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Seismic deblending of simultaneous crossline sources

Christian Reinicke Urruticoechea

July 8, 2015

Seismic deblending of simultaneous crossline sources

MASTER OF SCIENCE THESIS

for the degree of Master of Science in Applied Geophysics at
Delft University of Technology
ETH Zürich
RWTH Aachen University
by

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July 8, 2015

Department of Geoscience & Engineering	.	Delft University of Technology
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Delft University of Technology

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Abstract

This is the shortest abstract you have ever seen.

Acknowledgements

First of all I want to thank all the people who have participated in this project .. Remember, often more people have contributed to your final thesis than you initially would think of.

Delft, University of Technology
July 8, 2015

Christian Reinicke Urruticoechea

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Acronyms

DUT Delft University of Technology

Chapter 1

Introduction

Welcome to the standard layout for your IDEA LEAGUE MSc thesis written in L^AT_EX. L^AT_EX has a variety of advantages over conventional/ standard text editing programs, which you will soon enough discover yourself. L^AT_EX almost forms a standard in the Scientific Community, especially due to its effective and straightforward mathematical capabilities.

This is Chapter 1. If you want to know more about L^AT_EX you better read ? or use the extensive help available on the internet. . This 'hidden' index command helps you making an index at the end of your thesis. You can add this flag anywhere you want to make an index hit. You can see here also how to use acronyms, like Delft University of Technology ([DUT](#)). The acronyms are automatically listed in the corresponding section. Also, hyperlinks are created automatically with the developed class file, such that your digital PDF version of your thesis can be read dynamically. Have fun with L^AT_EX and your M.Sc. research project and good luck!

The purpose of the introduction is to tell readers why they should want to read what follows the introduction. This chapter should provide sufficient background information to allow readers to understand the context and significance of the problem. This does not mean, however, that authors should use the introduction to rederive established results or to indulge in other needless repetition. The introduction should (1) present the nature and scope of the problem; (2) review the pertinent literature, within reason; (3) state the objectives; (4) describe the method of investigation; and (5) describe the principal results of the investigation.

Part I

Theory

Chapter 2

Theory

This chapter describes the theory behind blending and deblending. First the detail hiding operator notation is explained. This notation is used to describe the forward model of seismic data. By introducing the blending operator the forward model is extended to the blended case. Next, the deblending method presented in [Mahdad et al. \(2011\)](#) is discussed to illustrate the concepts on which this thesis is based. At the end of the chapter the blending operator is analyzed in greater detail.

2-1 The Forward Model of Blending

2-1-1 Conventional Seismic Data

In the detail hiding operator notation ([Berkhout, 1982](#)) the recorded signal is considered discrete in terms of time t , receiver position x_r , and source position x_s . Thus, the measurements can be organized in a cube, $\mathbf{p}(\mathbf{t}, \mathbf{x}_r, \mathbf{x}_s)$ (see Figure 2-1). Each frequency slice of this new cube represents the data matrix, \mathbf{P} .

In the data matrix, \mathbf{P} , each column corresponds to a monochromatic common shot gather (see Figure 2-2), each row to a monochromatic common receiver gather, each diagonal to a monochromatic common offset gather, and each anti-diagonal to a monochromatic common midpoint gather.

According to the seismic forward model of [Berkhout \(1982\)](#) the data matrix, \mathbf{P} , can be represented by a matrix multiplication of the source matrix, \mathbf{S} , the impulse response of the earth, \mathbf{X} , and the receiver matrix, \mathbf{D} :

$$\mathbf{P} = \mathbf{D} \mathbf{X} \mathbf{S}. \quad (2-1)$$

In the source matrix, \mathbf{S} , each row and each column represent one source position (see Figure 2-3a). Thus, \mathbf{S} is a diagonal matrix. Each diagonal element s_{ii} captures one frequency

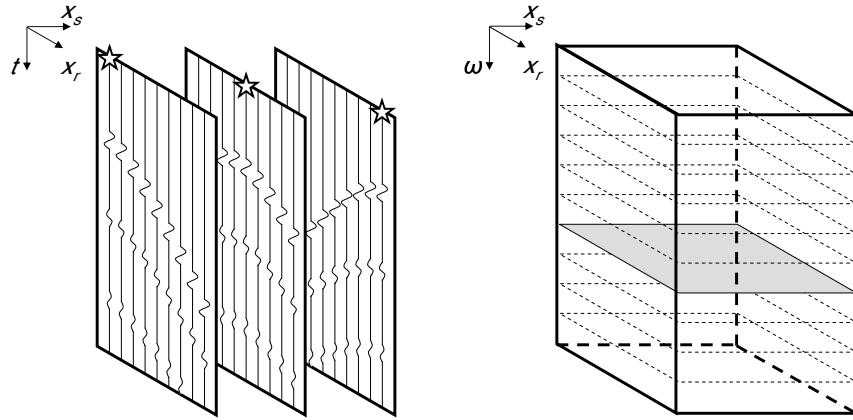


Figure 2-1: Illustration of the data matrix, \mathbf{P} , by [van Groenestijn \(2010\)](#). *Left:* The signal generated at the source position, x_s , is measured at receiver position, x_r , as a function of time, t . Thus, the discretized data is saved in a cube, $\mathbf{p}(t, \mathbf{x}_r, \mathbf{x}_s)$. *Right:* The cube on the right equals the left cube after a Fourier transform with respect to time. Each frequency slice of the right cube represents the data matrix, \mathbf{P} .

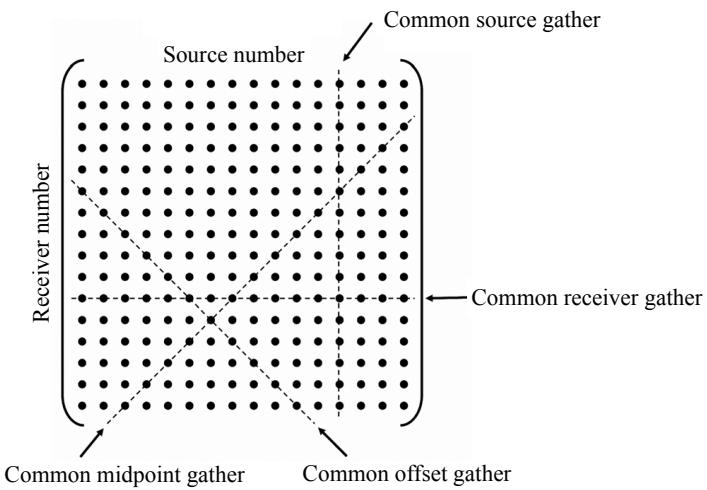


Figure 2-2: Illustration of the data matrix, \mathbf{P} , by [Mahdad et al. \(2011\)](#). The dotted lines indicate directions of common gathers.

