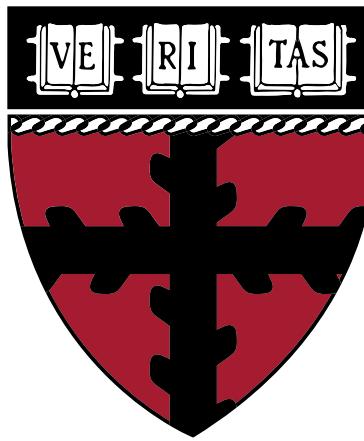


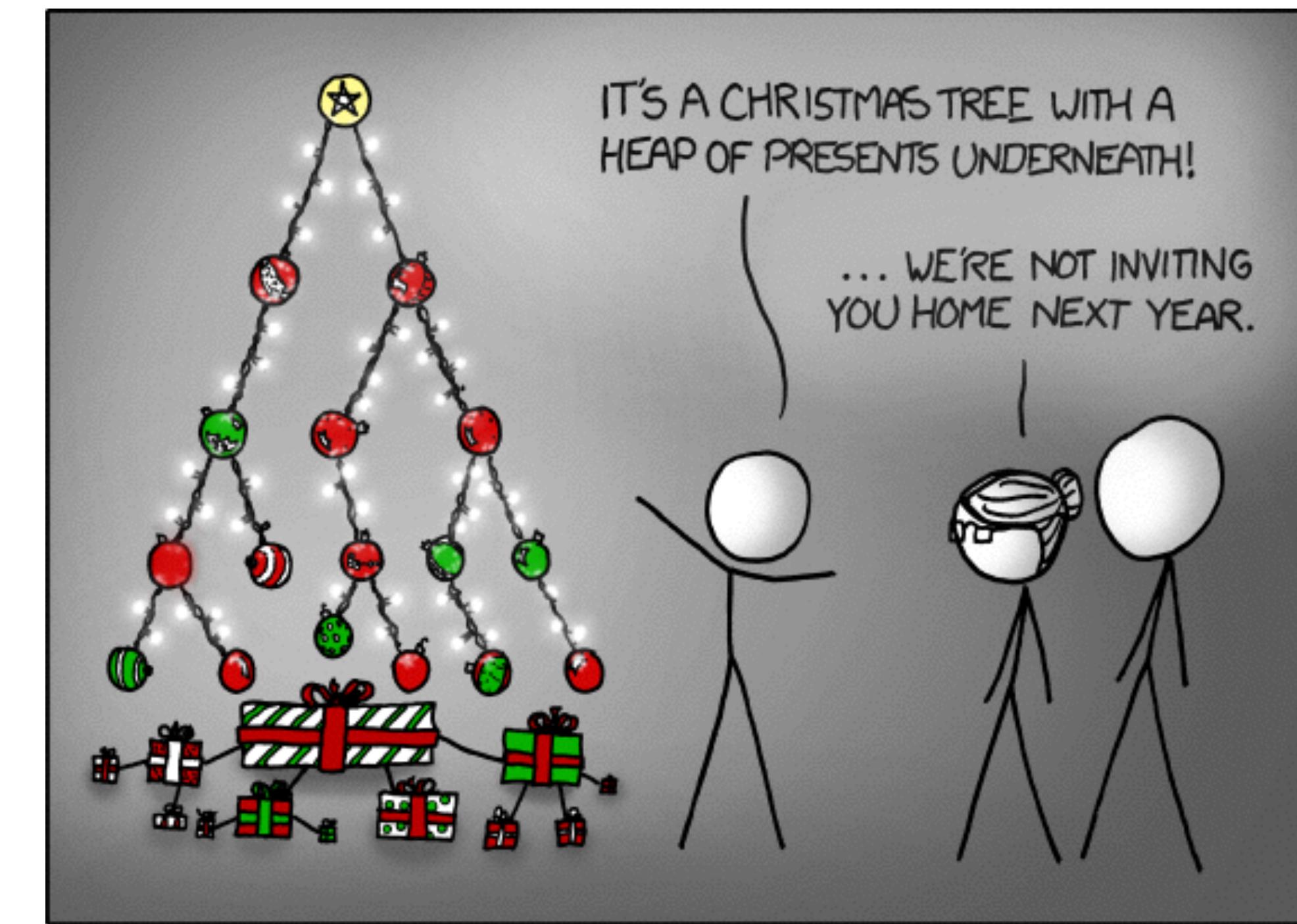
CS171 Visualization

Alexander Lex
alex@seas.harvard.edu

Graphs



HARVARD
School of Engineering
and Applied Sciences



[xkcd]

This Week

Reading: VAD, Chapters 9

Lecture 12: Text & Documents

Sections: D3 and JS Design Guidelines. HW1 Review.

Updates

Design Studio moved to Tuesday after Spring-Break

HW 4 consists of “only” the project proposal

Design Exercise

Data & Use Case by Augusto Sandoval

Student question: How to show this data?

ID

Gender

High School Type

Degree

Year of Admission

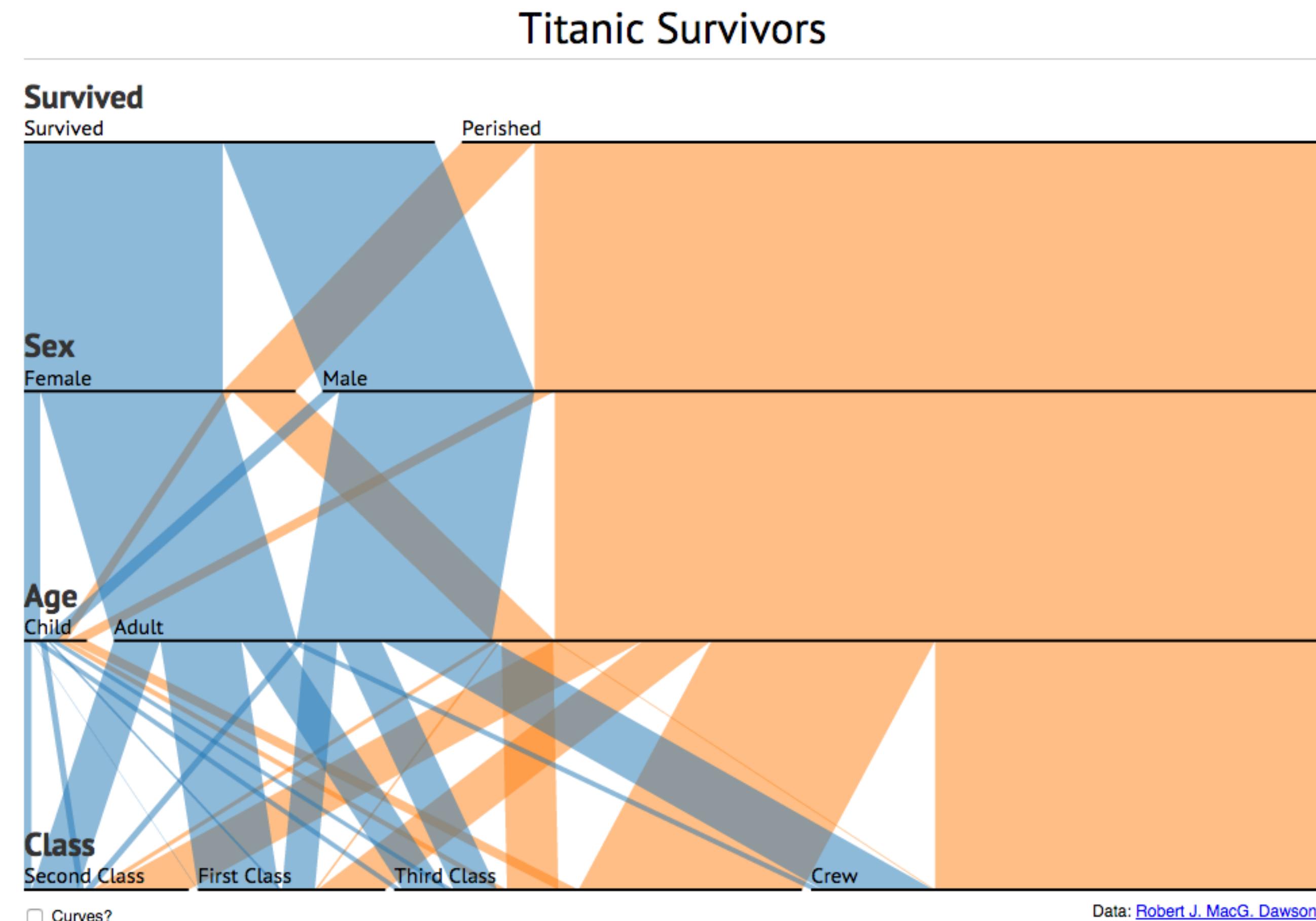
GPA

GPA z-score

Id	gender	Type of High Sch	Degree	Year of admission	GPA	GPA zscore by Degree
nNYliG0HwFTjdFNks1	M	Private	journalism	2012	0	-6.384275
eT+GiwpOBm4QJ3cZ	M	Public	engineering	2008	0.188888888	-5.895198
ryP0ztCYW26aMdUq	M	Private	Laws	2004	0	-5.730906
S034U/Z7g9IQXTuU9	M	Private	Arts	2012	0.266666666	-5.028417
9Z16bxKDeVDbGiiD8	F	Private	Arts	2012	1.666666667	-2.331488
4EI03gz2P0m1wkwAi	M	Private	engineering	2013	0.6	-4.865675
Ic+5vQGCtRba7j/vTxI	M	Private	engineering	2012	0.844444444	-4.363712
9Rqf6BCleCiywUVdG	F	Private	history	2012	0.76	-4.033634
iJtFP+NRF/yVVW2yLk	M	Private	agronomy	2012	0.84	-3.64938
nKiM2cmiLt5hXdGQp	M	Private	engineering	2009	1	-4.000308
2s9GWUyTNMwyl8al	M	Public	theology	2008	0.911111111	-3.627317
ug3OgnYirUcEUlmXtJ	F	Private	nursing	2011	1.733333333	-4.0063
Sm+XS3+8amJFzowV	M	Private	theology	2013	0.983333333	-3.507009
jrwfkQmu9YDTzWdEi	F	Public	nursing	2010	1.85	-3.495274
Jv6VtB+mIVY30ZYR4l	M	Private	business	2012	1.316666667	-3.428196
szP2BH1uaYrsk3w9JC	F	Private	COLLEGE	2012	1	-3.345934
ellKHcnNQ0fW9jxR94	F	Private	Laws	2013	1.253333333	-3.256467
qdY8dwFW0CxGdqUI	F	Private	nursing	2008	1.933333333	-3.250402

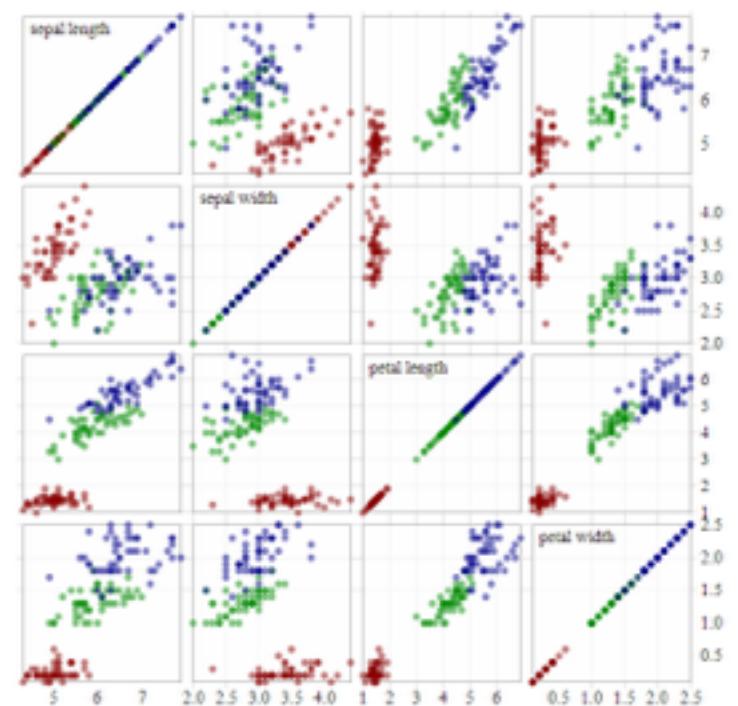
Visualizing Categorical Data

Example:
Parallel Sets

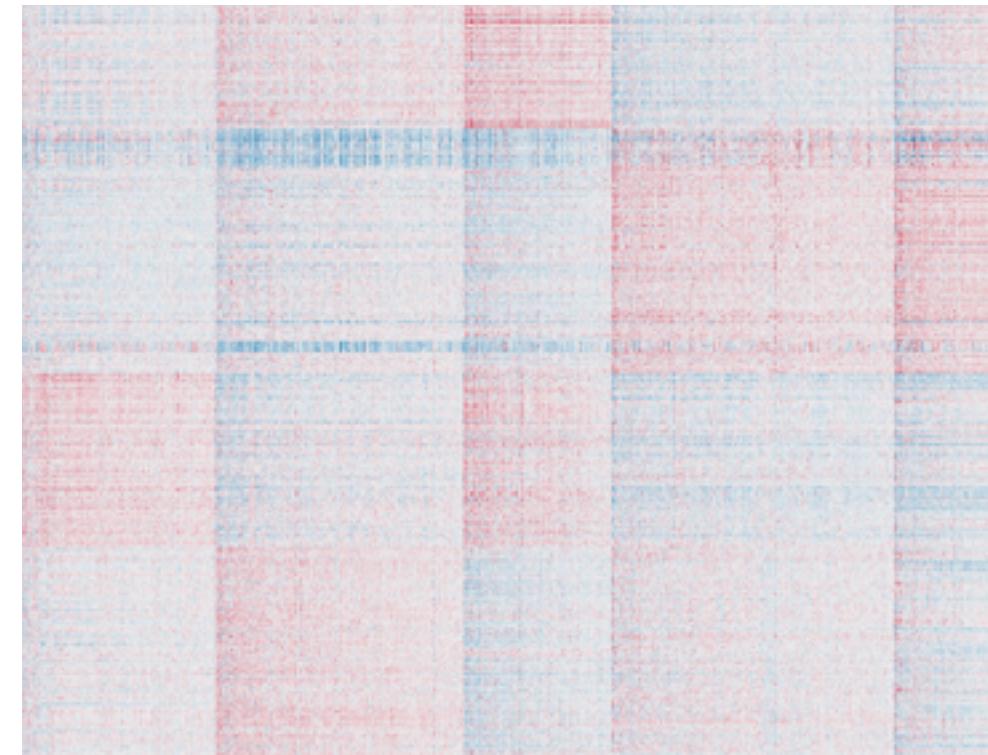


Last Week: Highdimensional Data

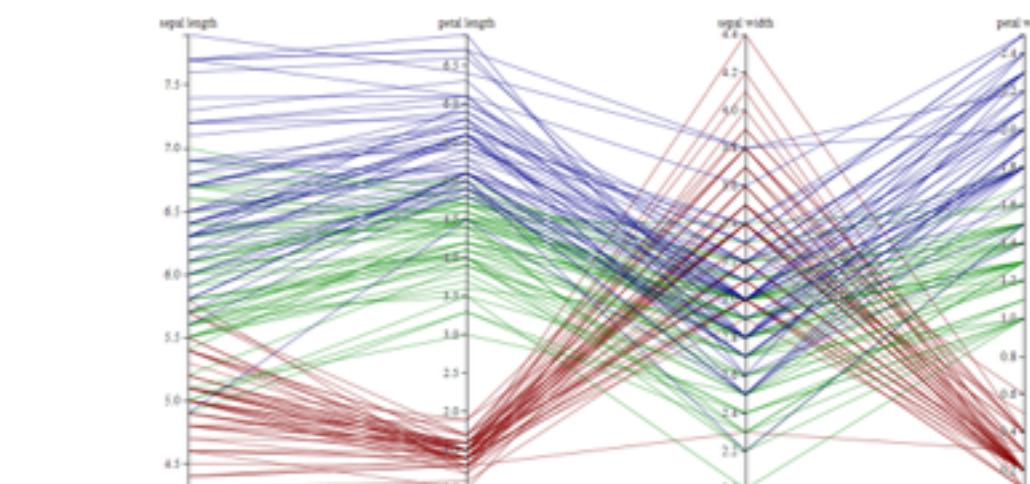
Analytic Component



Scatterplot Matrices
[Bostock]



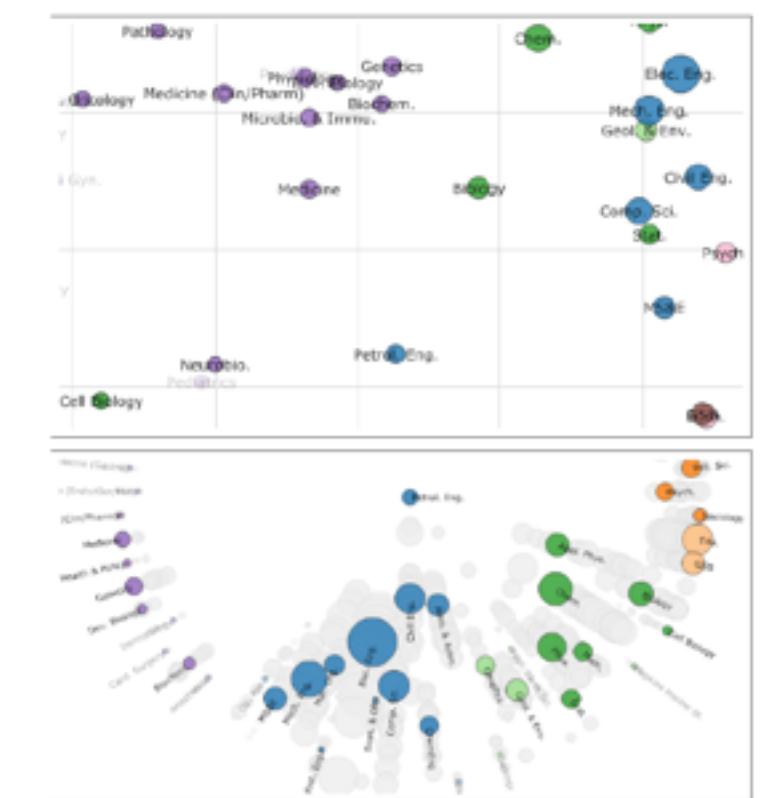
**Pixel-based visualizations /
heat maps**



Parallel Coordinates
[Bostock]



Multidimensional Scaling
[Doerk 2011]



[Chuang 2012]

no / little analytics

**strong analytics
component**

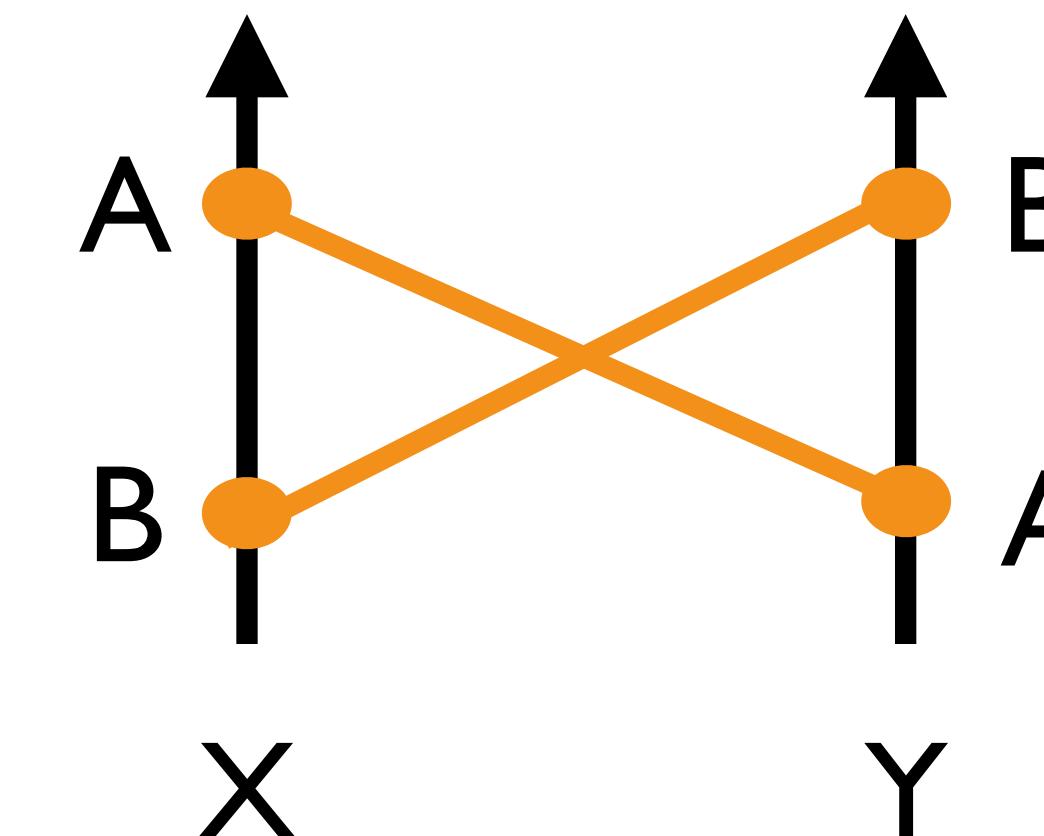
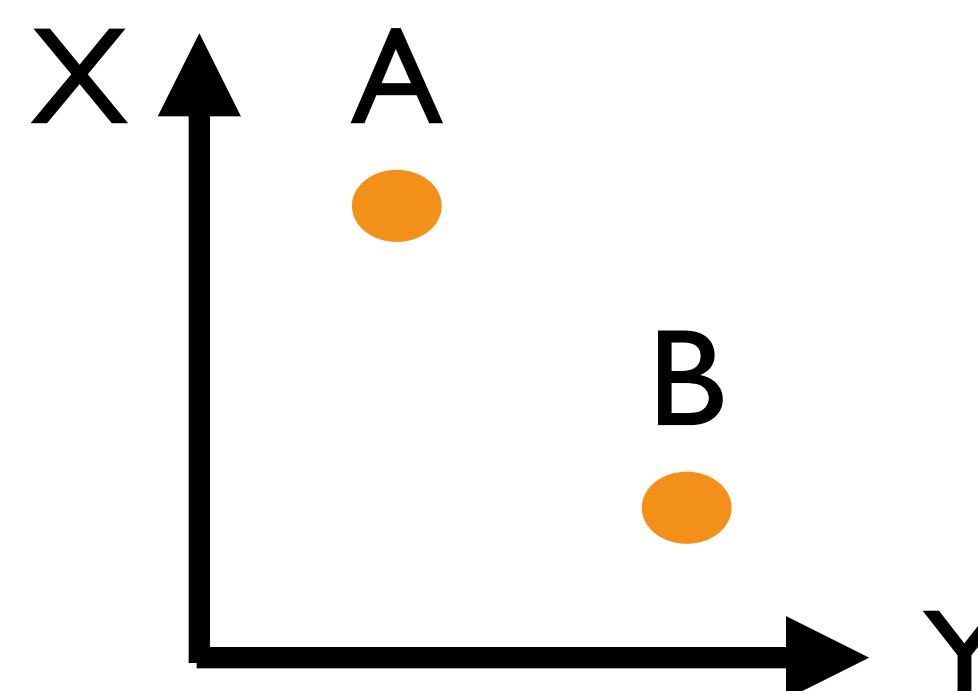
Geometric Methods

Parallel Coordinates (PC)

Inselberg 1985

Axes represent attributes

Lines connecting axes represent items



Parallel Coordinates

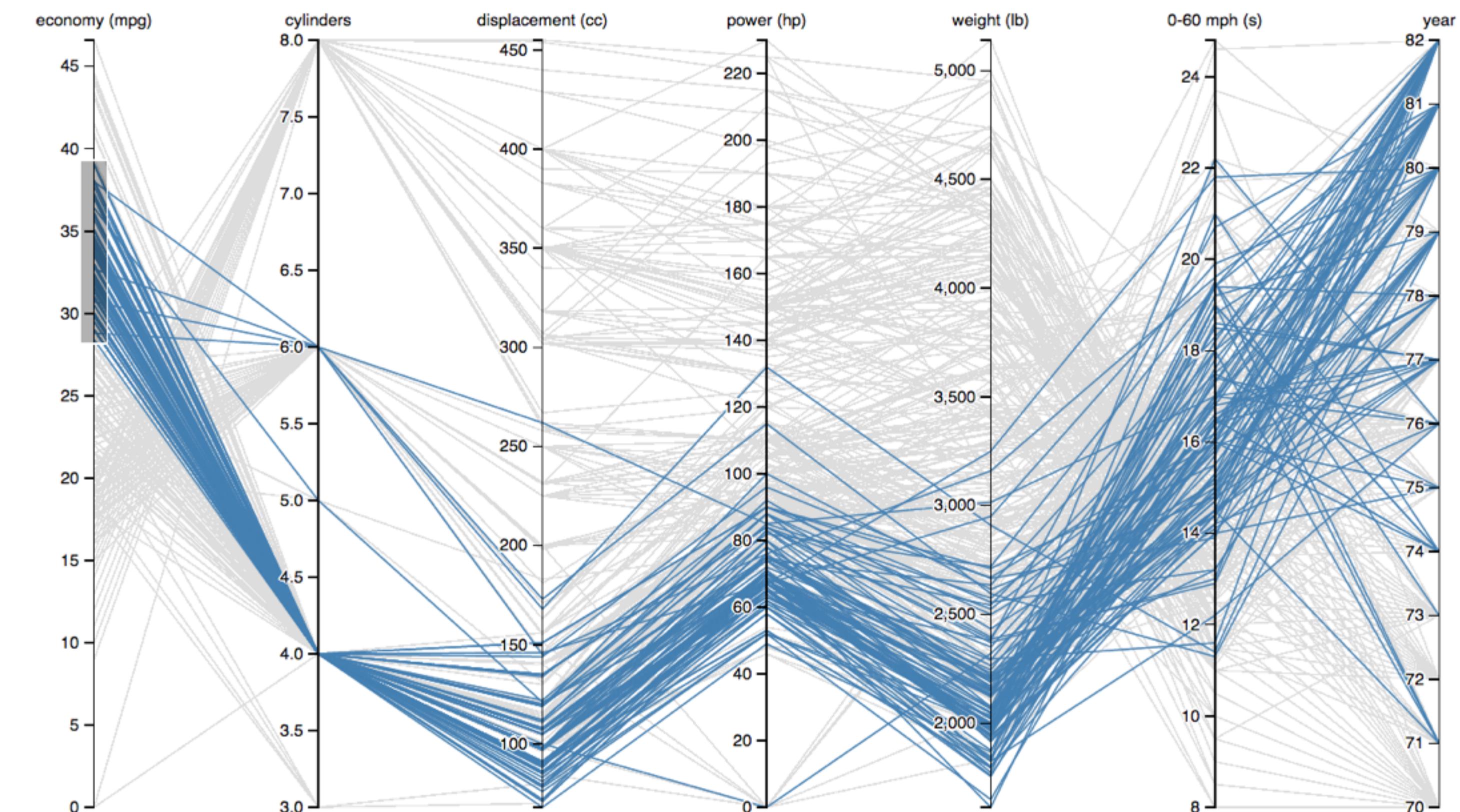
Each axis represents dimension

Lines connecting axis represent records

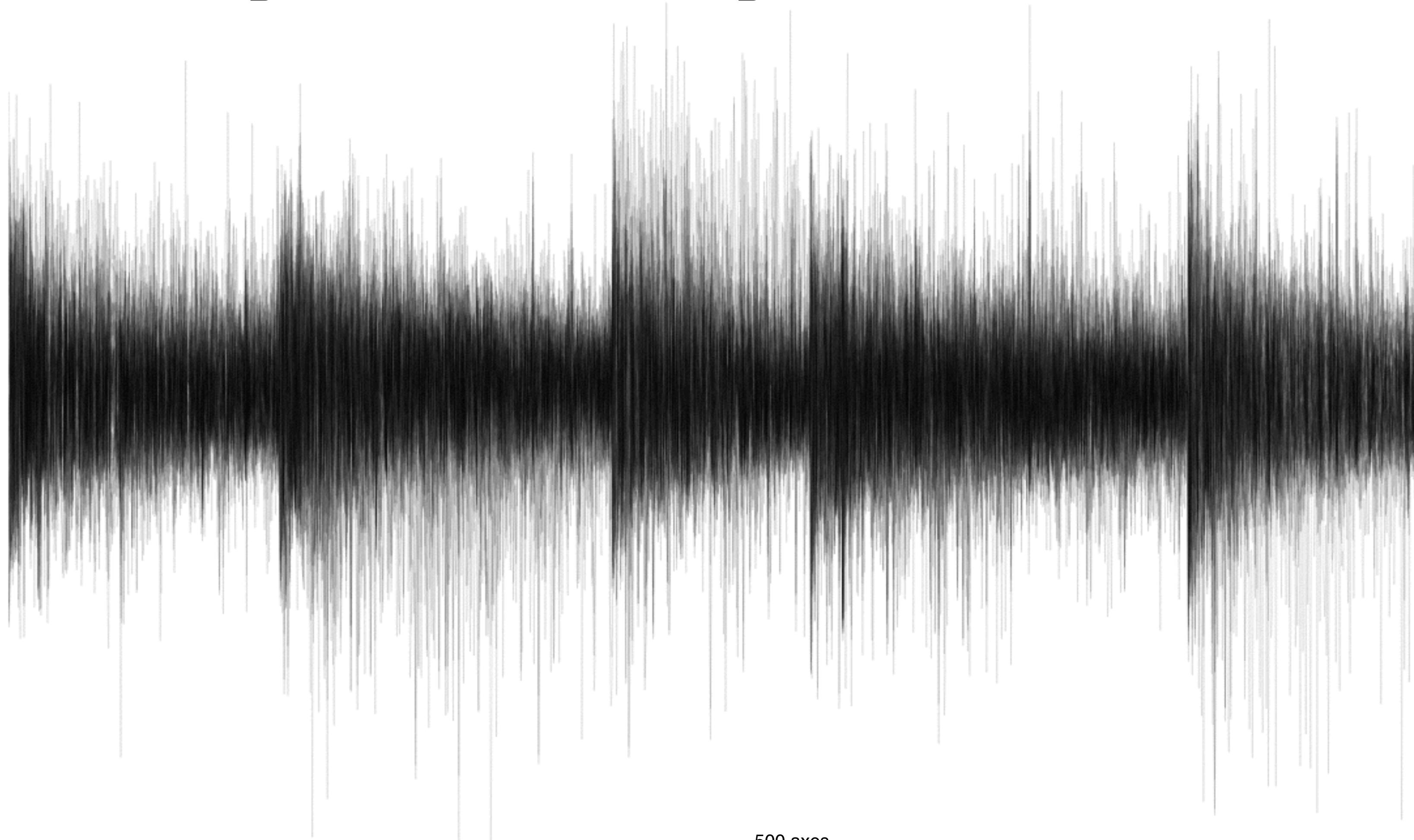
Suitable for

all tabular data types

heterogeneous data



PC Limitation: Scalability to Many Dimensions



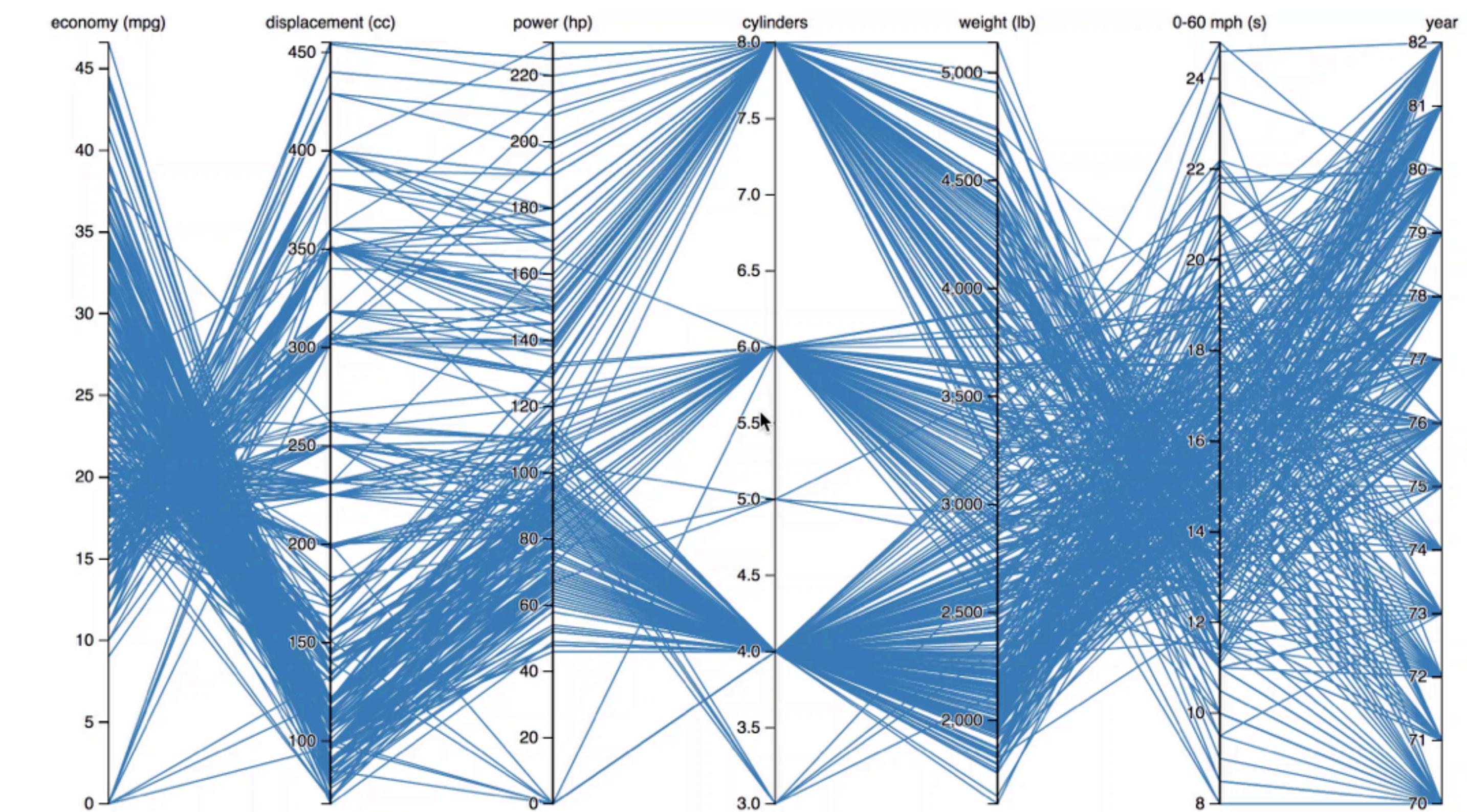
PC Limitations

Correlations only between adjacent axes

Solution: Interaction

Brushing

Let user change order



Parallel Coordinates

Shows primarily relationships between adjacent axis

Limited scalability (~50 dimensions, ~1-5k records)

Transparency of lines

Interaction is crucial

Axis reordering

Brushing

Filtering

Algorithmic support:

Choosing dimensions

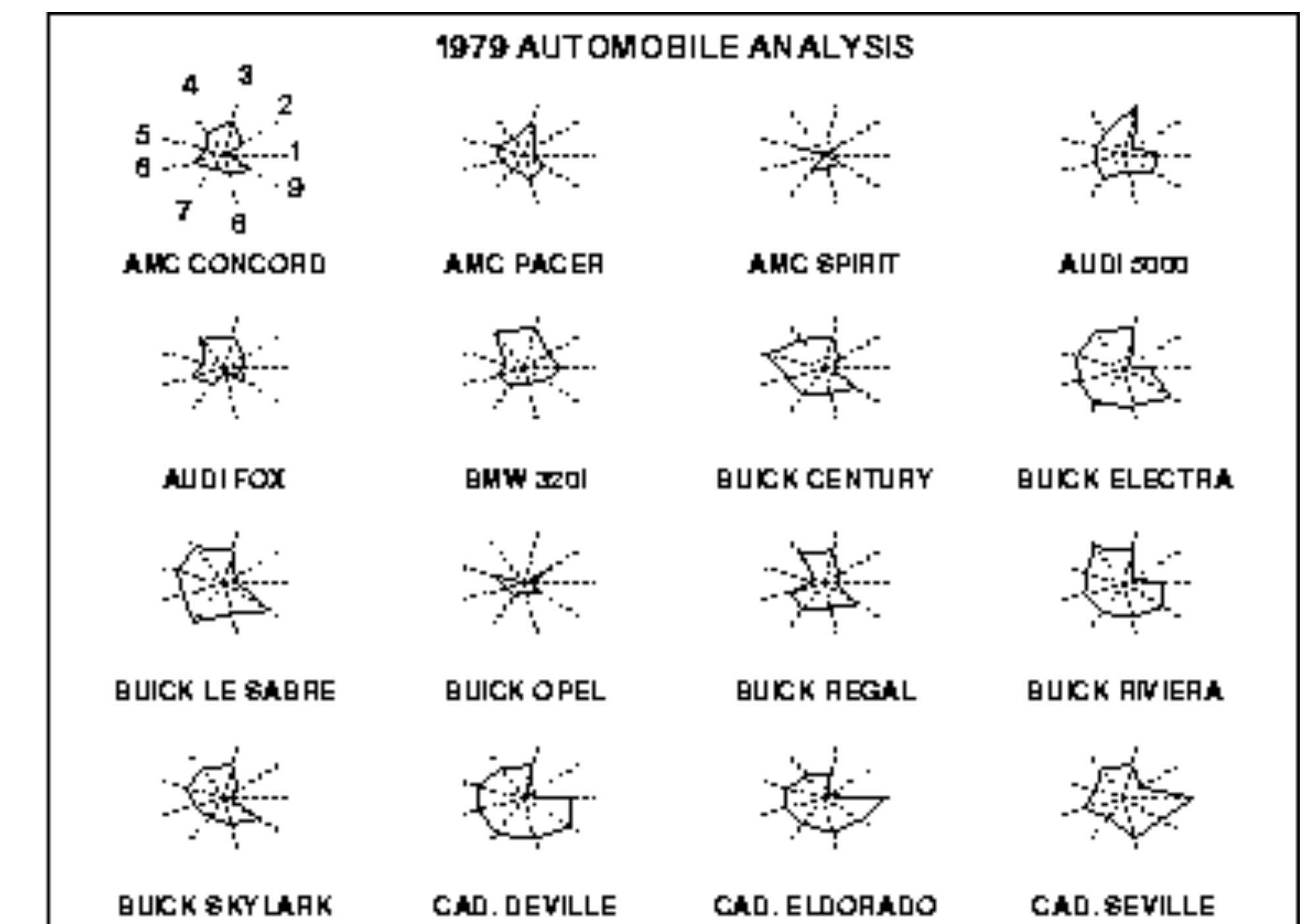
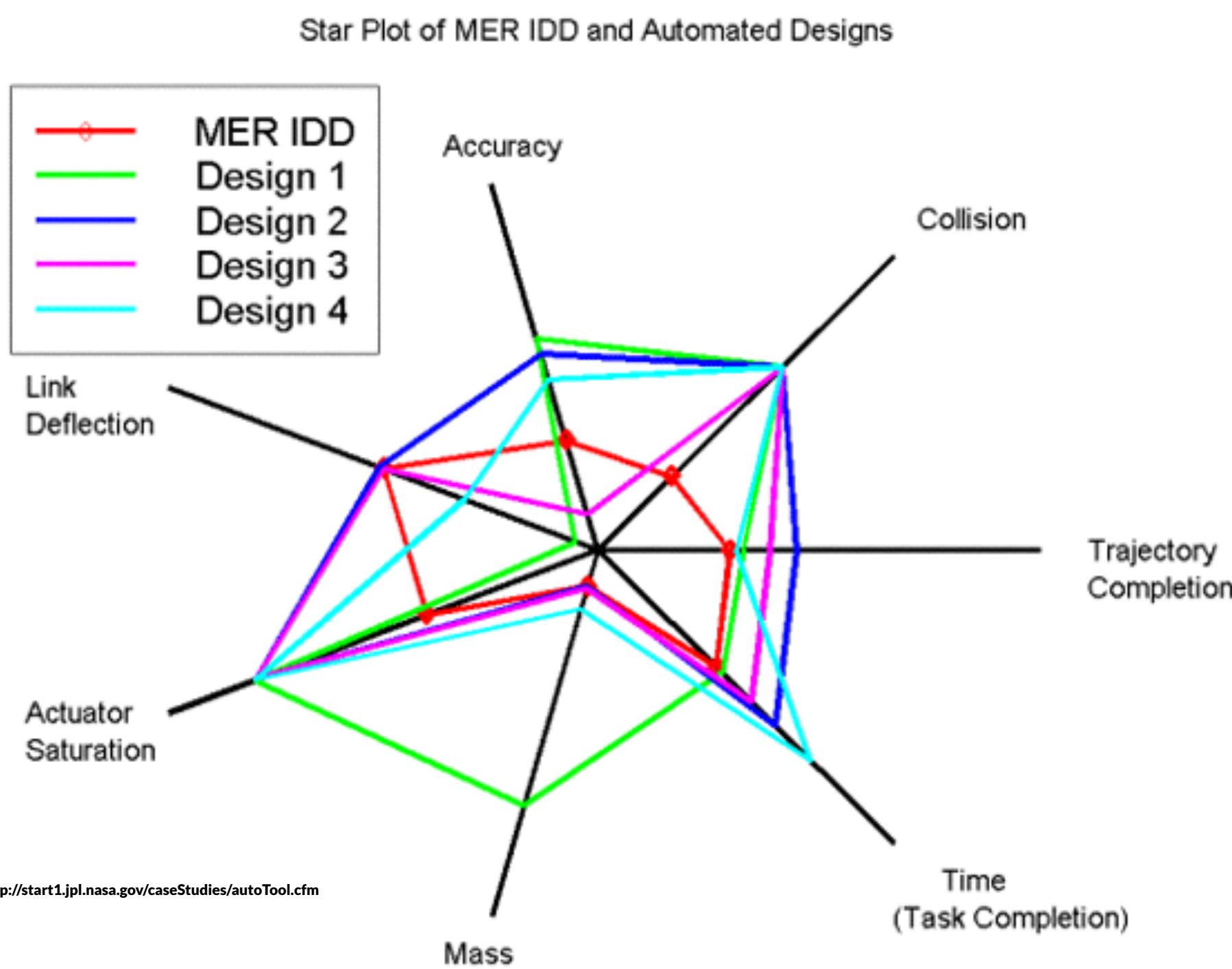
Choosing order

Clustering & aggregating records

Star Plot

[Coekin1969]

Similar to parallel coordinates
Radiate from a common origin



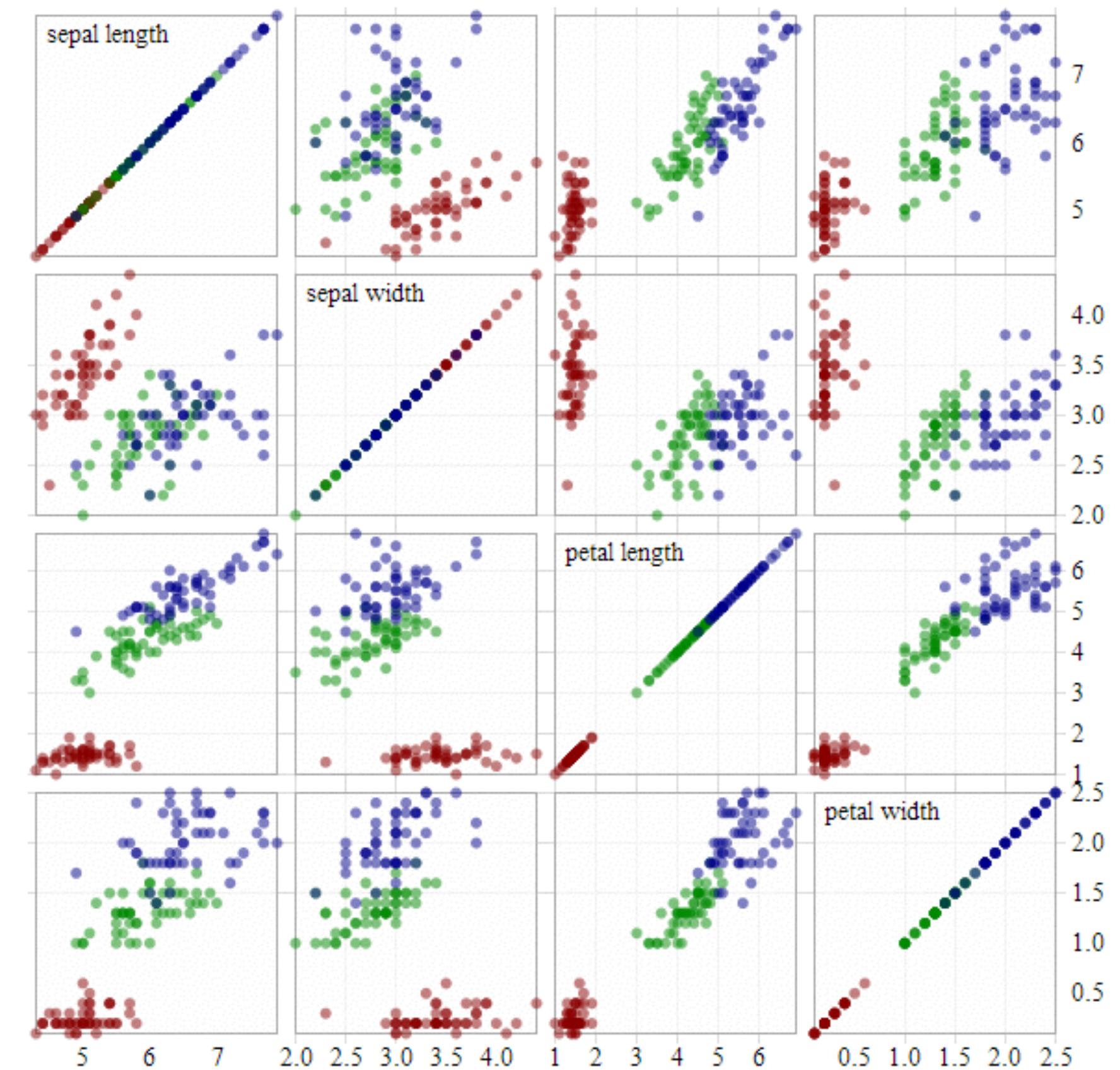
<http://blocks.org/kevinschaul/raw/8833989/>

