

```
import math
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

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ICS 635: Machine Learning

Homework 1

Part 1: Q1- Q3

Part 2: Q4 in [C.Edwards_Homework 1 Question 4.ipynb](#)

▼ QUESTION 1

Model Classes: For each situation below, would you use Regression, Classification, or Clustering models?

- Predicting the inches of rainfall tomorrow given the inches of rainfall over the past week (0.2 points) **Linear Regression**
- Predicting the type of skin cancer from an image of the skin (0.2 points) **Classification**
- Determining the best grouping students into grade buckets of A+, A, A-, B+, B, B-, C+, C, C-, and F (0.2 points) **Clustering**
- Forecasting the number of COVID-19 cases in 1 month given prior history (0.2 points) **Linear Regression**
- Face ID on a smartphone (0.2 points) **Classification**

▼ QUESTION 2: ROC Curve

▼ Code/Work

```
def calc_y_hat(x,x2):
    """
    Given logistic regression model
    Y_hat = 1/(1+e^-(3x-4x2+3))
    """

    y_hat = 1/(1 + math.exp(-((3*x)-(4*x2)+3)))

    return y_hat

#test
print(calc_y_hat(0,0)) #Expected: 0.952574...

    0.9525741268224334

def thresh(p,y_hat):
    """
    Classifies y_hat given threshold p
    """
    if y_hat>p:
        return 1
    return 0

#test
print(thresh(0.4,0.9)) #1
print(thresh(0.4,0.2)) #0

    1
    0

x1 = np.array([0, 0, 0, 1, 1, 1, 2, 2, 2, -1])
x2 = np.array([0, 1, 2, 0, 1, 2, 0, 1, 2, 0])
y = np.array([1,1,0,1,1,0,1,1,0,0])
y_hat = np.full(10,-1)
```

```
print(x1.shape)
print(x2.shape)
print(y.shape)
print(y_hat.shape)

(10,)
(10,)
(10,)
(10,)


data = {'x1':x1, 'x2':x2, 'y':y , 'y_hat': y_hat}
data

{'x1': array([ 0,  0,  0,  1,  1,  1,  2,  2,  2, -1]),
 'x2': array([0, 1, 2, 0, 1, 2, 0, 1, 2, 0]),
 'y': array([1, 1, 0, 1, 1, 0, 1, 1, 0, 0]),
 'y_hat': array([-1, -1, -1, -1, -1, -1, -1, -1, -1, -1])}

df = pd.DataFrame(data)
df
```

	x1	x2	y	y_hat	
0	0	0	1	-1	
1	0	1	1	-1	
2	0	2	0	-1	
3	1	0	1	-1	
4	1	1	1	-1	
5	1	2	0	-1	
6	2	0	1	-1	
7	2	1	1	-1	
8	2	2	0	-1	
9	-1	0	0	-1	

```
df['y_hat'] = df.apply(lambda x: calc_y_hat(x['x1'],x['x2']), axis=1)
df
```

	x1	x2	y	y_hat	
0	0	0	1	0.952574	
1	0	1	1	0.268941	
2	0	2	0	0.006693	
3	1	0	1	0.997527	
4	1	1	1	0.880797	
5	1	2	0	0.119203	
6	2	0	1	0.999877	
7	2	1	1	0.993307	
8	2	2	0	0.731059	
9	-1	0	0	0.500000	

```
#threshold calcs 0, 0.2, 0.4, 0.6, 0.8, 1
df['0'] = df.apply(lambda x: thresh(0,x['y_hat']), axis = 1)
df
```

	x1	x2	y	y_hat	0
0	0	0	1	0.952574	1
1	0	1	1	0.268941	1
2	0	2	0	0.006693	1
3	1	0	1	0.997527	1
4	1	1	1	0.880797	1
5	1	2	0	0.119203	1
6	2	0	1	0.999877	1

```
df['0.2'] = df.apply(lambda x: thresh(0.2,x['y_hat']), axis = 1)
df['0.4'] = df.apply(lambda x: thresh(0.4,x['y_hat']), axis = 1)
df['0.6'] = df.apply(lambda x: thresh(0.6,x['y_hat']), axis = 1)
df['0.8'] = df.apply(lambda x: thresh(0.8,x['y_hat']), axis = 1)
df['1'] = df.apply(lambda x: thresh(1,x['y_hat']), axis = 1)
```

df

	x1	x2	y	y_hat	0	0.2	0.4	0.6	0.8	1
0	0	0	1	0.952574	1	1	1	1	1	0
1	0	1	1	0.268941	1	1	0	0	0	0
2	0	2	0	0.006693	1	0	0	0	0	0
3	1	0	1	0.997527	1	1	1	1	1	0
4	1	1	1	0.880797	1	1	1	1	1	0
5	1	2	0	0.119203	1	0	0	0	0	0
6	2	0	1	0.999877	1	1	1	1	1	0
7	2	1	1	0.993307	1	1	1	1	1	0
8	2	2	0	0.731059	1	1	1	1	0	0
9	-1	0	0	0.500000	1	1	1	0	0	0

```
def cmatrix(actual,predicted):
    '''
    confusion matrix
    '''
    true_pos,false_neg,false_pos,true_neg = [0]*4

    for p,a in zip(predicted,actual):