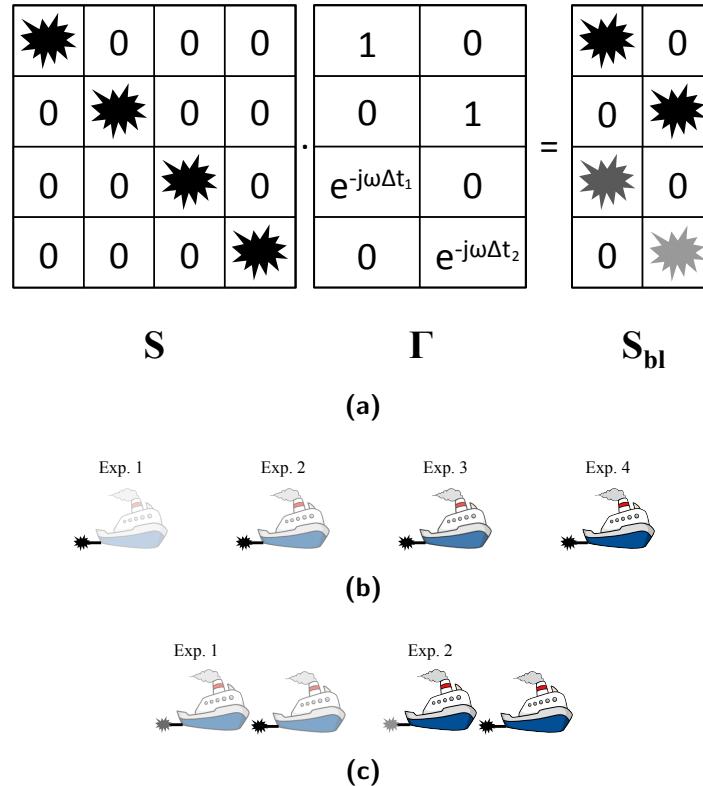


Figure 2-3: (a) A conventional source matrix, \mathbf{S} , is transformed to a blended source matrix, \mathbf{S}_{bl} , by applying the blending matrix, Γ . Each star represents a source, and the gray scale of the stars represents the relative firing time. (b) Illustration of conventional acquisition with one vessel. This acquisition set up is modeled by the source matrix \mathbf{S} . (c) Illustration of blended acquisition with two vessels. In this case the blended source matrix \mathbf{S}_{bl} models the acquisition set up. The experiment number is indicated on top of each drawing.

component of the source signature injected in the earth at the position $x_s = x_i$. By applying a Fourier transform to all frequency components of the element s_{ii} the source signature is obtained.

The impulse response of the earth, \mathbf{X} , describes how an impulse at the source location, x_s , is transformed in the earth into the signal at the receiver location, x_r .

\mathbf{D} is the receiver matrix, which converts the seismic wavefield at the receiver location x_r to the recorded signal. This includes the forward model of the receiver ghost.

In practice, one tries to retrieve the unknown earth response, \mathbf{X} , from the data, \mathbf{P} , by removing \mathbf{S} (signature) and \mathbf{D} (receiver deghosting).

2-1-2 Blended Seismic Data

For blended acquisition the recorded events belonging to different sources overlap as shown in the shot gather in Figure 2-4.

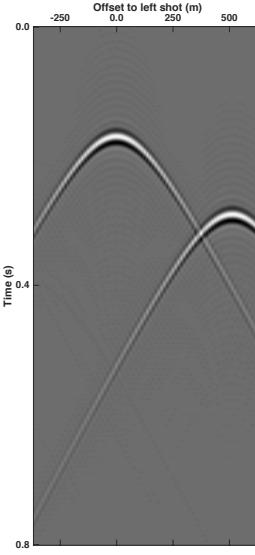


Figure 2-4: Common shot gather of two blended shots. The shot on the right is fired 120 ms after the left shot.

Blending can be captured in the forward model by introducing a blending matrix, Γ , which transforms the source matrix, \mathbf{S} , into a blended source matrix, \mathbf{S}_{bl} ,

$$\mathbf{S}_{bl} = \mathbf{S} \Gamma. \quad (2-2)$$

Each row of Γ represents one source, and each column of Γ represents one experiment (see Figure 2-3).

The blending matrix captures the physics of a blended acquisition as follows: An element γ_{ij} of the blending matrix includes a source i and an experiment j . The source i has a relative amplitude A_{ij} and a relative time delay t_{ij} with respect to the first source fired in the j^{th} experiment;

$$\gamma_{ij} = A_{ij} e^{-j\omega \Delta t_{ij}}. \quad (2-3)$$

If the source i is not fired in the j^{th} experiment the amplitude A_{ij} is zero.

Thus, the blending matrix selects specific sources from the source matrix and superimposes as visualized in Figure 2-3. From Figure 2-3 it also becomes clear that both the blending matrix, Γ , and the blended source matrix, \mathbf{S}_{bl} , have more rows than columns, i.e. there are more sources than experiments.

In the case of source blending the receiver matrix, \mathbf{D} , is not influenced by blending. And of course, the earth impulse response, \mathbf{X} , is independent of the acquisition design. Hence, the blended data can be written as;

$$\mathbf{P}_{bl} = \mathbf{D} \mathbf{X} \mathbf{S}_{bl} = \mathbf{D} \mathbf{X} \mathbf{S} \Gamma = \mathbf{P} \Gamma. \quad (2-4)$$



Figure 2-5: Flowchart belonging to the deblending method of [Mahdad et al. \(2011\)](#).

Note that, the blended data matrix, \mathbf{P}_{bl} , also has less columns, i.e. less experiments, than the unblended data matrix, \mathbf{P} .

2-2 Deblending

Before removing the receiver matrix, \mathbf{D} , and the source matrix, \mathbf{S} , one must remove the blending matrix, $\mathbf{\Gamma}$, from the blended data, \mathbf{P}_{bl} . This process is called deblending.

The deblending method in this thesis builds on the method of [Mahdad et al. \(2011\)](#). Therefore, the method of [Mahdad et al. \(2011\)](#) is described in great detail.

The basic workflow of the method of [Mahdad et al. \(2011\)](#) is summarized in Figure 2-5 and will be explained step by step in the following subsections.

2-2-1 Pseudo-Deblending

Unfortunately, the inverse problem of equation 2-4 is underdetermined, which means that there is not a unique solution for the unblended data, \mathbf{P} . Thus, additional constraints are required to deblend the data, which are sparsity of the signal in the x - t -domain and coherency of the signal in the f - k -domain.

The first estimate of the unblended data matrix, \mathbf{P} , is obtained by pseudo-deblending;

$$\mathbf{P}_{ps} = \mathbf{P}_{bl} \mathbf{\Gamma}^H. \quad (2-5)$$

Pseudo-deblending copies the blended data to the locations of all shots present in the blended shot and shifts them upward in time to compensate for the time delay. For example, Figure 2-6a and 2-6b shows the two pseudo-deblended shot gathers of the blended data in Figure 2-4.



Figure 2-6: Pseudo-deblended data, \mathbf{P}_{ps} , sorted in common shot gathers (a,b) and in a common receiver gather (c). The pseudo-deblended data of the right shot (a) and the left shot (b,c) were shifted by different time delays. The overlapping sources map in the pseudo-deblended shot gathers as coherent events, while they map as incoherent spikes in the pseudo-deblended receiver gather.