Scatterplot Matrices (SPLOM)

Matrix of size $d \times d$

Each row/column is one dimension

Each cell plots a scatterplot of two dimensions



Scatterplot Matrices

Limited scalability (~20 dimensions, ~500-1k records)

Brushing is important

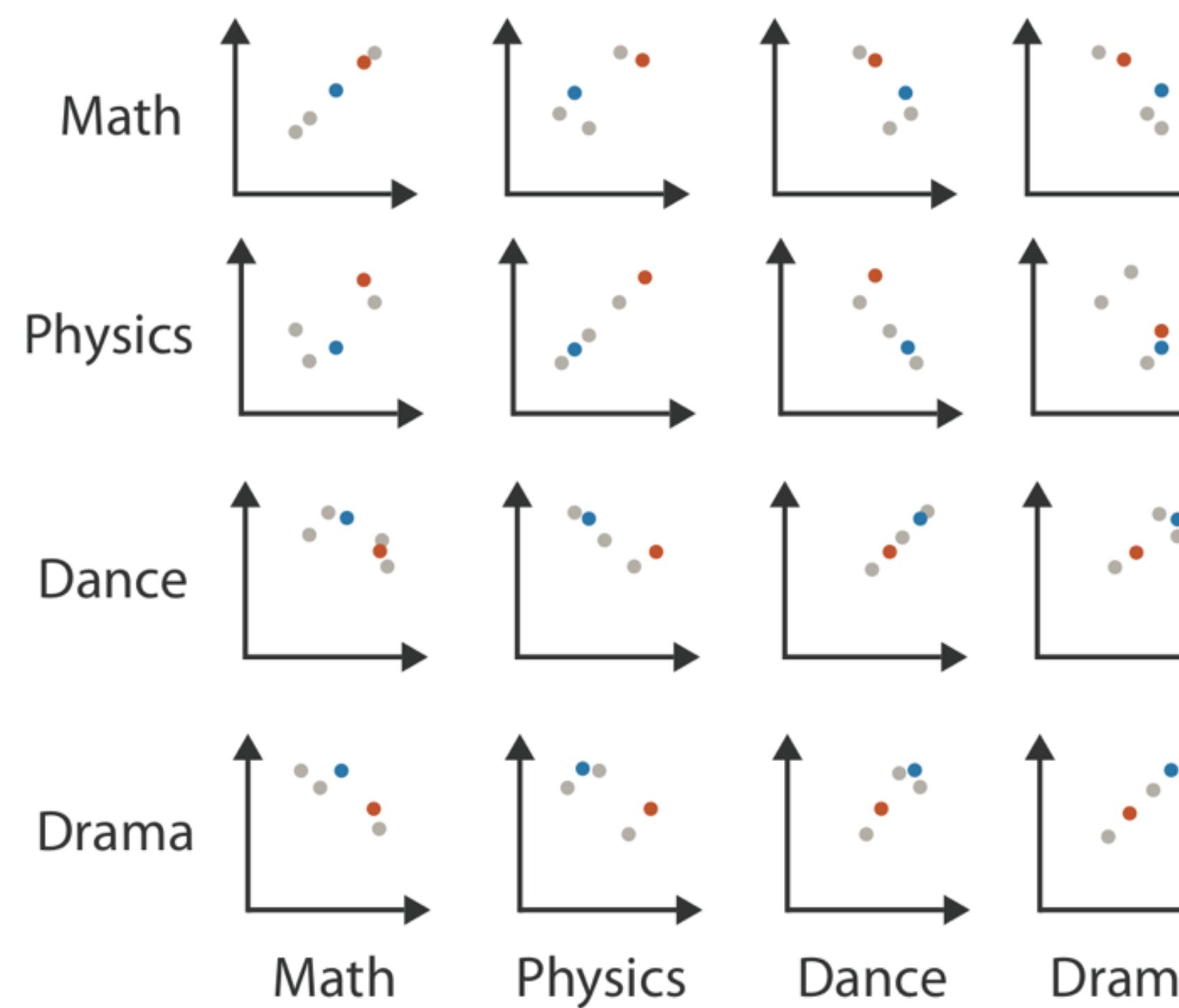
Often combined with “Focus Scatterplot” as F+C technique

Algorithmic approaches:
Clustering & aggregating records
Choosing dimensions
Choosing order

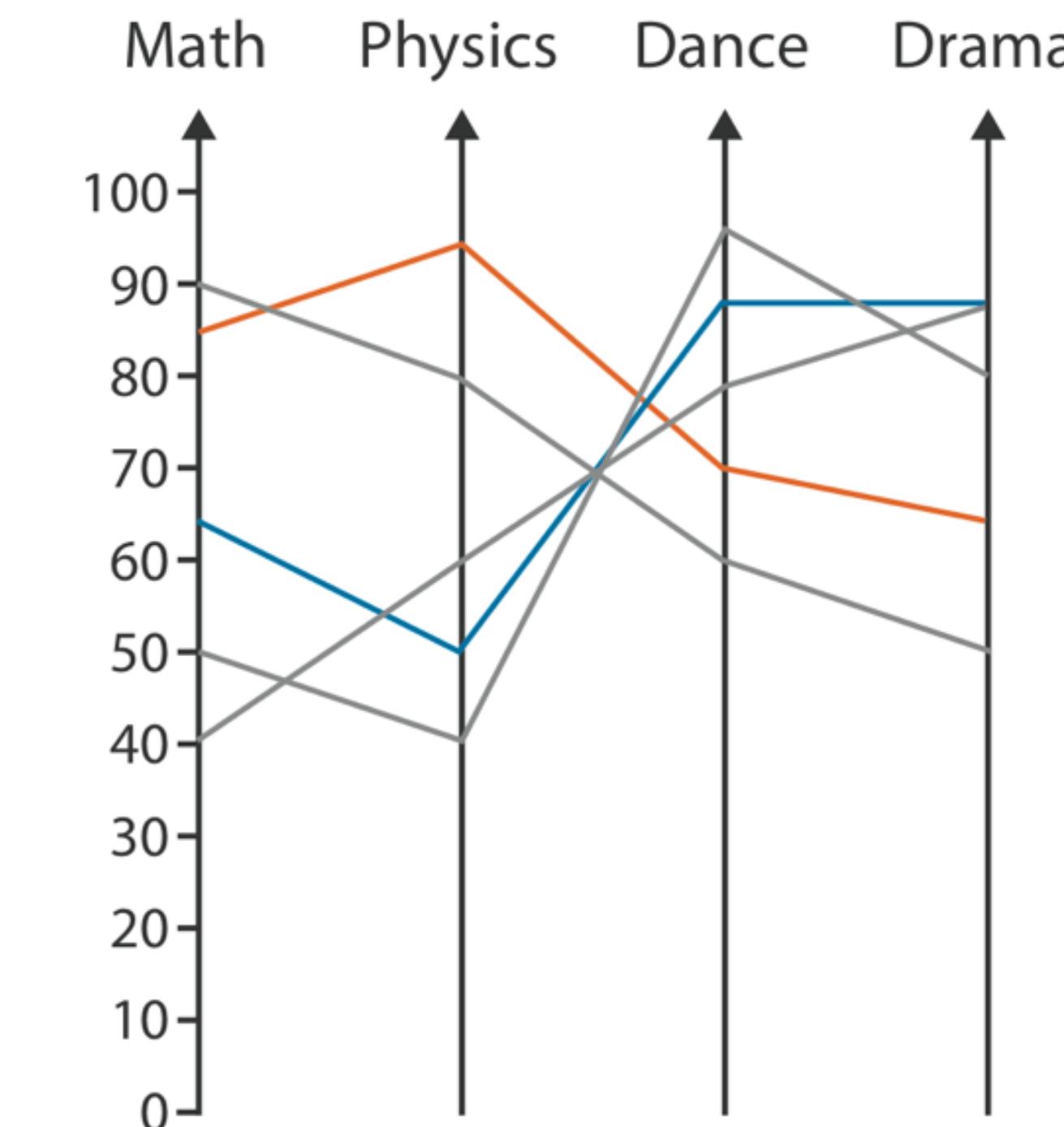
Table

	Math	Physics	Dance	Drama
	85	95	70	65
	90	80	60	50
	65	50	90	90
	50	40	95	80
	40	60	80	90

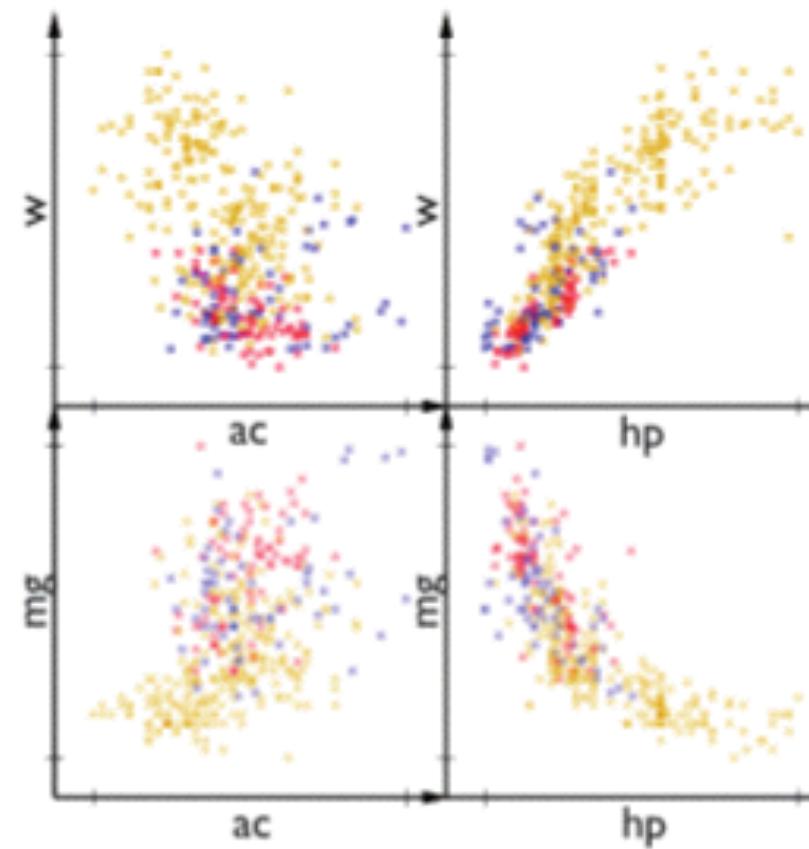
Scatterplot Matrix



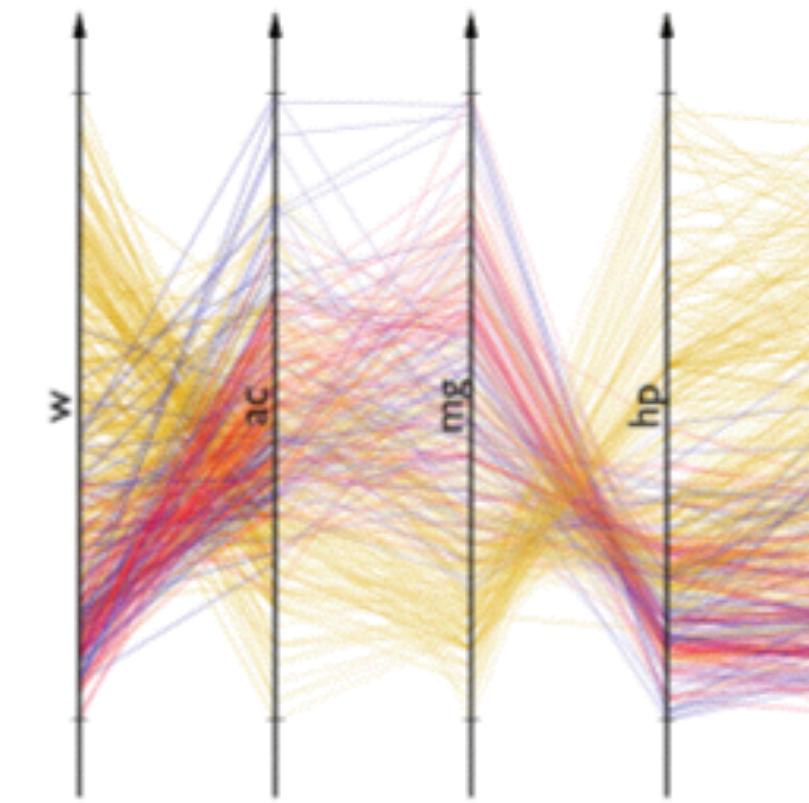
Parallel Coordinates



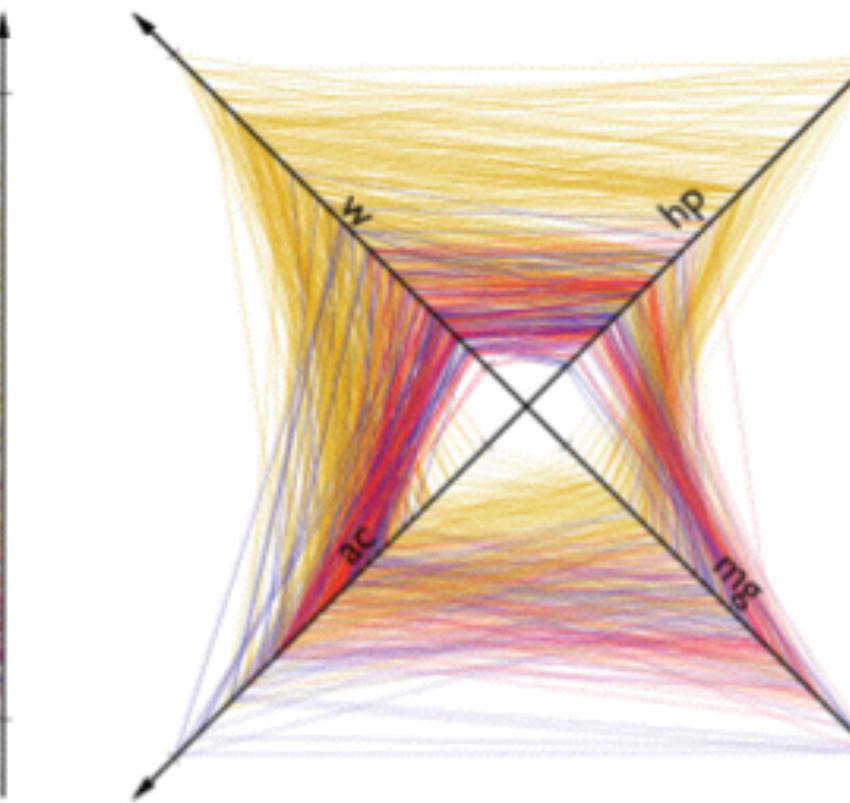
Flexible Linked Axes (FLINA)



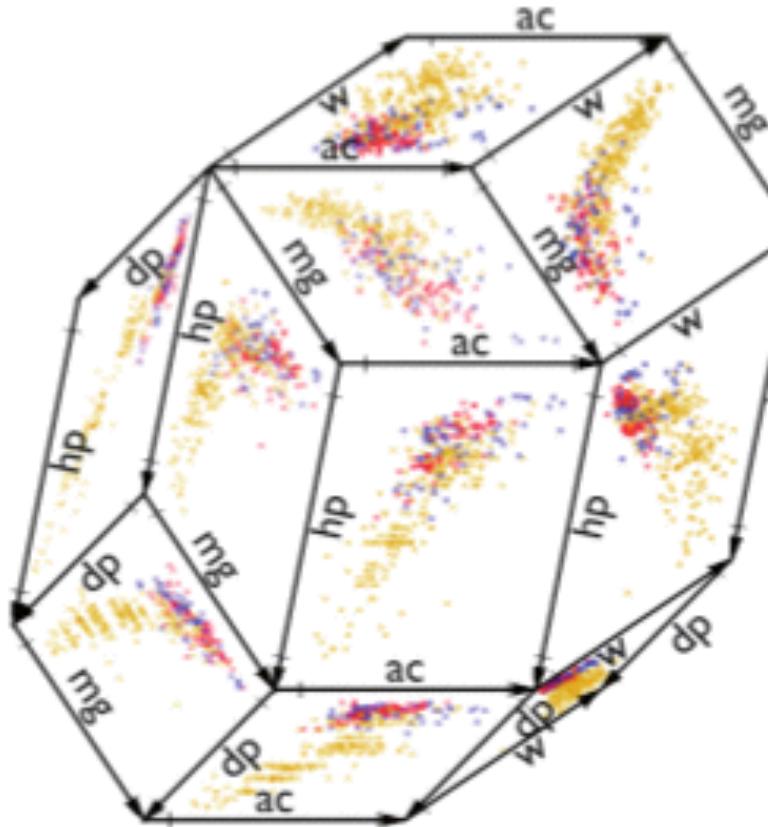
(a) scatterplots



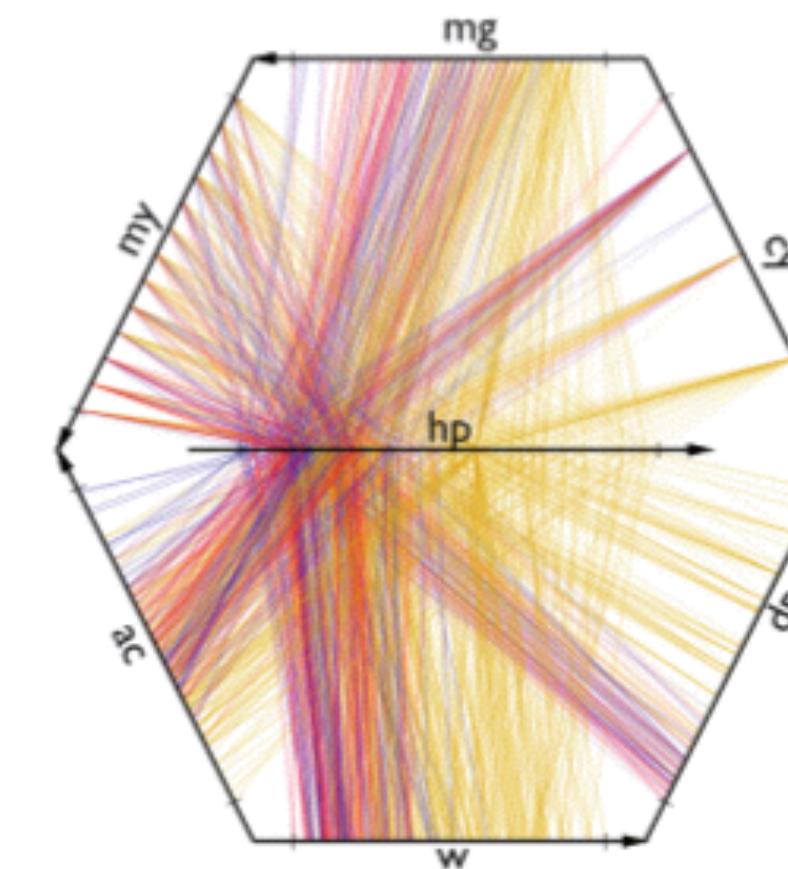
(b) Parallel Coordinates Plot



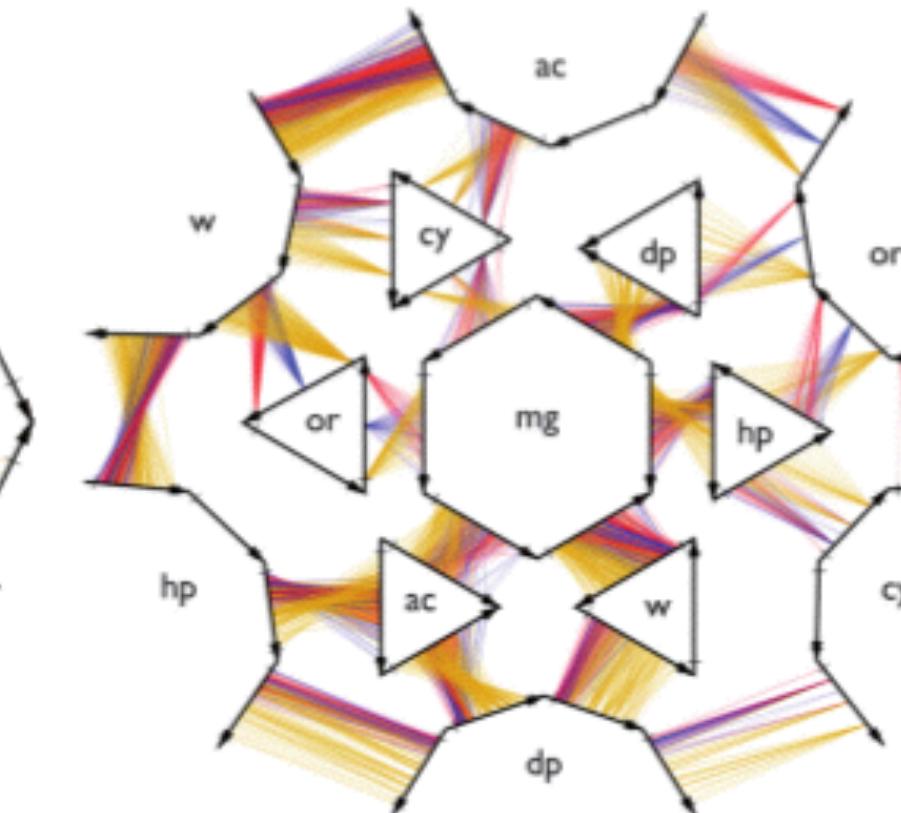
(c) radar chart



(d) Hyperbox



(e) Time Wheel



(f) Many-to-many PCP

Data Reduction

Sampling

Don't show every element, show a (random) subset

Efficient for large dataset

Apply only for display purposes

Outlier-preserving approaches

Filtering

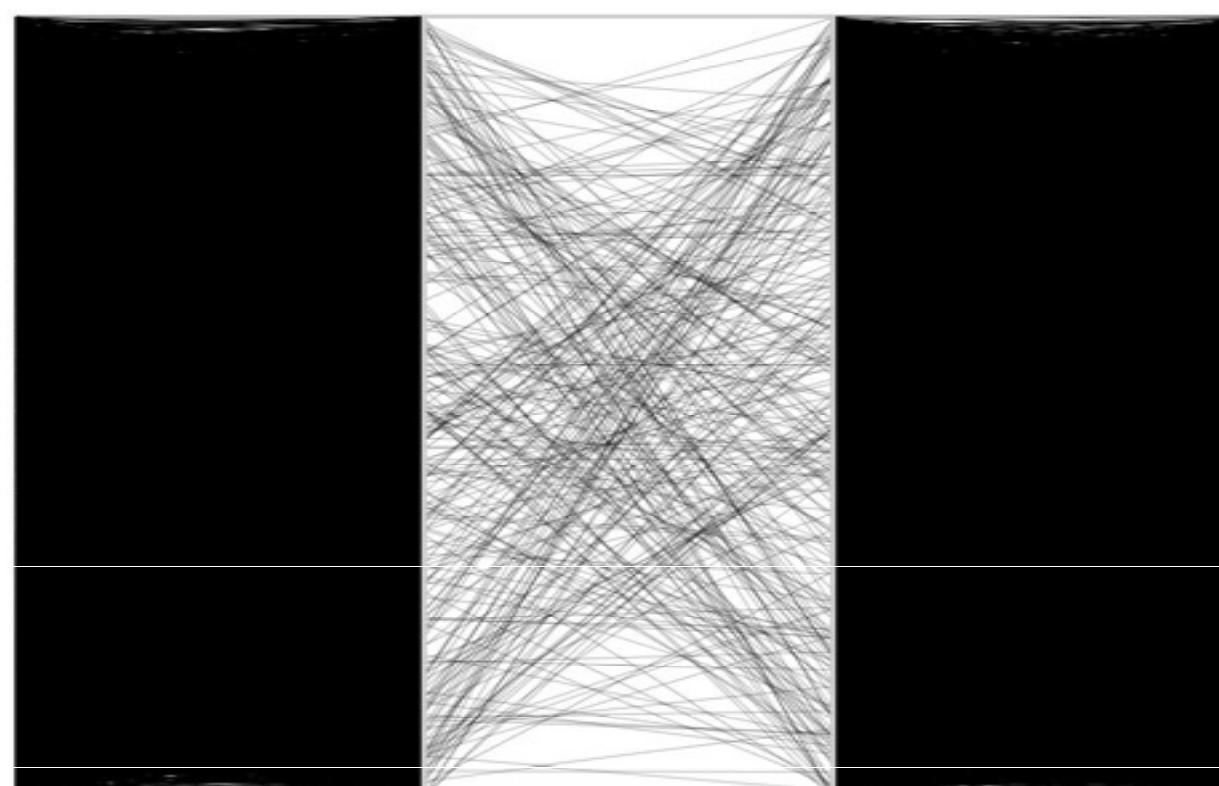
Define criteria to remove data, e.g.,

minimum variability

> / < / = specific value for one dimension

consistency in replicates, ...

Can be interactive, combined with sampling



[Ellis & Dix, 2006]

Pixel Based Methods

Pixel Based Displays

Each cell is a “pixel”, value encoded in color / value

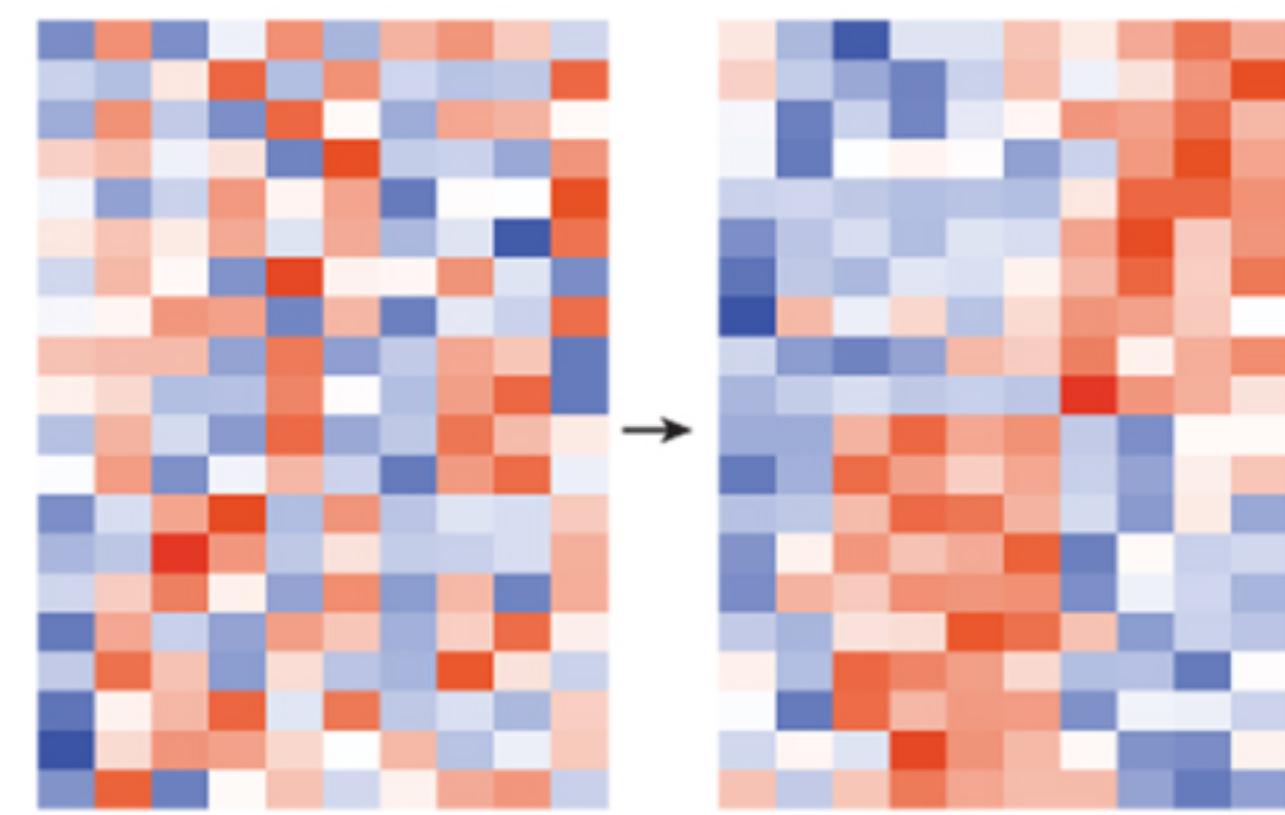
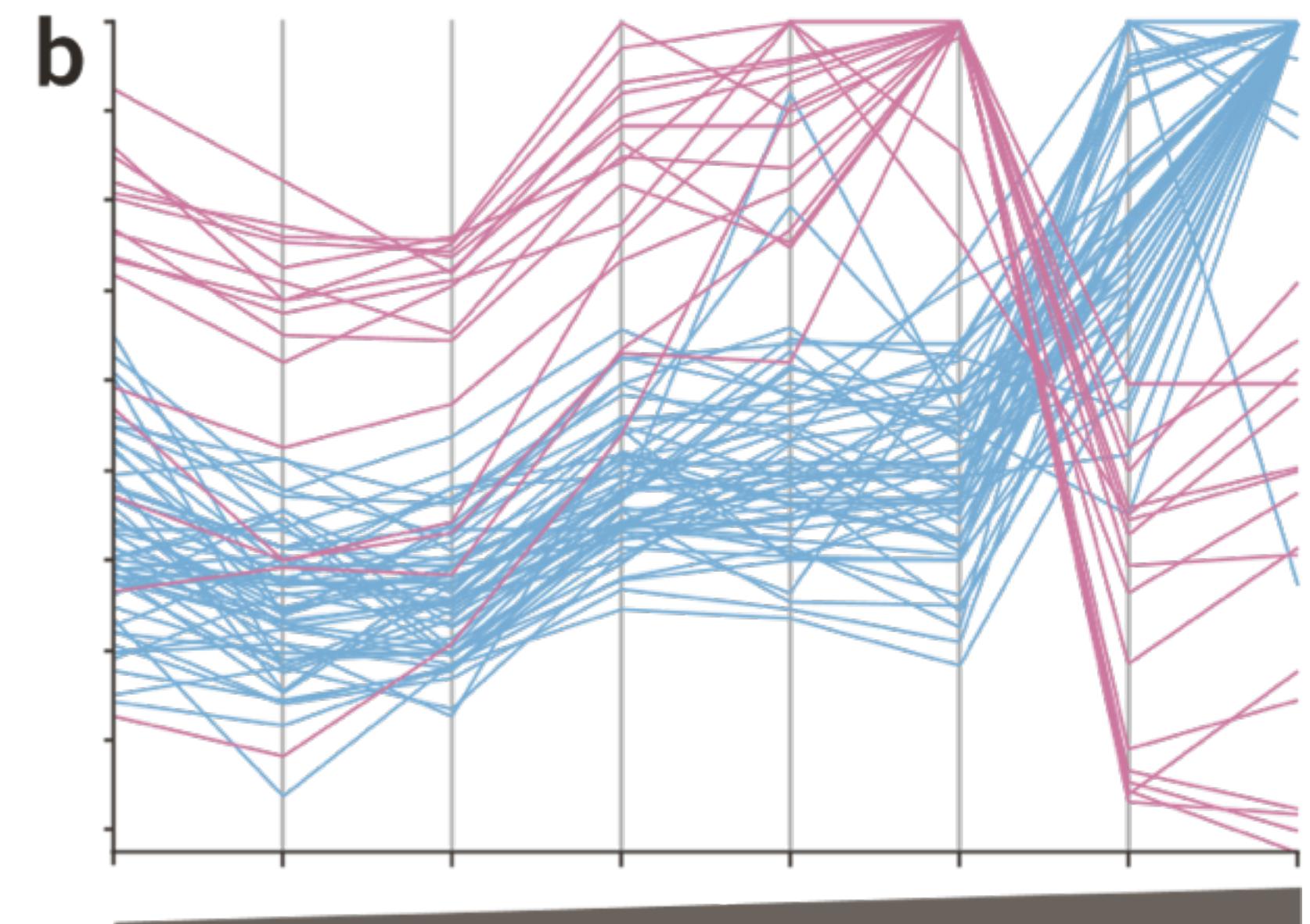
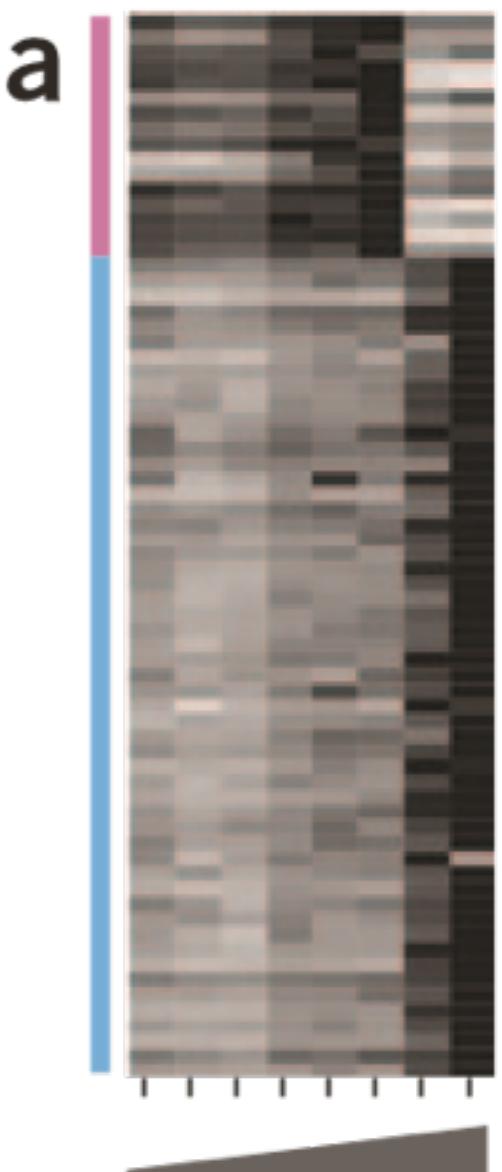
Meaning derived from ordering

If no ordering inherent, clustering is used

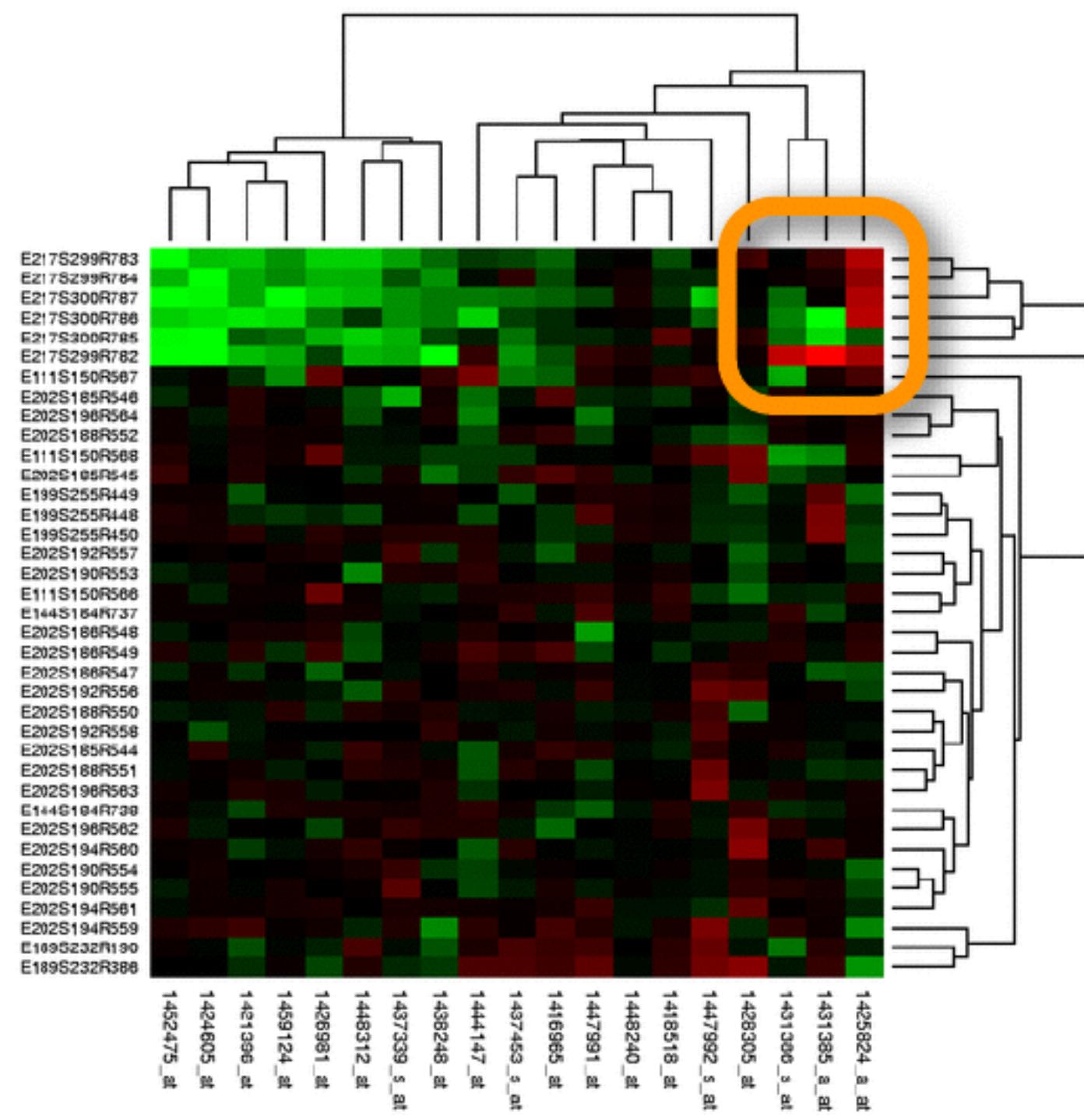
Scalable – 1 px per item

Good for homogeneous data

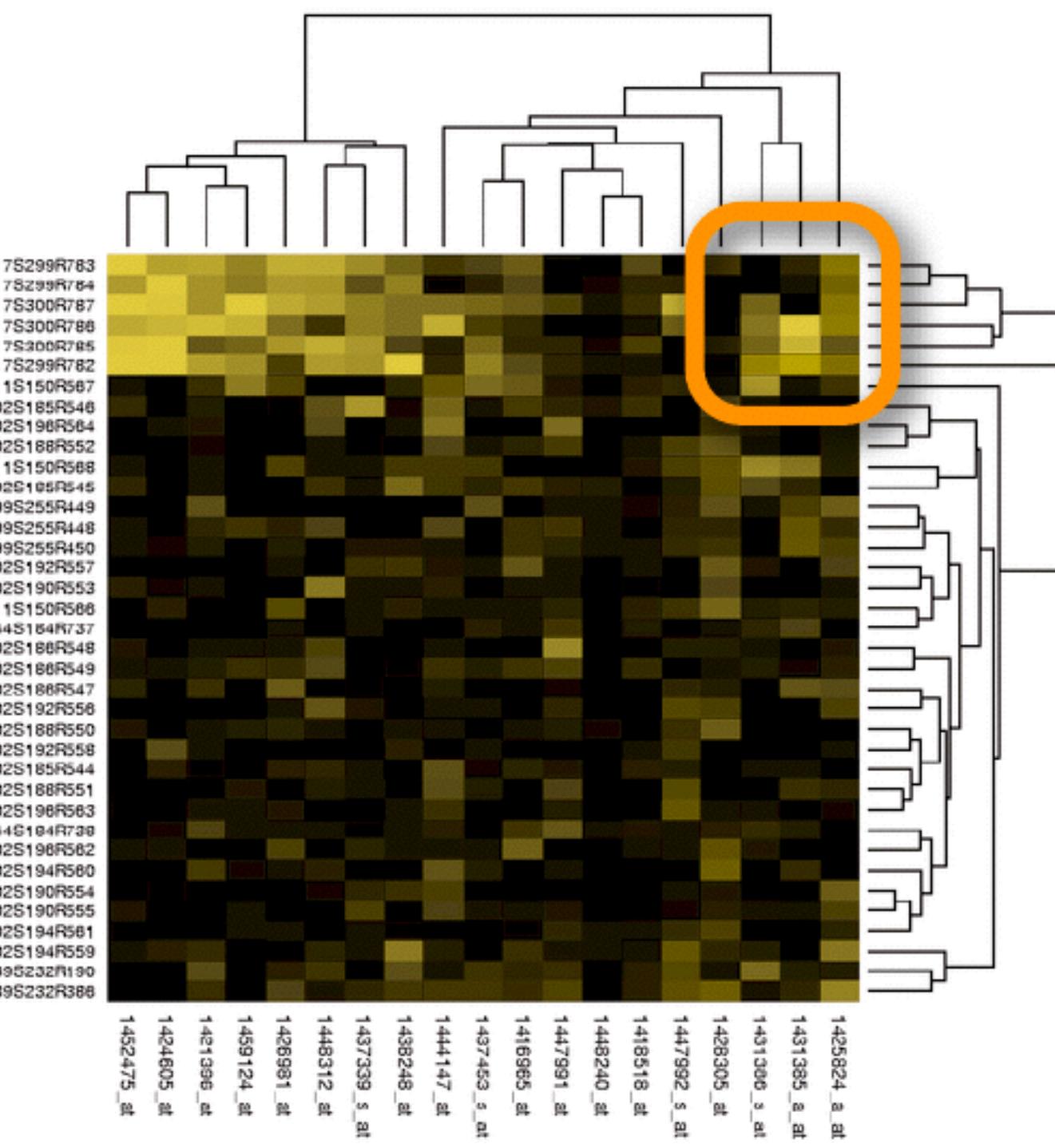
same scale & type



Bad Color Mapping

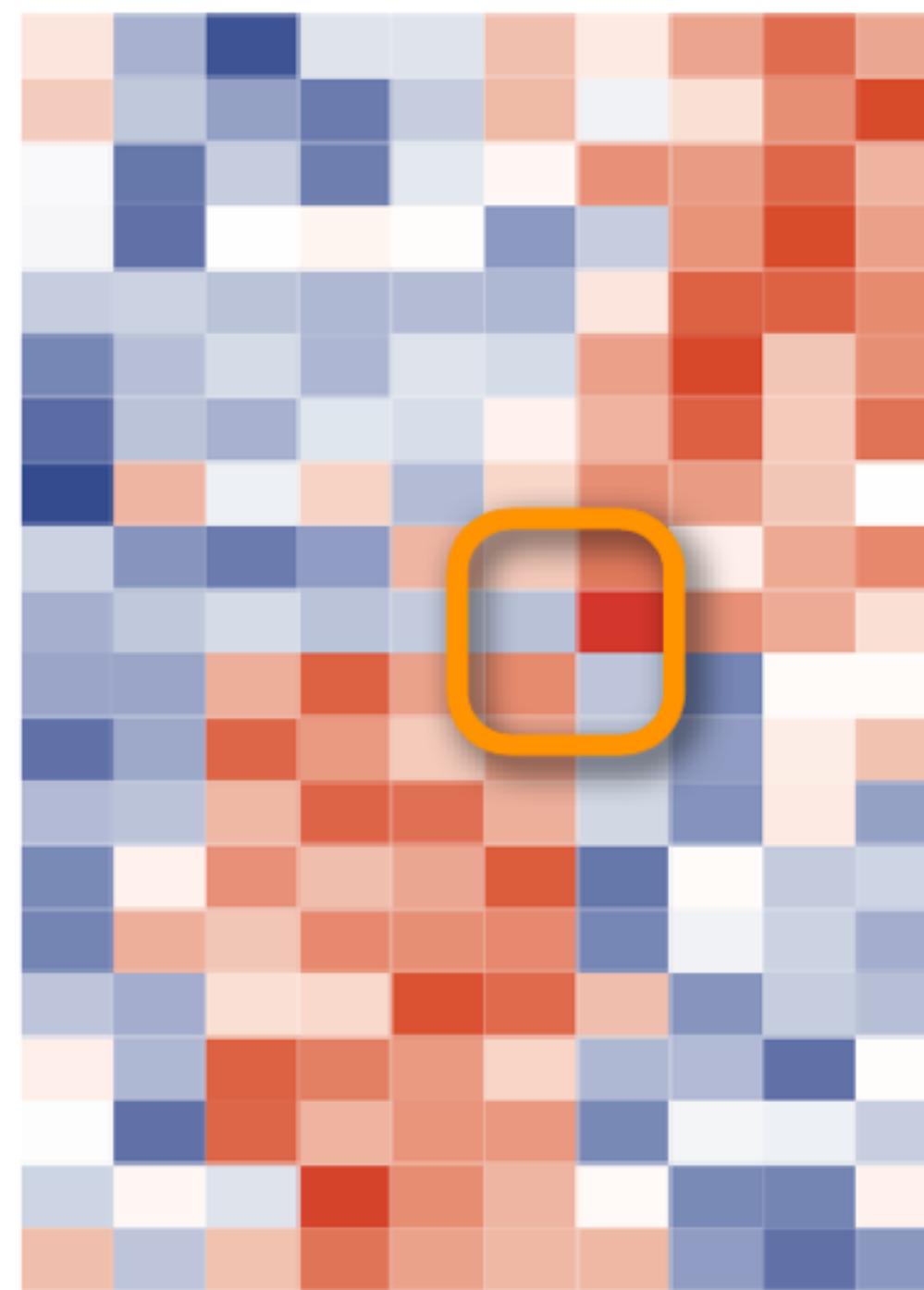


Normal Vision

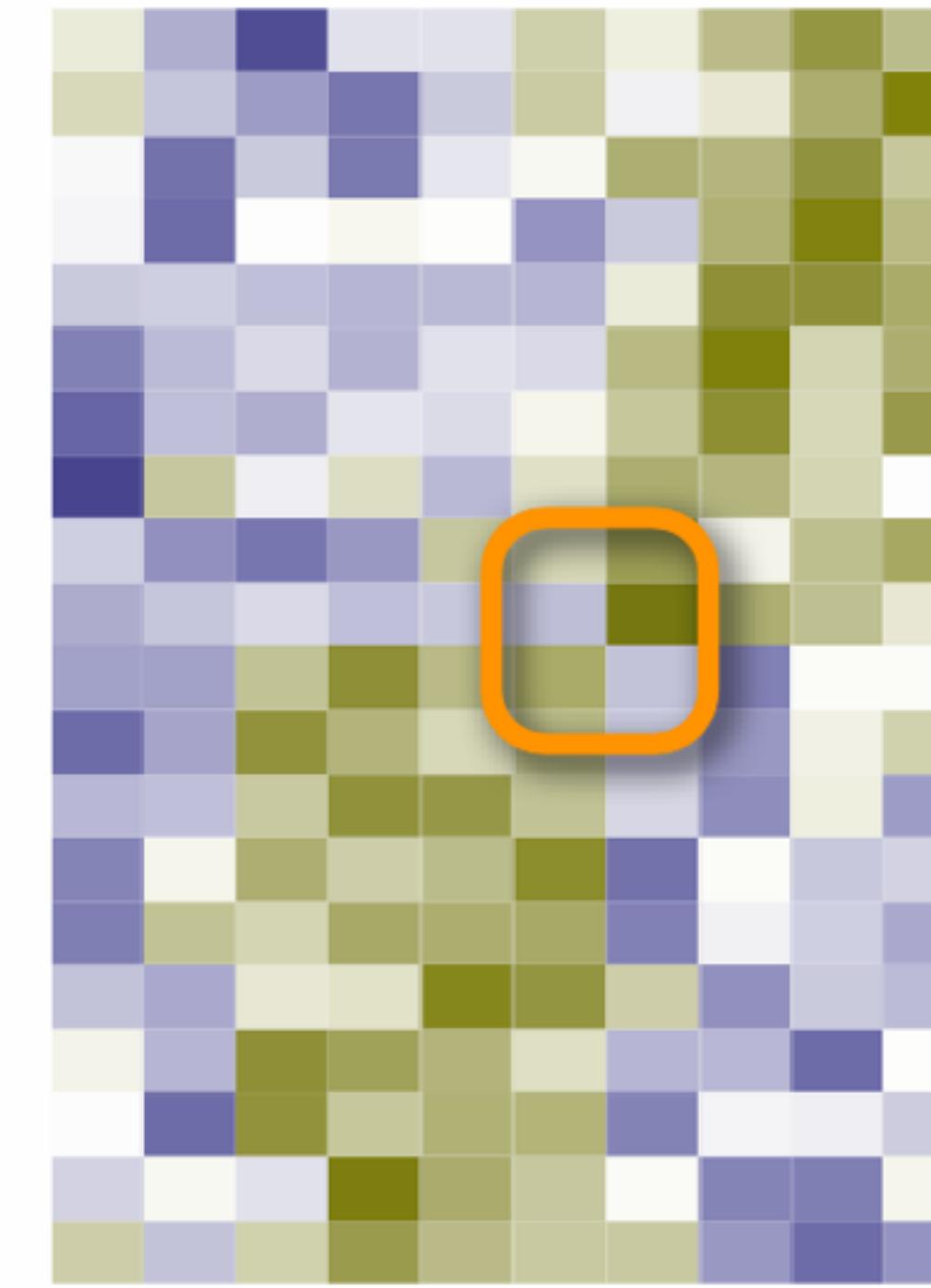


Deutanope Vision
("Red-Green Blindness")