        #print((p,a))
        if (p,a) == (1,1):
            true_pos += 1
            continue

        if (p,a) == (1,0):
            false_pos += 1
            continue

        if (p,a) == (0,1):
            false_neg += 1
            continue

        if (p,a) == (0,0):
            true_neg += 1
            continue

        else:
            print('should_not_reach')
    return {'TP':true_pos, 'FN': false_neg, 'FP': false_pos, 'TN':true_neg}

print(cmatrix(df['y'],df['0'])) #Expected TP:6 FN:0 FP:4 FN:0

{'TP': 6, 'FN': 0, 'FP': 4, 'TN': 0}
```

```

m_0 = cmatrix(df['y'],df['0'])
m_2 = cmatrix(df['y'],df['0.2'])
m_4 = cmatrix(df['y'],df['0.4'])
m_6 = cmatrix(df['y'],df['0.6'])
m_8 = cmatrix(df['y'],df['0.8'])
m_1 = cmatrix(df['y'],df['1'])

```

```
m_6
```

```
{'TP': 5, 'FN': 1, 'FP': 1, 'TN': 3}
```

```
#calculate y-axis: true positive rate    x-axis: false positive rate
```

```

def roc(m):
    '''
    tpr = true positive / true positive + false negative
    fpr = false positive/false positive + true negative
    '''
    tpr = m['TP']/(m['TP'] + m['FN'])
    fpr = m['FP']/(m['FP'] + m['TN'])

    return {'tp_rate': tpr, 'fp_rate':fpr}

```

```
print(roc(m_6)) #Expected {'tp_rate': 0.833... , fp_rate': 0.25}
```

```
{'tp_rate': 0.8333333333333334, 'fp_rate': 0.25}
```

```

print(roc(m_0))
print(roc(m_2))
print(roc(m_4))
print(roc(m_6))
print(roc(m_8))
print(roc(m_1))

```

```

{'tp_rate': 1.0, 'fp_rate': 1.0}
{'tp_rate': 1.0, 'fp_rate': 0.5}
{'tp_rate': 0.8333333333333334, 'fp_rate': 0.5}
{'tp_rate': 0.8333333333333334, 'fp_rate': 0.25}
{'tp_rate': 0.8333333333333334, 'fp_rate': 0.0}
{'tp_rate': 0.0, 'fp_rate': 0.0}

```

▼ ROC Curve

```

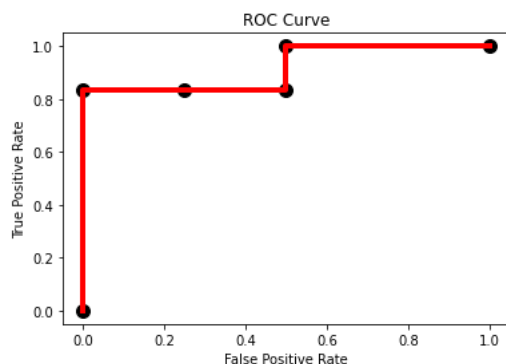
x = np.array([roc(m_0)['fp_rate'], roc(m_2)['fp_rate'], roc(m_4)['fp_rate'], roc(m_6)['fp_rate'],roc(m_8)['fp_rate'],roc(m_1)['fp_rate']])
y = np.array([roc(m_0)['tp_rate'], roc(m_2)['tp_rate'], roc(m_4)['tp_rate'], roc(m_6)['tp_rate'],roc(m_8)['tp_rate'],roc(m_1)['tp_rate']])

```

```

plt.plot(x, y, 'o', markersize = 10, color = 'black')
plt.plot(x,y, linewidth = 4, color = 'red')
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('ROC Curve')
plt.show()

```



▼ AUROC:

The AUROC score evaluates the efficiency of model on a scale from 0 to 1; where 1 indicated a perfect classifier.

▼ QUESTION 3: Evaluation Metrics

```
def new_thresh(y_hat):
    '''
    New decision threshold
    p >= 0.5
    '''
    if y_hat>=0.5:
        return 1
    return 0

df['0.5'] = df.apply(lambda x: new_thresh(x['y_hat']), axis = 1)
df
```

	x1	x2	y	y_hat	0	0.2	0.4	0.6	0.8	1	0.5	
0	0	0	1	0.952574	1	1	1	1	1	0	1	
1	0	1	1	0.268941	1	1	0	0	0	0	0	
2	0	2	0	0.006693	1	0	0	0	0	0	0	
3	1	0	1	0.997527	1	1	1	1	1	0	1	
4	1	1	1	0.880797	1	1	1	1	1	0	1	
5	1	2	0	0.119203	1	0	0	0	0	0	0	
6	2	0	1	0.999877	1	1	1	1	1	0	1	
7	2	1	1	0.993307	1	1	1	1	1	0	1	
8	2	2	0	0.731059	1	1	1	1	0	0	1	
9	-1	0	0	0.500000	1	1	1	0	0	0	1	

```
conf_matrix = cmatrix(df['y'],df['0.5'])
conf_matrix

{'TP': 5, 'FN': 1, 'FP': 2, 'TN': 2}

accuracy = (conf_matrix['TP']+conf_matrix['TN'])/(conf_matrix['TP']+conf_matrix['FN']+conf_matrix['FP']+conf_matrix['TN'])
precision = (conf_matrix['TP'])/(conf_matrix['TP']+conf_matrix['FP'])
recall = (conf_matrix['TP'])/(conf_matrix['TP']+conf_matrix['FN']) #sensativity
specificity= (conf_matrix['TN'])/(conf_matrix['TN']+conf_matrix['FP'])

print(f"Accuracy: {accuracy *100}")
print(f"Precision: {precision *100}")
print(f"Recall: {recall *100}")
print(f"Specificity: {specificity *100}")

Accuracy: 70.0
Precision: 71.42857142857143
Recall: 83.33333333333334
Specificity: 50.0
```

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