2-2-2 Common Receiver Gather

By transforming the data to another domain, e.g. to the common receiver domain, the interfering sources become incoherent and are visible as spiky noise (see Figure 2-6c). Therefore, the interfering sources can be attenuated with a noise filter.

2-2-3 Iterative Blending Noise Estimation

In an ideal case the noise generated by the interfering sources, the so called blending noise, is calculated with the unblended data,

$$\mathbf{N} = \mathbf{P}_{bl} \boldsymbol{\Gamma}^H - \mathbf{P} = \mathbf{P}_{ps} - \mathbf{P}. \quad (2-6)$$

Obviously, in practice the unblended data is unknown and must be estimated by adding extra constraints. The loop shown in Figure 2-5 applies the constraints to reduce the blending noise iteratively until the solution is obtained.

In the following all the quantities which are estimated are indicated with a hat. The steps of the iterative blending noise estimation are demonstrated in Figure 2-7.



Figure 2-7: (a) Pseudo-deblended receiver gather. The subfigures (b)-(f) illustrate each step of the deblending algorithm. For better visibility examples from the 5th iteration are chosen. (b) f - k -spectrum before (top) and after (bottom) f - k -filtering, (c) f - k -filtered common receiver gather, (d) after thresholding, (e) estimated source interference (f) estimated data.



(a) f - k -spectrum of an unblended common shot gather.

(b) The f - k -mask is determined by the minimum signal velocity in the subsurface. The white area of the filter equals one, the black area equals zero. Thus, the filter removes data which is mapped outside of the white signal cone.

Figure 2-8

F-K-Filtering

One of the constraints is coherency, i.e. by assuming the blending noise in Figure 2-6c is incoherent it can be removed. For this purpose the data is transformed from the space time to the wavenumber frequency domain where the spiky noise spreads over all wavenumber and frequency components (see Figure 2-7b, top).

The unblended data maps in the f - k -domain as a cone (see Figure 2-8a). The minimum (physical) velocity, v_{min} , of the subsurface determines the slope of the cone. This means that for a given frequency, f , the maximum wavenumber, k_{max} , is defined as;

$$k_{max} = \frac{f}{v_{min}}. \quad (2-7)$$

In the marine case the minimum velocity is usually the water velocity, $v_w = 1500 \text{ m s}^{-1}$.

For each frequency, f , wavenumbers above k_{max} are removed which results in a 2D f - k -filter as depicted in Figure 2-8b.

The f - k -filter removes the part of the blending noise, which maps outside of the signal cone. Thus, after transforming the data back to the space time domain the amplitudes of the spiky noise are attenuated (see Figure 2-7c).

Note that f - k -filtering can only reduce unaliased frequency components of the blending noise. In Figure 2-8b the highest unaliased frequency is defined by the point where the white cone intersects with the frequency axis, i.e. at 60 Hz.

The high cut frequency of the f - k -mask is set according to the highest frequency components in the data. The aliased blending noise will pass the f - k -filter and will be reduced afterwards by thresholding.

Thresholding

The second constraint for the estimation of the unblended data is sparsity of the signal in the space time domain.

After f - k -filtering the spiky noise is attenuated (see Figure 2-7c). Consequently, the signal amplitudes are now stronger than the noise amplitudes. This allows to define a threshold in the x - t domain, which is larger than the noise amplitudes and smaller than the highest signal amplitudes. Only amplitudes above the threshold are picked, i.e. only signal with strong amplitudes is selected (see Figure 2-7d).

Interference Estimation

The resulting thresholded data, $\bar{\mathbf{P}}$, is used to predict the source interference;

$$\hat{\mathbf{N}}_i = \bar{\mathbf{P}} (\mathbf{\Gamma} \mathbf{\Gamma}^H - \mathbf{I}), \quad (2-8)$$

which is illustrated in Figure 2-7e.

At each iteration the blending noise is attenuated further, such that the threshold can be lowered. Hence, the predicted source interference increases and approaches the true source interference.

Blending Noise Subtraction

The estimate of the unblended data matrix $\hat{\mathbf{P}}_i$ is updated by subtracting the noise from the pseudo-deblended data,

$$\hat{\mathbf{P}}_{i+1} = \mathbf{P}_{bl} \mathbf{\Gamma}^H - \hat{\mathbf{N}}_i, \quad (2-9)$$

which is shown in Figure 2-7f.

This process is repeated iteratively till convergence is reached. In this context convergence can be defined as the point where the difference $|\hat{\mathbf{P}}_{i+1} - \hat{\mathbf{P}}_i|$ drops below a predefined limit. Alternatively, one can set a maximum number of iterations.

Figure 2-9 shows the estimate of the unblended data for increasing iterations. One can observe that the blending noise is attenuated with every iteration, and the blended shot is successively attenuated.

Note that f - k -filtering lowers the noise level by removing unaliased blending noise. Next, the lowered noise level enables thresholding to reduce aliased frequency components of the blending noise. Thus, the combination of f - k -filtering and thresholding is very powerful.



Figure 2-9: Common receiver gather of the estimated data after 1, 5, 10, 15, 20 and 25 iterations.

2-3 Analysis of the Blending Matrix

In order to optimize the blended acquisition design, one must understand the properties of the blending matrix $\boldsymbol{\Gamma}$ and its influence on the deblending performance.

The blending matrix $\boldsymbol{\Gamma}$ determines the pseudo-deblended data,

$$\mathbf{P}_{ps} = \mathbf{P}\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H, \quad (2-10)$$

which is a superposition of the unblended data, \mathbf{P} , and the source interference, \mathbf{N} ,

$$\mathbf{P}_{ps} = \mathbf{P} + \mathbf{N}. \quad (2-11)$$

The more incoherent the source interference, \mathbf{N} , the better it can be removed by noise filters.

In the following the effect of the blending matrix, $\boldsymbol{\Gamma}$, on the product $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ and on the pseudo-deblended data is analyzed. For simplicity, it is assumed that the blending matrix, $\boldsymbol{\Gamma}$, only contains phase shift terms, $e^{-j\omega\Delta t}$, with an amplitude equal to 1 or 0. It is also assumed that each source is fired only once, unlike e.g. the shot repetition case (Wu, 2014).

Each row of $\boldsymbol{\Gamma}$ represents a source k and each column of $\boldsymbol{\Gamma}^H$ represents a source l with a complex conjugated phase term (see Figure 2-10). Hence, each element g_{kl} of the matrix $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ is the dot product between the k^{th} source and the complex conjugate of the l^{th} source.

Consequently, an element g_{kl} of the product $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ represents the overlap of the sources k and l for all experiments. The main diagonal of $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ refers to the overlap of each source with itself, which of course is perfect and therefore equal to 1. The off diagonal elements of $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ are either 0 if the associated sources do not overlap, or contain a phase shift, $e^{-j\omega\Delta t_{kl}}$.

In equation 2-10 the main diagonal elements of $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ copy the data matrix, \mathbf{P} , while the off-diagonal elements create the source interference, \mathbf{N} . If the elements g_{ik} along a sub-diagonal are in phase, they will shift the columns of the data matrix and apply a coherent phase shift to each of them (see Figure 2-11a). Instead if the elements g_{ik} along a sub-diagonal are out of phase, they will shift the columns of the data matrix and distort the phase of each column (see Figure 2-11b).