Good Color Mapping

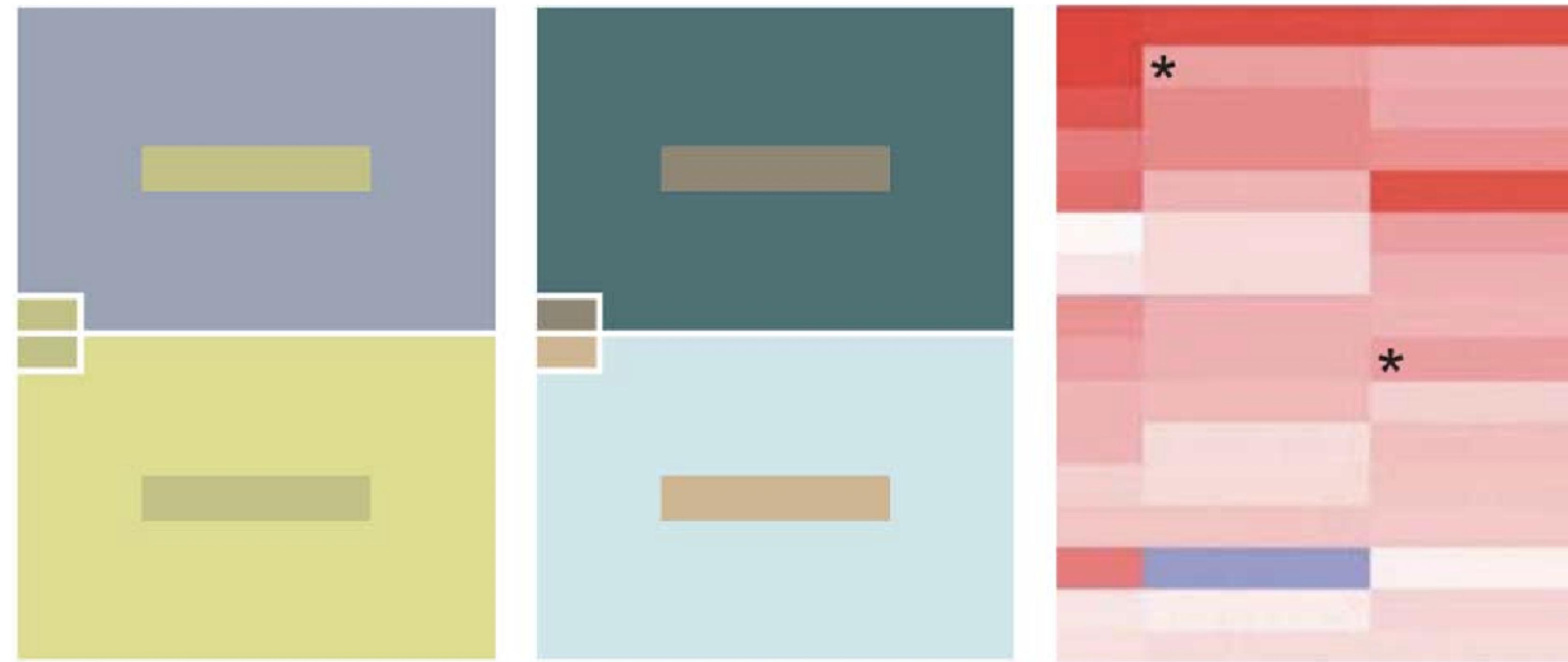


Normal Vision



Deuteranope Vision
("Red-Green Blindness")

Color is relative!



Clustering

Classification of items into “similar” bins

Based on similarity measures

Euclidean distance, Pearson correlation, ...

Partitional Algorithms

divide data into set of bins

bins either manually set (e.g., k-means) or automatically determined (e.g., affinity propagation)

Hierarchical Algorithms

Produce “similarity tree” – dendrogram

Bi-Clustering

Clusters dimensions & records

Fuzzy clustering

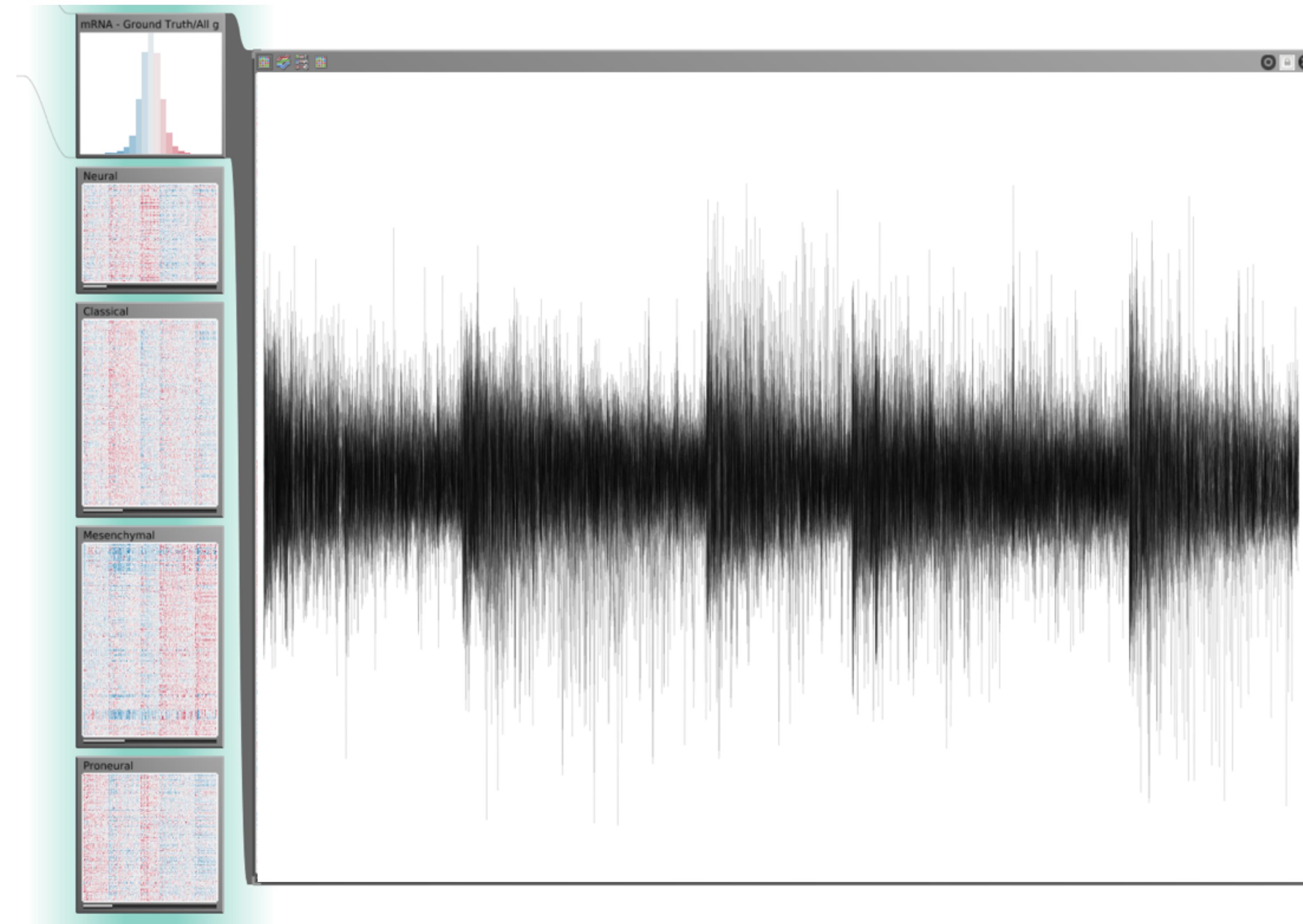
allows occurrence of elements in multiples clusters

Clustering Applications

Clusters can be used to
order (pixel based techniques)
brush (geometric techniques)
aggregate

Aggregation
cluster more homogeneous than whole dataset
statistical measures, distributions, etc. more meaningful

Clustered Heat Map



Dimensionality Reduction

Dimensionality Reduction

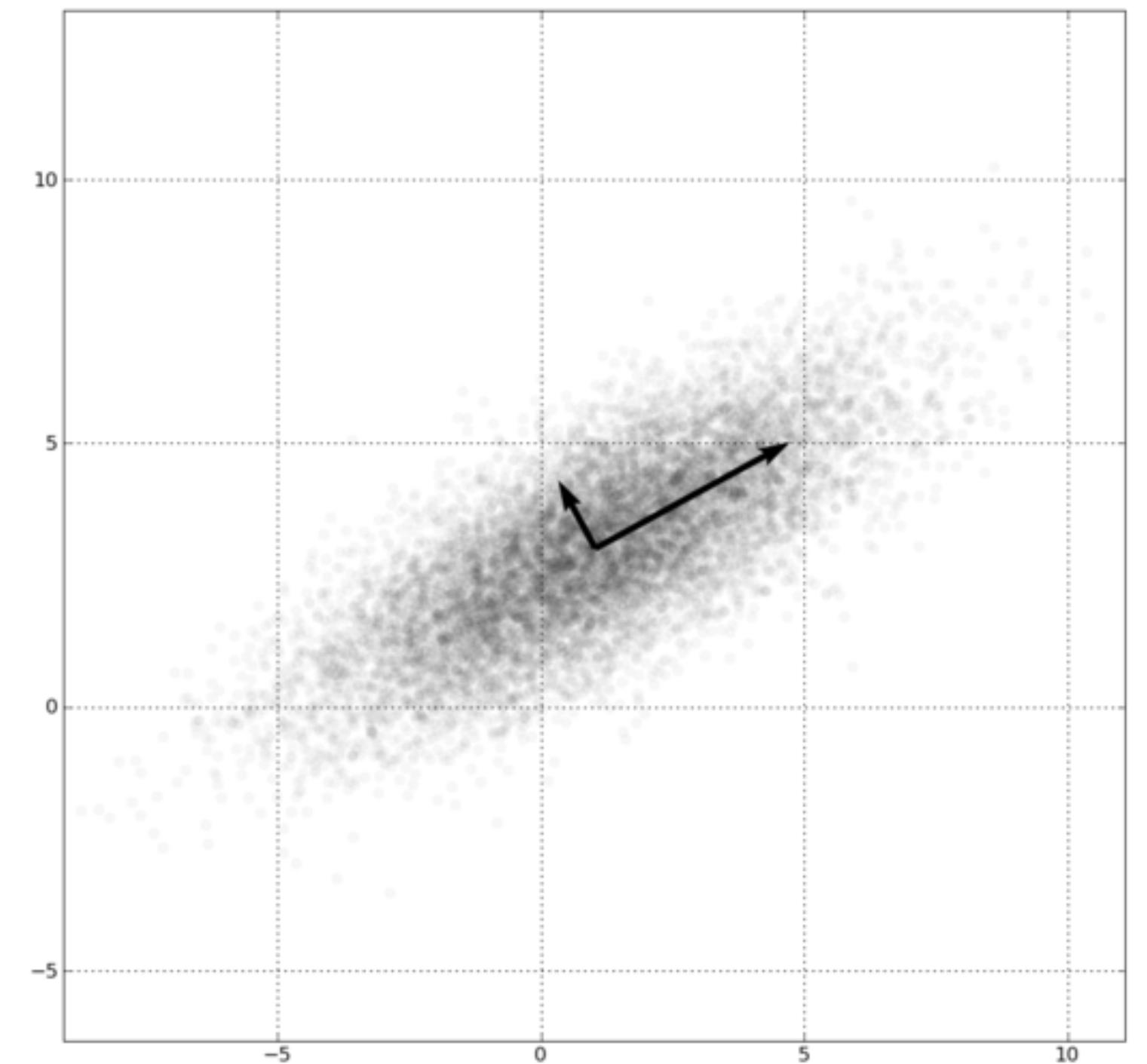
Reduce high dimensional to lower dimensional space

Preserve as much of variation as possible

Plot lower dimensional space

*Principal Component Analysis
(PCA)*

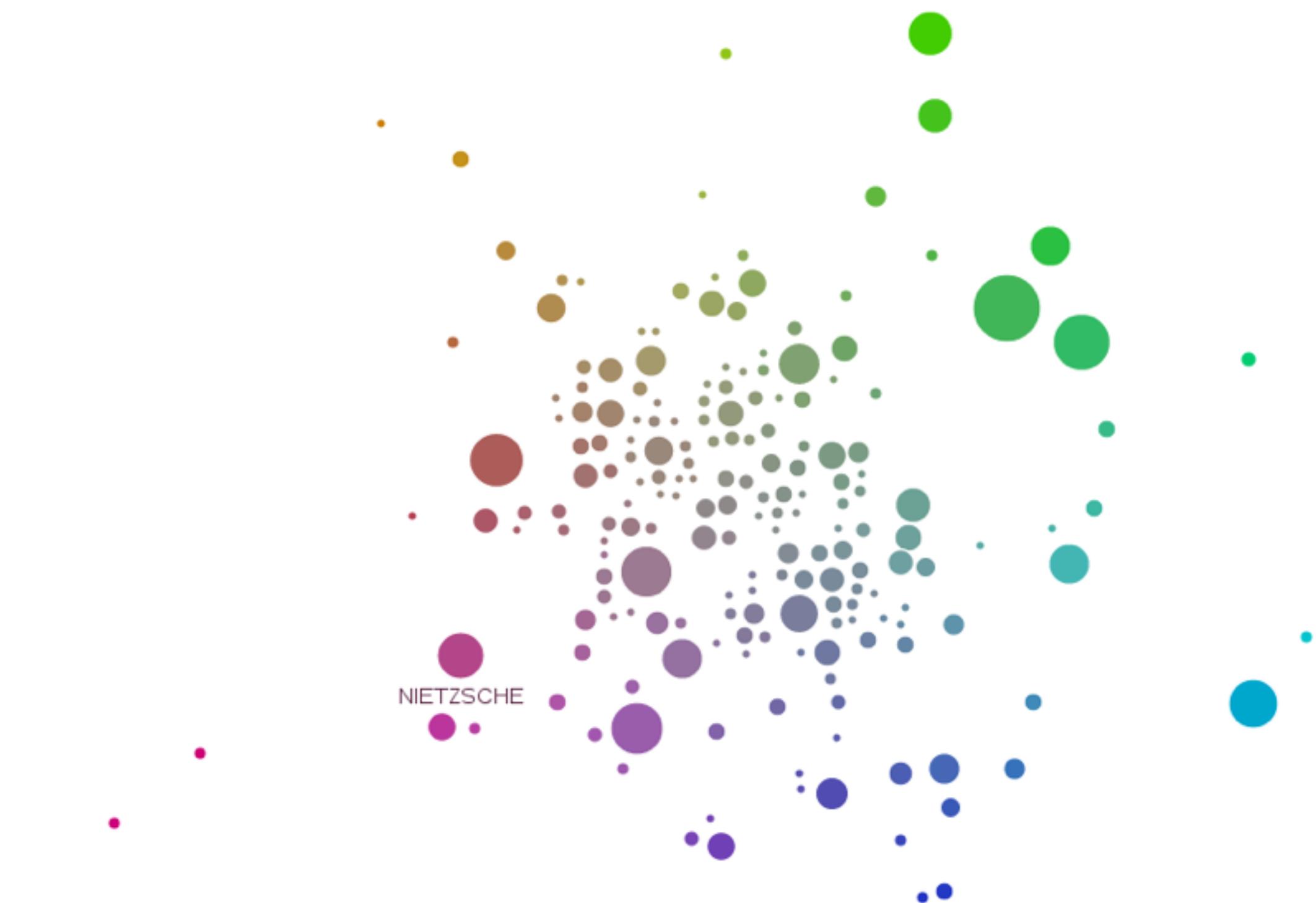
linear mapping, by order of variance



Multidimensional Scaling

Nonlinear, better suited for
some DS

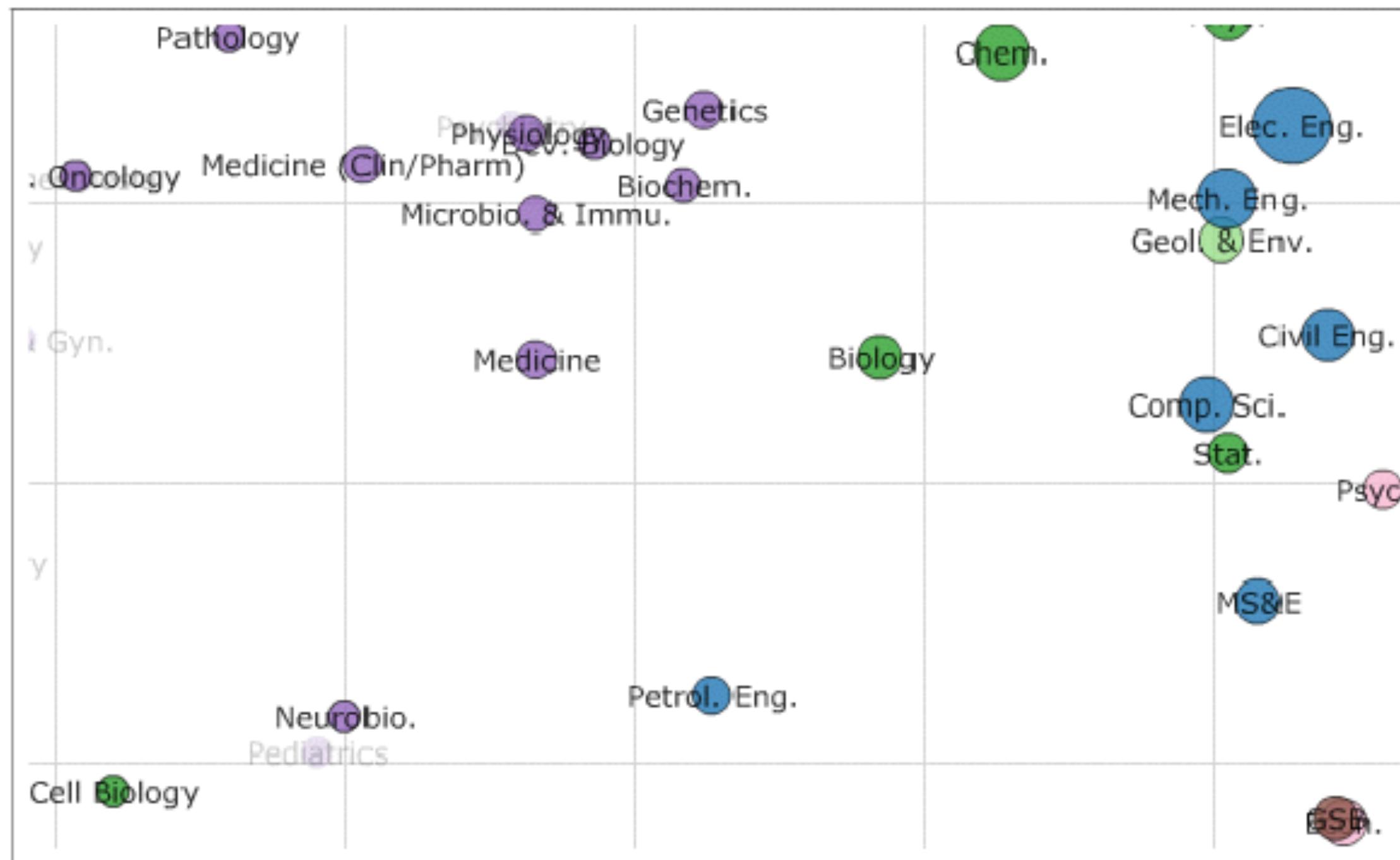
Popular for text analysis



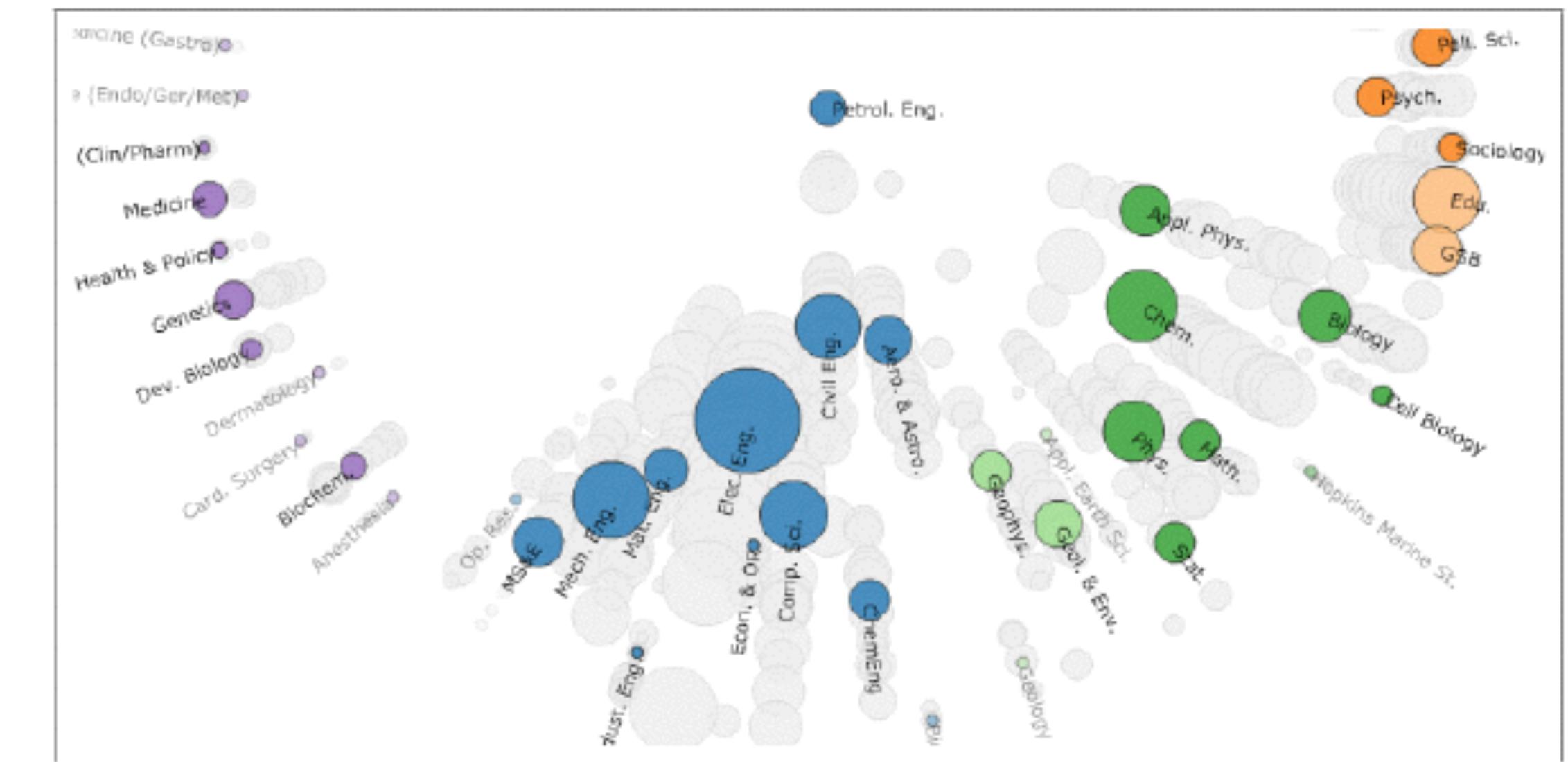
[Doerk 2011]

Can we Trust Dimensionality Reduction?

Topical distances between departments in a 2D projection



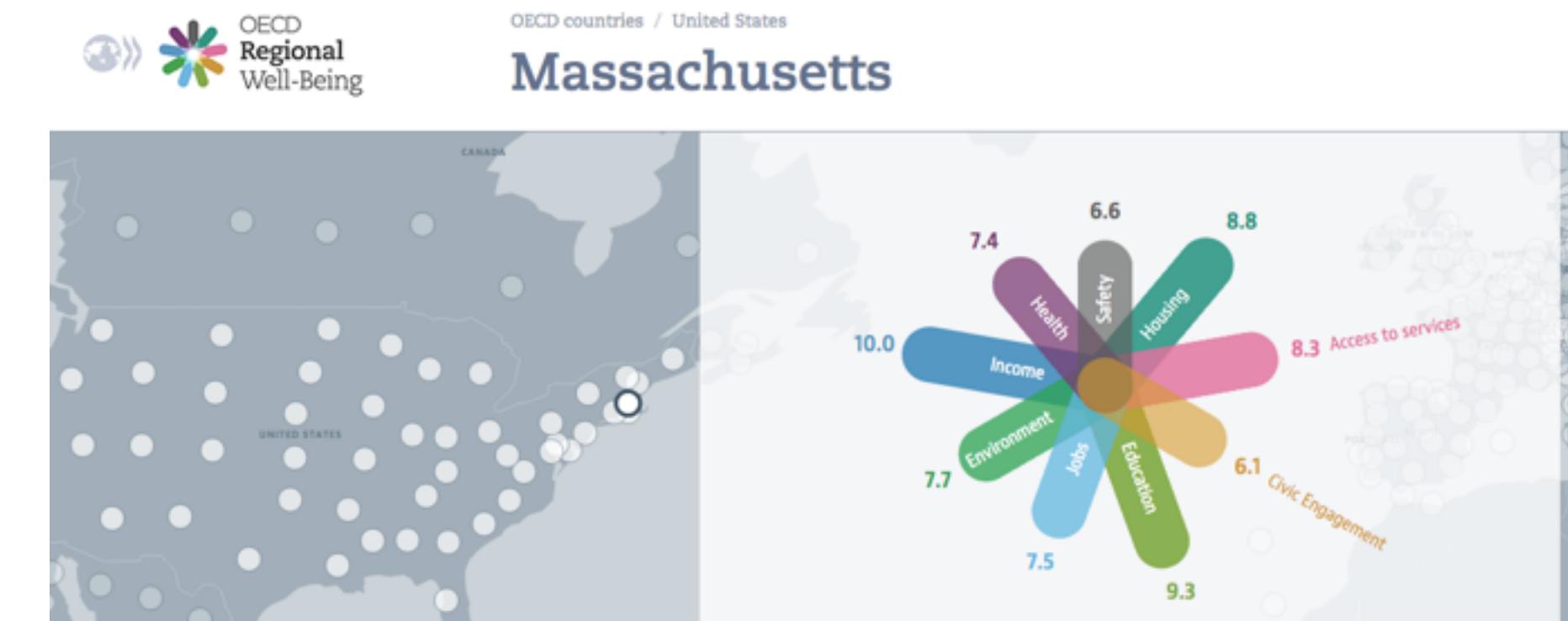
Topical distances between the selected Petroleum Engineering and the others.



[Chuang et al., 2012]

Design Critique

OECD: <http://goo.gl/QfxHfv>



Explore the map to find out how life is across OECD regions and discover regions with similar well-being.

Each region is measured in nine topics important for well-being. The values of the indicators are expressed as a score between 0 and 10. A high score indicates better performance relative to the other regions.

Help

Regions with similar well-being in other countries



Canada
Alberta



Germany
Saarland



United Kingdom
Wales



Ireland
Southern and Eastern

Well-being in detail

Access to services

Massachusetts reaches **8.3** /10 points in **Access to services**.

This puts the region in position **6** /51 regions in United States.

Compared across all OECD regions, the region is in the **top 28%** in **Access to services**.



Civic Engagement

Massachusetts reaches **6.1** /10 points in **Civic Engagement**.

This puts the region in position **5** /51 regions in United States.

Compared across all OECD regions, the region is in the **top 43%** in **Civic Engagement**.



Education

Massachusetts reaches **9.3** /10 points in **Education**.

This puts the region in position **18** /51 regions in United States.



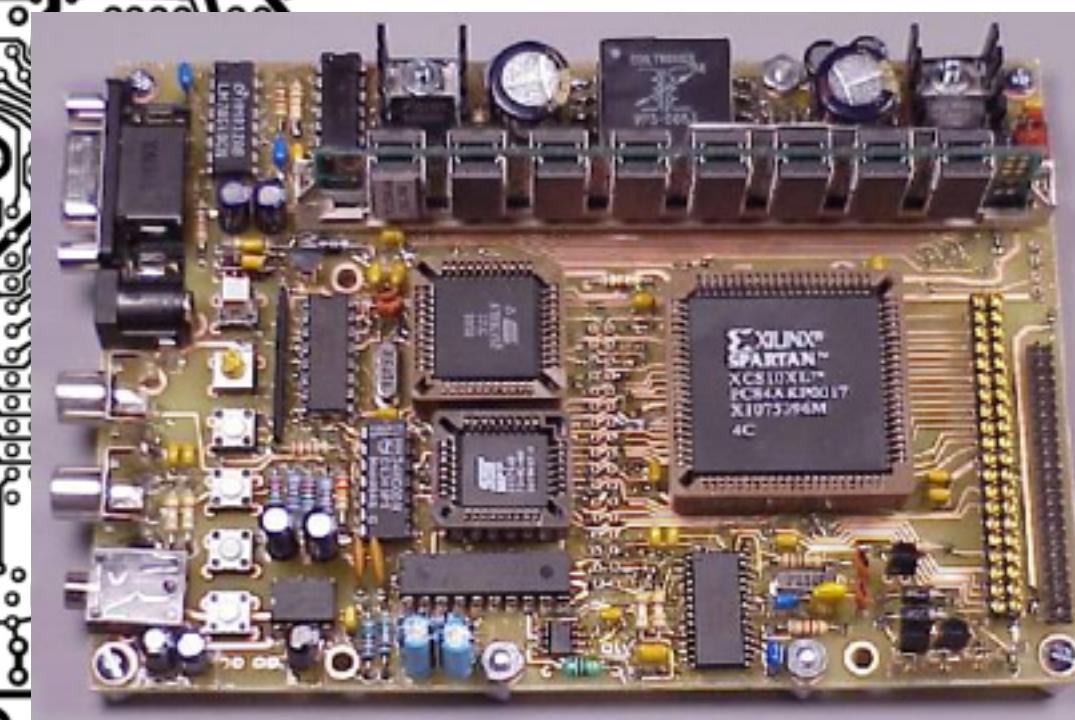
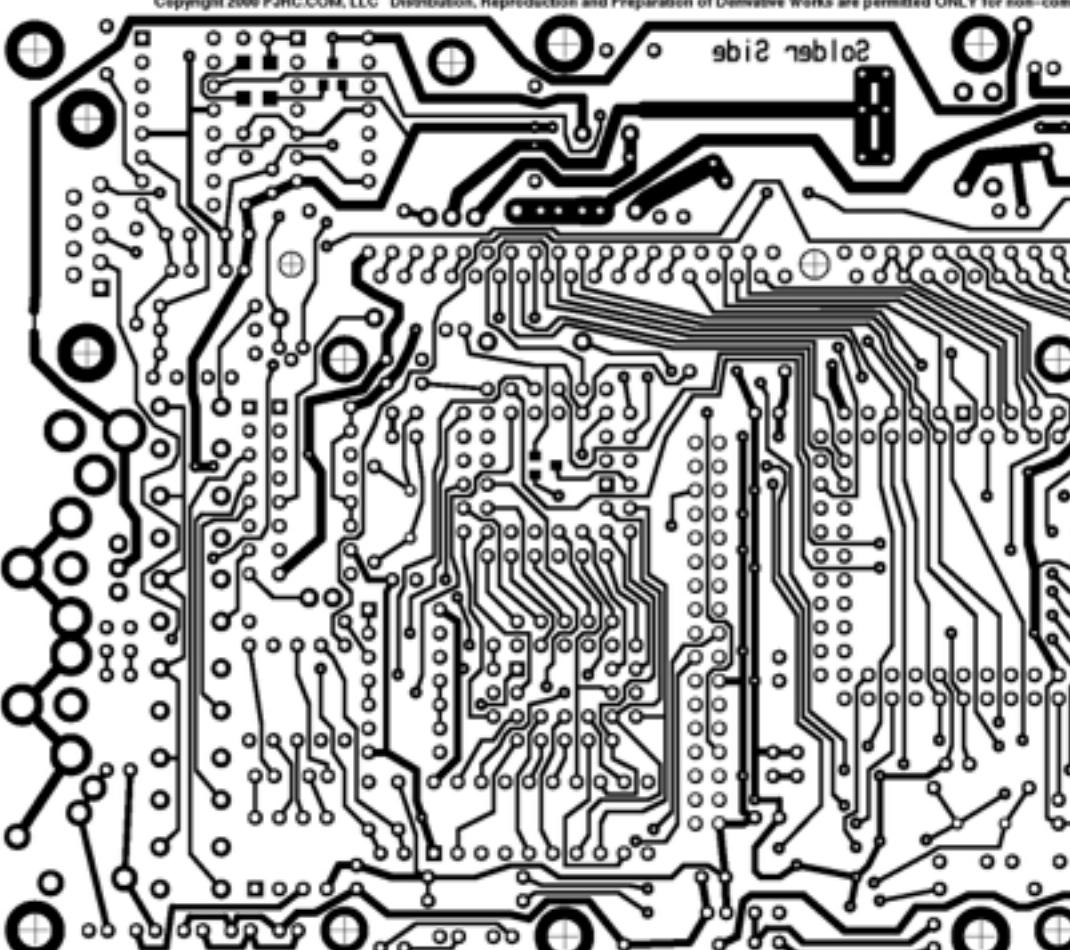
<http://www.oecdregionalwellbeing.org/>

Graph Visualization

Based on Slides by HJ Schulz and M Streit

Applications of Graphs

Without graphs,



Google

page rank

Suche

Erweiterte Suche

Alles

Mehr

Das Web

Seiten auf Deutsch

Seiten aus Deutschland

Alle

Letzte 24 Stunden

Standardansicht

Verwandte Suchbegriffe

Mehr Text

Mehr Optionen

Ungefähr 254.000.000 Ergebnisse (0,10 Sekunden)

PageRank – Wikipedia

Der PageRank-Algorithmus ist ein Verfahren, eine Menge verlinkter Dokumente, wie beispielsweise das World Wide Web, anhand ihrer Struktur zu bewerten bzw. ...

Der PageRank-Algorithmus - Geschichte - Kritik - Siehe auch de.wikipedia.org/wiki/PageRank - Im Cache - Ähnliche Seiten

PageRank Check / PageRank Echtheitsprüfung / PR Check 00 Oct

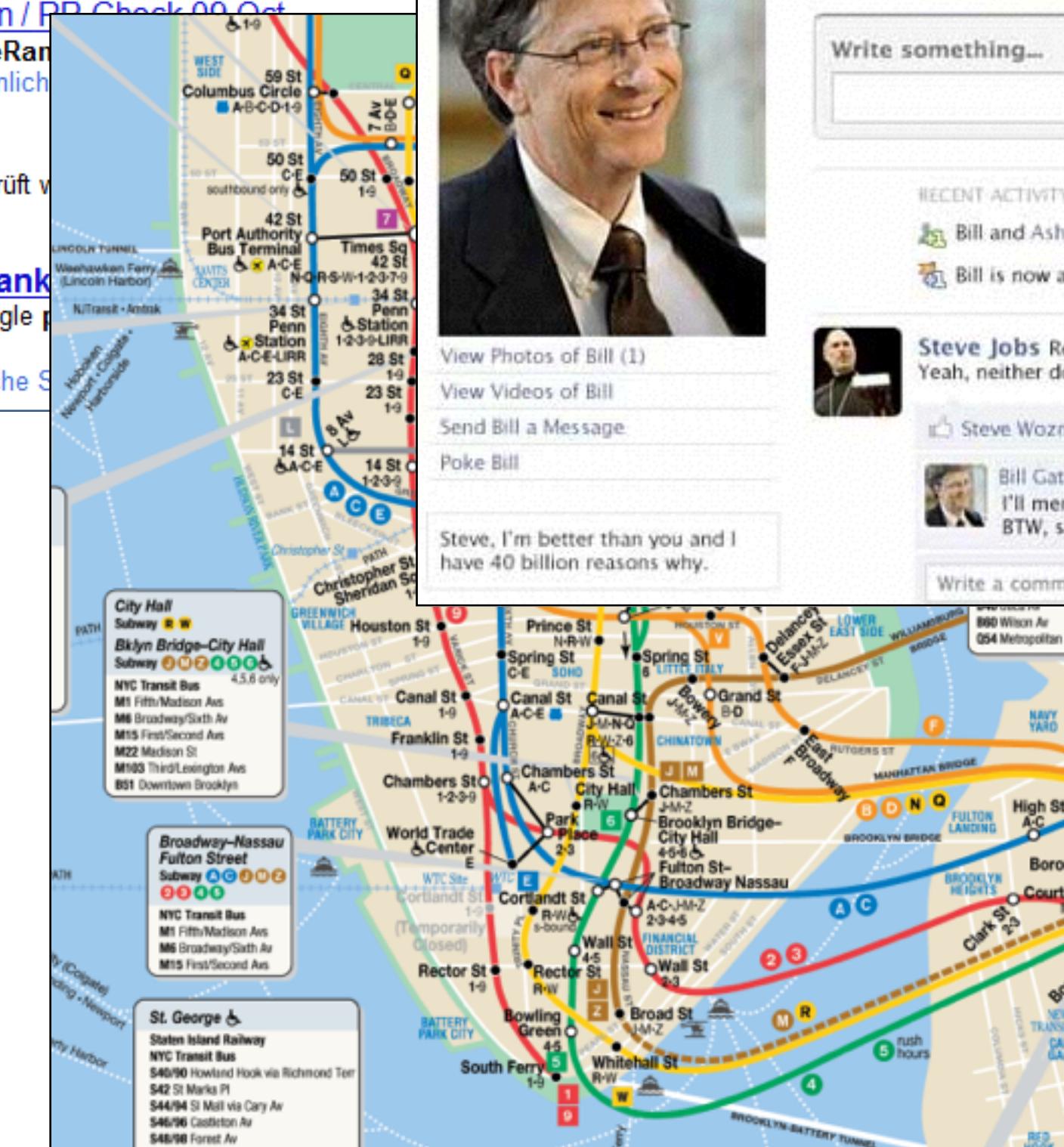
Führen Sie hier eine PageRank-Echtheitsprüfung / einen PageRank-Check durch. www.database-search.com/sys/pre-check.php - Im Cache - Ähnliche Seiten

Google PageRank Check

Mit diesem Tool kann der Google PageRank einer Seite überprüft werden. www.gaijin.at/olsgrank.php - Im Cache - Ähnliche Seiten

Google PageRank Checker - Check Google page rank

Page Rank Checker is a completely free service to check Google page rank online. You can use our online page rank check tool or a small pagerank button. www.prchecker.info/check_page_rank.php - Im Cache - Ähnliche Seiten



facebook Home Profile Friends Bill Gates

Bill Gates just bought Azerbaijan!

Wall Info Photos Boxes Notes

Write something...

