$

(e)  $\{\{0\}\} \cap A$ .

$\{\{0\}\}$

(f)  $\{\{\{0\}\}\} \cap A$ .

empty

(g)  $\{0\} \cup A$ .

$\{0, \{0\}, \{0, \{0\}\}\}$

(h)  $\{\{0\}\} \cup A$ .

$\{0, \{0\}, \{0, \{0\}\}\}$

(i)  $\{\{\{0\}\}\} \cup A$ .

$\{0, \{0\}, \{0, \{0\}\}, \{\{0\}\}\}$

**Question 4.** For two sets  $A$  and  $B$  of real numbers, the set  $A \cdot B$  is defined by,

$$A \cdot B = \{ab : a \in A, b \in B\}.$$

Determine each of the following sets.

1)  $A \cdot B$  for  $A = \{\frac{1}{2}, 1, \sqrt{2}\}$  and  $B = \{\sqrt{2}, 2, 4\}$ .

$\{\frac{\sqrt{2}}{2}, 1, 2, \sqrt{2}, 4, 2\sqrt{2}, 4\sqrt{2}\}$

2)  $\mathbb{R} \cdot \mathbb{R}$ .

$\mathbb{R}$

3)  $\mathbb{R} \cdot C$  where  $C \subseteq \mathbb{R}$  with  $|C| = 2$ .

$\mathbb{R}$

**Question 5.** For  $A = \{1, 2\}$ ,  $B = \{-1, 0, 1\}$  and the universal set  $U = \{-2, -1, 0, 1, 2\}$ , determine

(a)  $A \cup B$ .

$\{-1, 0, 1, 2\}$

(b)  $A \cap B$ .

$\{1\}$

(c)  $A - B$ .

$\{2\}$

(d)  $\overline{B}$ .

$$\{-2, 2\}$$

(e)  $A \times B$ .

$$\{(1,-1), (1,0), (1,1), (2,-1), (2,0), (2,1)\}$$

**Question 6.** Give examples of three sets  $A, B$  and  $C$  such that

(a)  $A \subseteq B \not\subseteq C$ .

$$A = \{1\}$$

$$B = \{1, 2\}$$

$$C = \{3\}$$

(b)  $A \subseteq B, B \in C$  and  $A \cap C = \emptyset$ .

$$A = \{1\}$$

$$B = \{1, 2\}$$

$$C = \{\{1, 2\}, 3\}$$

(c)  $A \in B, A \subset B$  and  $A \not\subseteq C$ .

$$A = \{1\}$$

$$B = \{\{1\}, 1, 2\}$$

$$C = \{3\}$$

(d)  $A \in B, A \not\subseteq B$  and  $B \in C$ .

$$A = \{1\}$$

$$B = \{\{1\}, 2\}$$

$$C = \{\{\{1\}, 2\}, 1\}$$