Figure 2-11c and 2-11d display the f - k -spectra of the pseudo-blended data for constant and random firing time delays respectively. In the case of constant firing time delays almost all of the energy maps in the signal cone. In the case of random firing time delays a significant part of the energy maps outside of the signal cone. Therefore, the coherency constraint requires random firing delays.

Of course, the degree of incoherency of the source interference, \mathbf{N} , also depends on whether the sources blended in an experiment are selected randomly, or in a spatially coherent pattern. For example, one expects the source interference to be more incoherent if in each experiment randomly picked sources are blended, than if in each experiment adjacent sources are blended (see Figure 2-12).

In 2D blending only adjacent sources can be blended, thus, the blended sources cannot be selected randomly. This changes when blending is extended to 3D: Within the crossline direction sources can be selected randomly and blended.

This might need some extra explanation and plot!

$$\begin{array}{c}
 \text{source } k \\
 \left[\begin{array}{cc} e^{-j\omega\Delta t_i} & 0 \\ 0 & e^{-j\omega\Delta t_k} \\ e^{-j\omega\Delta t_j} & 0 \\ 0 & e^{-j\omega\Delta t_l} \end{array} \right] \cdot \left[\begin{array}{cccc} & & & (\text{source } l)_* \\ e^{+j\omega\Delta t_i} & 0 & e^{+j\omega\Delta t_j} & 0 \\ 0 & e^{+j\omega\Delta t_k} & 0 & e^{+j\omega\Delta t_l} \end{array} \right] = \left[\begin{array}{cccc} 1 & 0 & e^{-j\omega\Delta t_{ij}} & 0 \\ 0 & 1 & 0 & e^{-j\omega\Delta t_{kl}} \\ e^{-j\omega\Delta t_{ji}} & 0 & 1 & 0 \\ 0 & e^{-j\omega\Delta t_{lk}} & 0 & 1 \end{array} \right] = \Gamma \Gamma^H
 \end{array}$$

Figure 2-10: Illustration of the matrix product, $\Gamma\Gamma^H$. In this notation Δt_k refers to the phase shift of the source k , and Δt_{kl} refers to the phase shift between the sources k and l , $\Delta t_{kl} = \Delta t_k - \Delta t_l$.



Figure 2-11: Comparison of the pseudo-deblended receiver gather for (a) constant firing time delays of 100 ms, and (b) random firing time delays between 0 ms and 100 ms. (c) and (d) show the f - k -spectra of (a) and (b) respectively.

$$\begin{array}{c}
 \begin{array}{|c|c|} \hline e^{-j\omega\Delta t_i} & 0 \\ \hline 0 & e^{-j\omega\Delta t_k} \\ \hline 0 & e^{-j\omega\Delta t_l} \\ \hline e^{-j\omega\Delta t_j} & 0 \\ \hline \end{array} \cdot \begin{array}{c} \text{(source l)}_* \\ \hline \end{array} = \begin{array}{|c|c|c|c|} \hline 1 & 0 & 0 & e^{-j\omega\Delta t_{ij}} \\ \hline 0 & 1 & e^{-j\omega\Delta t_{kl}} & 0 \\ \hline 0 & e^{-j\omega\Delta t_{lk}} & 1 & 0 \\ \hline e^{-j\omega\Delta t_{ji}} & 0 & 0 & 1 \\ \hline \end{array} \\
 \Gamma \qquad \qquad \qquad \Gamma^H \qquad \qquad \qquad \Gamma \Gamma^H
 \end{array}$$

Figure 2-12: The blending matrix, Γ , is obtained by interchanging the 3rd and 4th row of the blending matrix in Figure 2-10. In acquisition this is equivalent to moving source 3 to experiment 2, and source 4 to experiment 1. A random permutation of the rows of the blending matrix spreads the off-diagonal elements of the matrix product, $\Gamma\Gamma^H$. The elements are not assembled on the sub-diagonals anymore.

Chapter 3

Crossline Deblending (3D)

This thesis suggests to blend crossline sources, i.e. in combination with the movement of the seismic vessel one effectively blends sources in 3D.

The deblending method of [Mahdad et al. \(2011\)](#) described in section [2-2](#) is designed for 2D blended data. In this thesis I will explain how each step of the Mahdad method can be applied to 3D data as well, and I will demonstrate its performance.

First, the data sorting will be modified such that the blended 3D data can be described using the same forward model as in section [2-1](#). Second, the f - k -filter will be extended to an f - k_x - k_y -filter to remove noise in crossline and inline direction. The presented data sorting will allow to maintain all other steps of the deblending algorithm of [Mahdad et al. \(2011\)](#) unchanged.

3-1 Data Sorting

Data Matrix

In 3D acquisition the sources and receivers are distributed on a 2D surface. Thus, their locations are defined by their crossline and inline positions, (x, y) . Each data point which is measured by a source receiver pair at a specific time is therefore described by 5 coordinates: Time t , receiver crossline and inline position (x_r, y_r) , and source crossline and inline position (x_s, y_s) .

The 5D data "cube" will be again reorganized in a 2D data matrix according to [van Dedem \(2002\)](#) (see Figure [3-1](#)). For this data sorting a 1D Fourier transform with respect to time is performed and a frequency slice is selected. This reduces the data array from 5 to 4 dimensions.

The 4D data array is sorted in a 2D data matrix, \mathbf{P} , with as many rows as receivers and as many columns as sources. The total number of sources is obtained by multiplying the number of crossline and inline sources. The total number of receivers is obtained likewise. Assume



Figure 3-1: Illustration of the data matrix \mathbf{P} for 3D data (van Dedem, 2002). y_r and y_s represent the inline receiver and source positions. x_r and x_s represent the crossline receiver and source positions. Each row refers to a 3D common receiver gather and each column to a 3D common shot gather. A sub-matrix with fixed receiver and source inline positions (y_r, y_s) is equivalent to a data matrix for 2D acquisition.

there are N_{sx} sources per crossline. The sources of the first crossline are assigned to the first N_{sx} columns of the data matrix, the sources of the second crossline are assigned to the next N_{sx} columns of the data matrix, etc. The cross- and inline receivers are sorted in the rows of the data matrix in analogy. For example, one row of the data matrix, \mathbf{P} , in Figure 3-1 represents a common receiver gather. The data of this such a common receiver gather is shown in Figure 3-2, where each hyperbolic event refers to the sources of one crossline.

Blending matrix

As described in section 2-3 each row of the blending matrix, Γ , captures one source. For extension to 3D the sources of the first crossline are saved in the top N_{sx} rows of the blending matrix, followed by the sources of the second crossline etc. (see Figure 3-3). The elements in the j^{th} column of the blending matrix, Γ , select the sources which are blended in the j^{th} experiment and give each source a time delay. For example, the first column of the blending matrix in Figure 3-3b describes that in the first experiment sources 1 and 3 are blended with a time delay of Δt_1 .

Keep this sentence for later: This framework allows to blend any source combination independent of the cross- and inline positions of the involved sources.

With the new data and blending matrix sorting one can already apply deblending to 3D data.