RECENT ACTIVITY

Bill and Ashton Kutcher are now friends. · Comment · Like

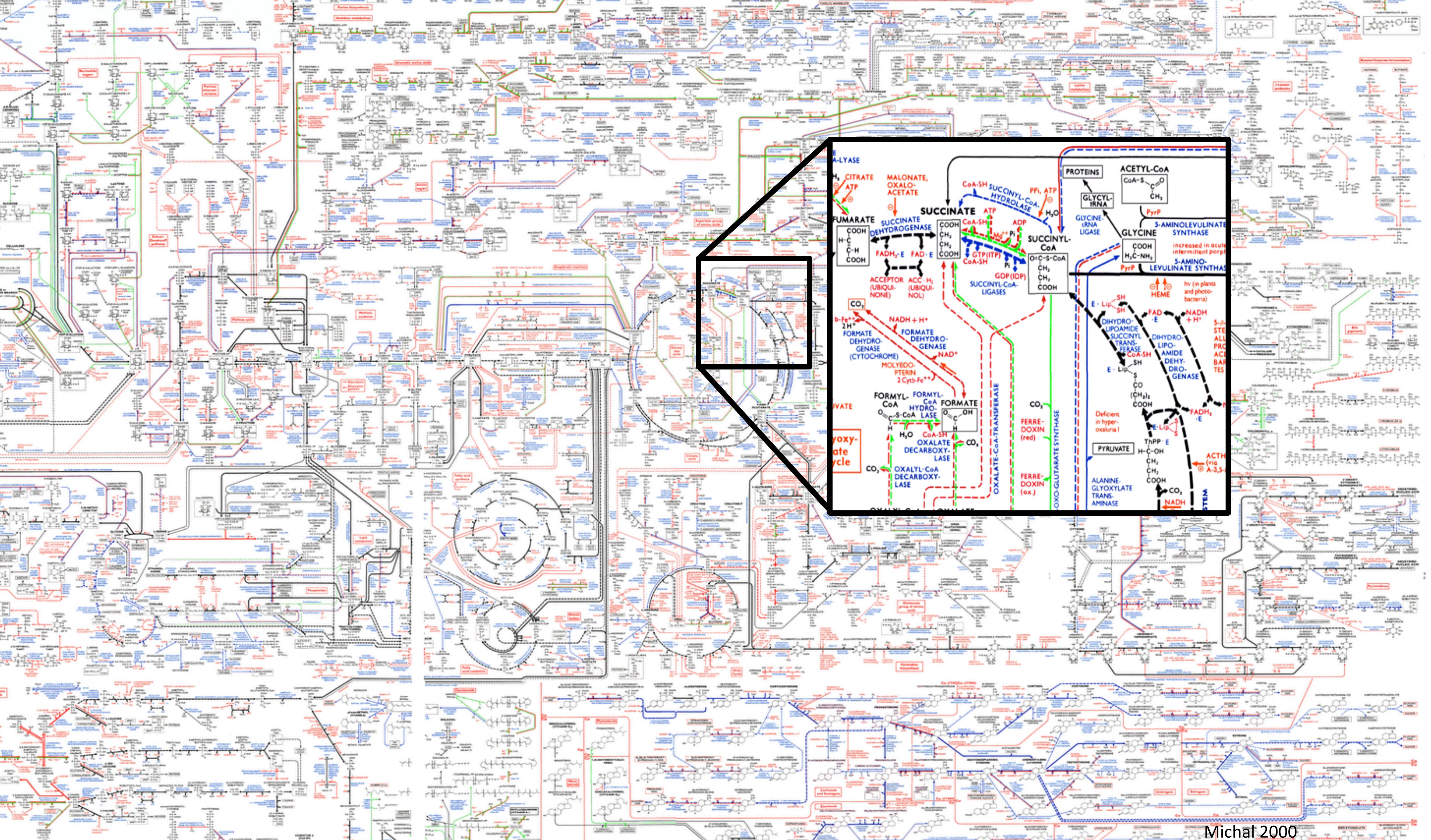
Bill is now a fan of Tool Academy and Project Runway. · Comment

Steve Jobs Remember that OS you made that was awesome? Yeah, neither do I. at 4:45pm March 26 · Comment · Like

Steve Wozniak liked this.

Bill Gates at 4:48pm March 26 I'll mention that to the 88.9% market share I have. BTW, saw the new iPod shuffle. It looks like a tampon.

Write a comment...



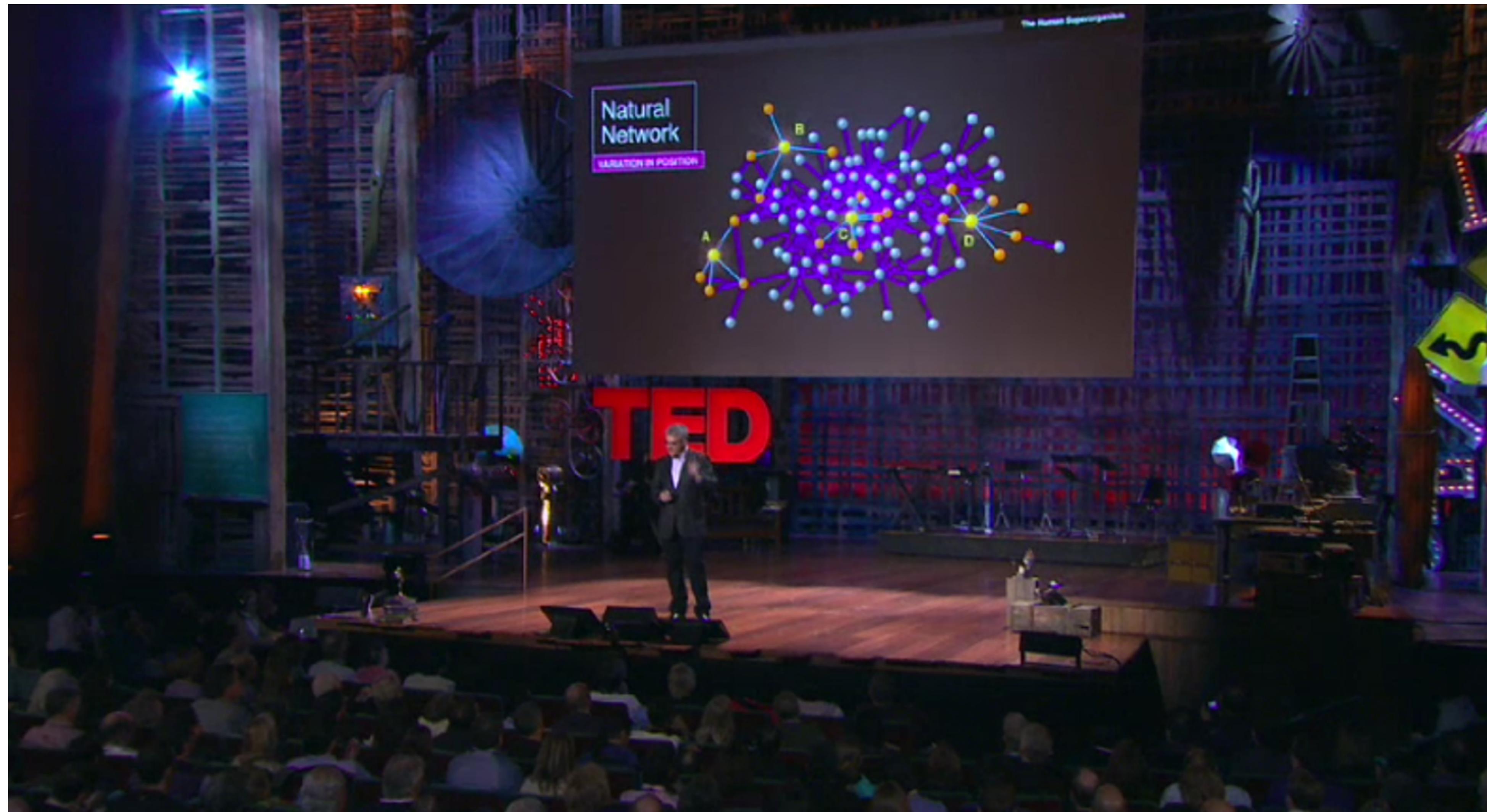
Michał 200



facebook

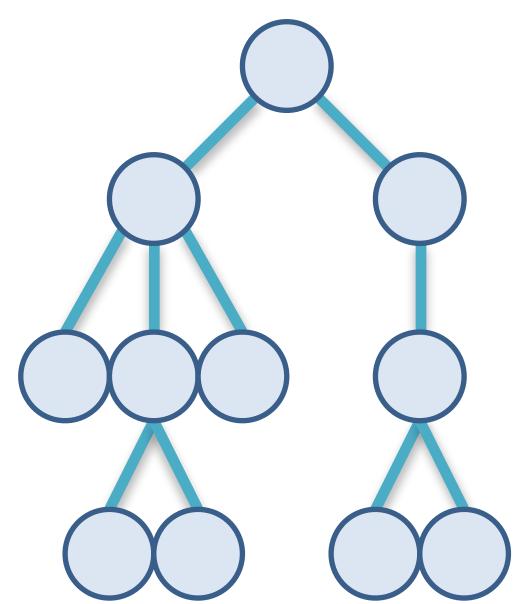
December 2010

Graph Visualization Case Study

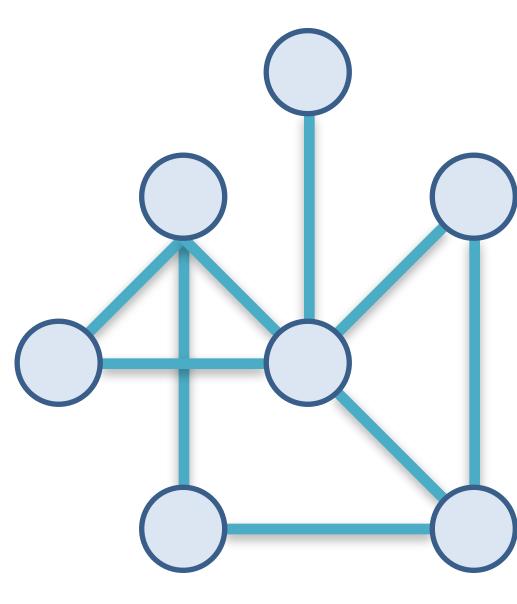


Graph Theory fundamentals

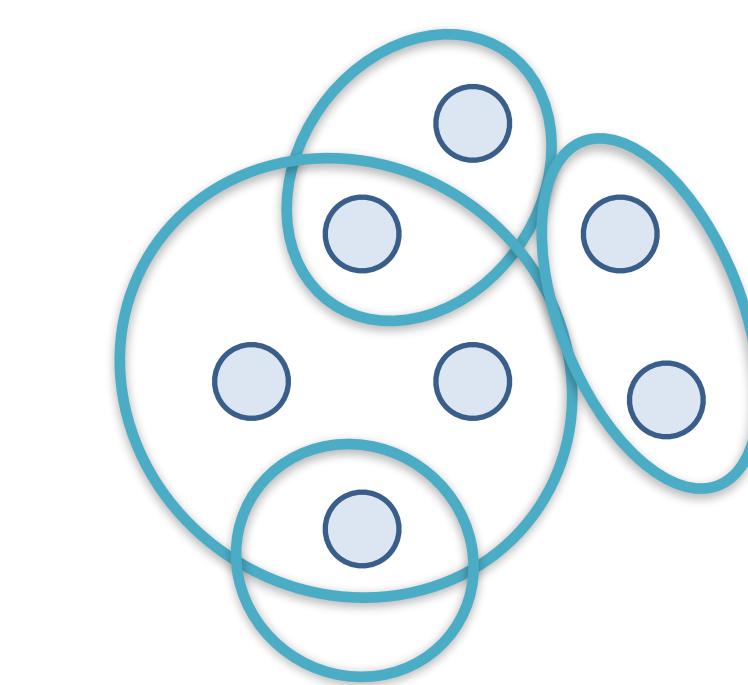
Tree



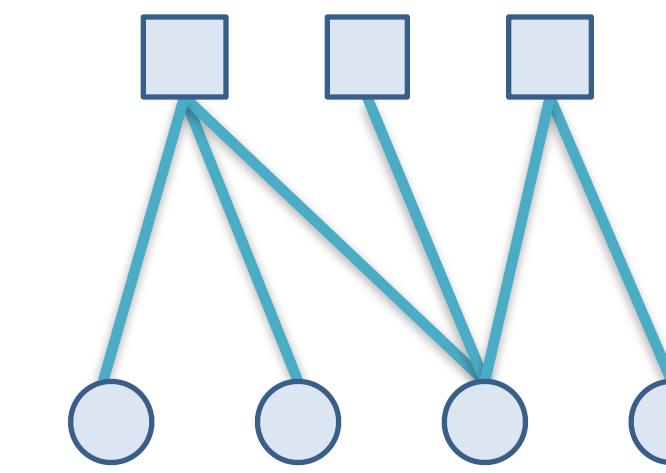
Network



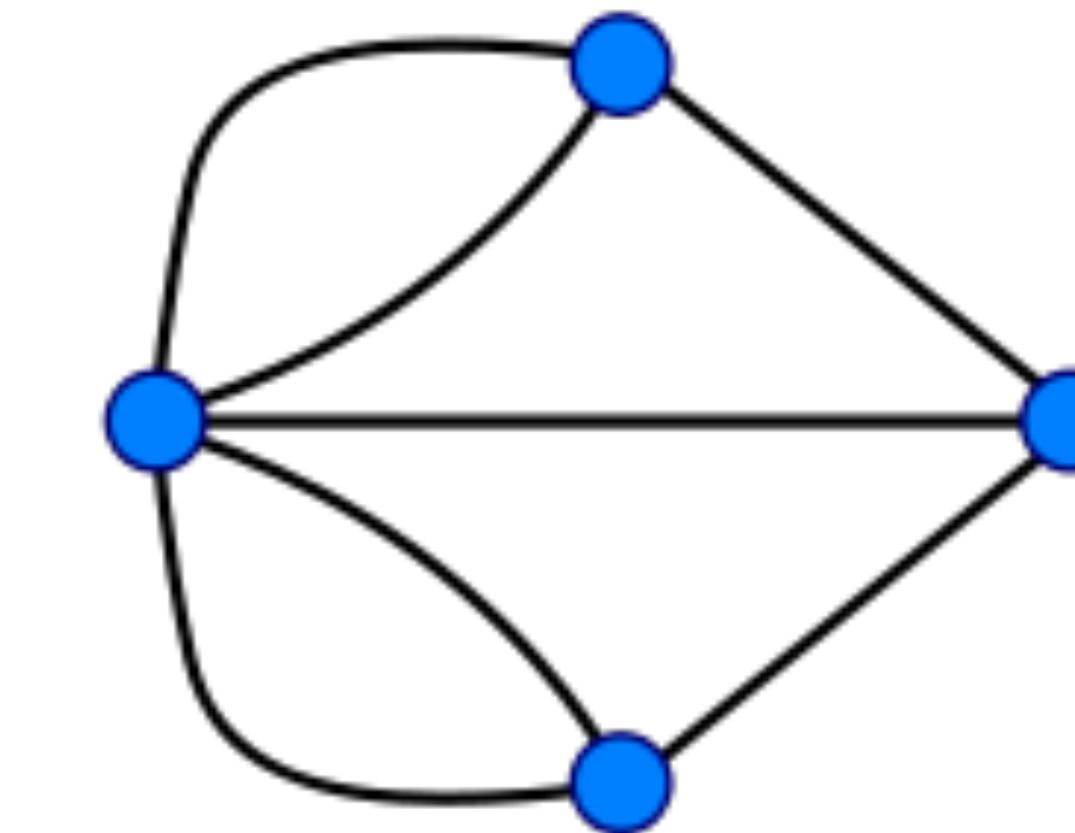
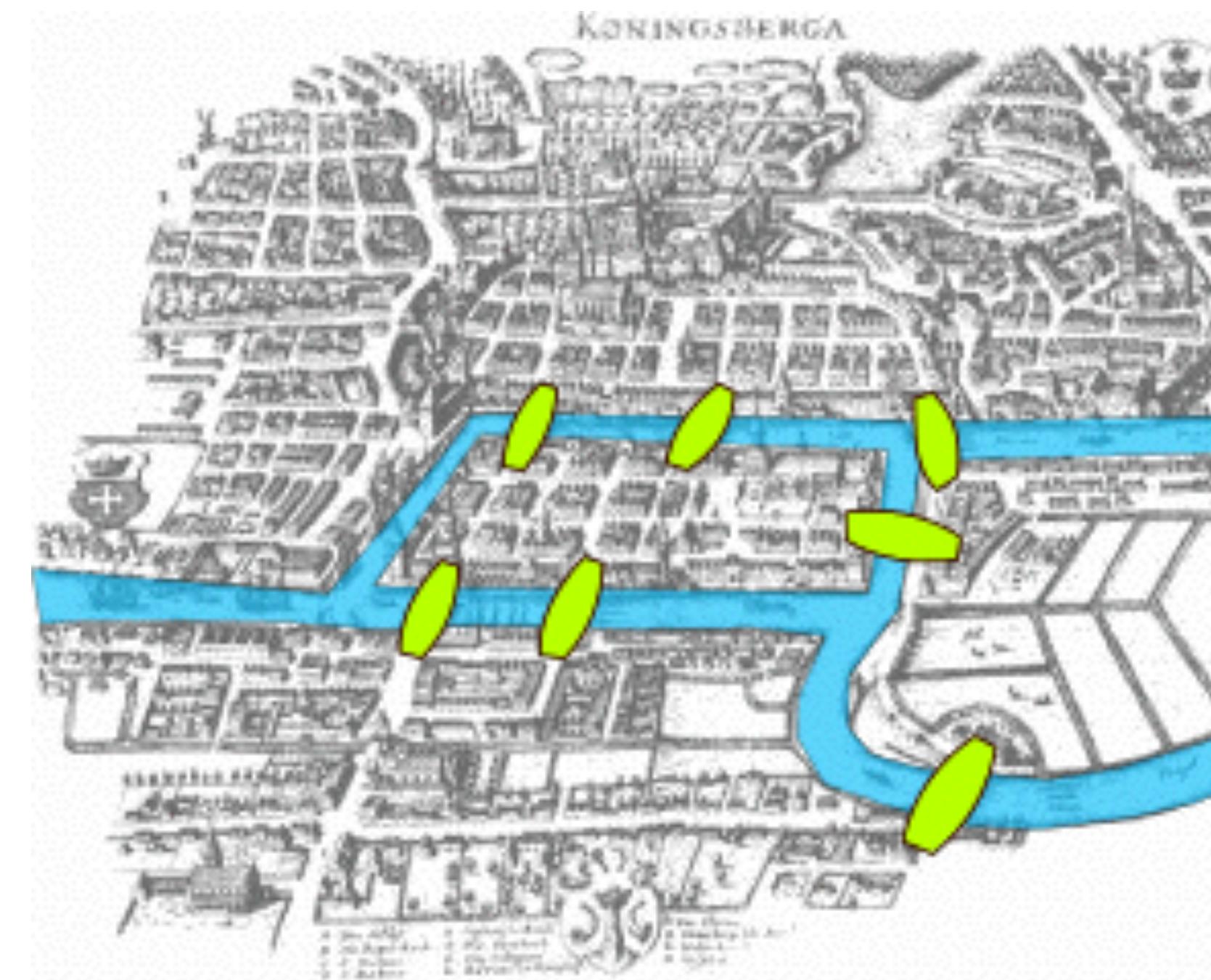
Hypergraph



Bipartite Graph



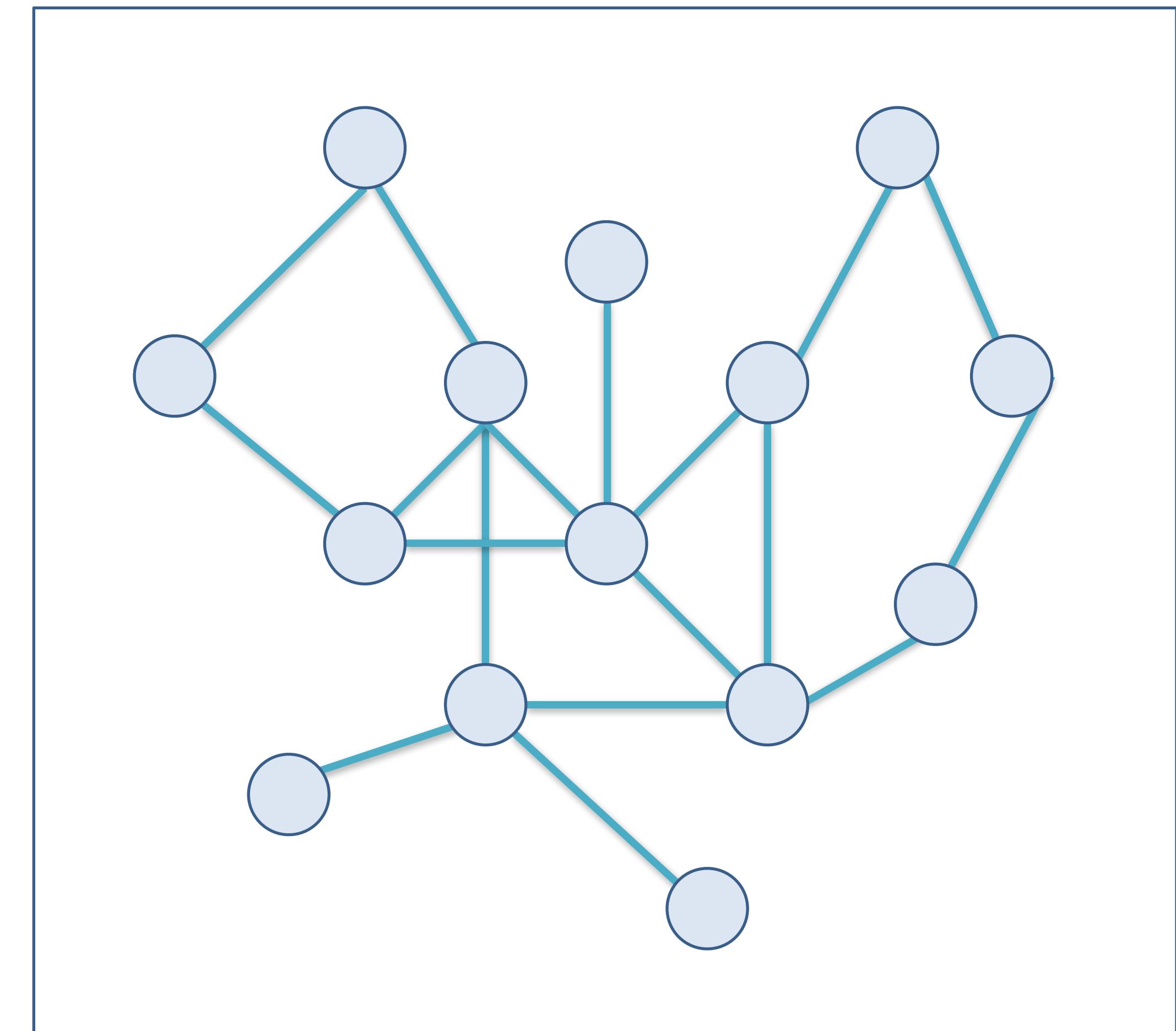
Königsberg Bridge Problem (1736)



Find a Hamiltonian Path (path that visits each vertex exactly once).
Want to make 1 million \$? Develop $O(n^k)$ algorithm.

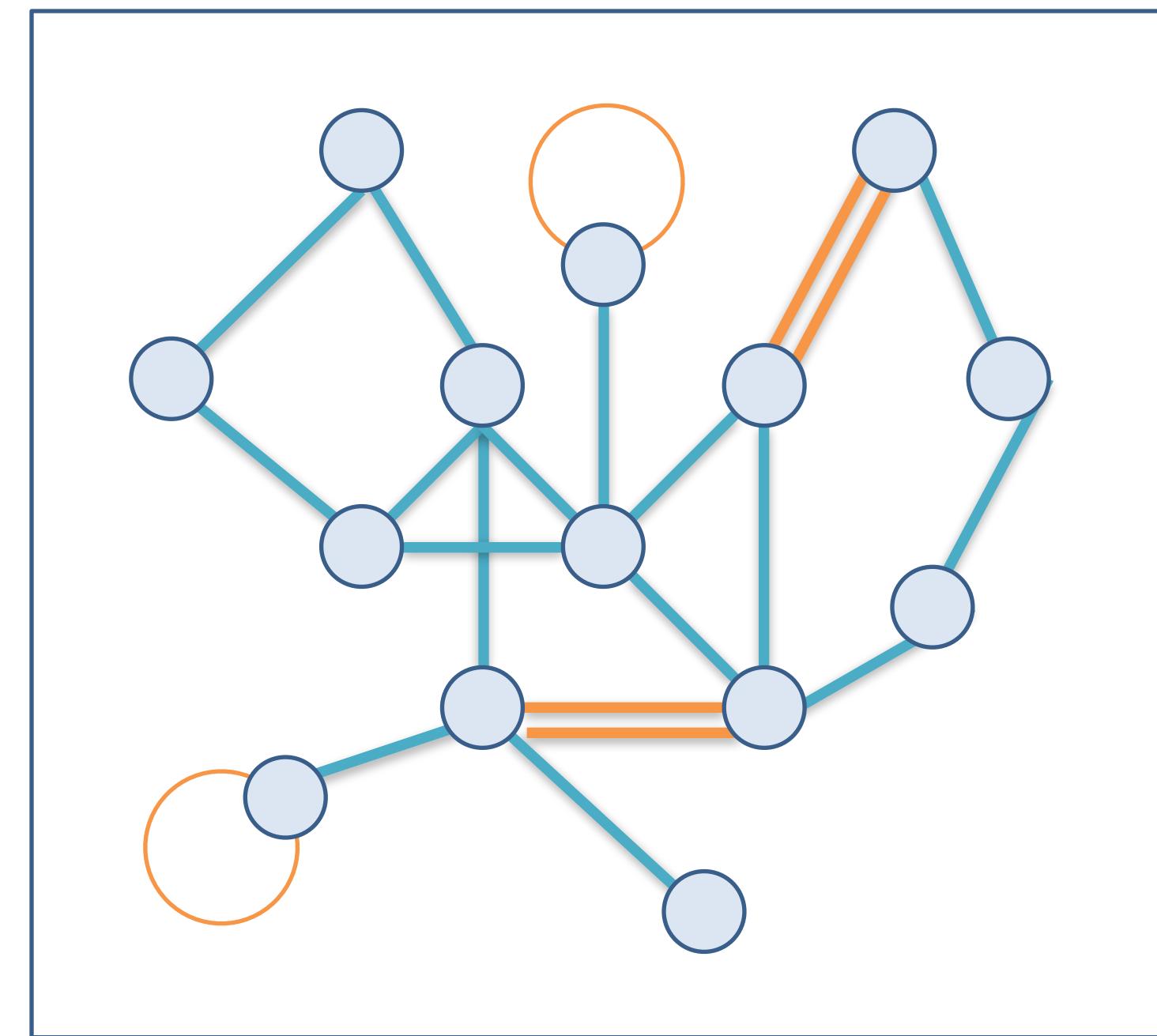
Graph Terms (1)

A graph $G(V,E)$ consists of a set of **vertices** **V** (also called nodes) and a set of **edges** **E** connecting these vertices.



Graph Terms (2)

A simple graph $G(V,E)$ is a graph which contains **no multi-edges** and **no loops**

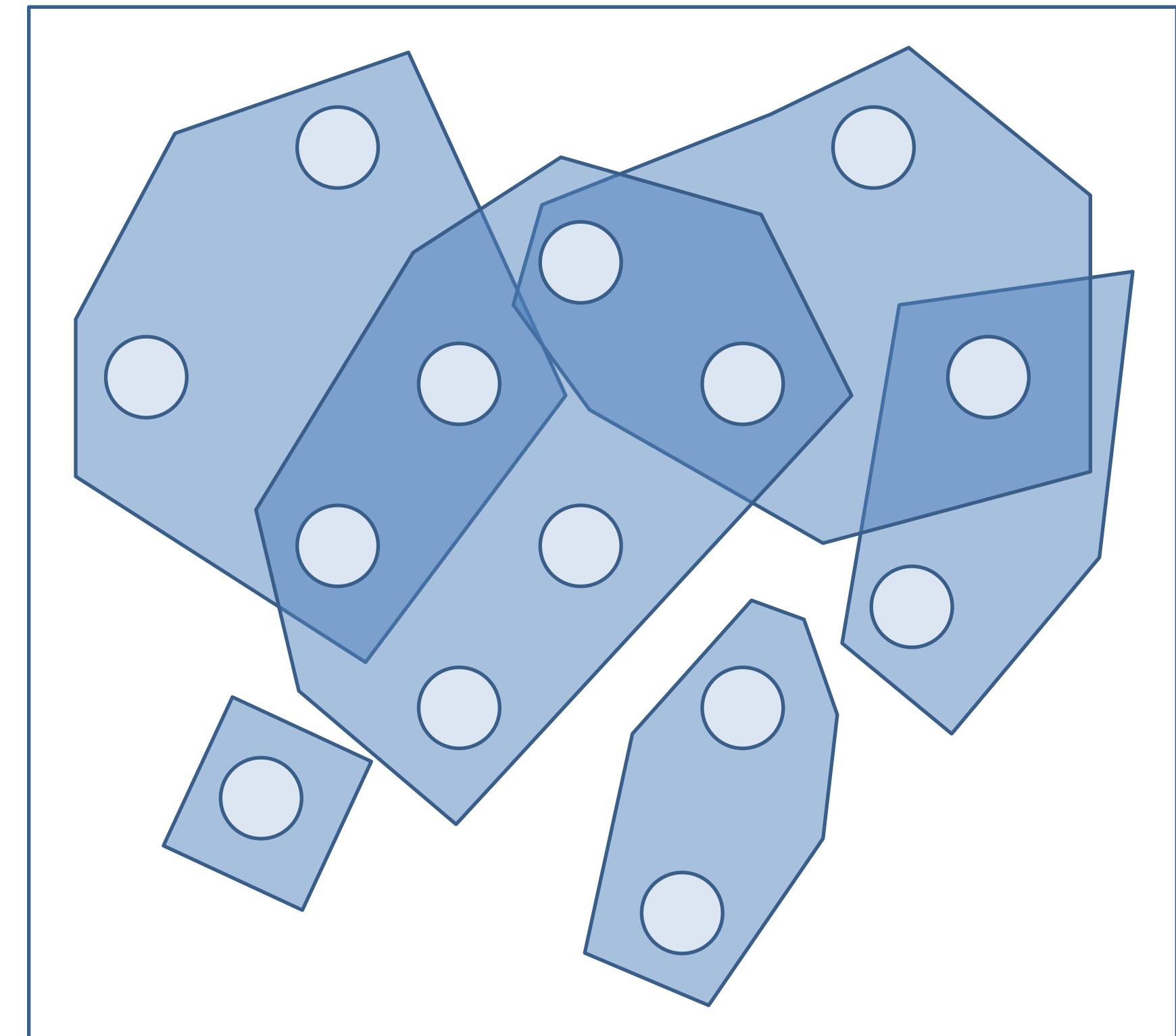


Not a simple graph!
→ A *general graph*

Graph Terms (3)

A directed graph (digraph) is a graph that discerns between the edges $A \rightarrow B$ and $A \leftarrow B$.

A hypergraph is a graph with edges connecting any number of vertices.

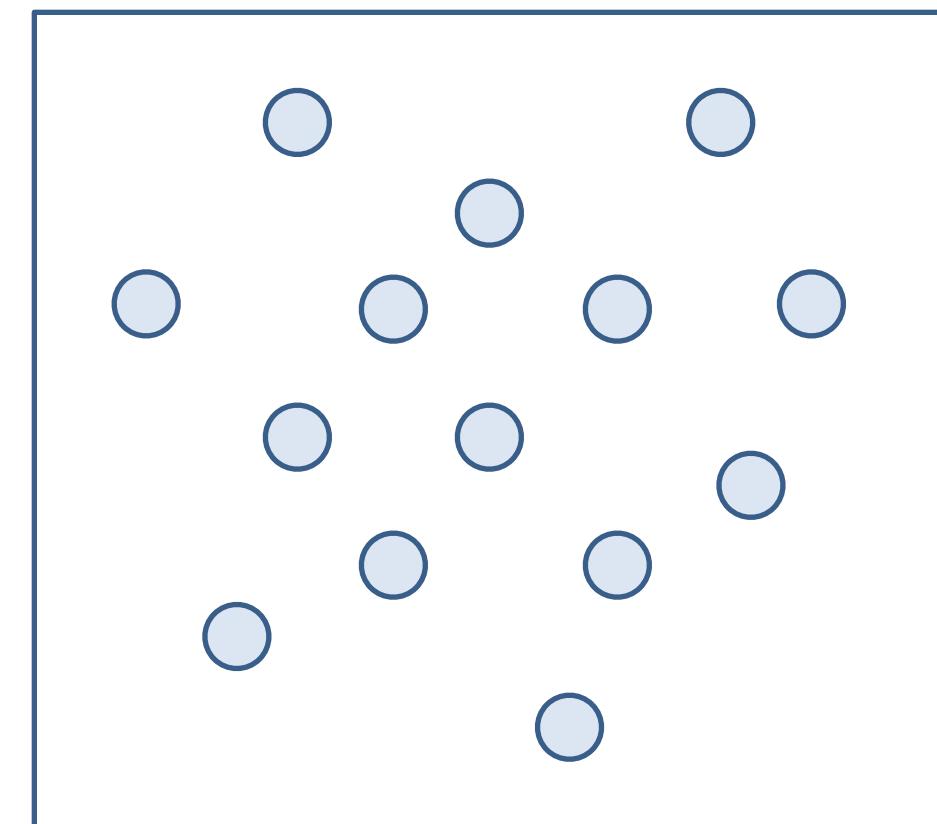


Hypergraph Example

Graph Terms (4)

Independent Set

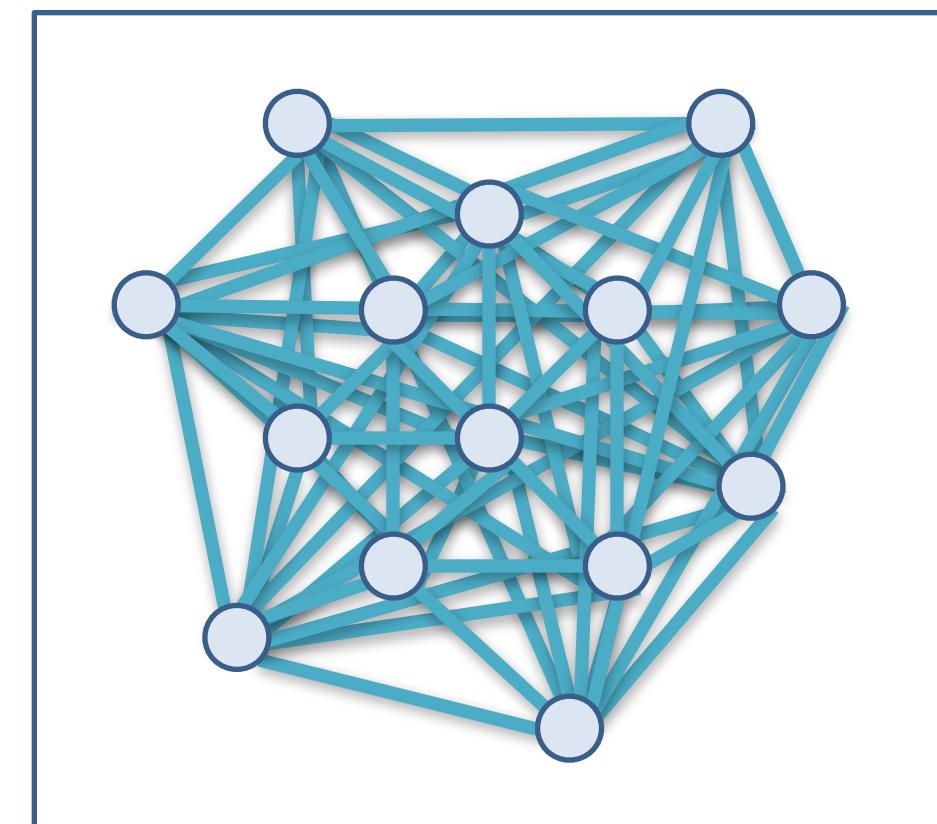
G contains no edges



Independent Set

Clique

G contains all possible edges

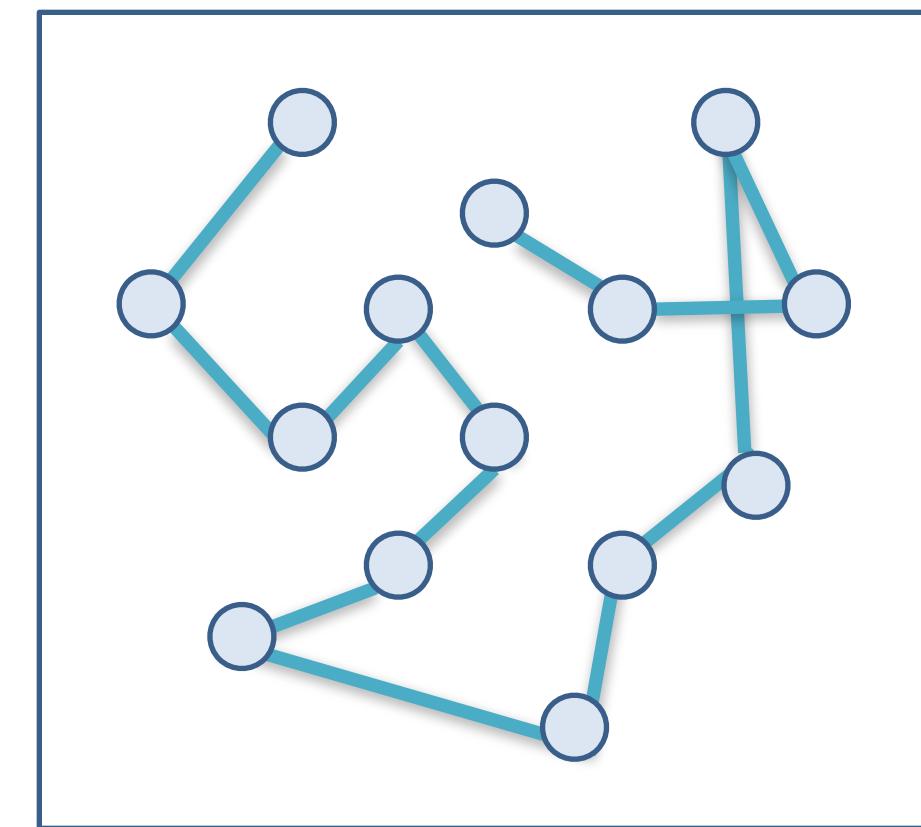


Clique

Graph Terms (5)

Path

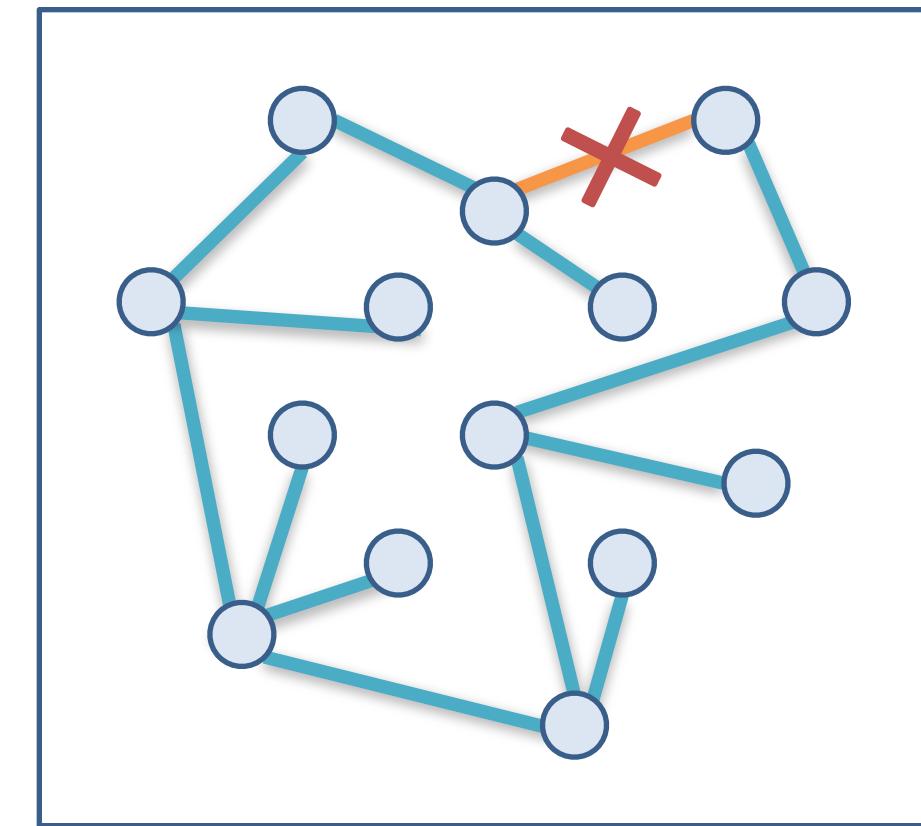
G contains only edges that can be consecutively traversed



Path

Tree

G contains no cycles



Tree

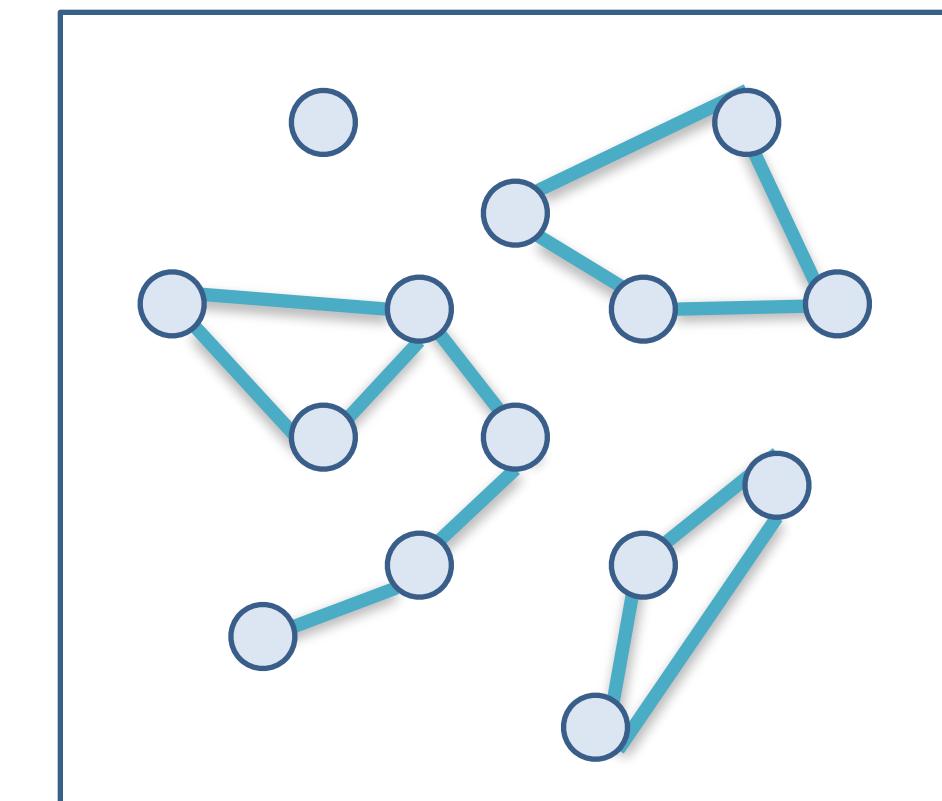
Network

G contains cycles

Graph Terms (6)

Unconnected graph

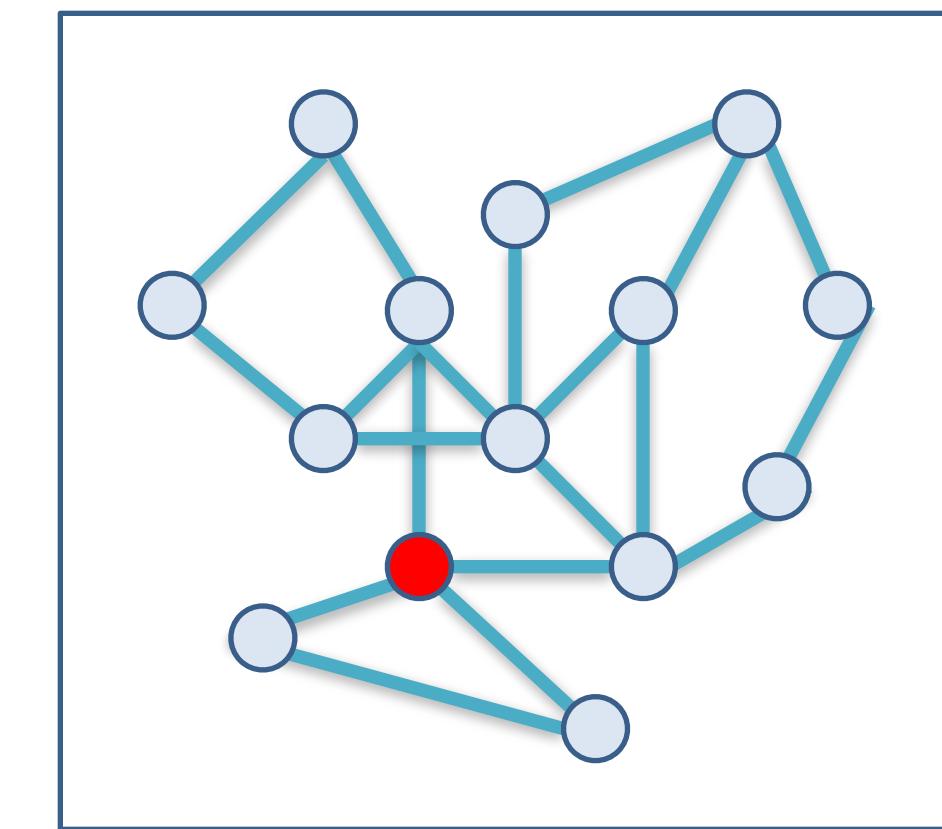
An edge traversal starting from a given vertex cannot reach any other vertex.