The number of total rows in the 2nd subfigure must be changed from N_{sy} to $N_{sx} \times N_{sy}$.

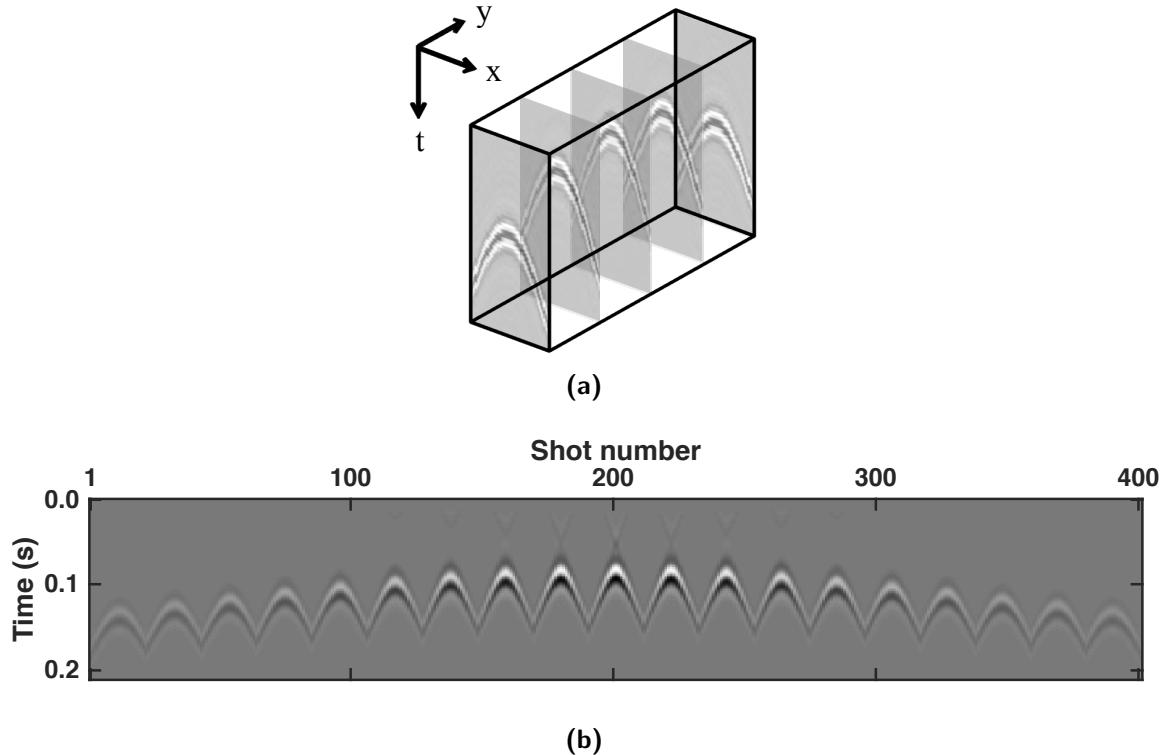


Figure 3-2: (a) Common receiver gather of a 3D data set with crossline (x) and inline (y) sources.
 (b) Resorting data set. Individual crossline sections are plotted next to each other in 2D. For visibility both subfigures only show a reduced part of the data.

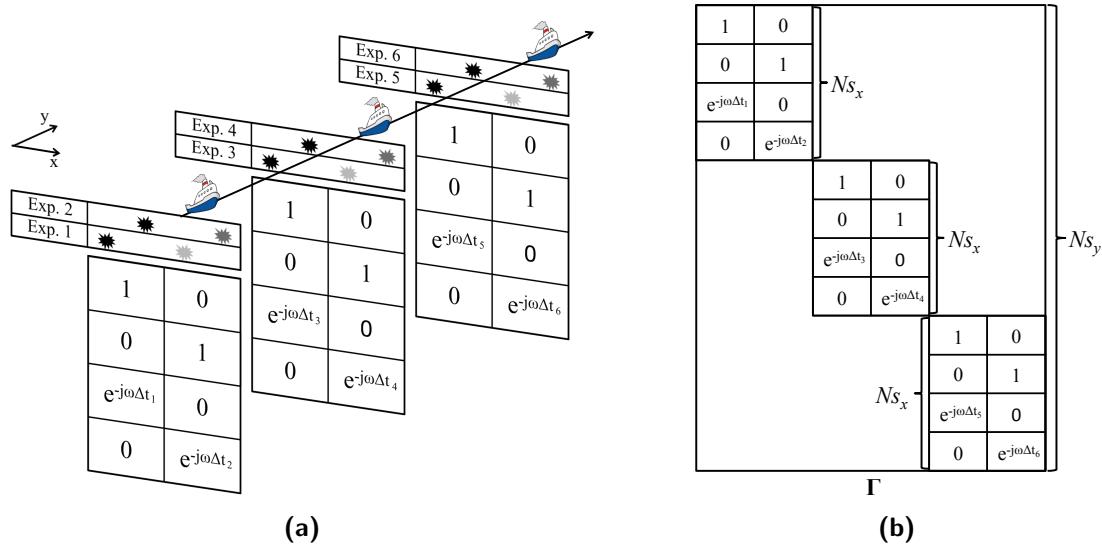


Figure 3-3: Illustration of the blending matrix, Γ , for 3D acquisition. (a) At each of the N_{s_y} inline position the crossline sources (x direction) are blended. Each of these 2D blending processes is described by a 2D blending matrix, which has as many rows as there are crossline sources, N_{s_x} . (b) The 2D blending matrices are assembled in a single 3D blending matrix, Γ , which has N_{s_x} by N_{s_y} rows.

3-2 3D f-k-k Filter

In section 2-2-3 the 2D f - k filter was introduced. In 3D there are two spatial direction (x , y), i.e. the filter can be extended to a 3D f - k_x - k_y -filter.

The deblending method is applied to common receiver gathers. Thus, one picks a single receiver, which is a data cube, $\mathbf{p}(t, x_s, y_s)$. The common receiver gather, $\mathbf{p}(t, x_s, y_s)$, is transformed to the f - k_x - k_y -domain by applying an n-dimensional Fourier transform. Next, a constant frequency slice is selected. This leaves a 2D matrix, which captures the cross- and inline wavenumbers (k_x , k_y) (see Figure 3-4a). Again the minimum velocity, v_{min} , and the frequency, f , determine the maximum wavenumber, k_{max} , according to equation 2-7. The total wavenumber, k_T , must be smaller than the maximum wavenumber, k_{max} ,

$$k_T = \sqrt{k_x^2 + k_y^2} < k_{max}. \quad (3-1)$$

Hence the signal "cone" is defined by a circle (see Figure 3-4b). This is repeated for each frequency component, such that the overall f - k_x - k_y -mask is a 3D cone (see Figure 3-4). Finally, this mask is computed for each receiver gather.



Figure 3-4: Illustration of the 3D f - k_x - k_y -filter. (a) and (b) show a 40 Hz frequency slice of the f - k_x - k_y -spectrum, where k_x and k_y refer to the crossline and inline wavenumber respectively. (a) is the spectrum of the data in Figure 3-2b, and (b) is the corresponding filter mask. The white area equals 1 and the black area is 0. (c) and (d) display the f - k_x - k_y -spectrum sorted according to section 3-1, i.e. each sub-cone refers to one crossline. Note that the sorting implies that the wavenumber axis is a mix of crossline and inline wavenumbers. For this reason the wavenumber axis has no labels. (c) represents the data and (d) the filter mask.

Chapter 4

Results

This chapter presents the major results of this thesis. First, an optimal blending pattern for simultaneous crossline sources will be derived. Then, the advantages of a 3D $f\text{-}k_x\text{-}k_y$ -filter towards a 2D $f\text{-}k$ -filter will be shown. Finally, the feasibility of the suggested acquisition design will be proven on a synthetic 3D data set.

4-1 Blending pattern

An incoherent blending pattern is crucial for good deblending performance (see section 2-3). Thus, a measure of incoherency and deblending quality will be introduced. Then, the possibilities of creating an incoherent blending pattern are presented. Finally, the effect of incoherency and of the maximum firing time delay on the deblending performance will be demonstrated.

Incoherency Measure

In this thesis only the incoherency of the acquisition design is considered. Thus, the blending matrix, Γ , or more precisely the product $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ determines the incoherency.

In section 2-3 it was shown that for an incoherent blending pattern the elements, $e^{-j\omega\Delta t_{kl}}$, along a sub-diagonal of the product $\boldsymbol{\Gamma}\boldsymbol{\Gamma}^H$ should be out of phase. Therefore, the phase variability of the sub-diagonal elements will be used to quantify incoherency.

Note that the sub-diagonal elements, $e^{-j\omega\Delta t_{kl}}$, map in the complex plane on a circle with radius 1 (see Figure 4-1).

The sum of the elements along the k^{th} sub-diagonal can be constructive or destructive, depending on the phase variability. Thus, the absolute value of the sum measures the incoherency of an individual sub-diagonal. The resulting value is squared in order to put it in terms of energy;

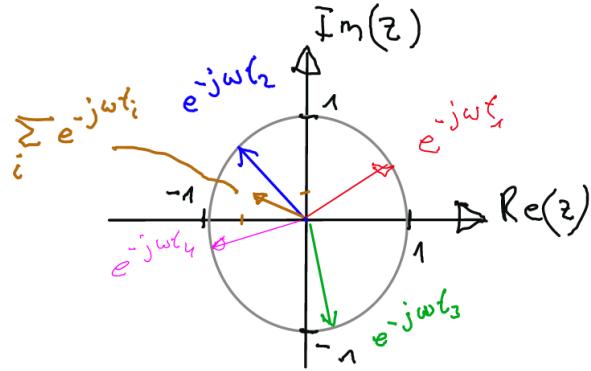


Figure 4-1: Illustration of the sub-diagonal elements in the complex number plane. The elements have unit length and variable phase. The absolute value of their sum depends on the phase coherency of the elements.

$$\left| \sum_{j-i=k} \mathbf{\Gamma}\mathbf{\Gamma}_{ij}^H(\omega) \right|^2. \quad (4-1)$$

For example, if all elements are in phase the length of their sum is maximized. The more the elements are out of phase, i.e. the more incoherent they are, the smaller is the length of the summed elements.

For illustration a blending matrix, $\mathbf{\Gamma}$, is generated and inserted in equation 4-1. This yields an output for each sub-diagonal, which is shown in Figure 4-2. The spike is caused by the elements on the main diagonal of $\mathbf{\Gamma}\mathbf{\Gamma}^H$, which are all equal to 1, i.e. in phase. For a perfectly incoherent blending design the elements on a sub-diagonal cancel and the plot becomes a perfect spike.

The closer Figure 4-2 comes to a spike the more incoherent is the blending pattern. Thus, considering Figure 4-2 the incoherency, μ , is measured as the ratio between the amplitude of the spike and the sum of all amplitudes.

In terms of the sub-diagonals of $\mathbf{\Gamma}\mathbf{\Gamma}^H$ this is the ratio between the squared absolute value of the summed main diagonal and the sum of all squared absolute summed sub-diagonals;

$$\mu(\omega) = \frac{\left| \sum_{j-i=0} \mathbf{\Gamma}\mathbf{\Gamma}_{ij}^H(\omega) \right|^2}{\sum_{k=1-N_s}^{N_s-1} \left(\left| \sum_{j-i=k} \mathbf{\Gamma}\mathbf{\Gamma}_{ij}^H(\omega) \right|^2 \right)}. \quad (4-2)$$

Note that N_s is the number of sources, i.e. the matrix $\mathbf{\Gamma}\mathbf{\Gamma}^H$ has N_s rows and columns.

Up to now, the incoherency is computed for each frequency separately. In order to account for all frequencies at once the nominator and denominator in equation 4-2 are summed over all frequency components;

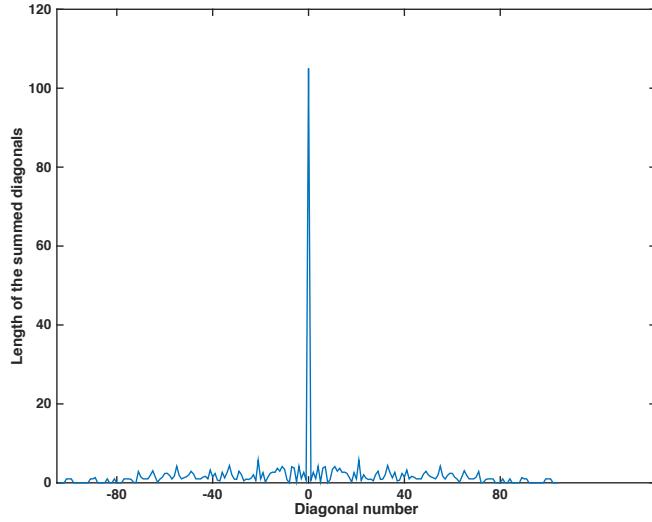


Figure 4-2: The sub-diagonal elements, $e^{-j\omega\Delta t_{kl}}$, of the product $\mathbf{\Gamma}\mathbf{\Gamma}^H$ are summed. The length of each output is plotted. The spike is caused by the main diagonal elements of $\mathbf{\Gamma}\mathbf{\Gamma}^H$ because they are all in phase.

$$\mu = \frac{\sum_{\omega} \left(\left| \sum_{j-i=0} \mathbf{\Gamma}\mathbf{\Gamma}_{ij}^H(\omega) \right|^2 \right)}{\sum_{\omega} \left(\sum_{k=1-N_s}^{N_s-1} \left(\left| \sum_{j-i=k} \mathbf{\Gamma}\mathbf{\Gamma}_{ij}^H(\omega) \right|^2 \right) \right)}. \quad (4-3)$$

For example, for a perfectly incoherent blending pattern only the sum along the main diagonal ($k = 0$) is non zero. Thus, the nominator and the denominator in equation 4-3 are identical, the incoherency equals 1.

In contrast, for a perfectly coherent blending pattern all sub-diagonal elements are in phase. Consequently, the sum along the main diagonal is of the same magnitude as the sum along the sub-diagonals. The nominator in equation 4-3 becomes significantly smaller than the denominator, and the incoherency is nearly 0.