Unconnected Graph

Articulation point

Vertices, which if deleted from the graph, would break up the graph in multiple sub-graphs.

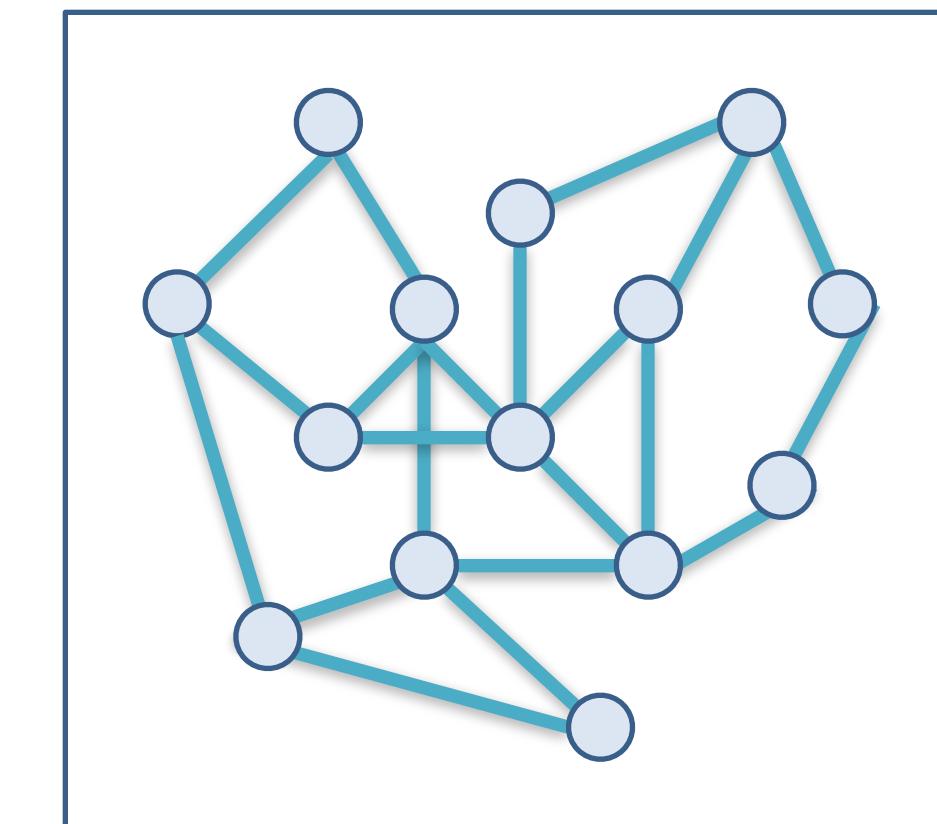


Articulation Point (red)

Graph Terms (7)

Biconnected graph

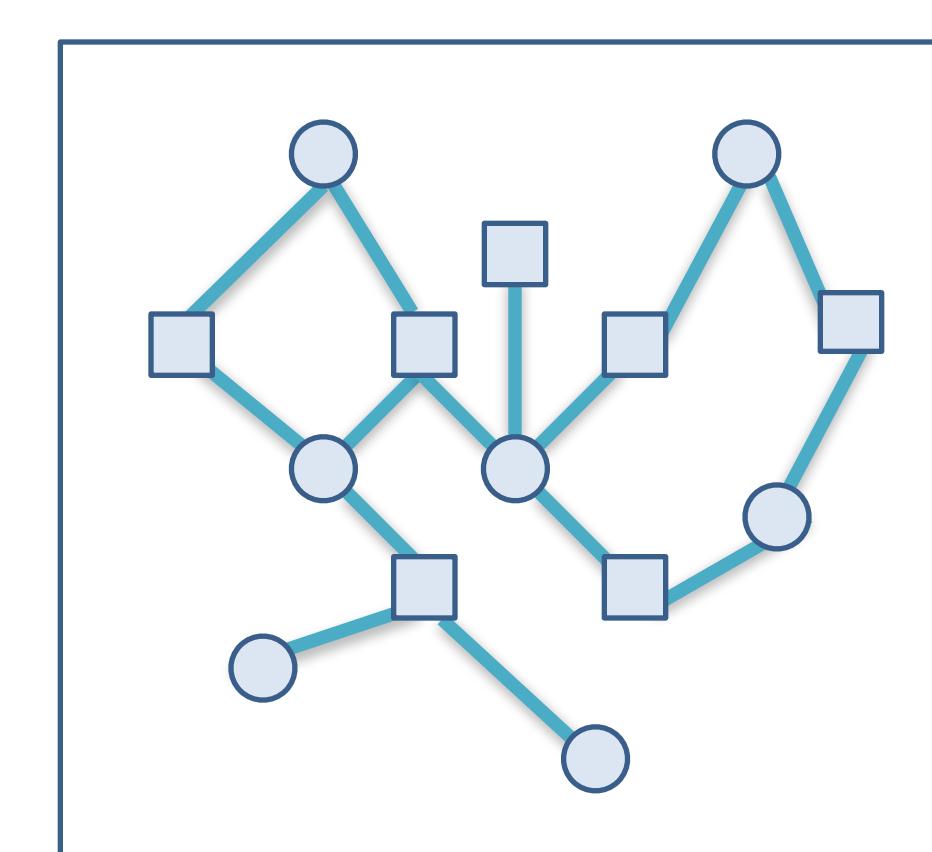
A graph without articulation points.



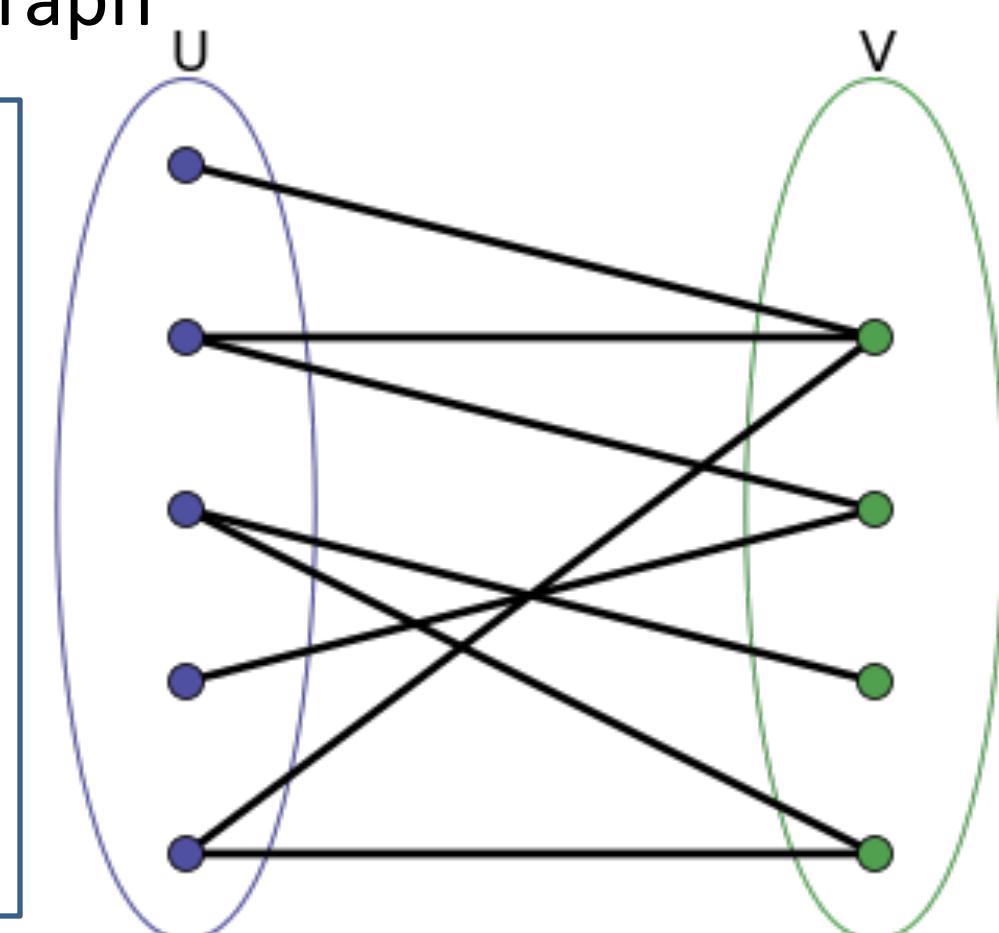
Biconnected Graph

Bipartite graph

The vertices can be partitioned in two independent sets.



Bipartite Graph



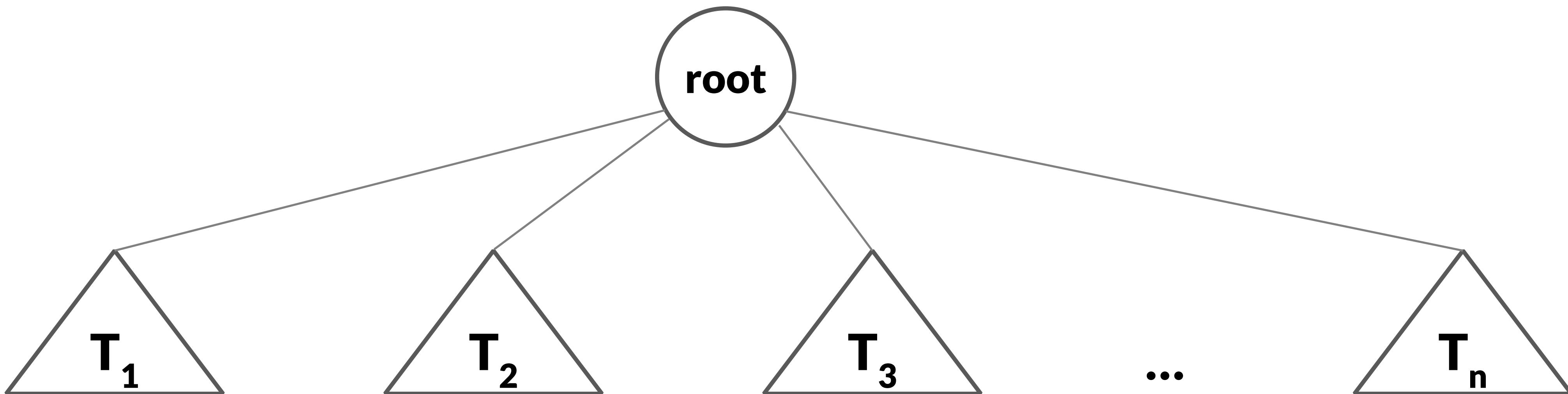
Tree

A graph with no cycles - or:

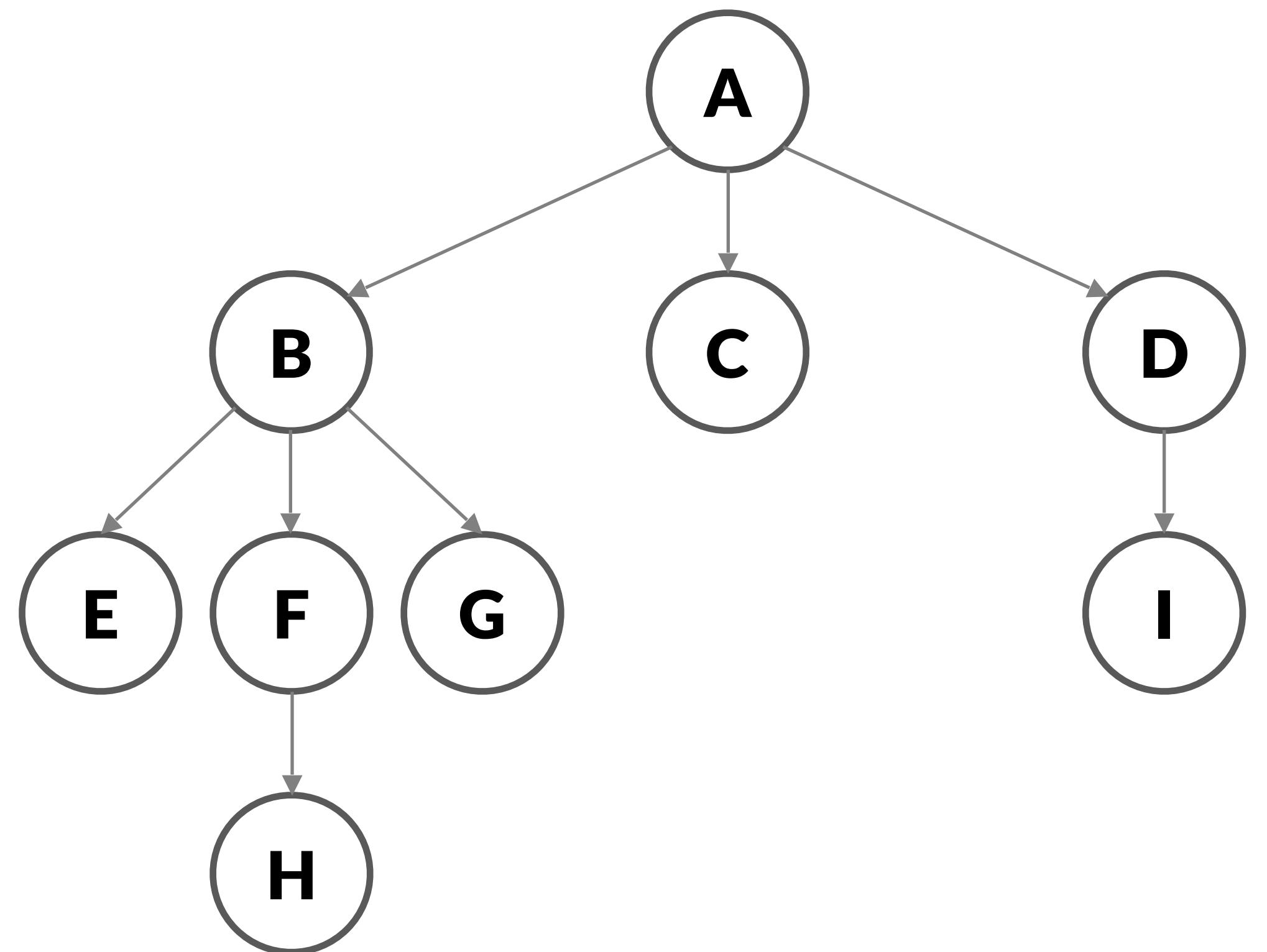
A collection of nodes

contains a root node and 0-n subtrees

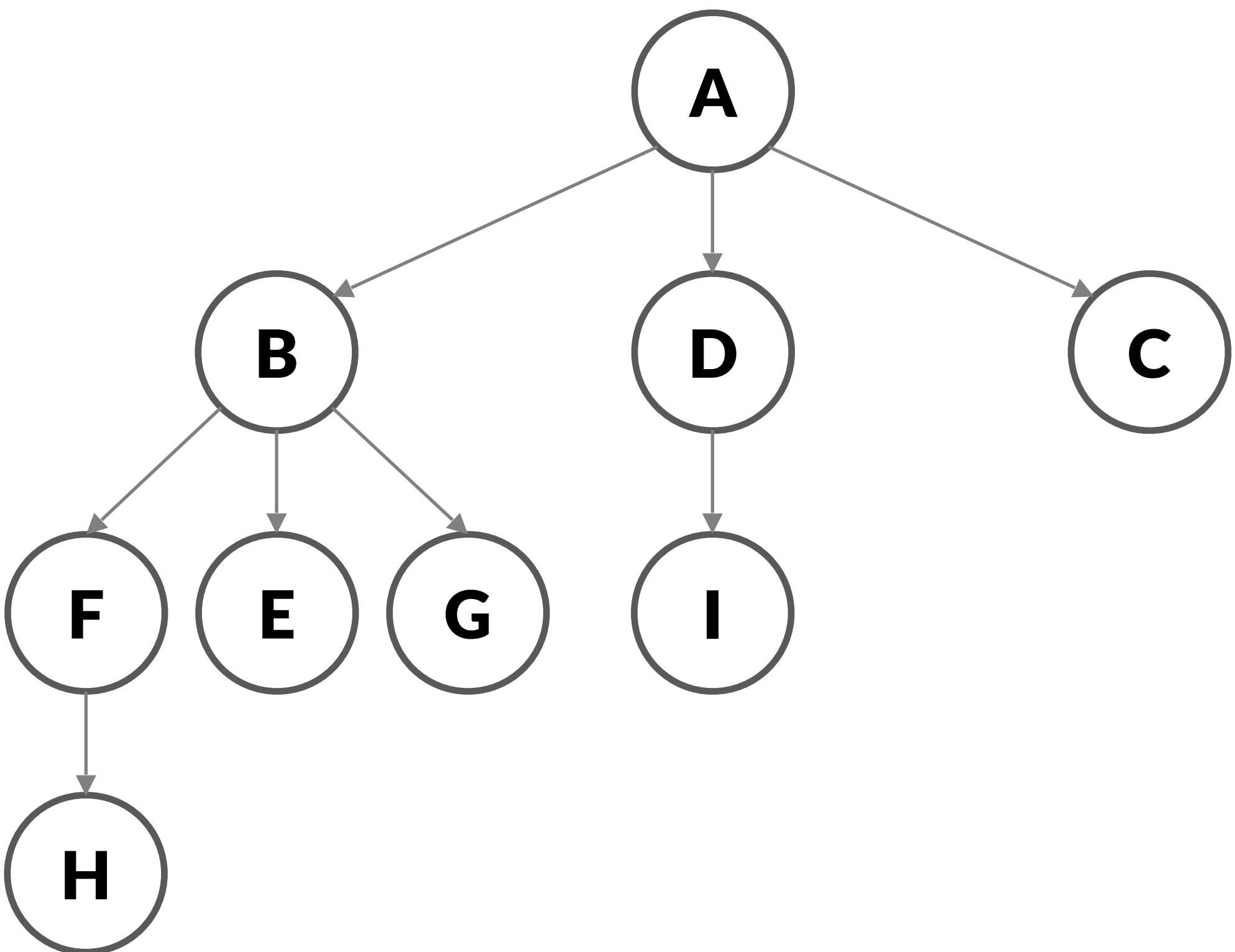
subtrees are connected to root by an edge



Ordered Tree



≠



Binary Trees

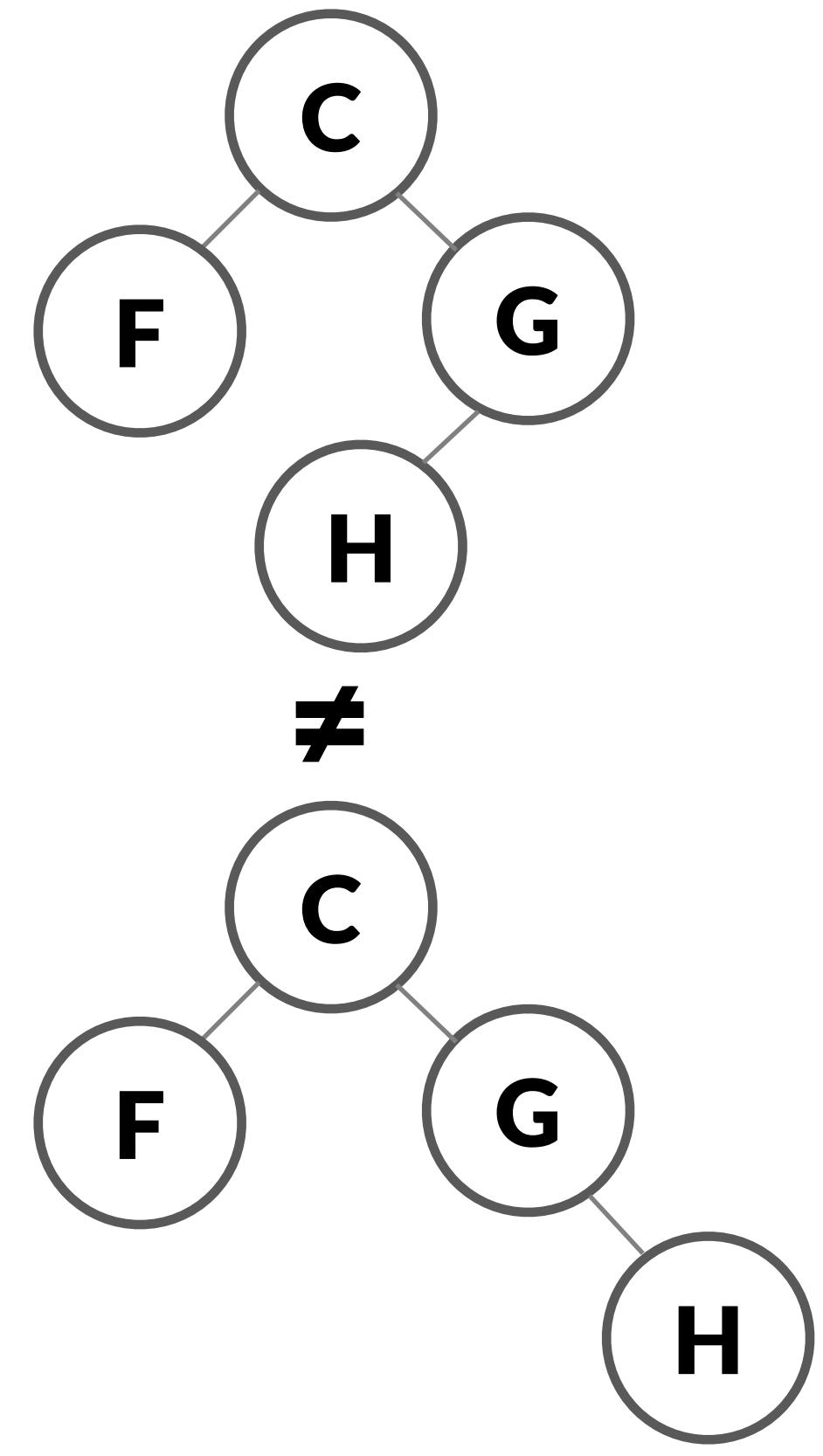
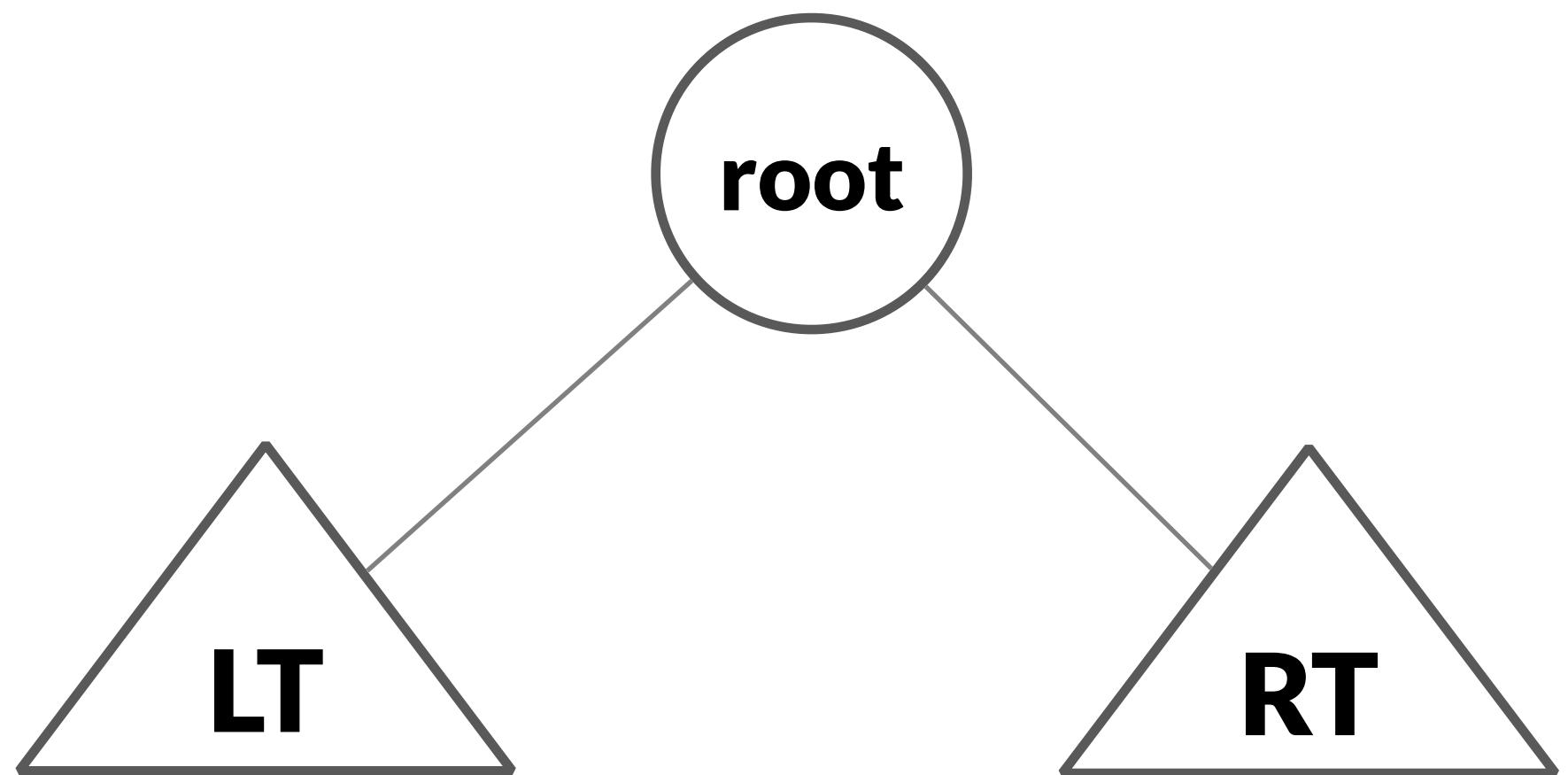
Contains no nodes, or

Is comprised of three disjoint sets of nodes:

a root node,

a binary tree called its left subtree, and

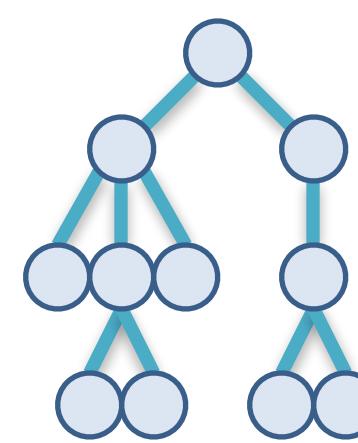
a binary tree called its right subtree



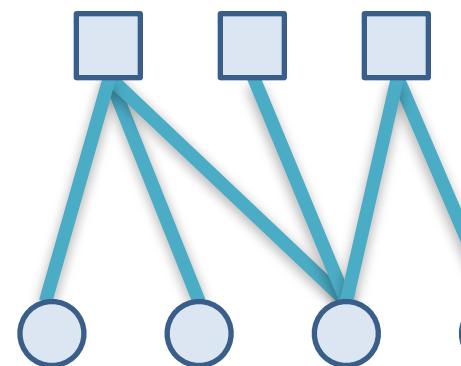
Different Kinds of Graphs

Over 1000 different graph classes

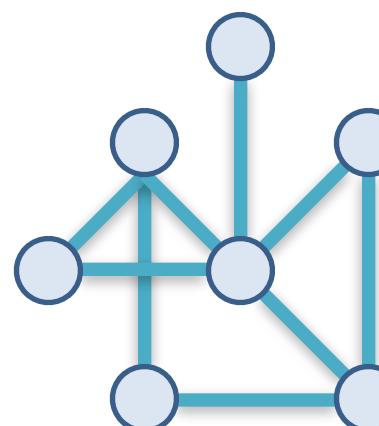
Tree



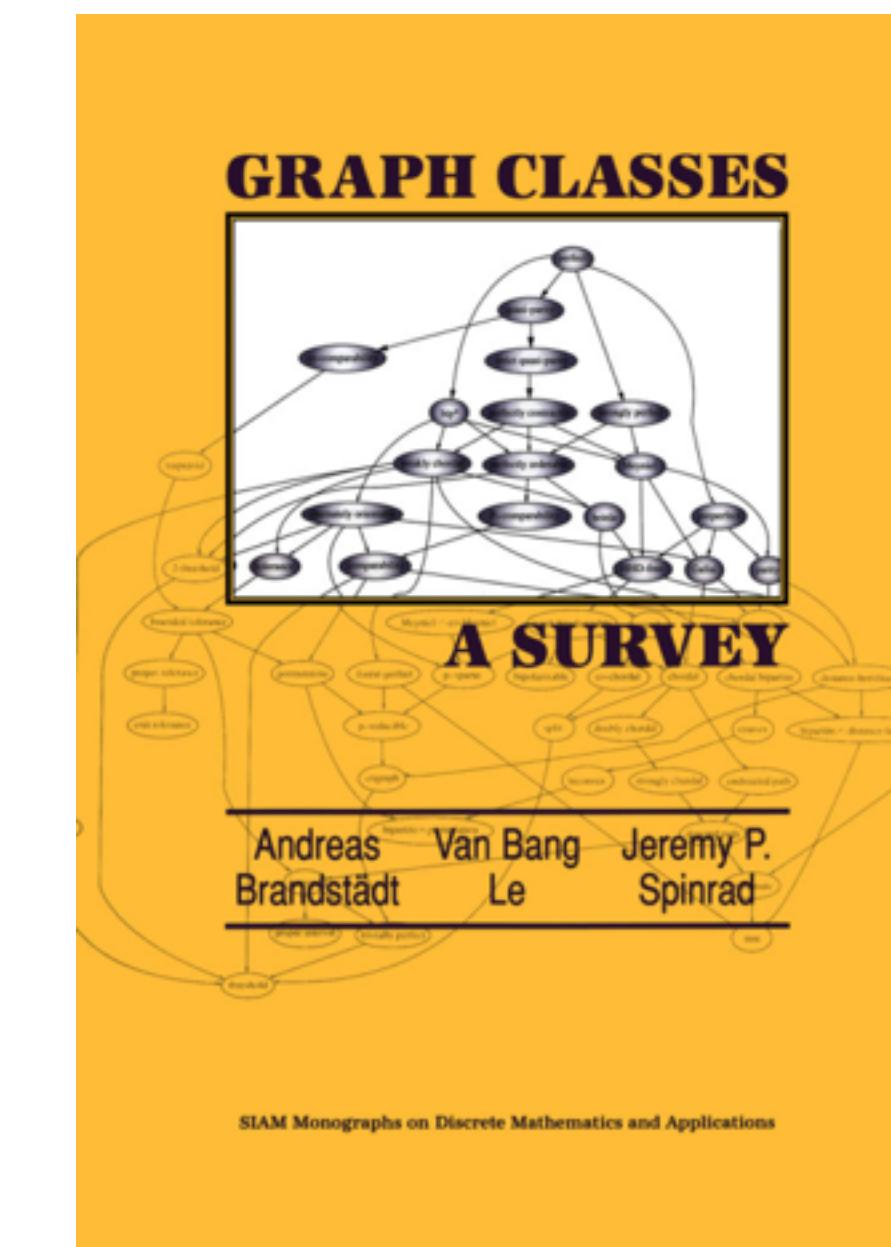
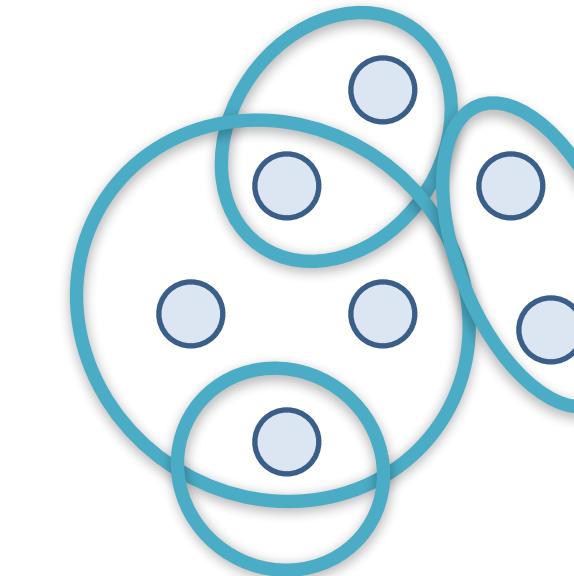
Bipartite Graph



Network



Hypergraph



A. Brandstädt et al. 1999

Graph Measures

Node degree $\deg(x)$

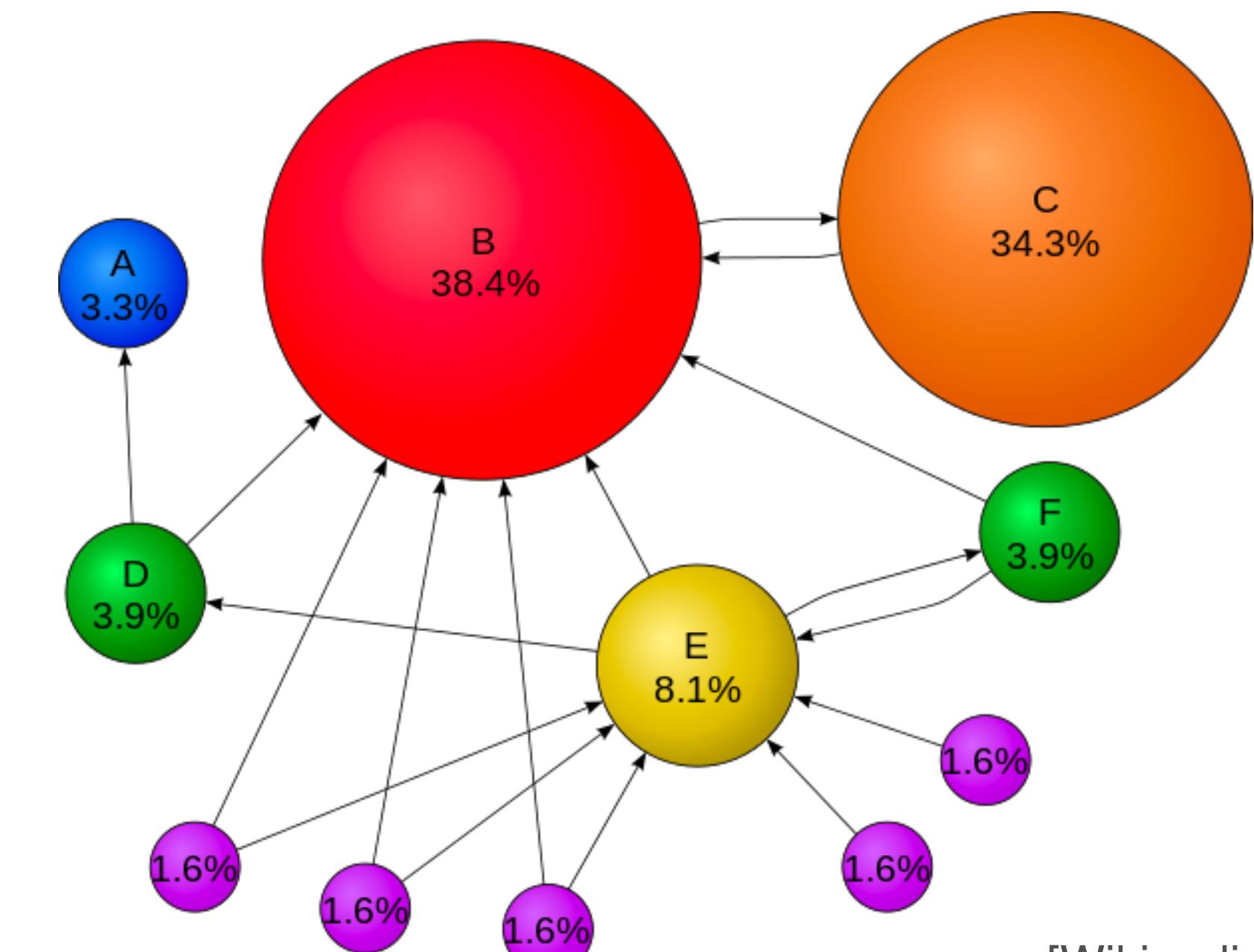
The number of edges being incident to this node. For directed graphs indeg/outdeg are considered separately.

Diameter of graph G

The longest shortest path within G.

Pagerank

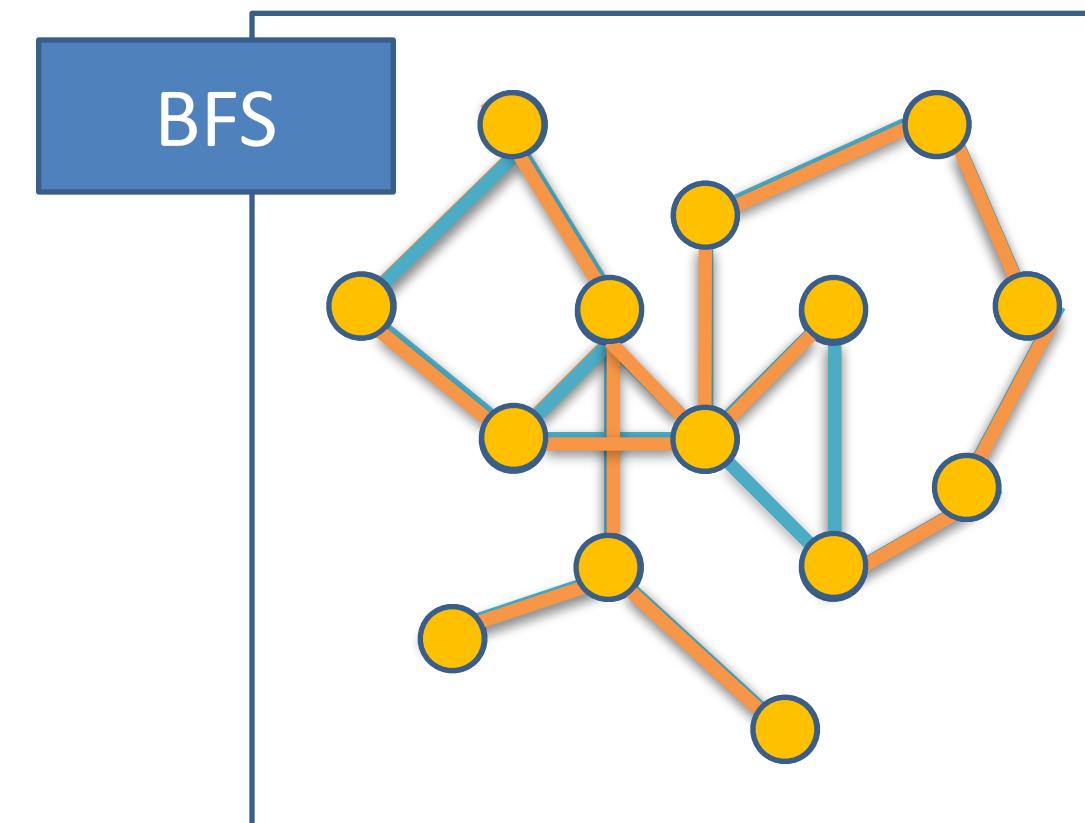
count number & quality of links



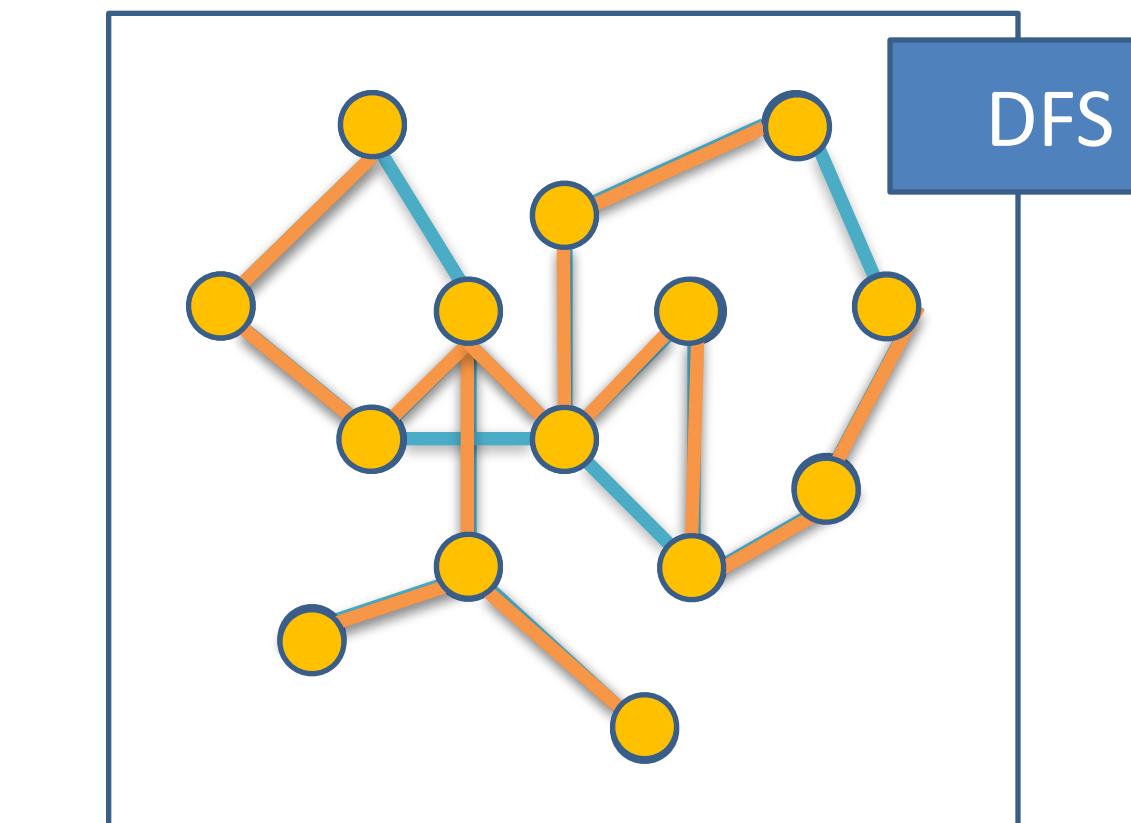
[Wikipedia]

Graph Algorithms (1)

Traversal: Breadth First Search, Depth First Search



- generates neighborhoods
- hierarchy gets rather wide than deep
- solves single-source shortest paths (SSSP)



- classical way-finding/back-tracking strategy
- tree serialization
- topological ordering

Hard Graph Algorithms (NP-Complete)

Longest path

Largest clique

Maximum independent set (set of vertices in a graph, no two of which are adjacent)

Maximum cut (separation of vertices in two sets that cuts most edges)

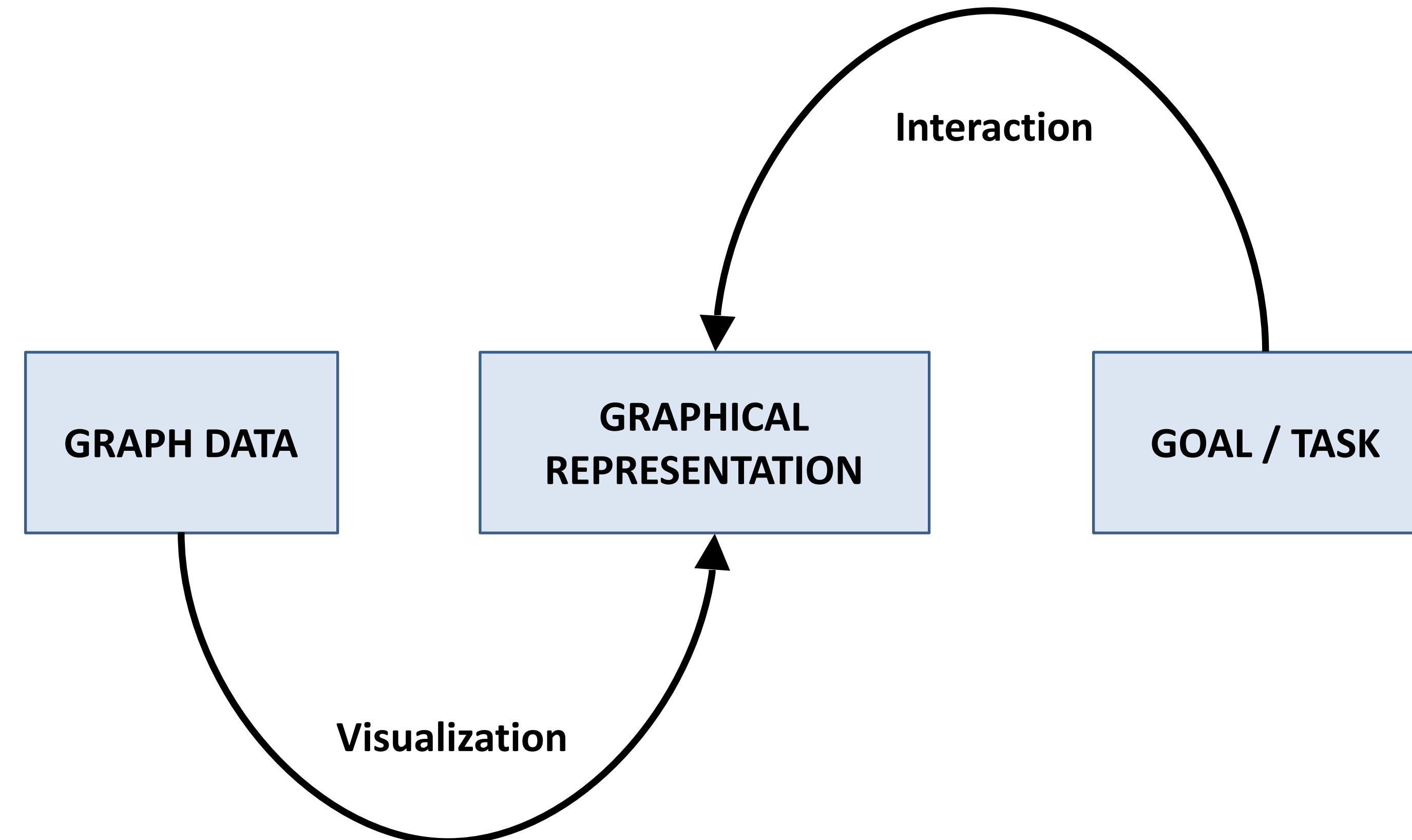
Hamiltonian path/cycle (path that visits all vertexes once)

Coloring / chromatic number (colors for vertices where no adjacent v. have same color)

Minimum degree spanning tree

Graph and Tree Visualization

Setting the Stage



How to decide which **representation** to use for which **type of graph** in order to achieve which kind of **goal**?

Different Kinds of Tasks/Goals

Two principal types of tasks: **attribute-based (ABT)** and **topology-based (TBT)**

Localize – find a single or multiple nodes/edges that fulfill a given property

- ABT: Find the edge(s) with the maximum edge weight.
- TBT: Find all adjacent nodes of a given node.

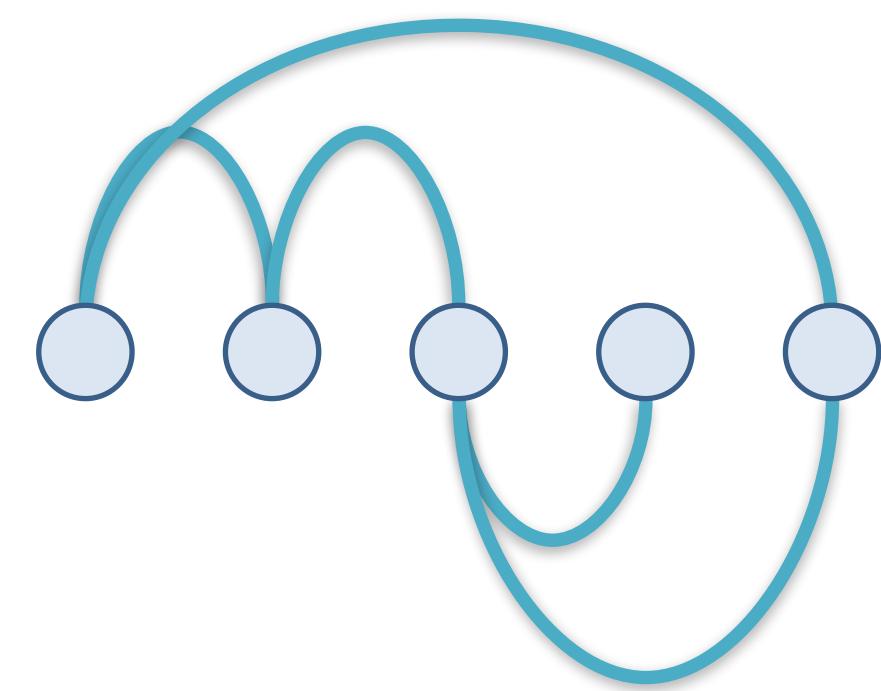
Quantify – count or estimate a numerical property of the graph

- ABT: Give the number of all nodes.
- TBT: Give the indegree (the number of incoming edges) of a node.

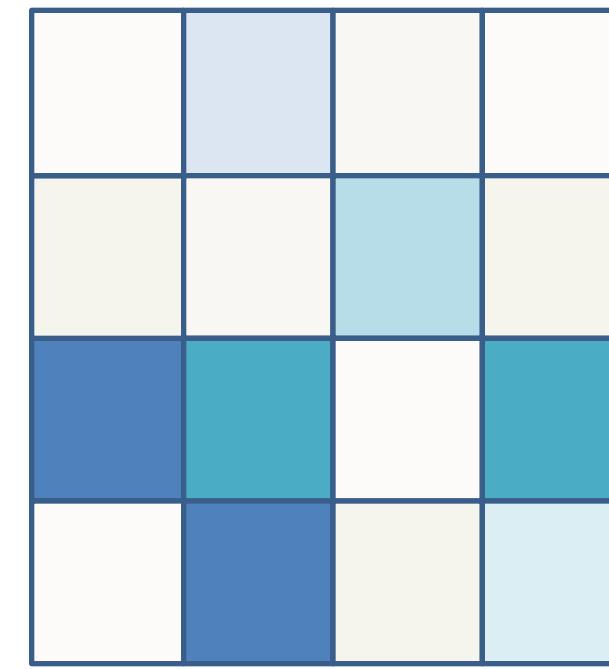
Sort/Order – enumerate the nodes/edges according to a given criterion

- ABT: Sort all edges according to their weight.
- TBT: Traverse the graph starting from a given node.

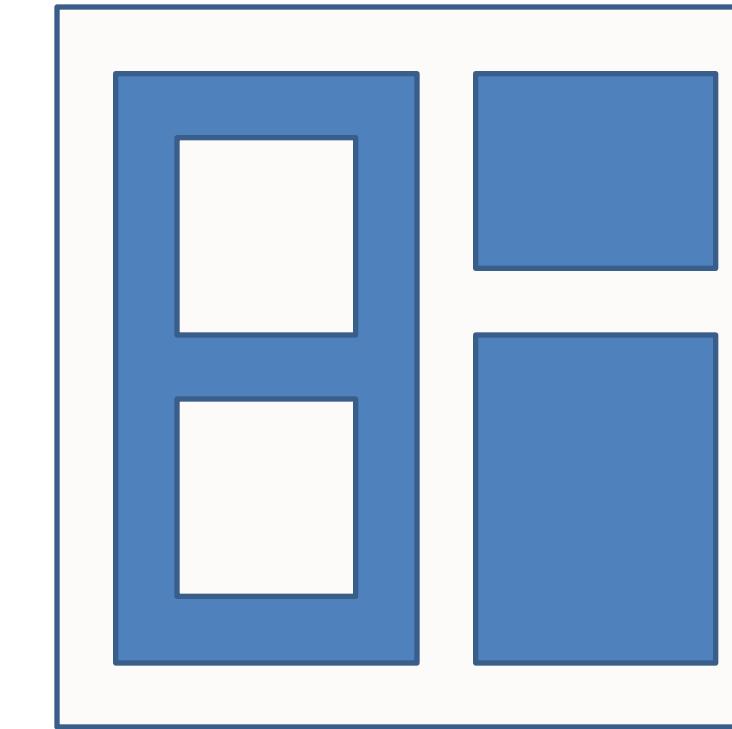
Three Types of Graph Representations



Explicit
(Node-Link)



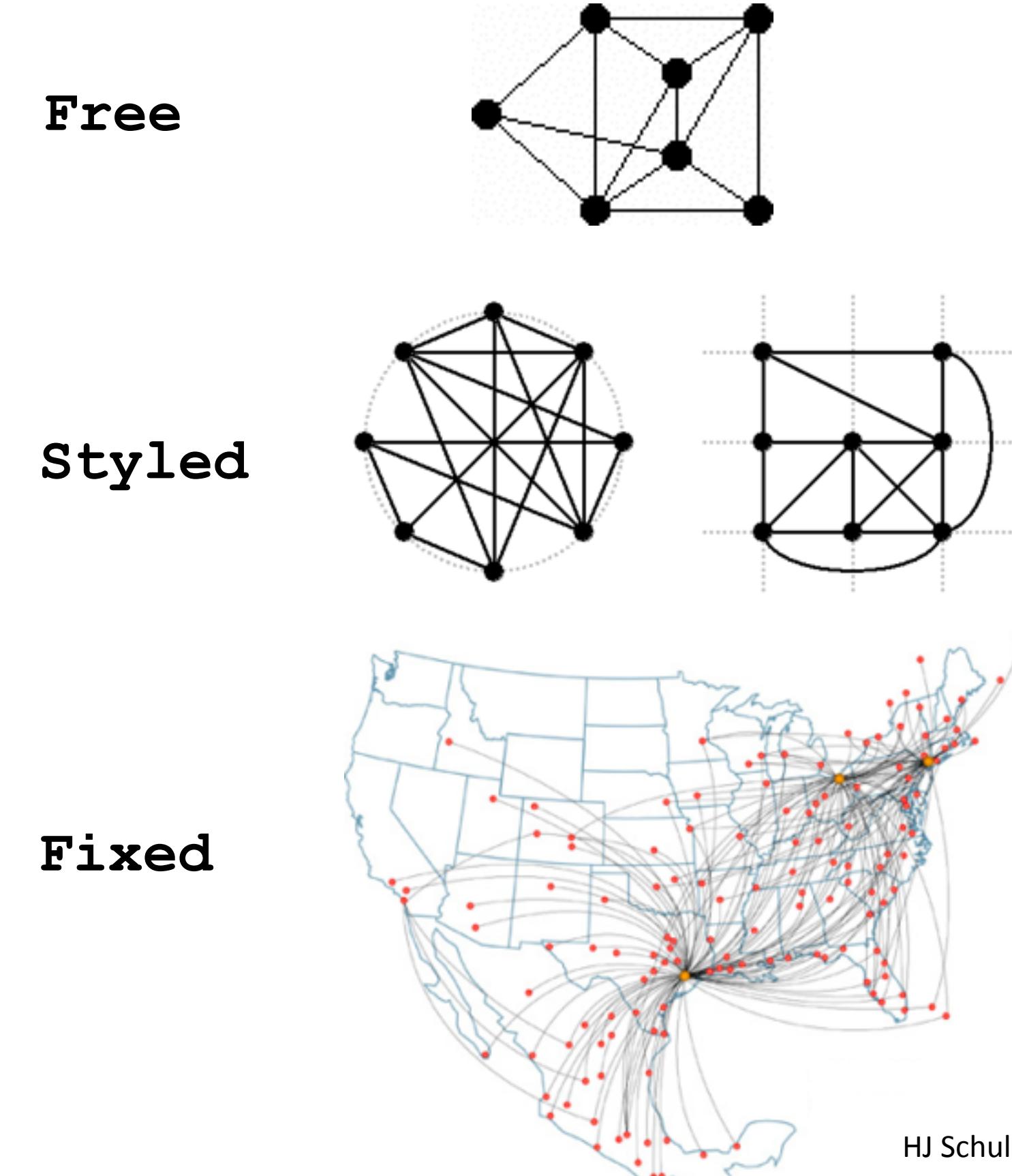
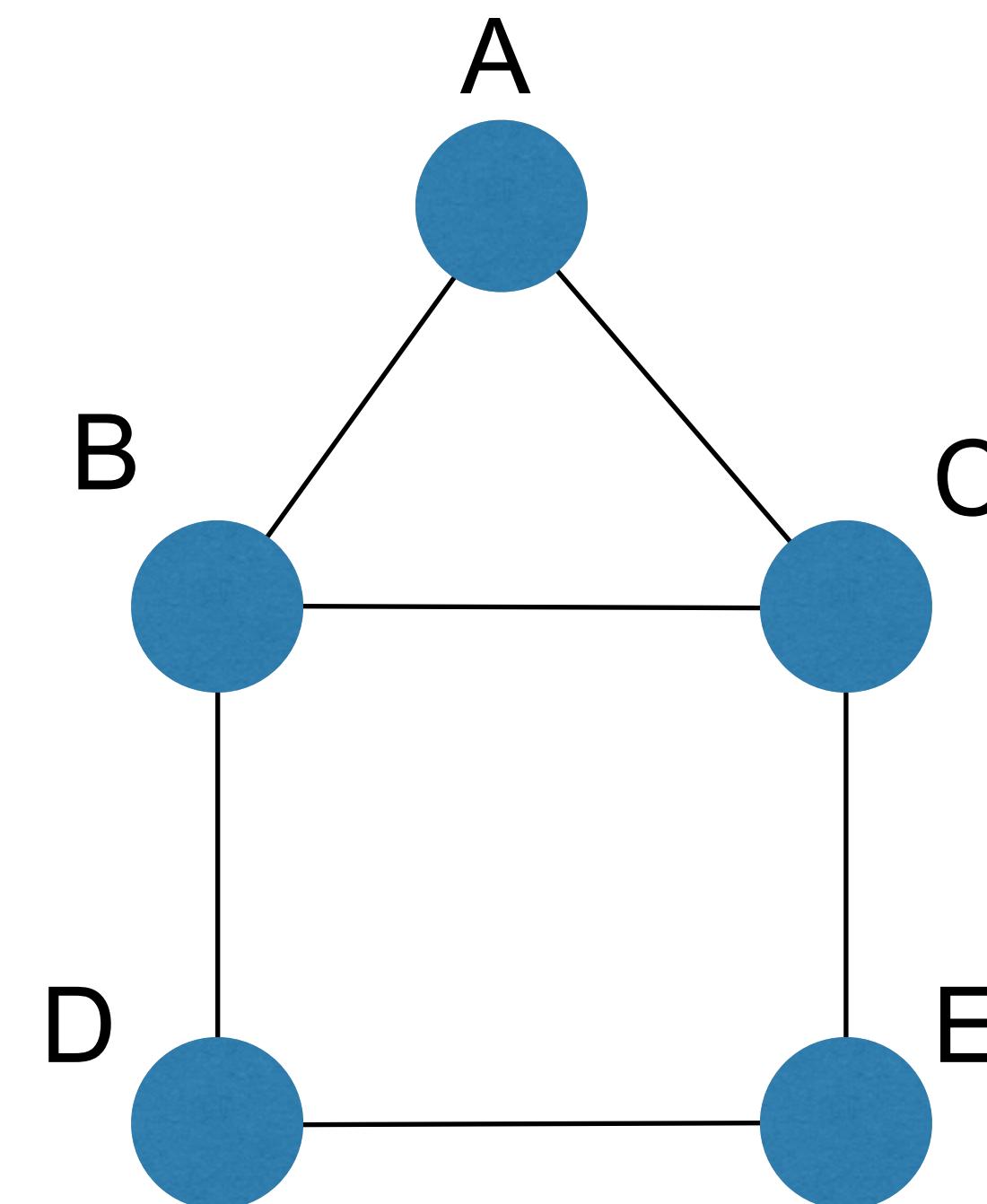
Matrix



Implicit

Explicit Graph Representations

Node-link diagrams: vertex = point, edge = line/arc



Criteria for Good Node-Link Layout

Minimized **edge crossings**

Minimized **distance** of neighboring nodes

Minimized **drawing area**

Uniform edge **length**

Minimized edge **bends**

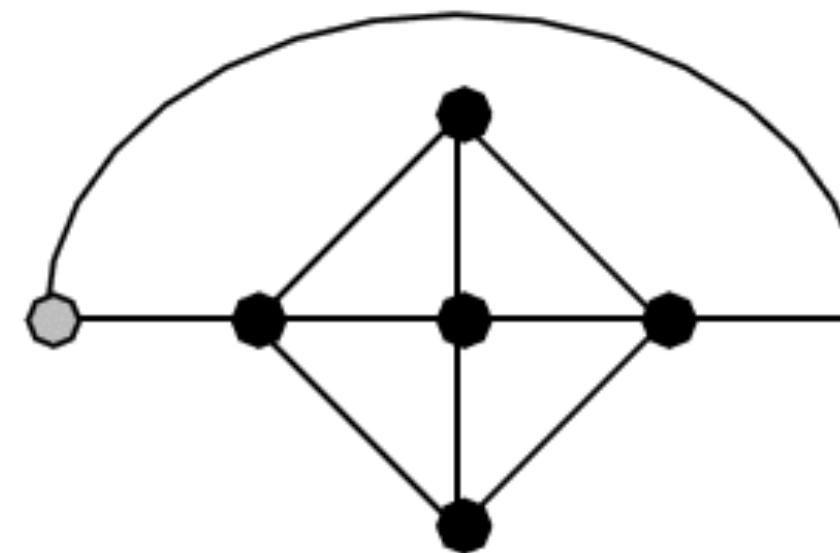
Maximized **angular distance** between different edges

Aspect ratio about 1 (not too long and not too wide)

Symmetry: similar graph structures should look similar

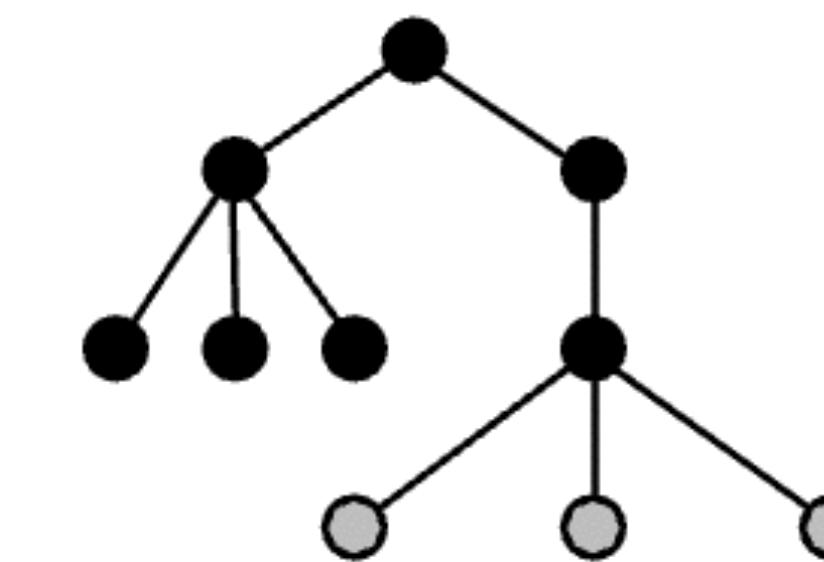
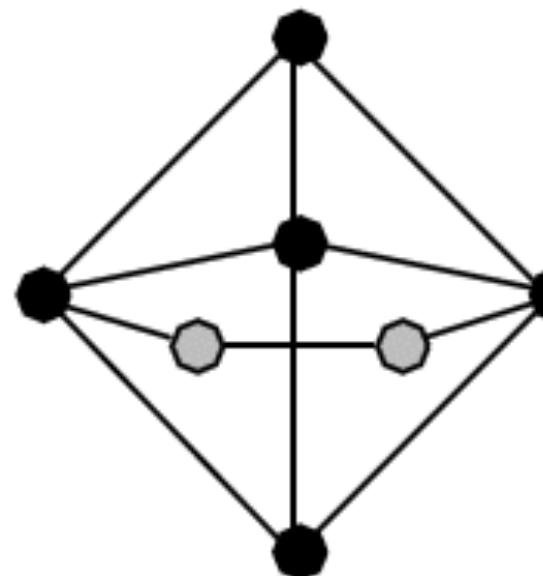
Conflicting Criteria

Minimum number
of edge crossings



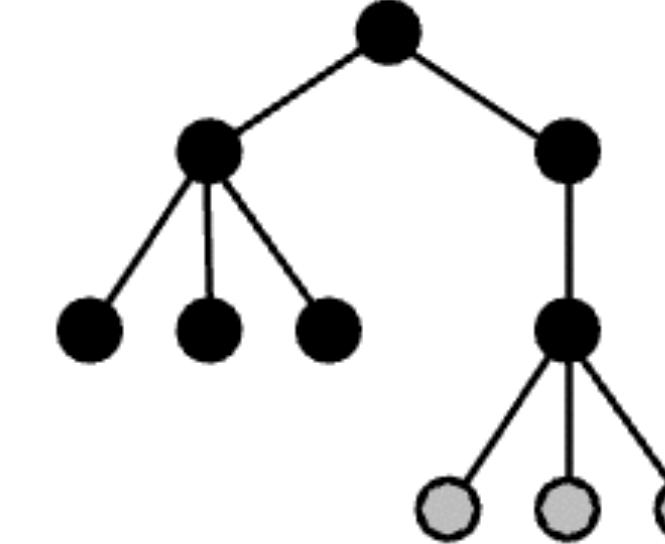
vs.

Uniform edge
length



Space utilization

vs.



Symmetry

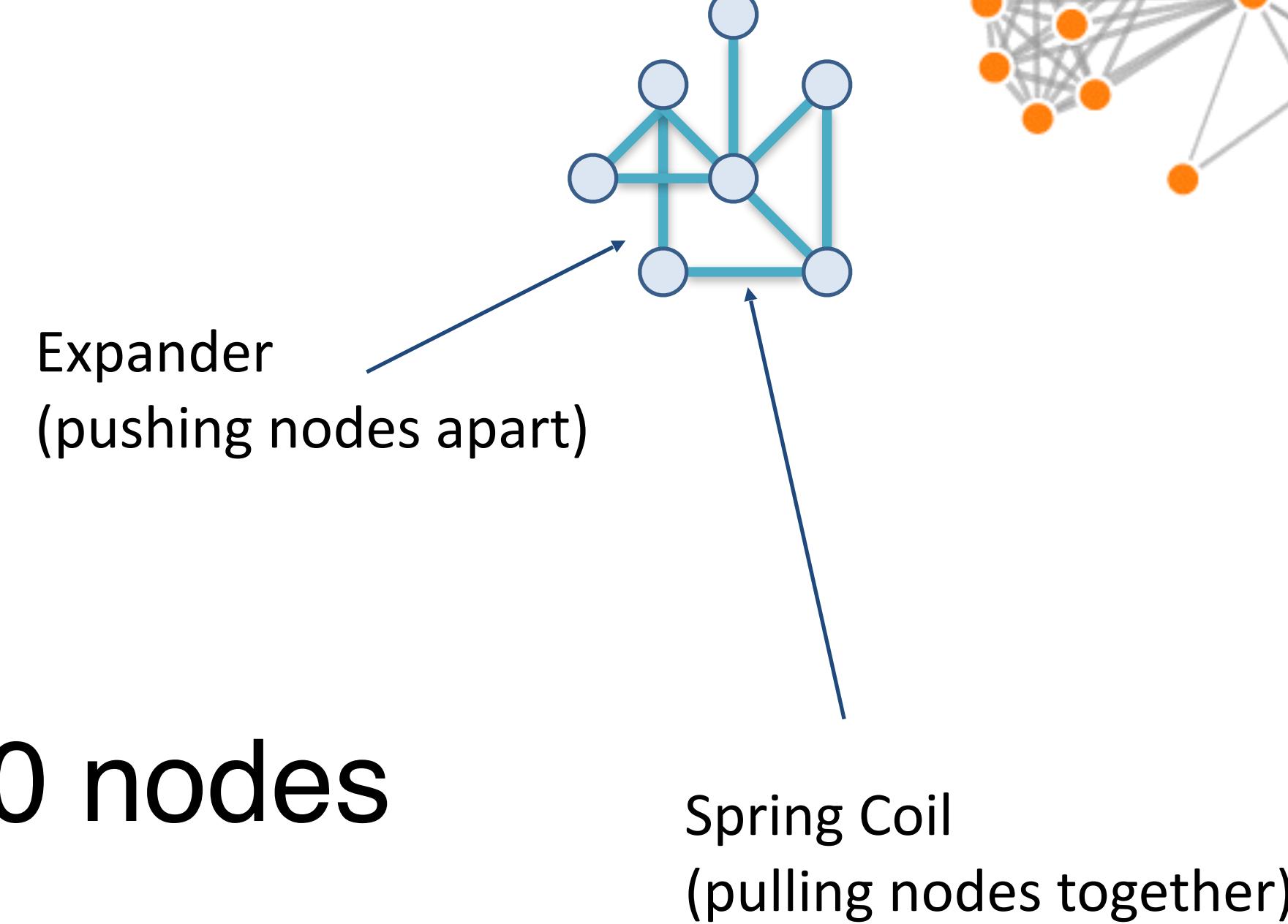
Force Directed Layouts

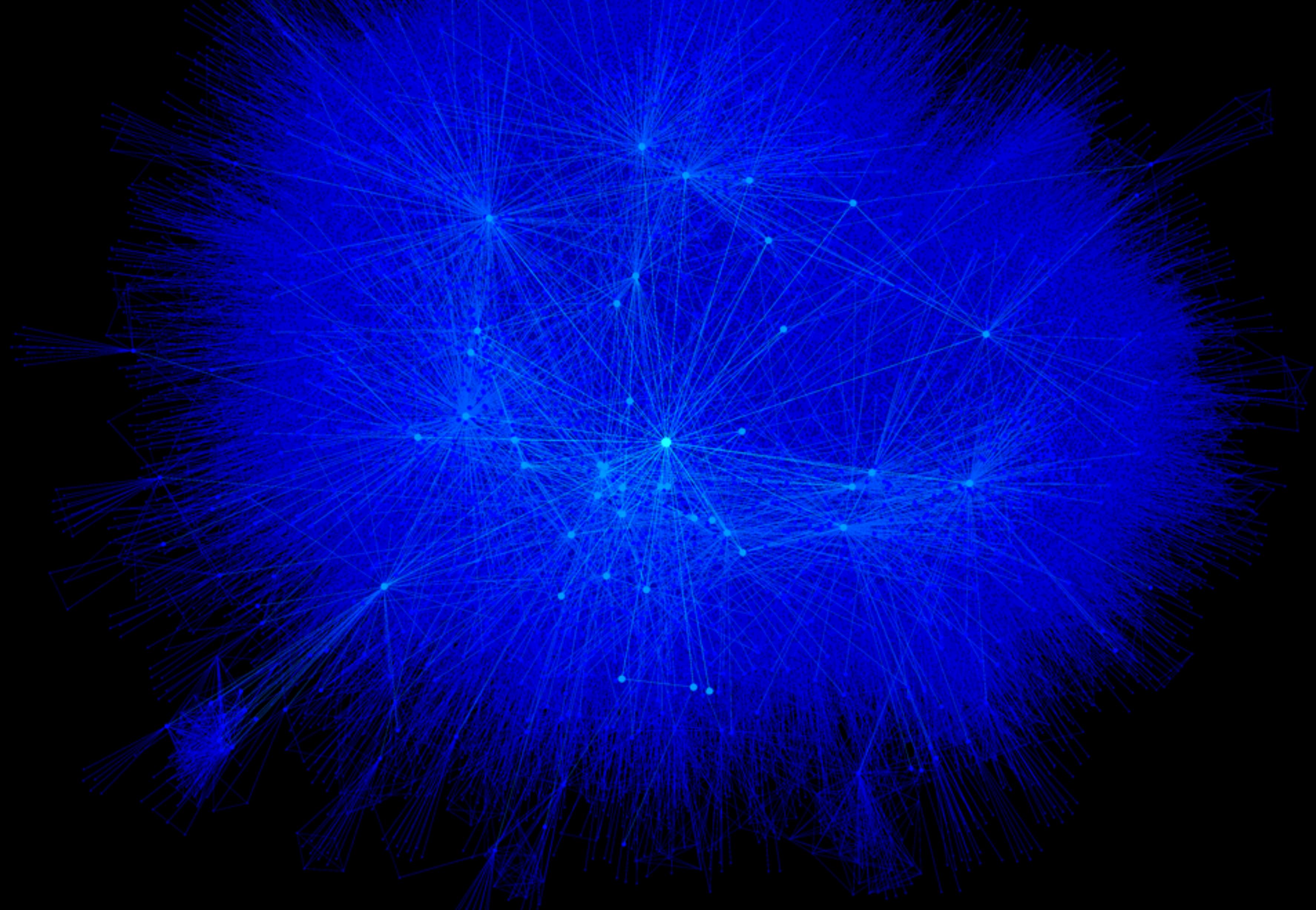
Physics model:
edges = springs,
vertices = repulsive magnets

in practice: damping

Computationally
expensive: $O(n^3)$

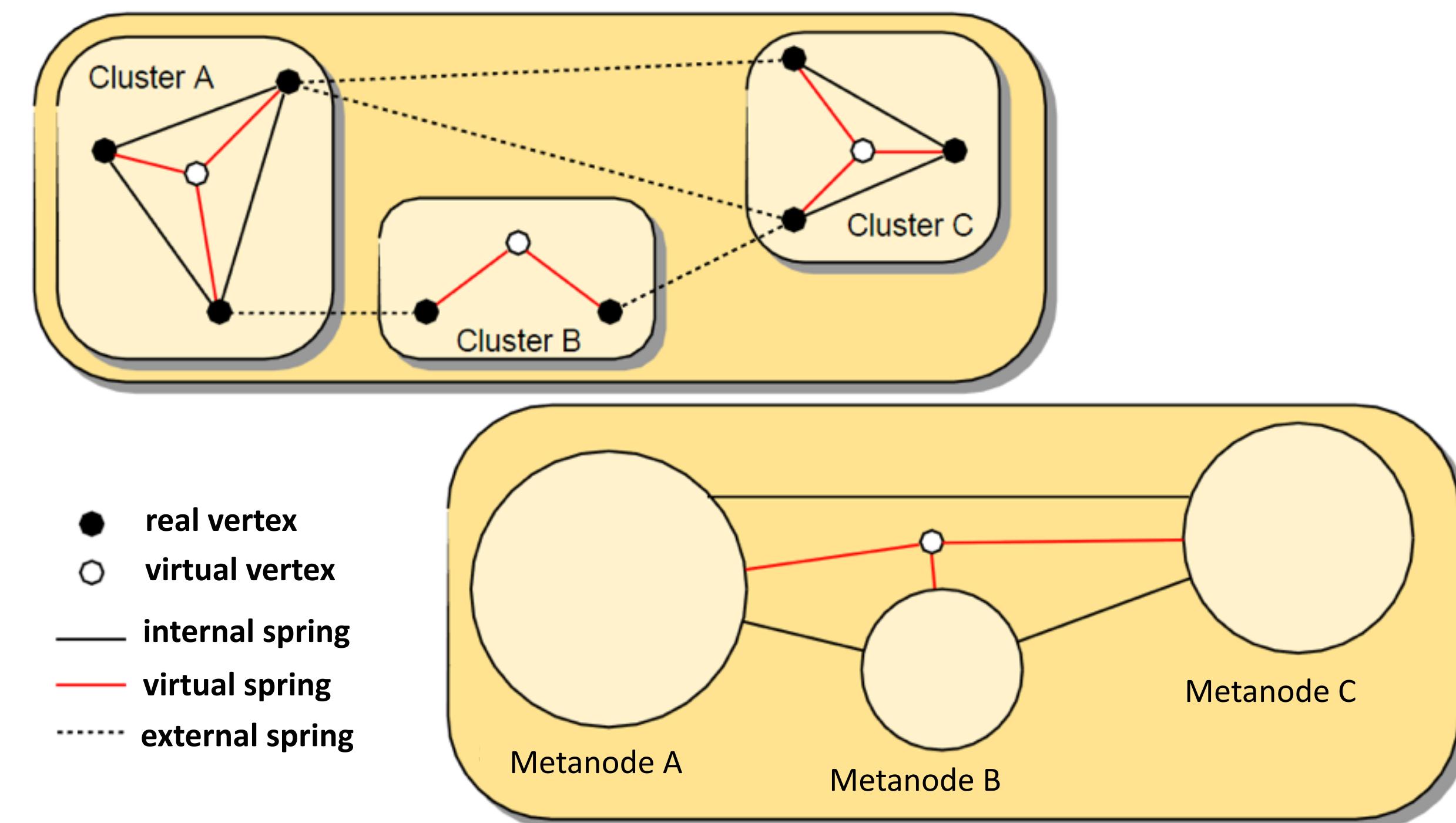
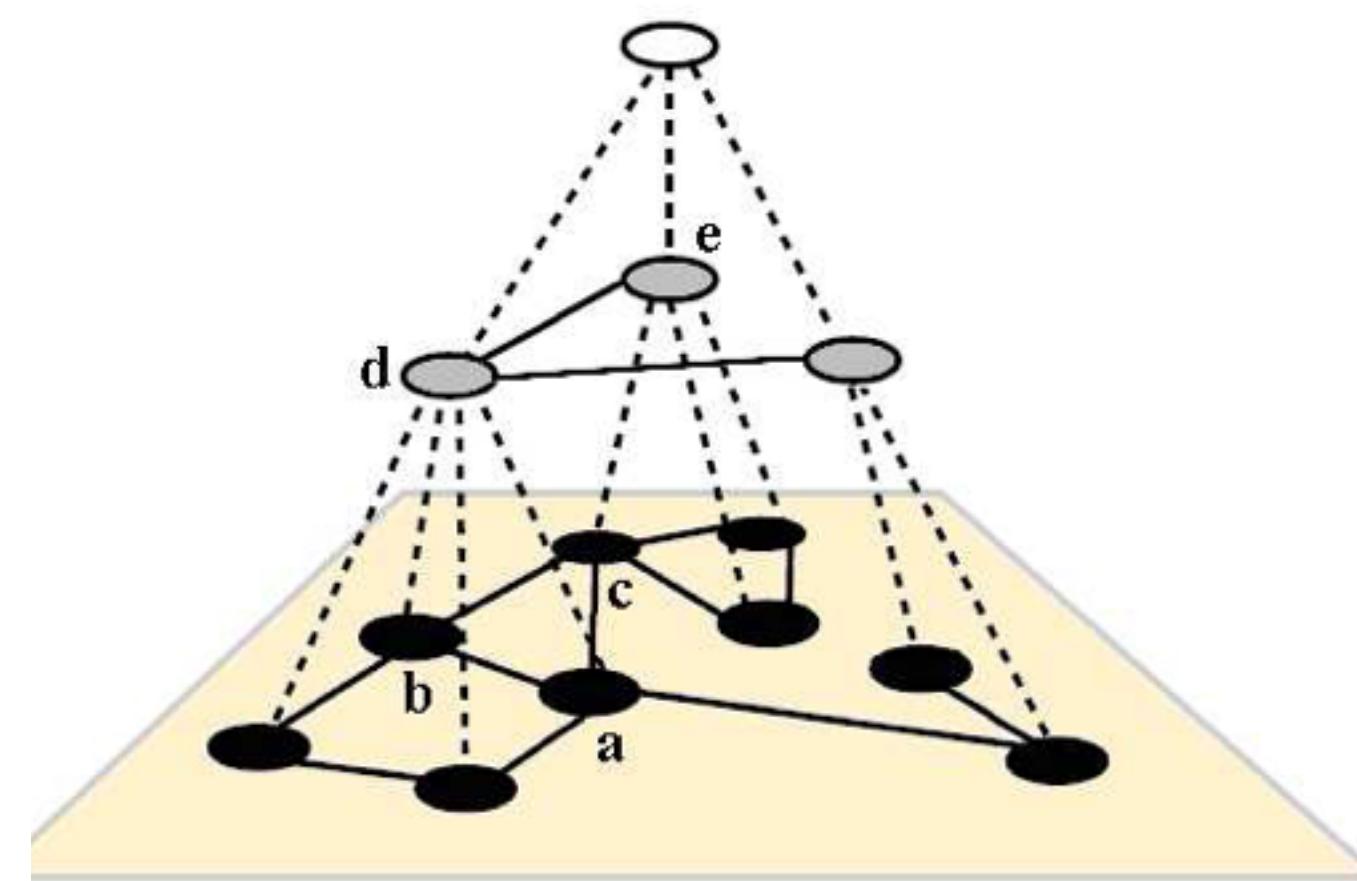
Limit (interactive): ~1000 nodes





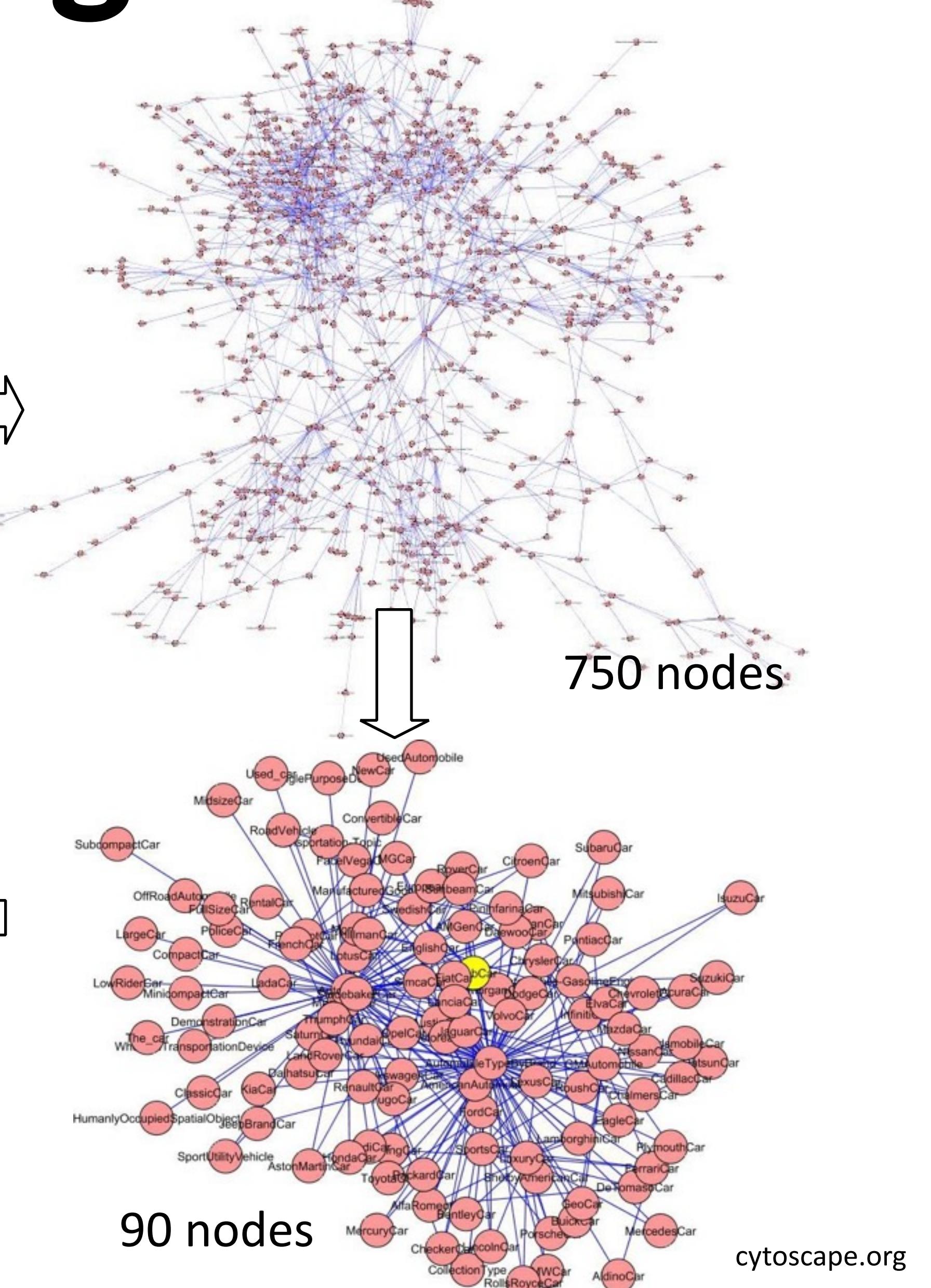
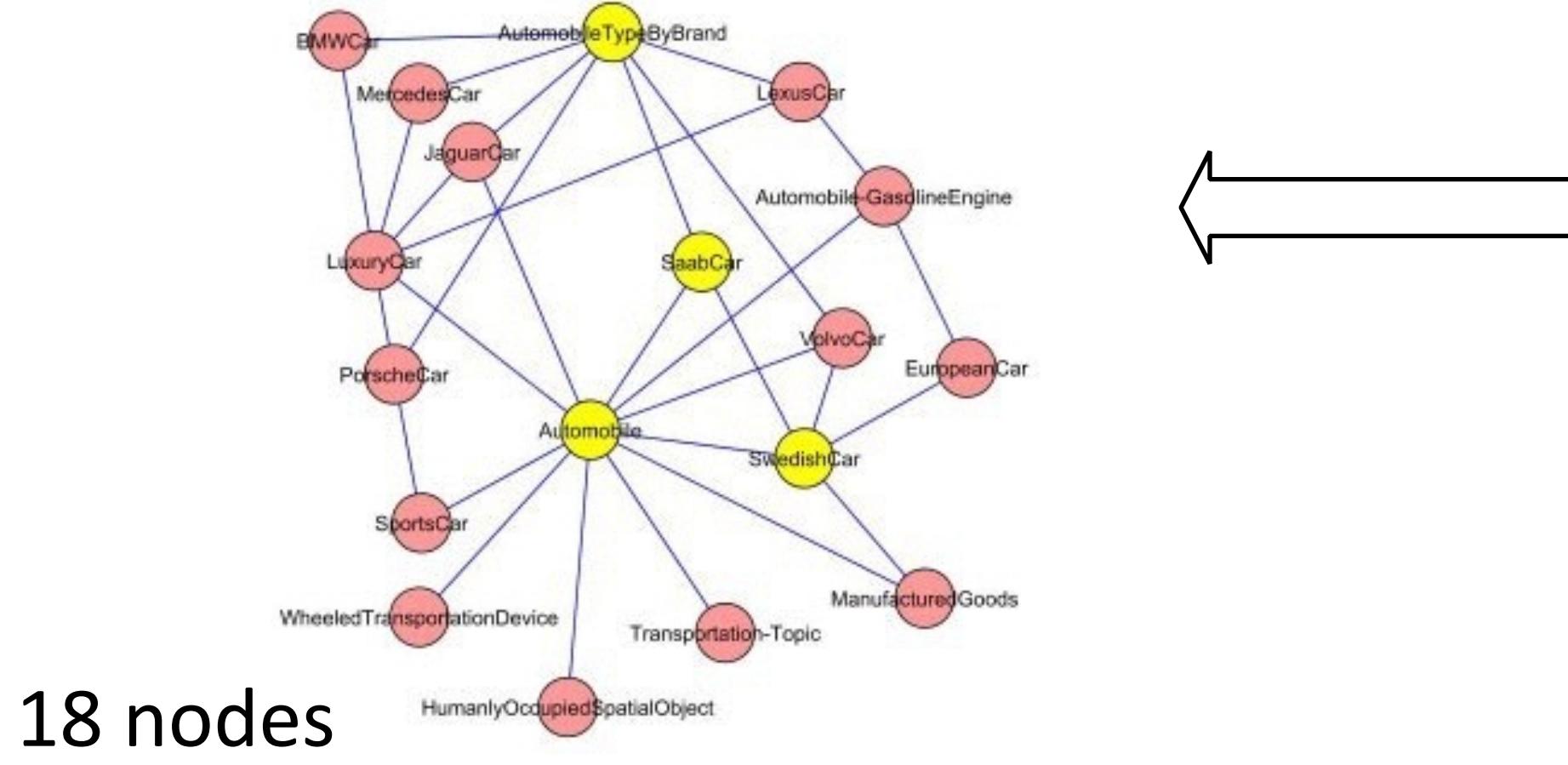
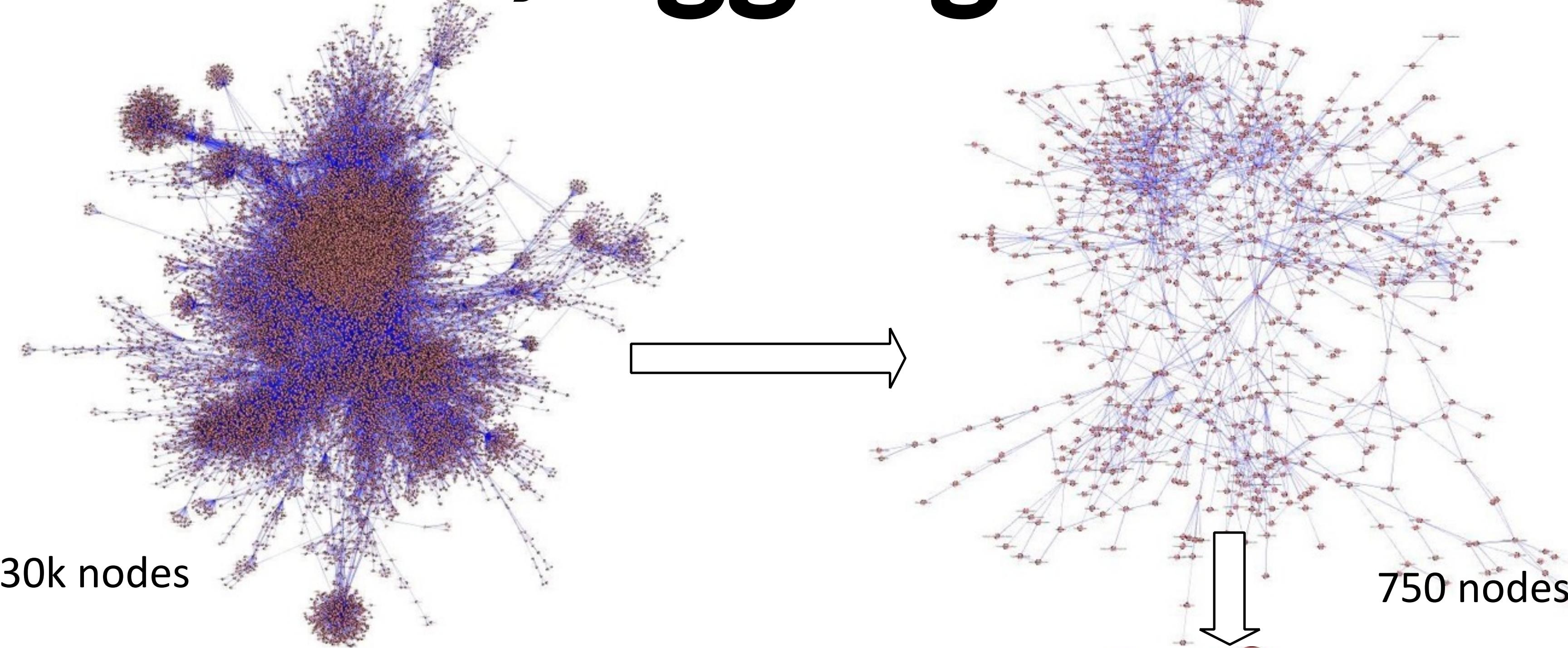
Giant Hairball