Deblending Performance Measure

The following data examples are synthetic data, i.e. the unblended data is known. Therefore, the deblending performance can be measured with the quality factor, Q , which is defined by Ibrahim and Sacchi (2015) as;

$$Q = 10 \cdot \log_{10} \left(\frac{\|\text{Unblended data}\|_2^2}{\|\text{Unblended data} - \text{Deblended data}\|_2^2} \right). \quad (4-4)$$

Incoherent Blending Patterns

This thesis considers the following blended acquisition set up: The sources are assembled in crossline direction and move towards inline direction due to the vessel movement (see

Figure 3-3a). As a consequence each experiment can blend sources which belong to the same crossline. The inline source sampling rate must be sufficiently small to avoid spatial aliasing. Thus, the sources within one crossline must be blended and recorded before the vessel reaches the next inline position.

Based on this set up there are three possibilities to blend the sources incoherently.

Temporal incoherency: The sources are blended with random time delays.

Spatial incoherency: One can randomly picks sources for each experiment.

Mixed incoherency: Temporal and spatial incoherency can be combined, i.e. randomly picked sources are blended with random time delays.

First, the sources can be blended with random time delays (temporal incoherency). Second, one can randomly pick sources for each experiment (spatial incoherency). Third, temporal and spatial incoherency can be combined, i.e. randomly picked sources are blended with random time delays.

In the following these blending patterns will applied to a synthetic data set (see Figure 4-3a, 4-4a, 4-4e). Next, the data is deblended with the 3D deblending algorithm of chapter 3.

The deblending results are shown in Figure 4-3 and 4-4. The results suggest that only spatial incoherency is not sufficient to deblend the data (see Figure 4-3b, 4-4b, 4-4f). By introducing random firing time delays the deblended data improves significantly as shown in Figure 4-3c, 4-4c, 4-4g). A combination of both spatial and temporal incoherency enhances the deblended data further (see Figure 4-3d, 4-4d, 4-4h).

Make a sketch of the set up of the synthetic data.

The deblending performance is quantified with a quality factor, Q , which is defined by Ibrahim and Sacchi (2015) as;

$$Q = 10 \cdot \frac{\|\text{Unblended data}\|_2^2}{\|\text{Unblended data} - \text{Deblended data}\|_2^2}. \quad (4-5)$$

Figure 4-5 illustrates the quality factor for the 3 blending patterns as a function of the maximum firing time delay. The plot confirms the previous observations: Only spatial incoherency limits the deblended data quality, whereas temporal incoherency allows to achieve significantly better deblending performance. The combination of spatial and temporal incoherency can even enhance the result further.



Figure 4-3: These 3D common receiver gathers are sorted according to section 3-1. The unblended synthetic data (a) is used to simulate a blended acquisition with 3 experiments per crossline and 7 shots per experiment. The maximum firing time delay is 400 ms. The sources are blended in three different patterns: (b) Randomly selected sources are blended without time delay, (c) neighboring sources are blended with random time delays, (d) randomly picked sources are blended with random time delays. Next, the blended data sets are deblended. The corresponding deblending results are illustrated in (b) to (d).

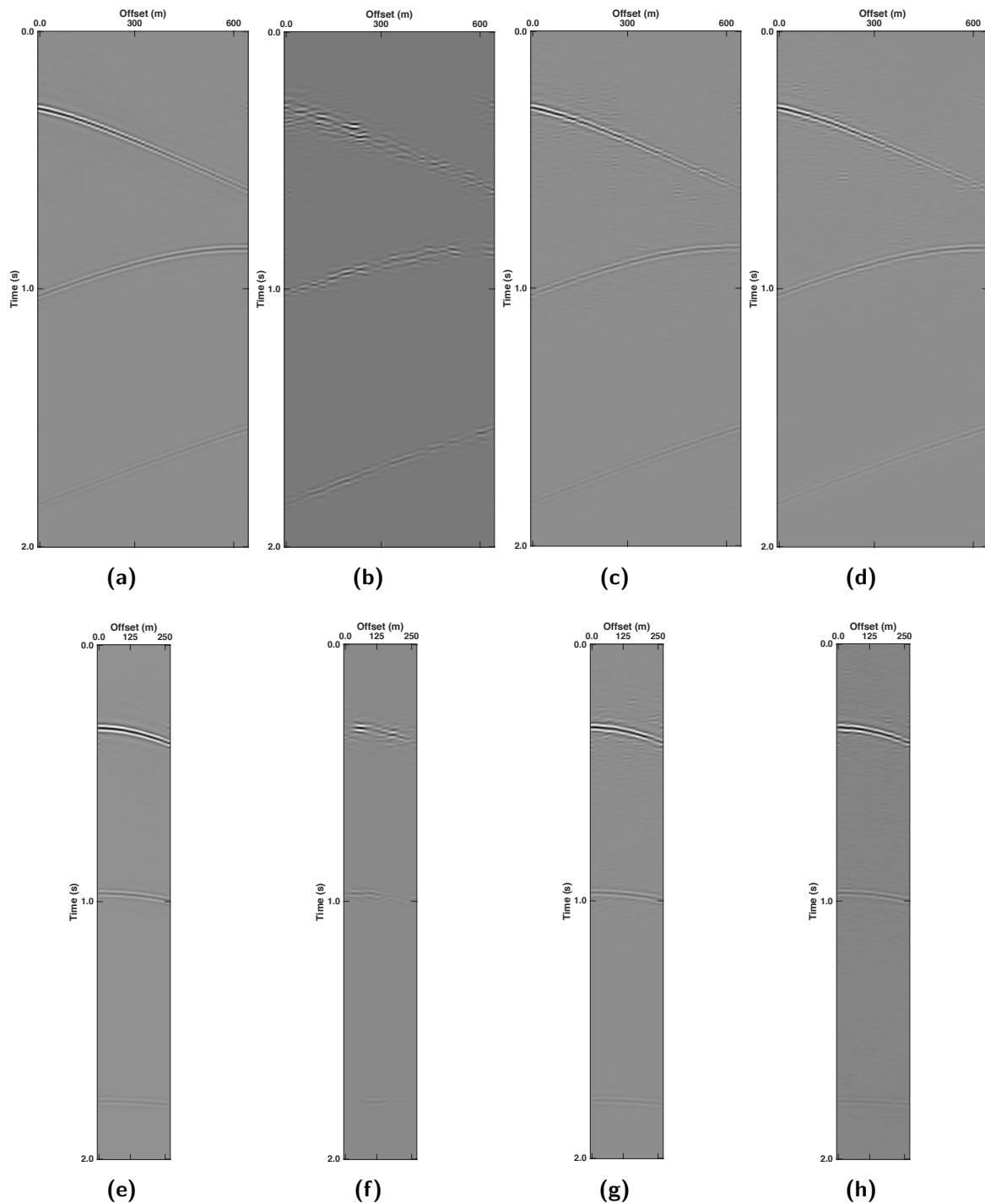


Figure 4-4: (a)-(d) show inline slices of the data shown in Figure 4-3. (e)-(h) display the corresponding crossline slices.

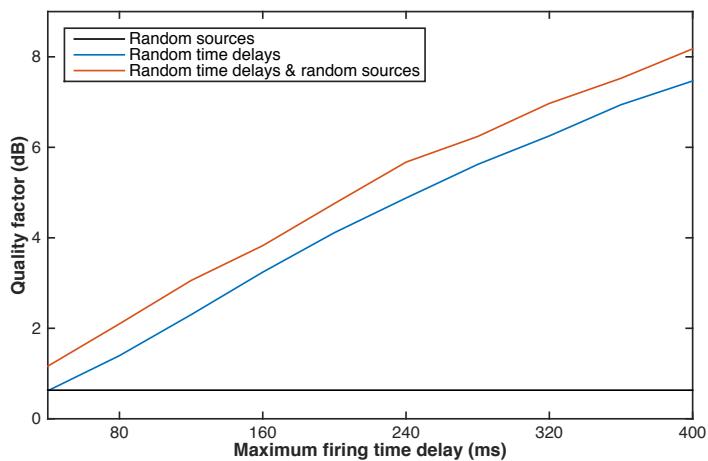


Figure 4-5: The 3 suggested blending patterns are simulated with maximum firing time delays between 40 ms and 400 ms. The quality factors are computed with respect to the unblended data and illustrated as a function of the maximum firing time.

4-2 3D FKK Filter Performance

4-3 Feasibility

Chapter 5

Incoherency

When multiple sources are applied in one experiment the wavefields of the individual sources overlap. [Mahdad et al. \(2011\)](#) presented a method to separate the overlapping wavefields: A key step is pseudo-deblending, which yields the the desired unblended data superimposed by so called blending noise. This noise is generated by the overlap of the individual sources and can be removed with noise filters. However, if the individual wavefields overlap coherently, the blending noise will also be coherent and cannot be removed. In other words it is crucial to fire the sources incoherently.

In this chapter the incoherency of the source overlap is analyzed by considering three questions: Which factors control the incoherency? How can the incoherency be measured? How can the incoherency be maximized for an optimal deblending result?

5-1 Incoherency Control Factors

The deblended data can be represented by

$$\mathbf{P}_{\text{debl}} = \mathbf{X} \mathbf{S} \boldsymbol{\Gamma} \boldsymbol{\Gamma}^H. \quad (5-1)$$

Each of the matrices in the above equation influences the degree of incoherency of the source overlap. First, the contribution of the Earth \mathbf{X} is neglected because it cannot be controlled in a seismic experiment. Second, the source signature \mathbf{S} , in particular its time duration, determines the required minimum time delay between sources to avoid an overlap. Consequently, when designing an acquisition with simultaneous sources one must take into account the source signature. Thirdly, the incoherency is strongly dependent on the blending matrix $\boldsymbol{\Gamma}$ because it captures the firing pattern, i.e. it knows which sources are superimposed and the time delays between the sources in a given experiment. Therefore, the main focus of the incoherency analysis will be on the blending matrix $\boldsymbol{\Gamma}$.

5-2 Quantification of Incoherency

A mathematical tool to express incoherency is the autocorrelation function $R(\tau)$,

$$R(\tau) = \int_{\mathbb{R}} f^*(x)f(x + \tau) dx. \quad (5-2)$$

For example, in a 1D case the autocorrelation of a fully incoherent function is a spike at zero lag. If a coherent or repetitive pattern is present in a function the autocorrelation will also have non zero amplitudes at other lags.

For comparative purposes the incoherency of a function $f(x)$ should be quantified. It is suggested to measure incoherency μ as the ratio of the squared zero lag autocorrelation and the sum of the squared autocorrelation amplitudes,

$$\mu = \frac{R(\tau = 0)^2}{\sum_{\tau} R(\tau)^2}. \quad (5-3)$$

This expression quantifies incoherency as a number between 0 and 1. A fully incoherent function $f(x)$ yields an autocorrelation which is a perfect spike. Thus, the ratio in equation 5-3 equals 1. For a perfectly coherent function $f(x)$ the ratio in equation 5-3 is nearly zero.

The incoherency strongly depends on the blending matrix Γ which is a 3D array. Before applying an autocorrelation the blending matrix Γ is transformed to time domain. The time domain blending matrix is denoted as γ . It has the dimensions

$$\dim(\gamma) = \text{Sources} \times \text{Experiments} \times \text{Time}. \quad (5-4)$$

If a source s_i is fired in an experiment e_i at a time t_i the element (s_i, e_i, t_i) of γ is 1, else it is 0. If the source is not a perfect spike its amplitude can smear out across several time samples in the matrix γ .

The incoherency of the blending matrix γ can be quantified by replacing the 1D autocorrelation in equation 5-2 and 5-3 with a 3D autocorrelation, which can be written as,

$$R(\tau_1, \tau_2, \tau_3) = \iiint_{\mathbb{R}^3} f^*(x, y, z)f(x + \tau_1, y + \tau_2, z + \tau_3) dx dy dz. \quad (5-5)$$

The calculation of the 3D autocorrelation function requires significant computational power such that symmetry properties of the autocorrelation should be exploited to reduce the cost. Symmetry with respect to the origin, but using convn in Matlab I cannot access it

The elements of the resulting 3D autocorrelation array are a measure for the correlation between wavefields at a specific source, experiment and time lag. For example, if in each experiment adjacent sources are fired with a constant time delay Δt , the 3D autocorrelation will yield a high amplitude at the source lag 1, experiment lag 0 and time lag Δt .

Combining equations 5-3 and 5-5 the incoherency of the time domain blending matrix γ can be expressed as,

$$\mu = \frac{R(\tau_1 = 0, \tau_2 = 0, \tau_3 = 0)^2}{\sum_{(\tau_1, \tau_2, \tau_3)} R(\tau_1, \tau_2, \tau_3)^2}. \quad (5-6)$$

5-3 Optimization of Incoherency

Relate the incoherency estimate to the quality factor of the deblending. Point out that the quality factor is very sensitive to the time incoherency while the incoherency with respect to experiments or sources has less impact on the deblending performance.

5-4 Fingerprint of the Incoherency in the Blending Matrix Γ

To achieve a better understanding of the blending process the relation between the incoherency quantification and the blending matrix Γ is assessed.

In frequency domain the blending matrix has the dimension,

$$\dim(\boldsymbol{\Gamma}) = \text{Sources} \times \text{Experiments} \times \text{Frequency}, \quad (5-7)$$

where each element is a complex number $a e^{-j\omega t}$.

Mahdad et al. (2011)

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Appendix A

The back of the thesis

A-1 An appendix section

A-1-1 An appendix subsection with C++ Listing

```
//  
// C++ Listing Test  
//  
#include <stdio.h>  
for( int i=0;i<10;i++)  
{  
    cout << "Ok\n";  
}
```

1
6

A-1-2 A Matlab Listing

```
%  
% Comment  
%  
n=10;  
for i=1:n  
    disp('Ok');  
end
```

5

Appendix B

Yet another appendix

B-1 Another test section

Ok, all is well.

Index

LaTeX, 1