Address Computational Scalability: Multilevel Approaches



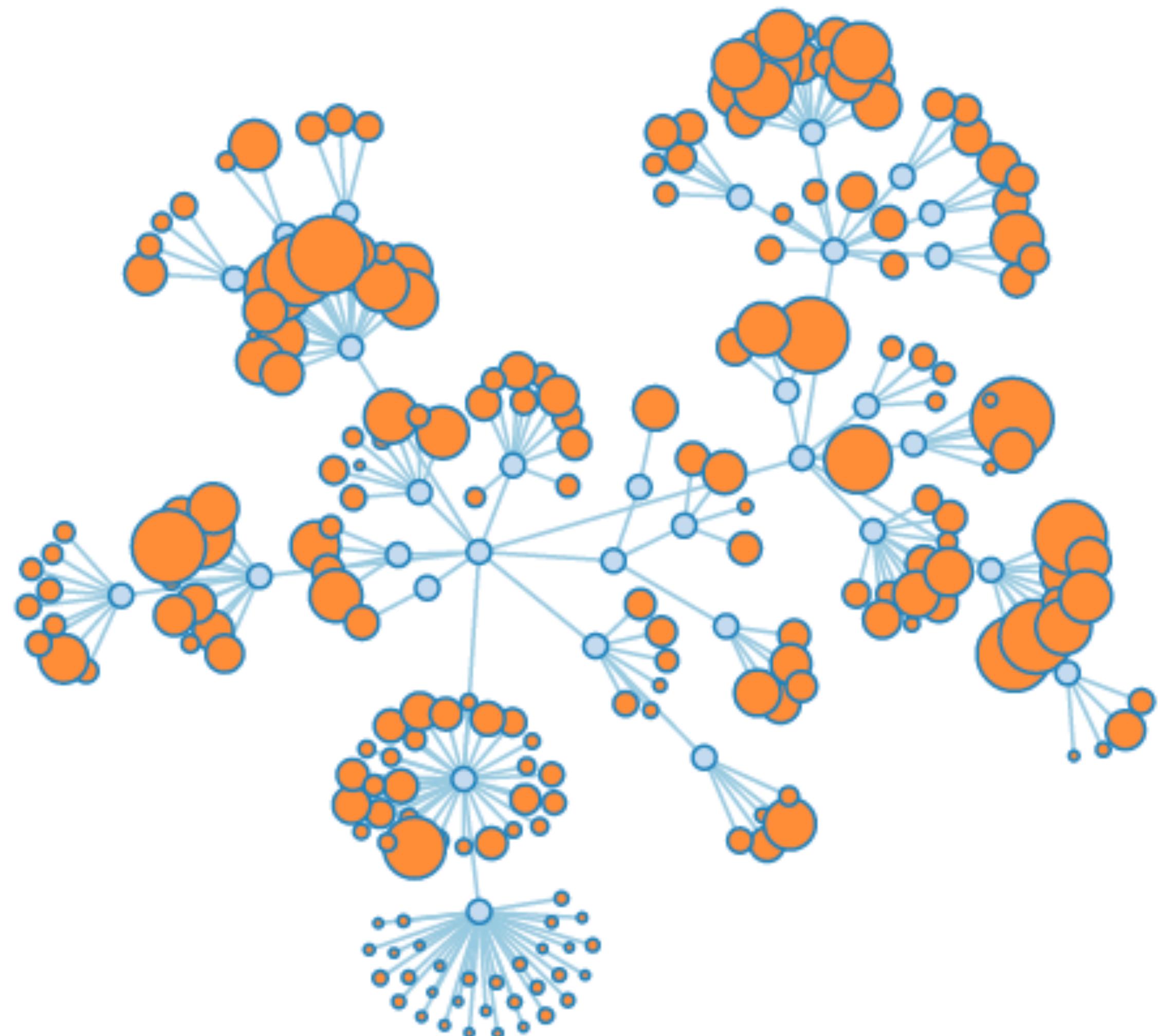
[Schulz 2004]

Abstraction/Aggregation



Collapsible Force Layout

Supernodes: aggregate of nodes
manual or algorithmic clustering

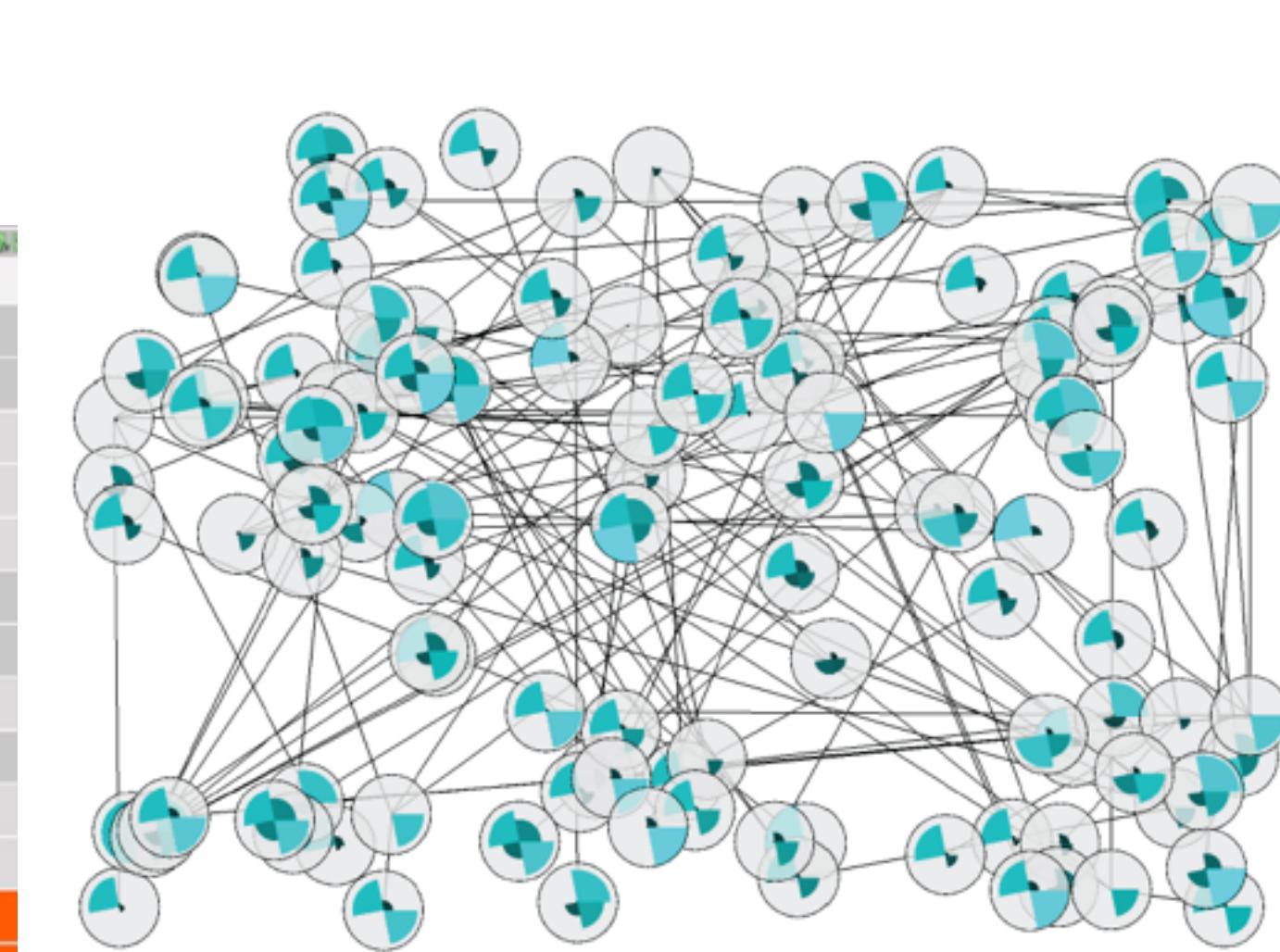
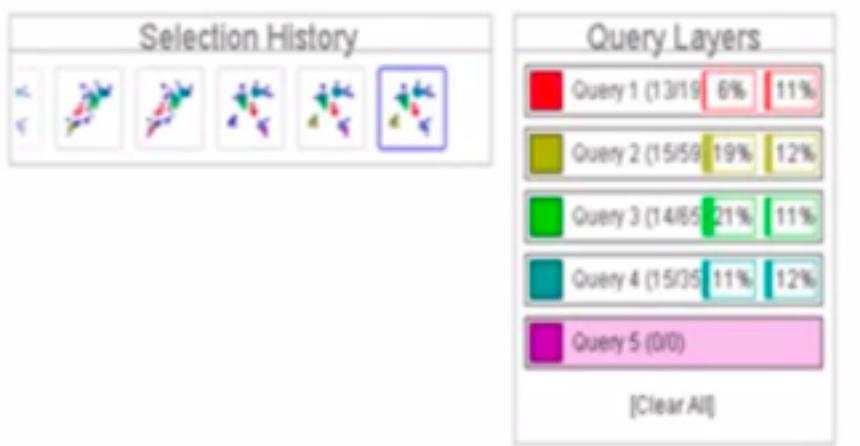
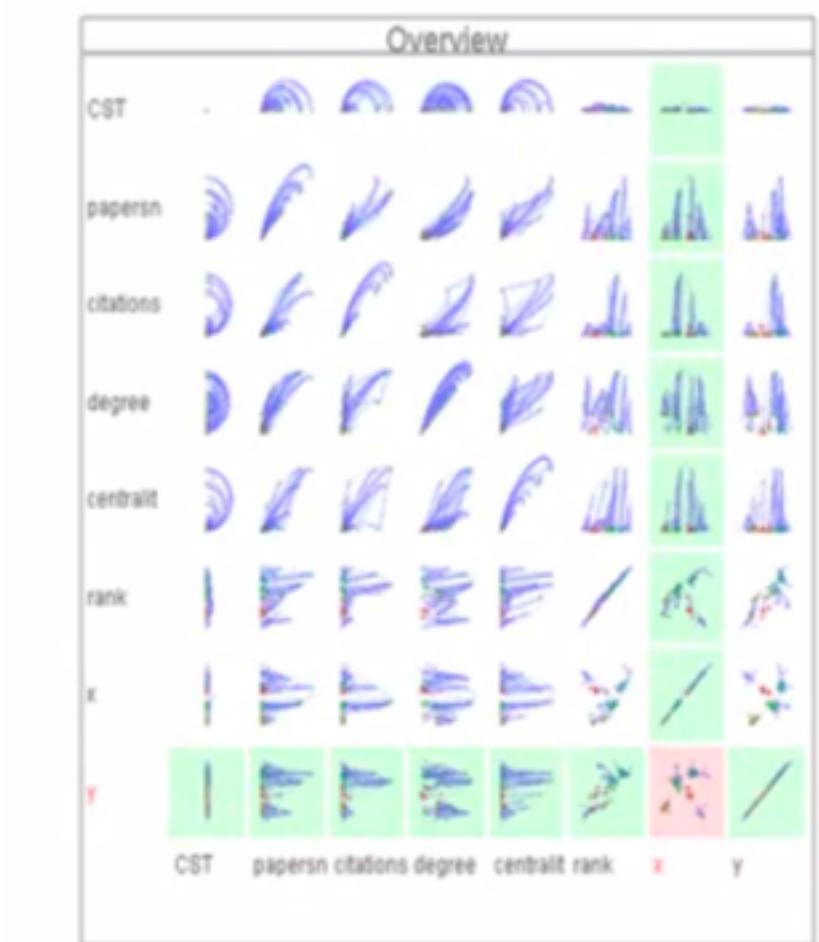
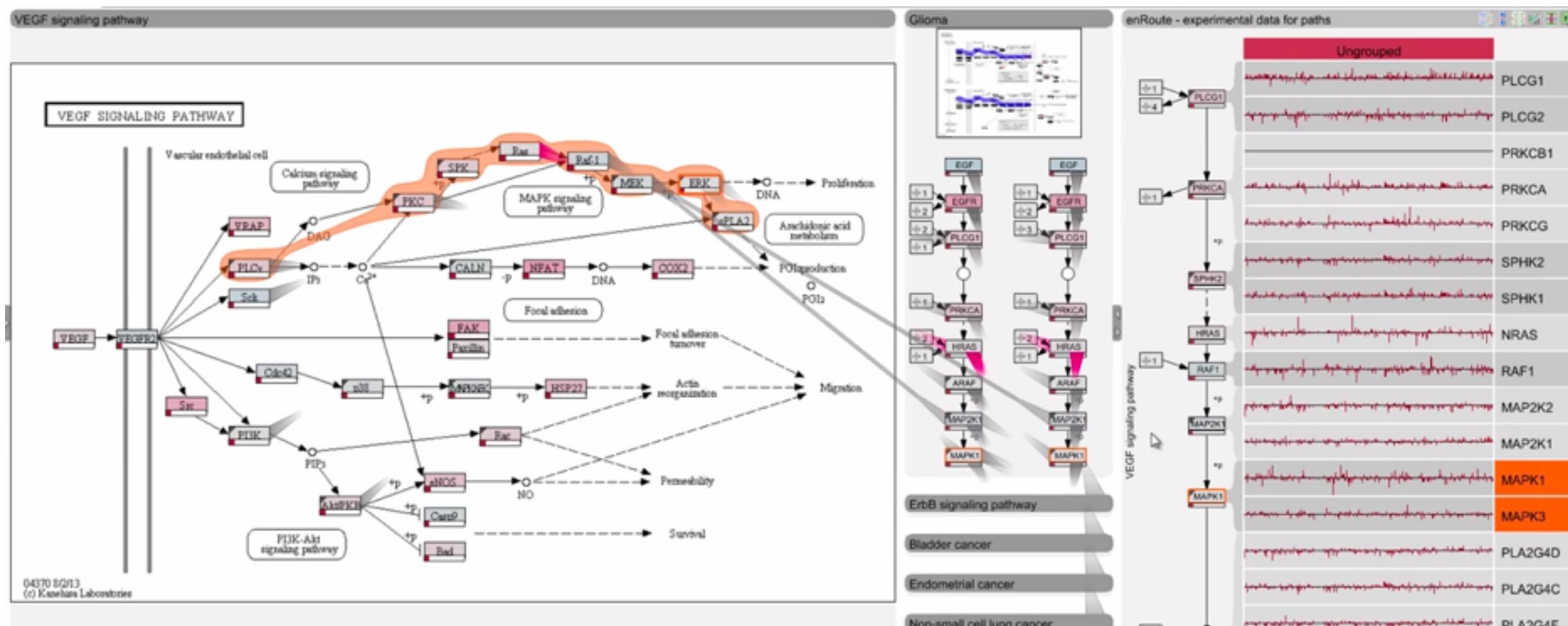


Node Attributes

Coloring

Position

Multiple Views / Path extraction

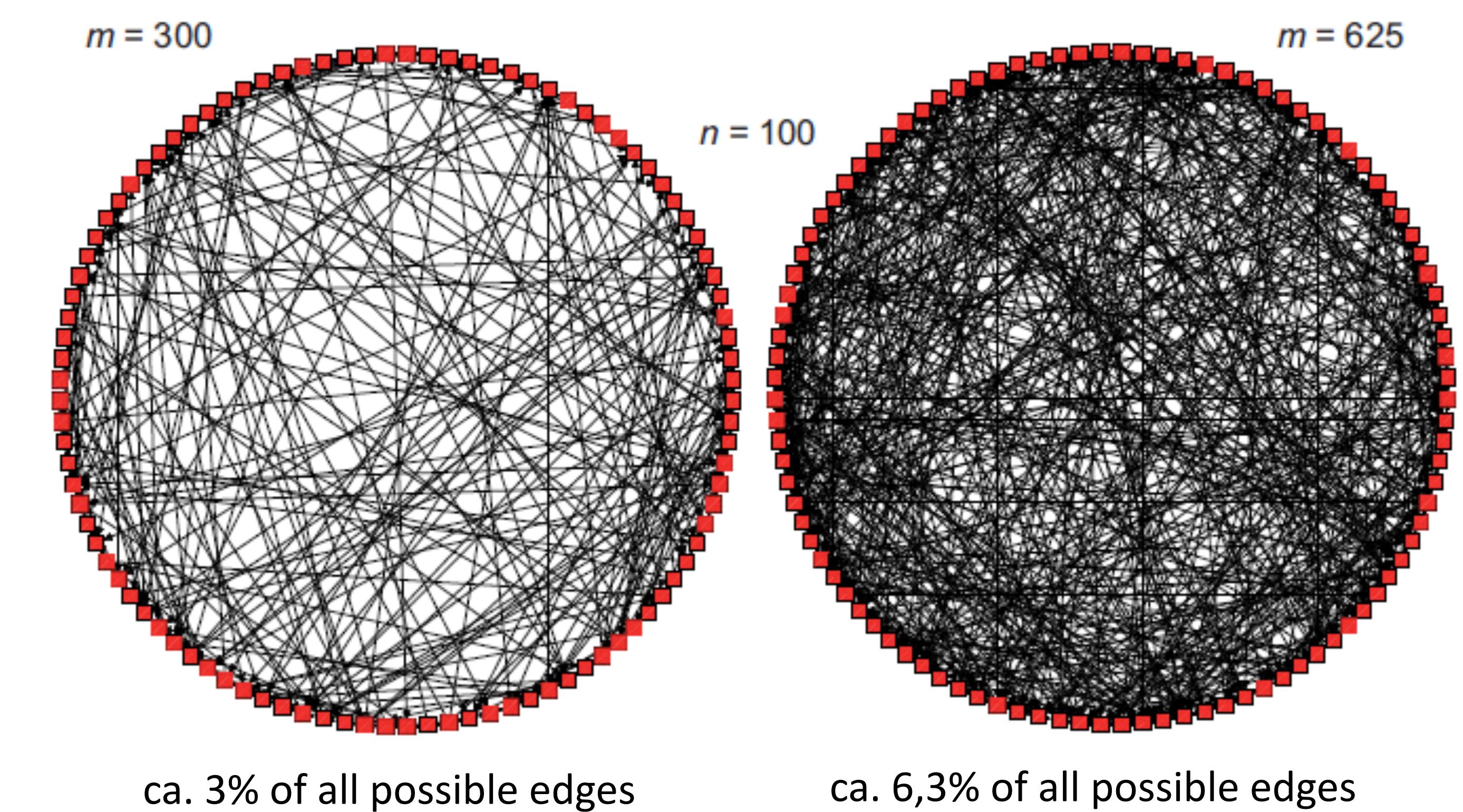


Styled / Restricted Layouts

Circular Layout

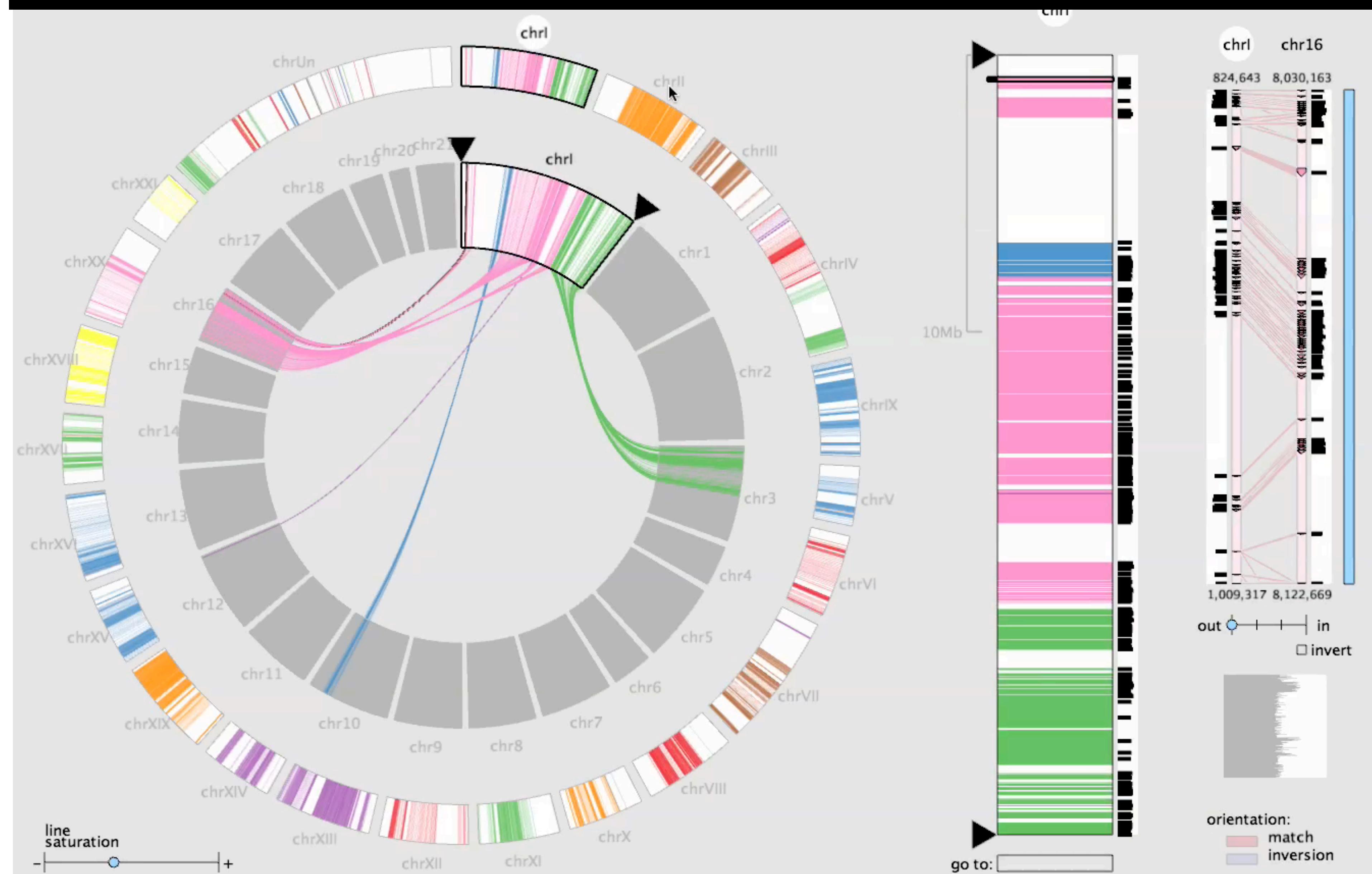
Node ordering

Edge Clutter

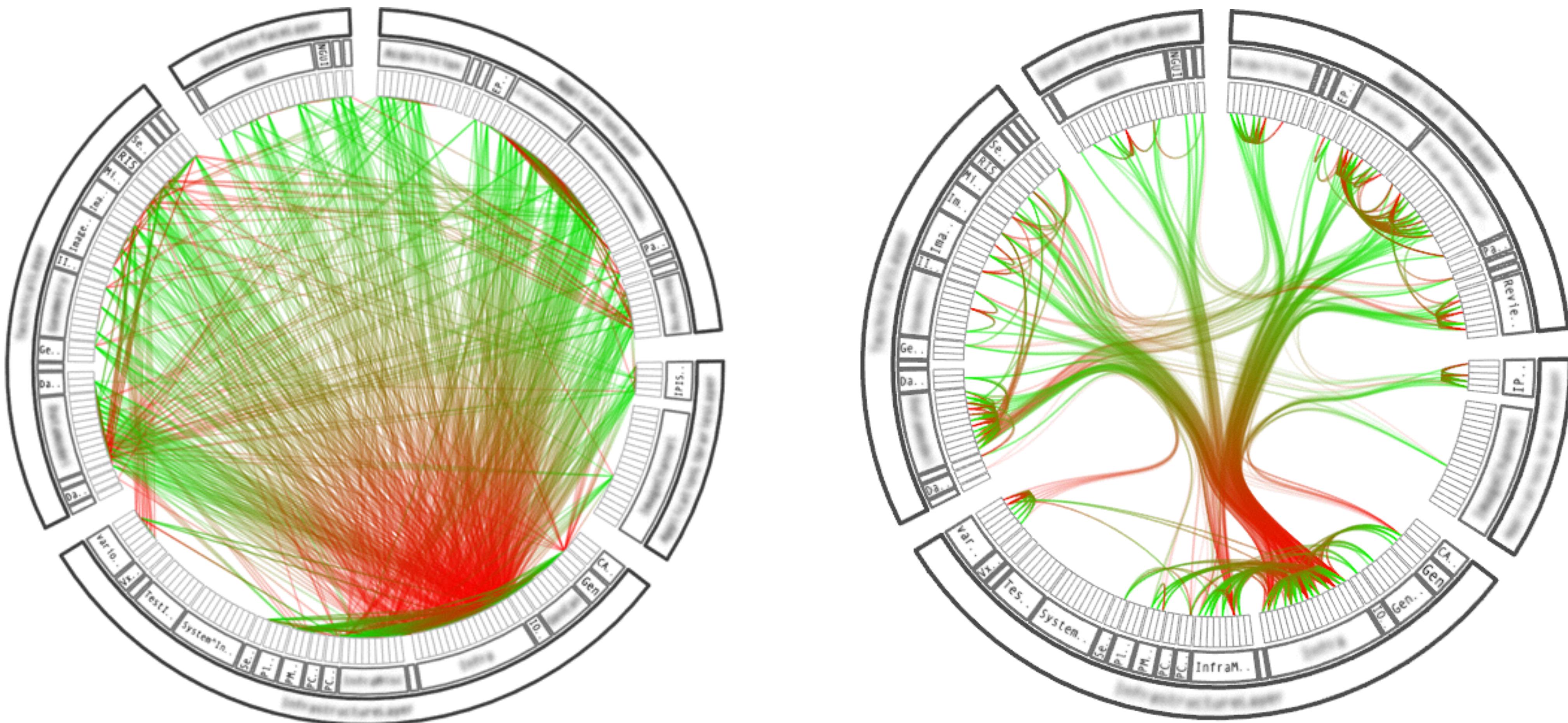


Example: MizBee

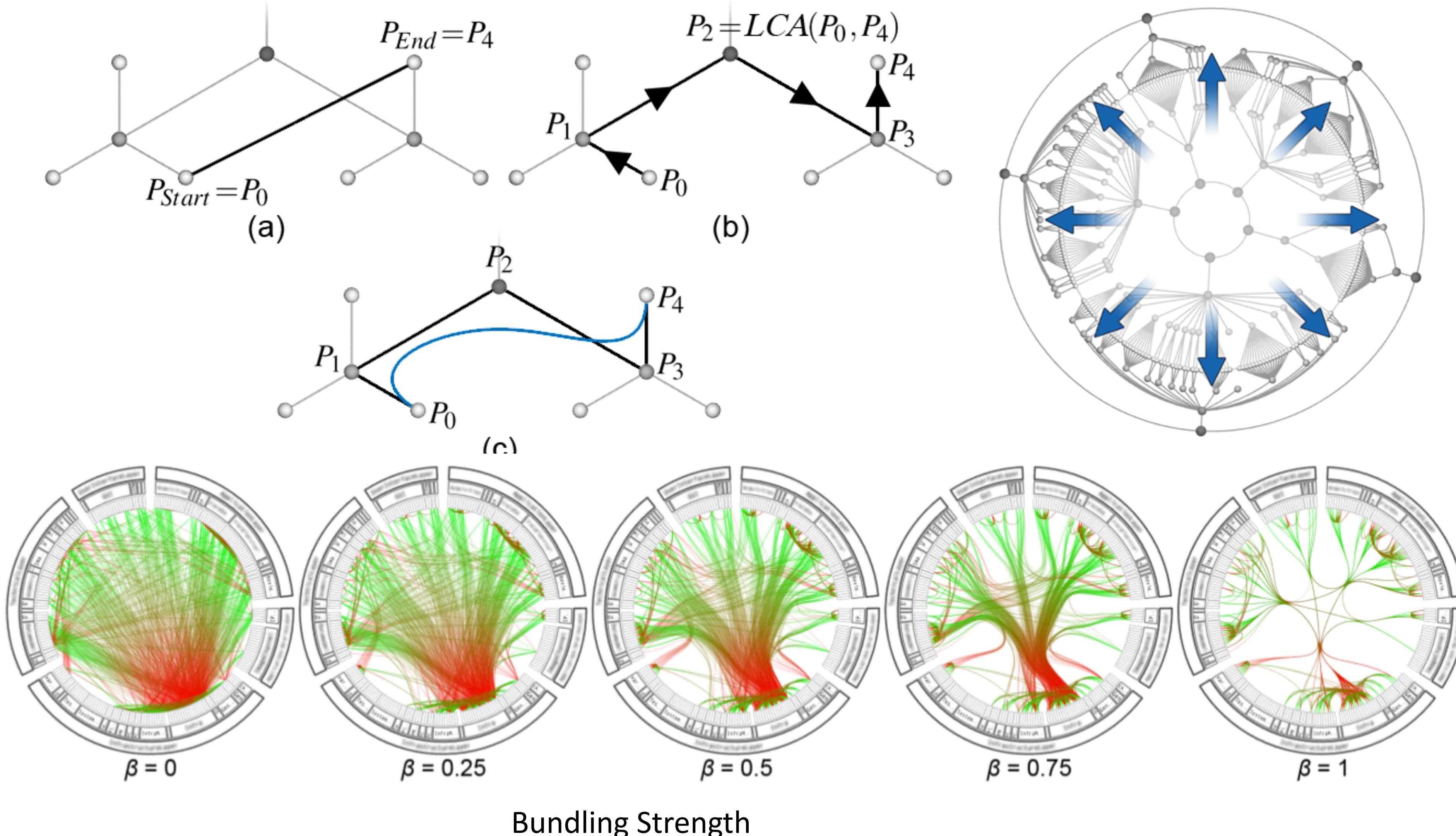
[Meyer et al. 2009]



Reduce Clutter: Edge Bundling



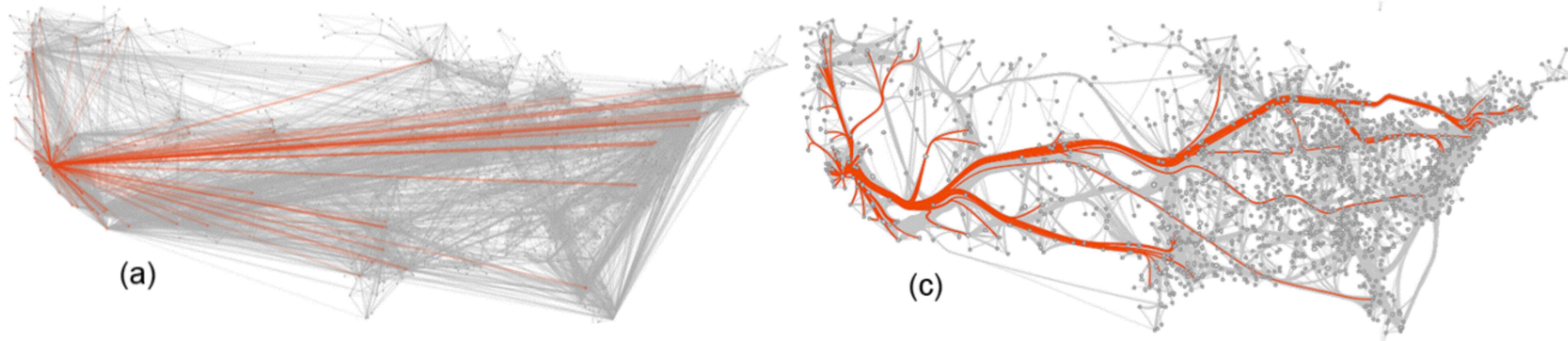
Hierarchical Edge Bundling



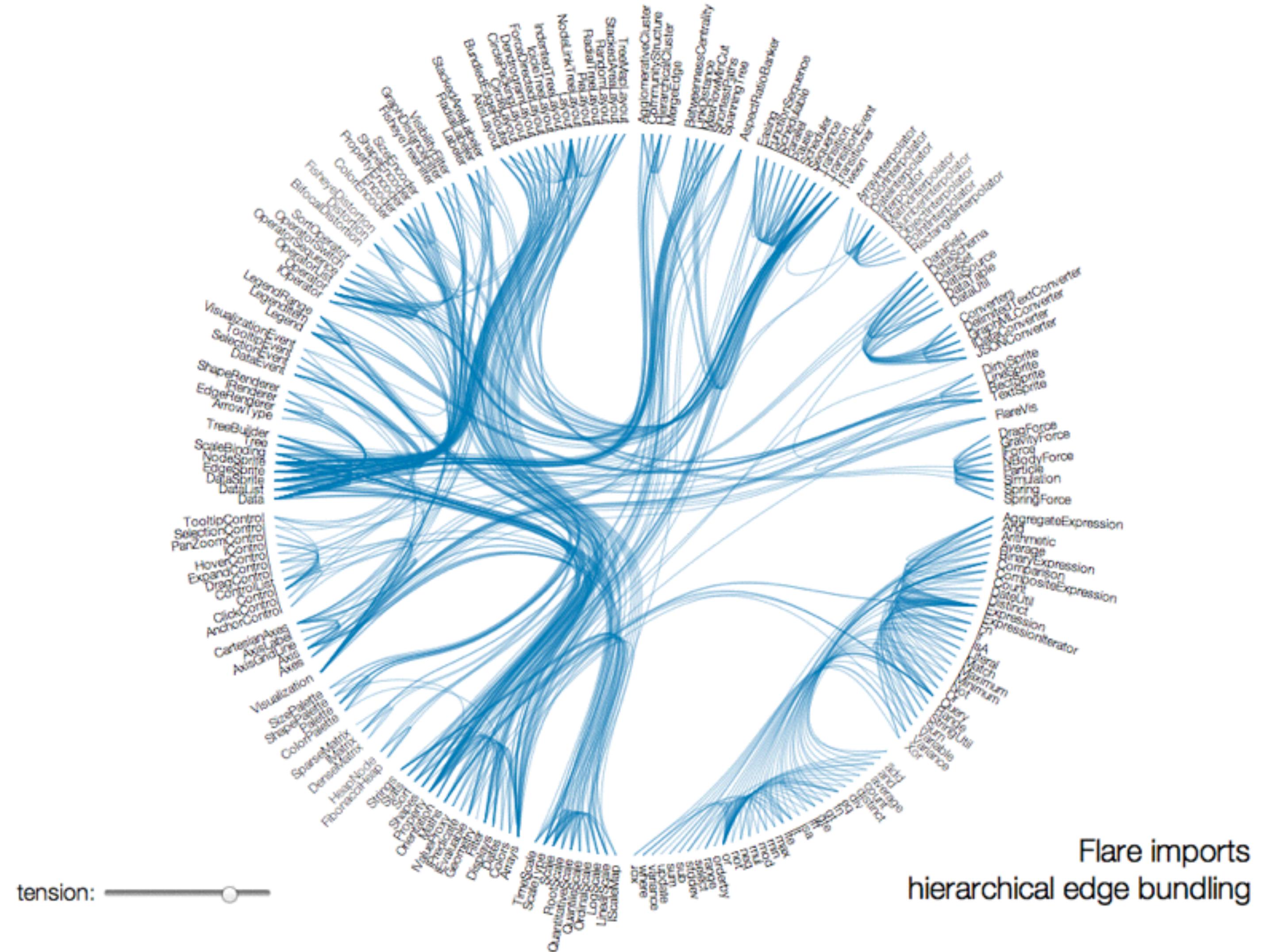
Fixed Layouts

Can't vary position of nodes

Edge routing important



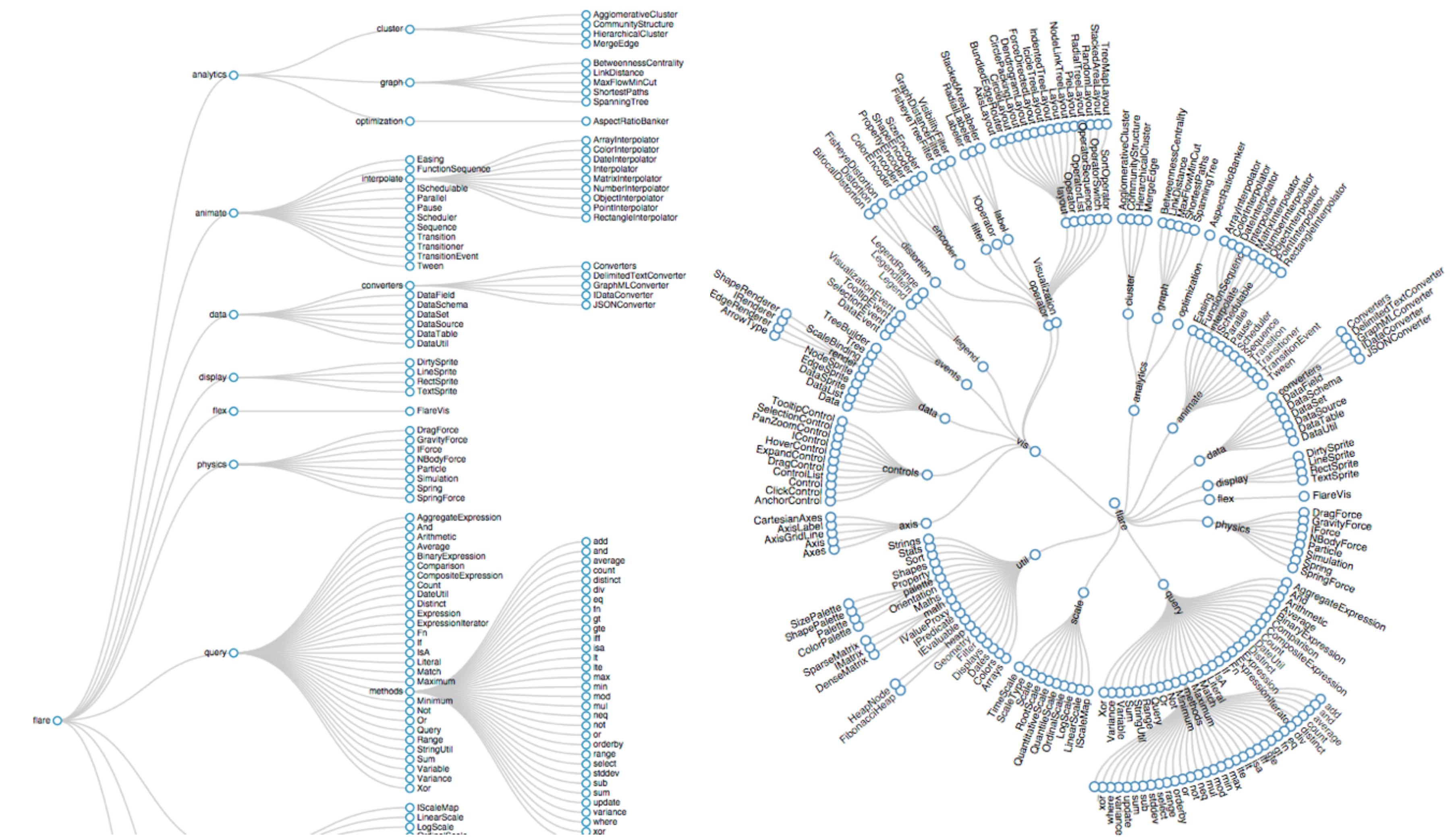
Bundling Strength



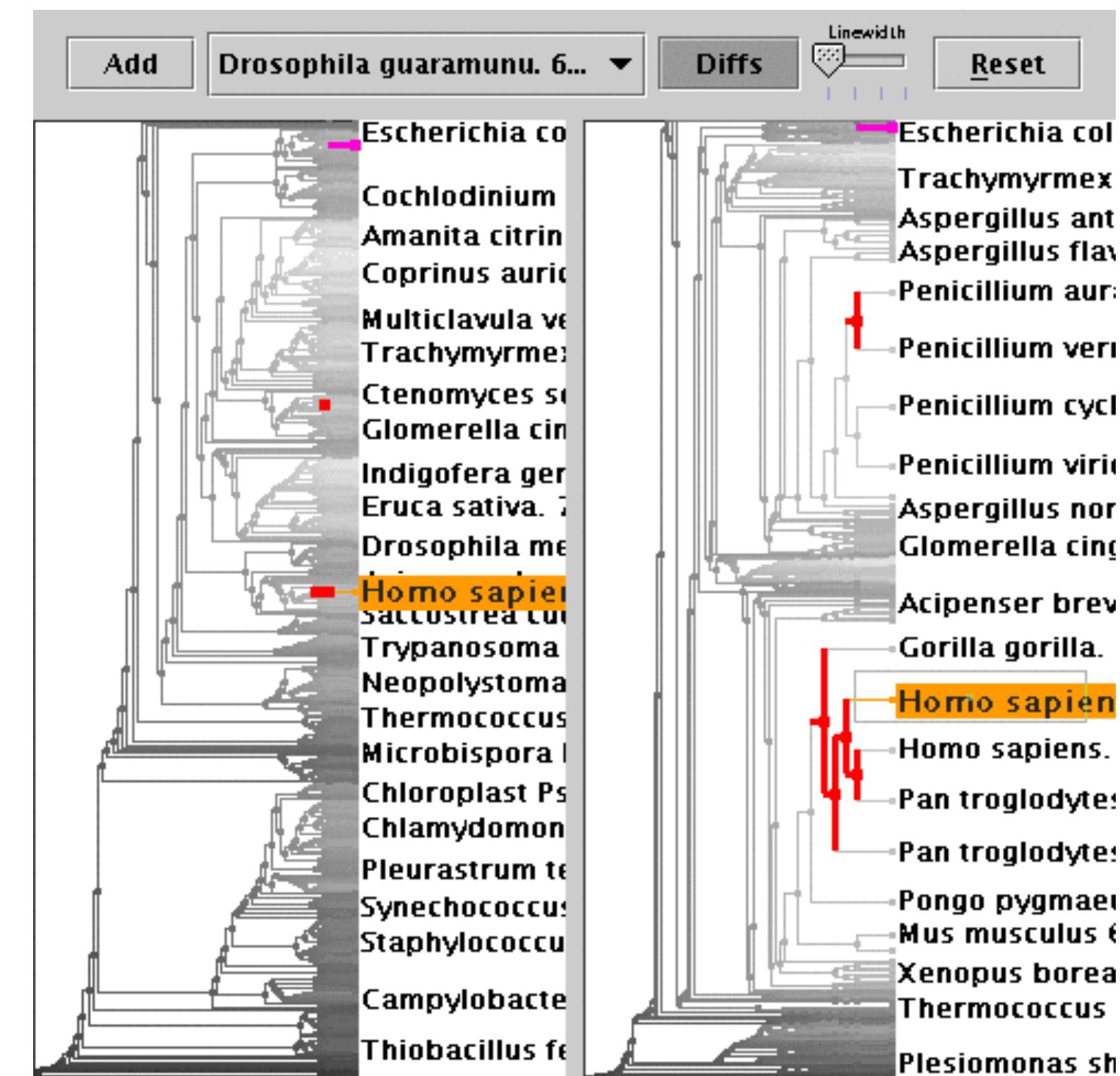
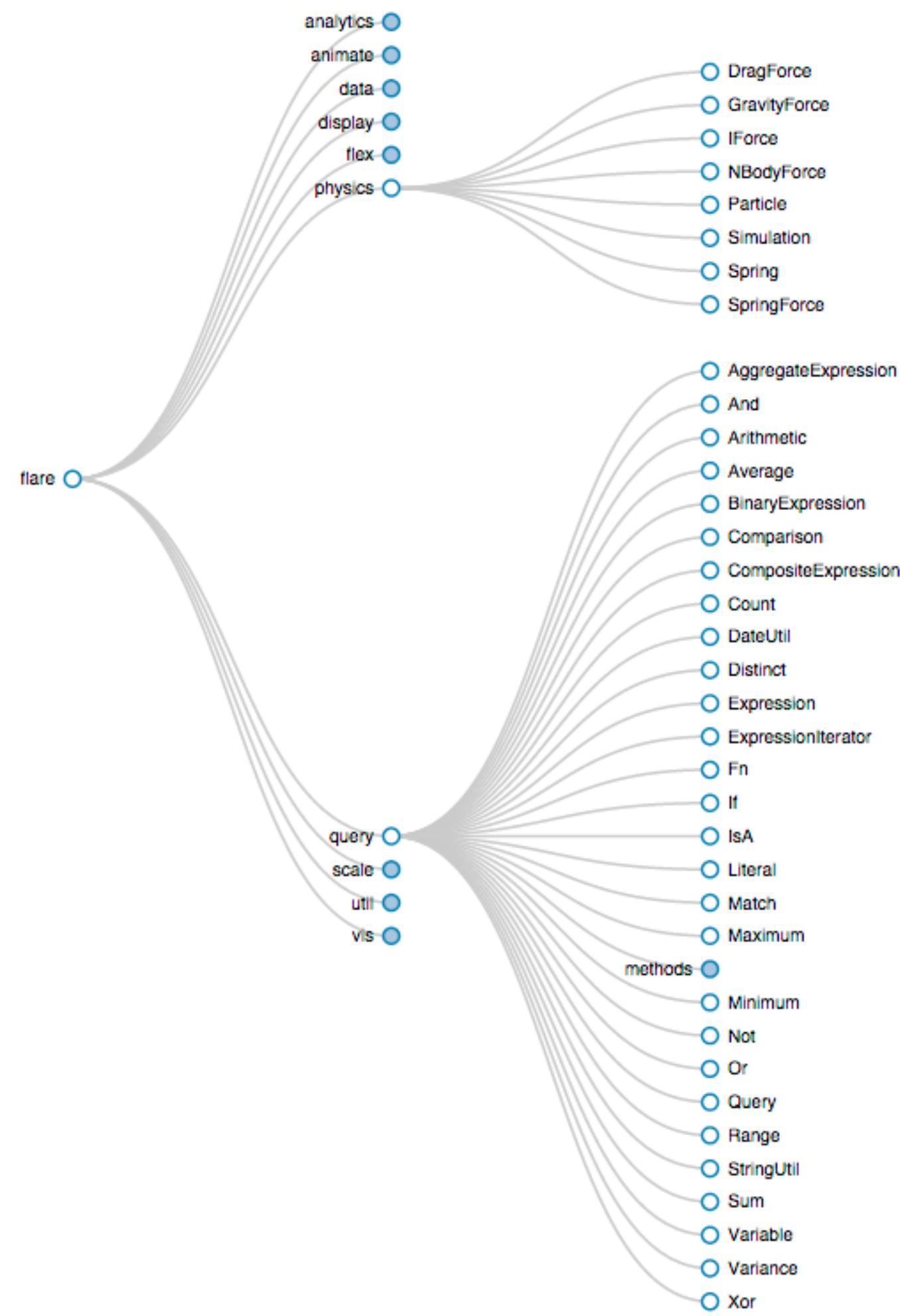
Explicit Tree Visualization

Reingold– Tilford layout

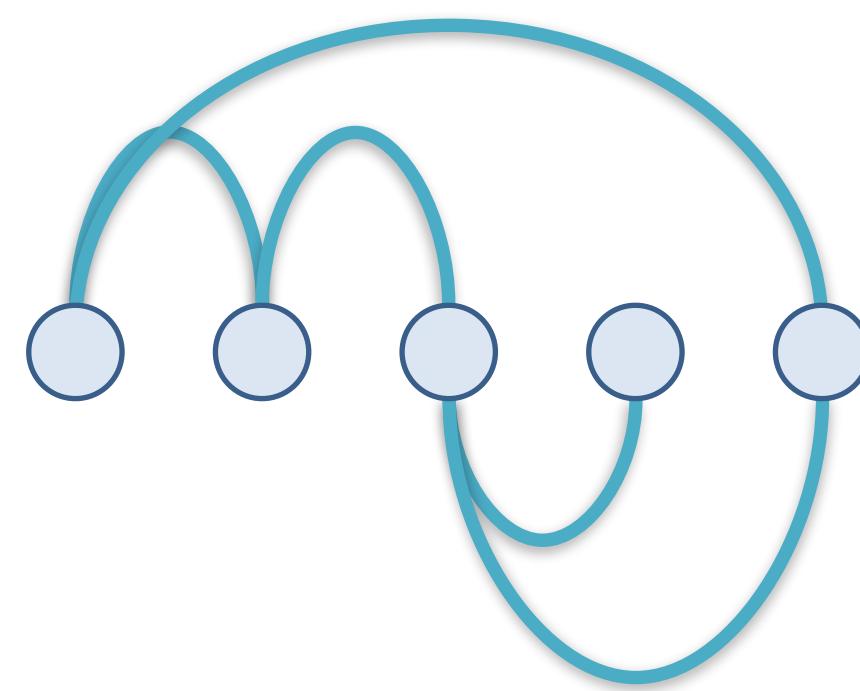
<http://billmill.org/pymag-trees/>



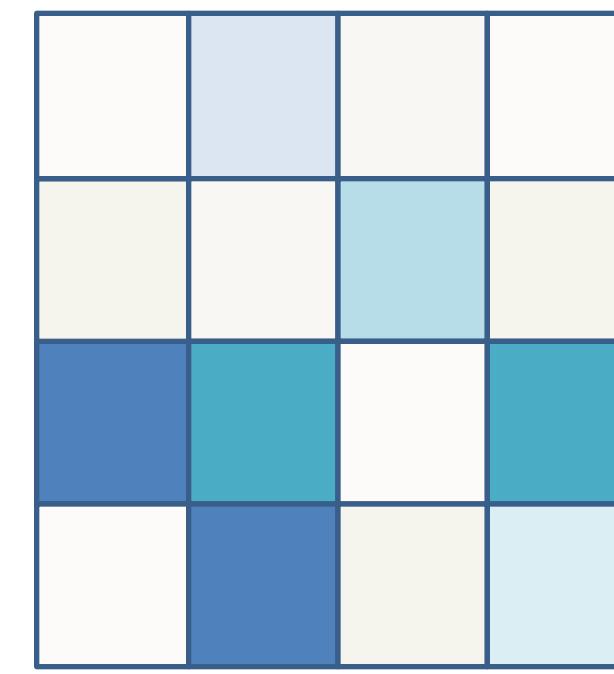
Tree Interaction, Tree Comparison



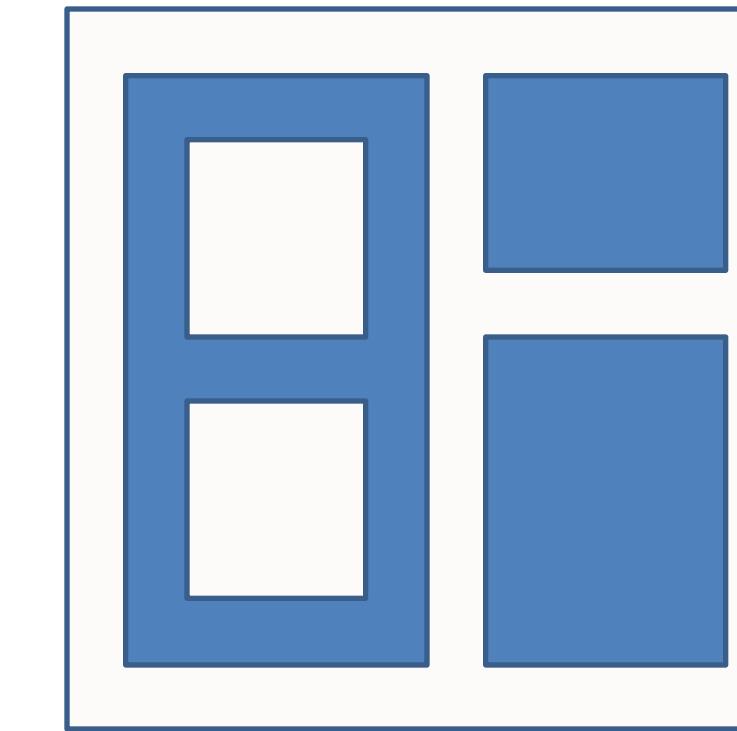
Matrix Representations



Explicit
(Node-Link)



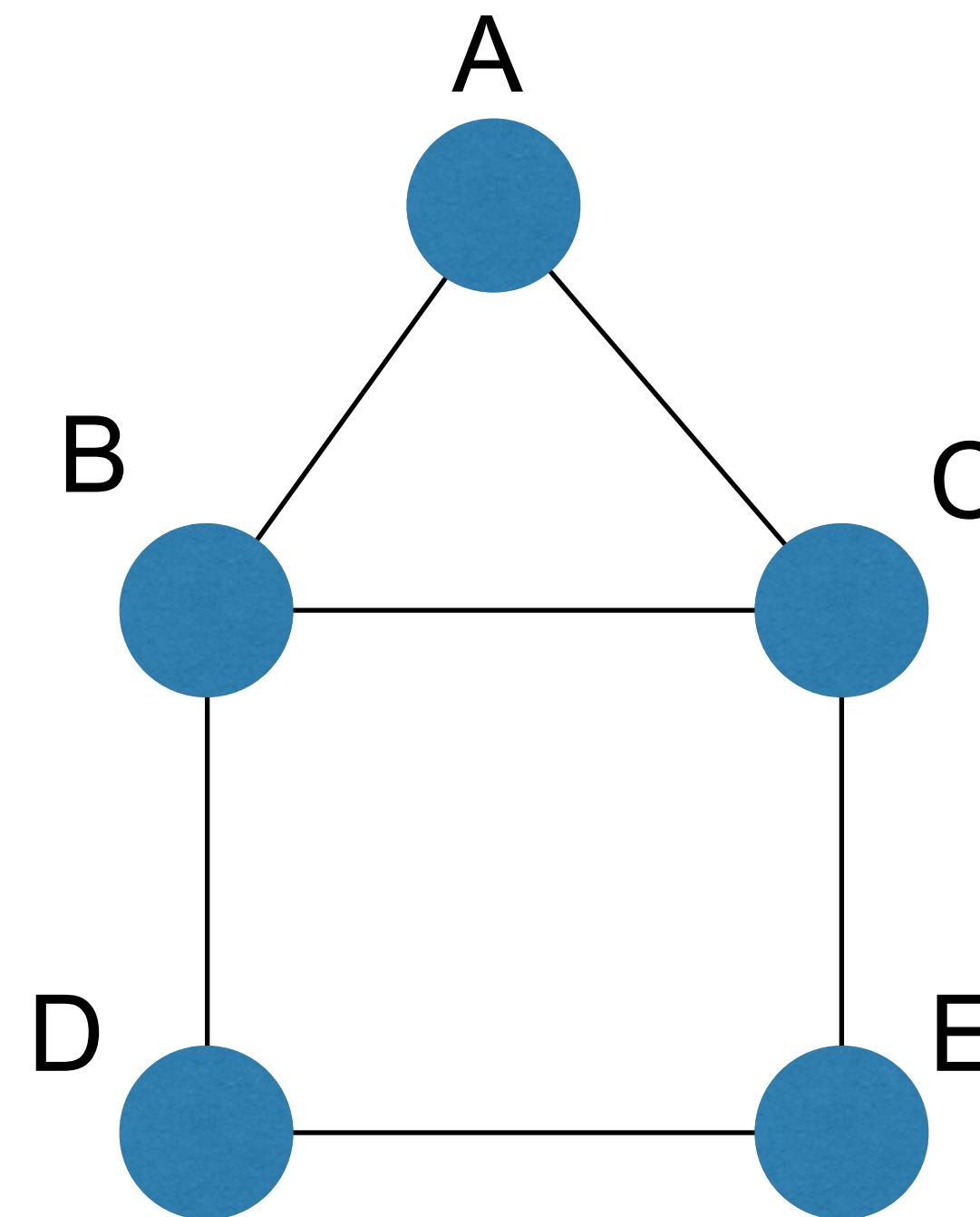
Matrix



Implicit

Matrix Representations

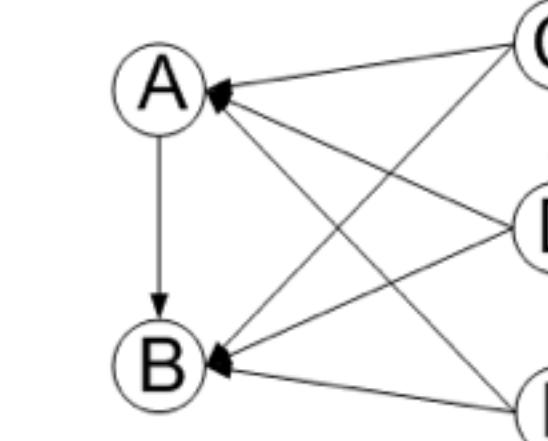
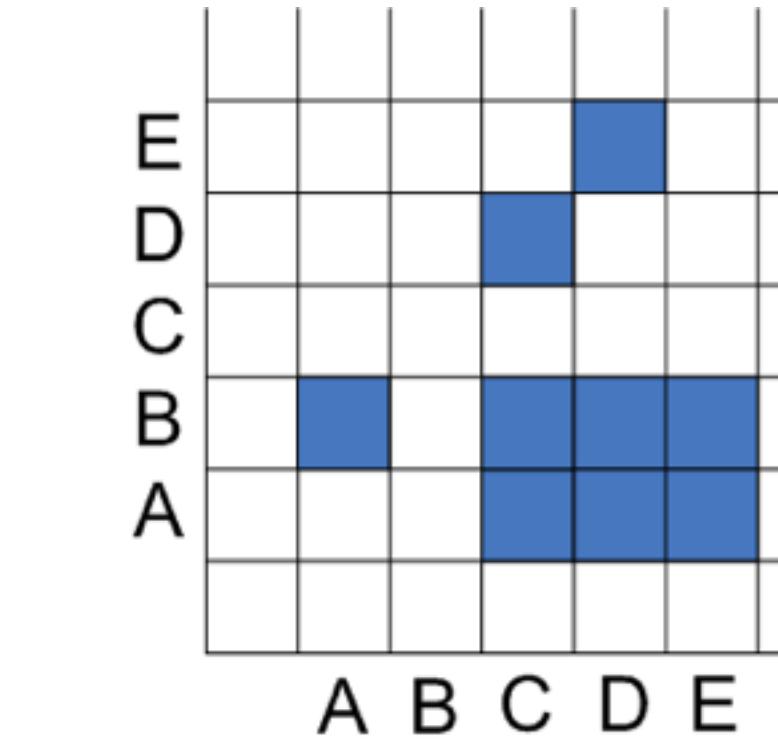
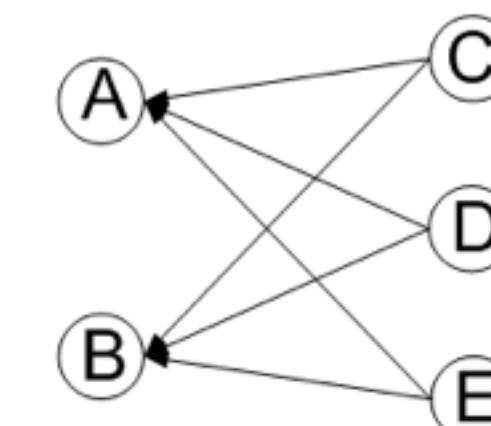
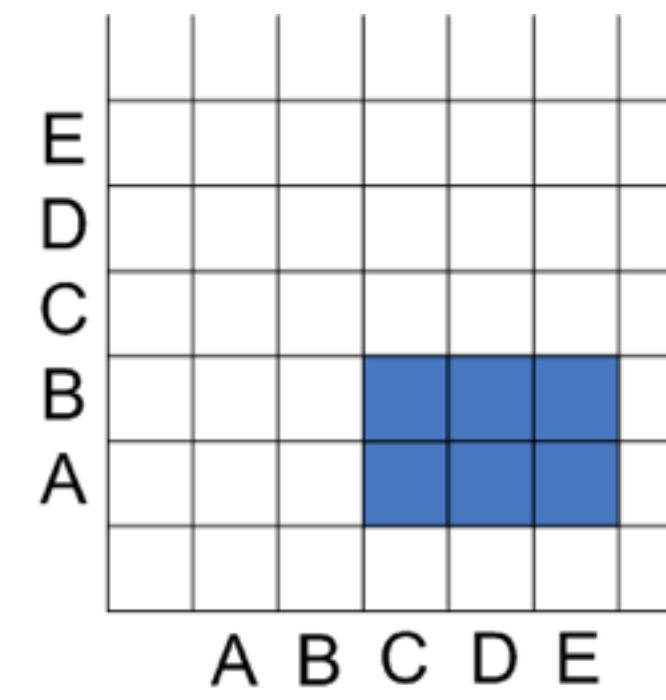
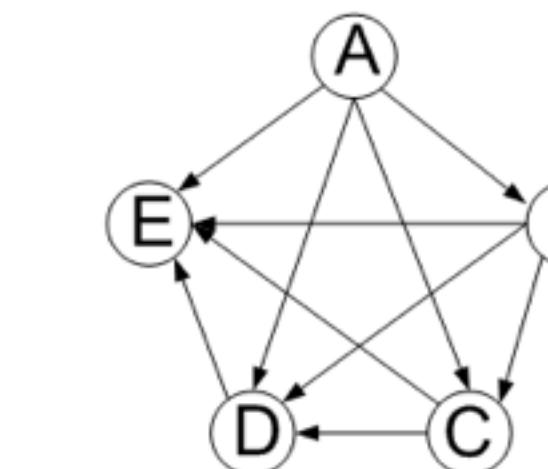
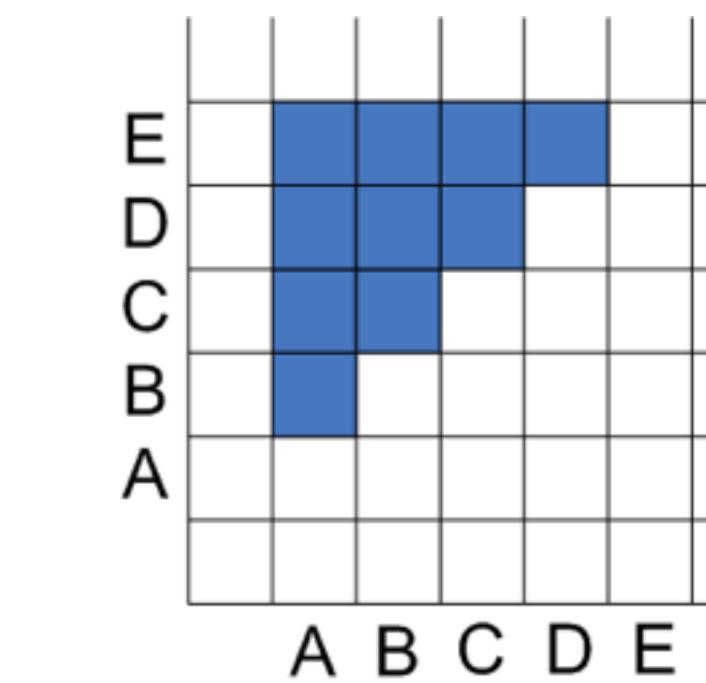
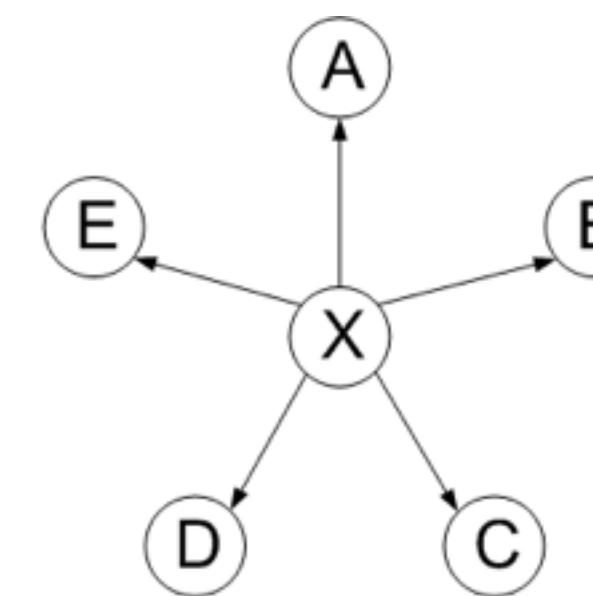
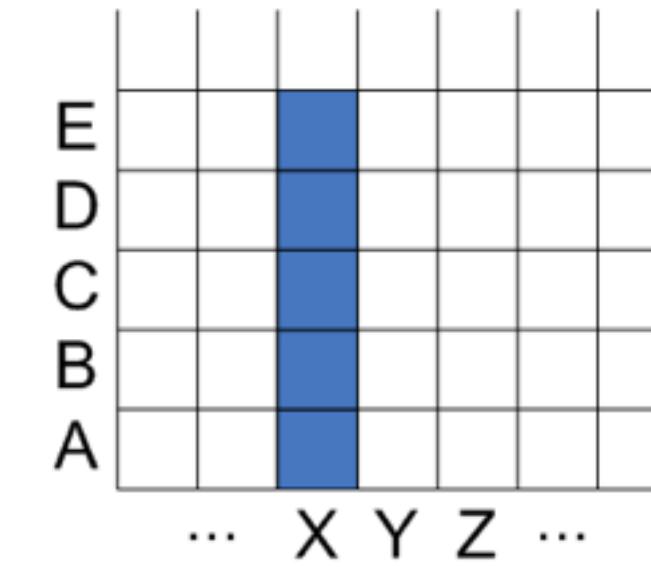
Instead of node link diagram, use adjacency matrix



A	B	C	D	E
A				
B				
C				
D				
E				

Matrix Representations

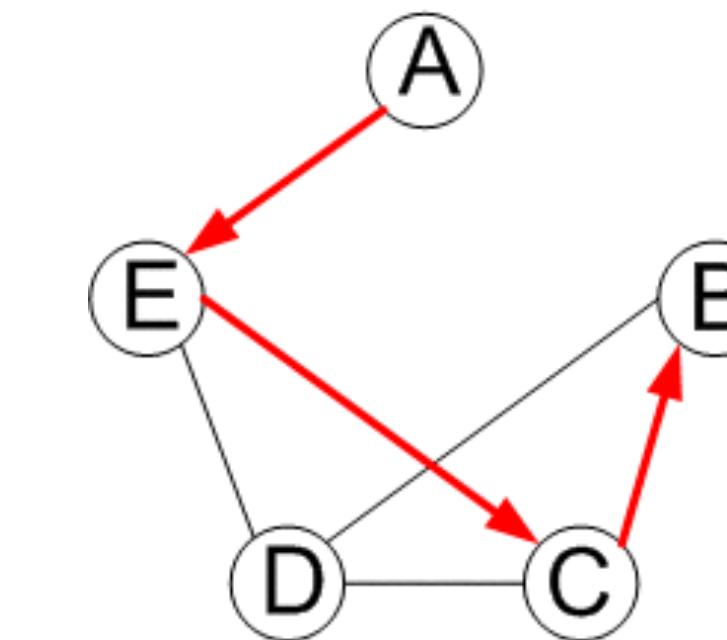
Examples:



Matrix Representations

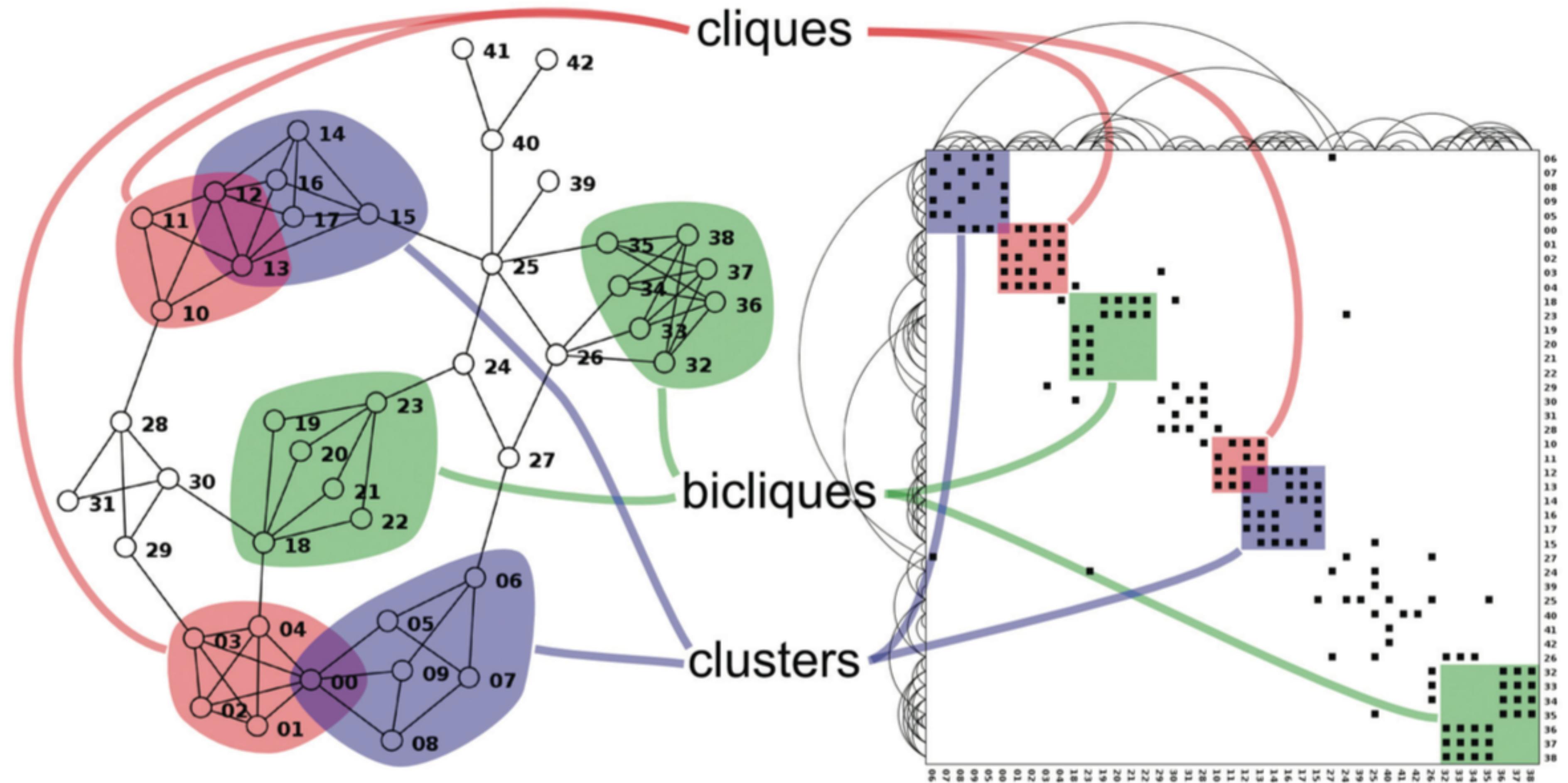
	A	B	C	D	E	F	G	H
A								
B								
C								
D								
R O M								
E								
F								
G								
H								

Well suited for
neighborhood-related TBTs

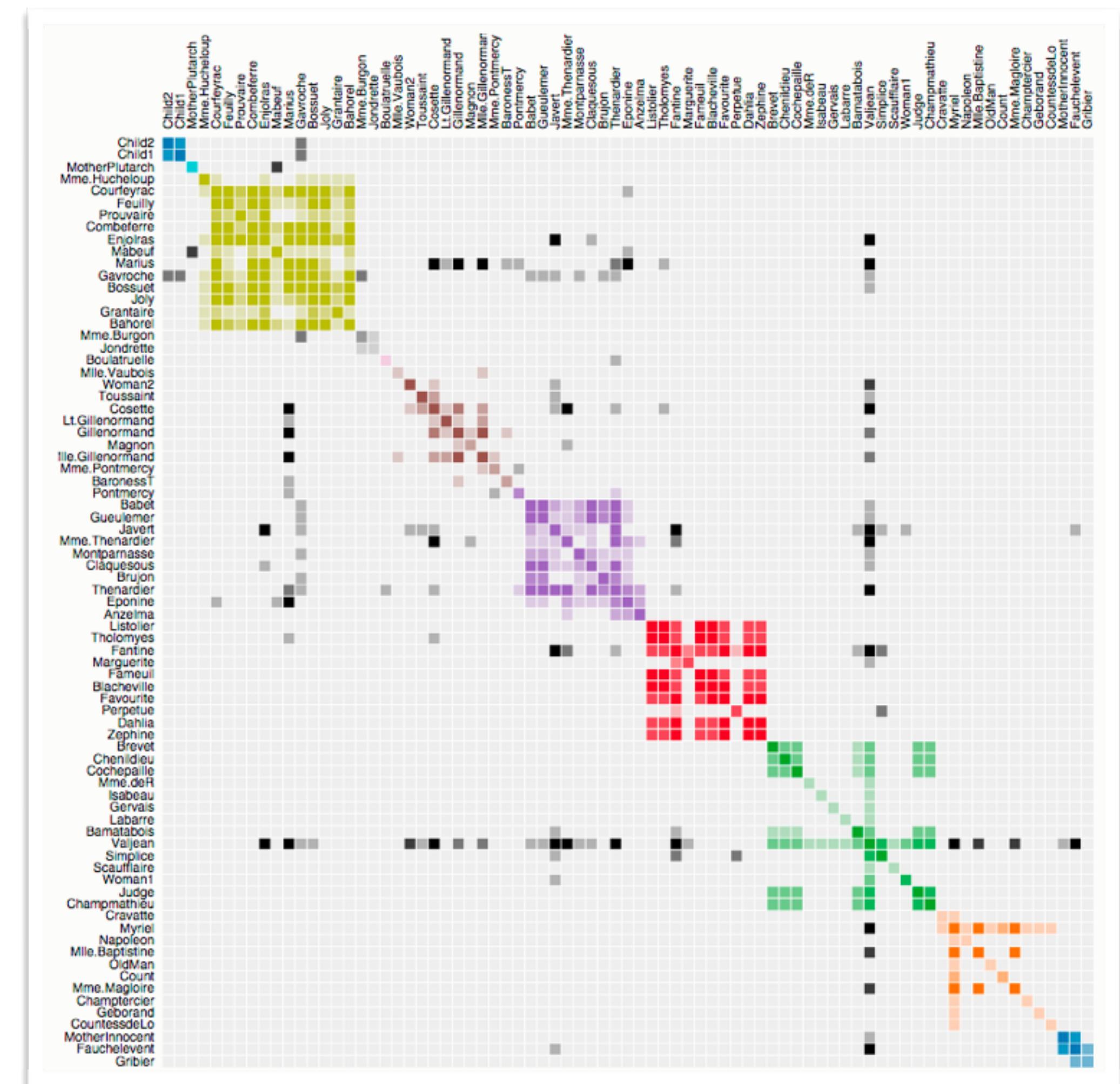
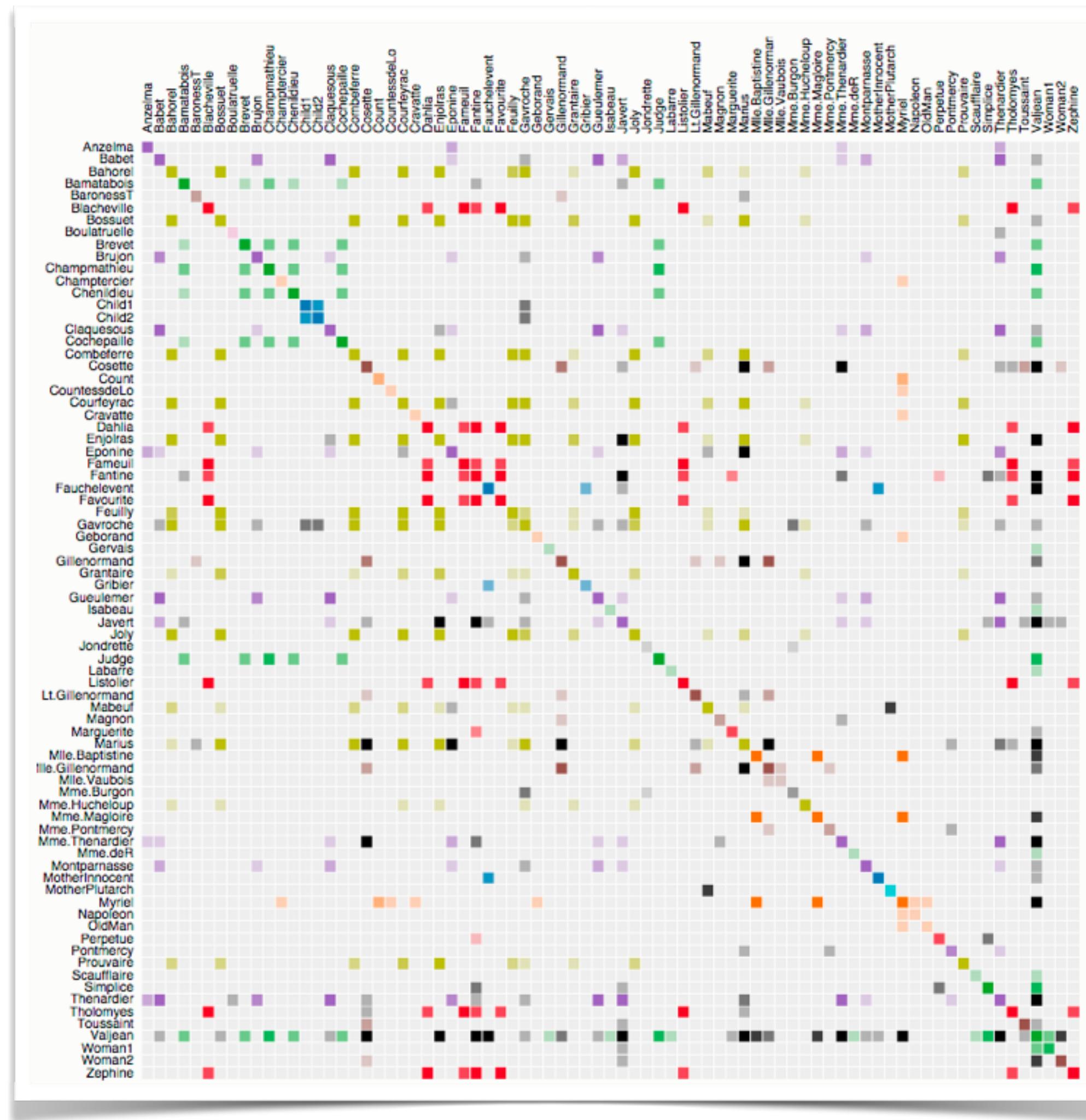


	A	B	C	D	E
E			red		
D				blue	
C					red
B			red	blue	
A					blue

Not suited for
path-related TBTs



Order Critical!



Matrix Representations

Pros:

can represent **all graph classes** except for hypergraphs

puts **focus on the edge set**, not so much on the node set

simple grid -> **no elaborate layout** or rendering needed

well suited for **ABT on edges** via coloring of the matrix cells

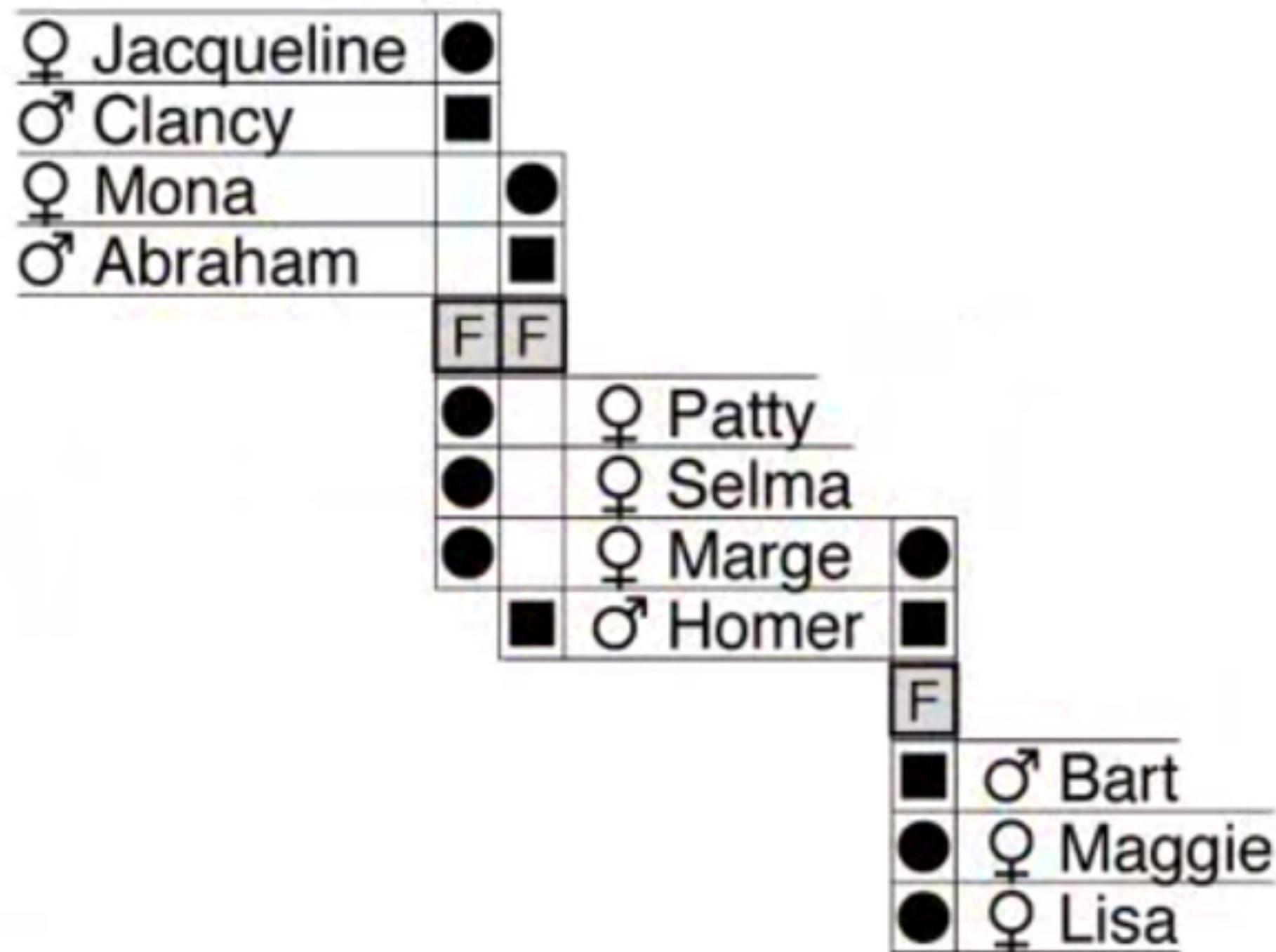
well suited for **neighborhood-related TBTs** via traversing rows/columns

Cons:

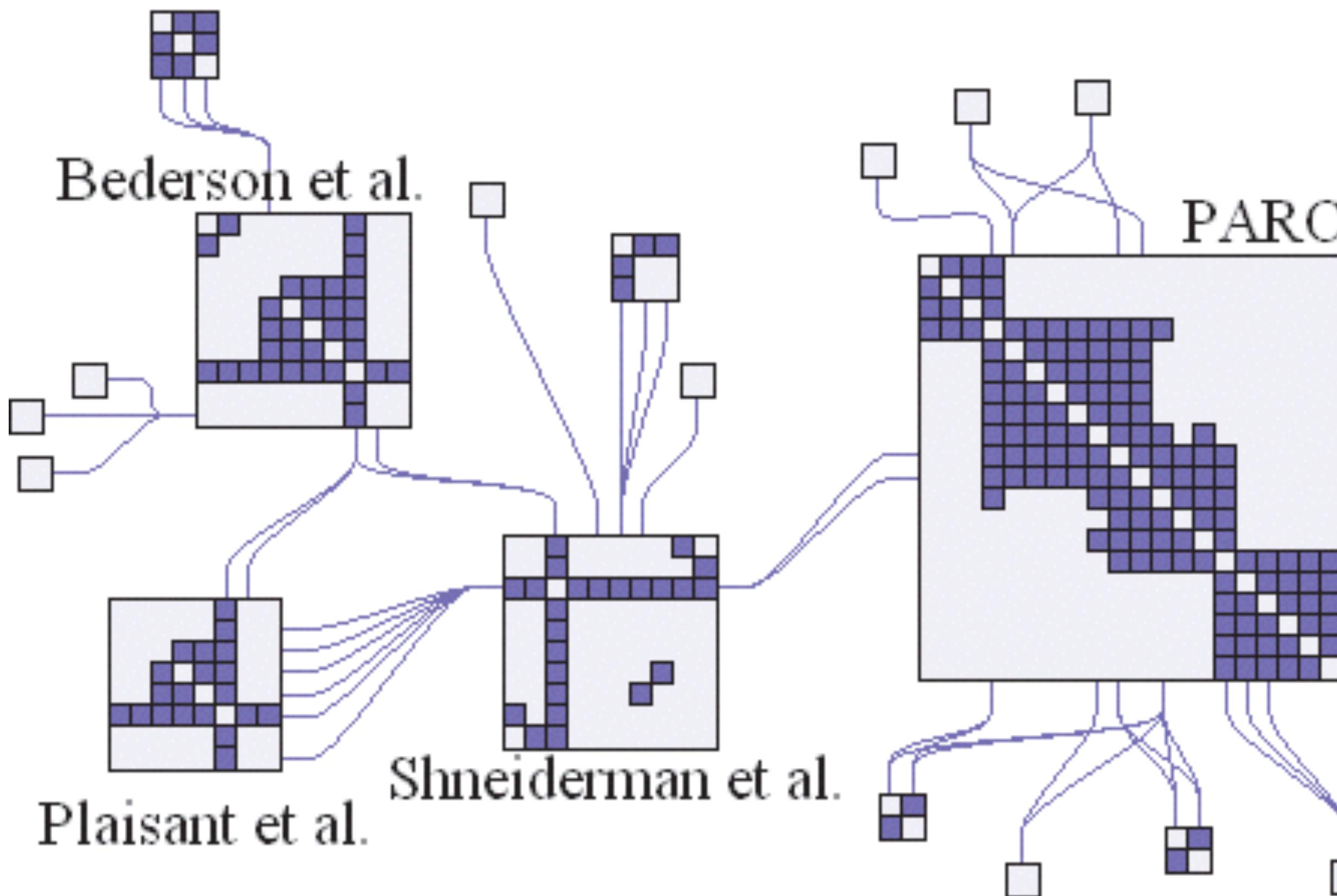
quadratic screen space requirement (any possible edge takes up space)

not suited for path-related TBTs

Special Case: Genealogy

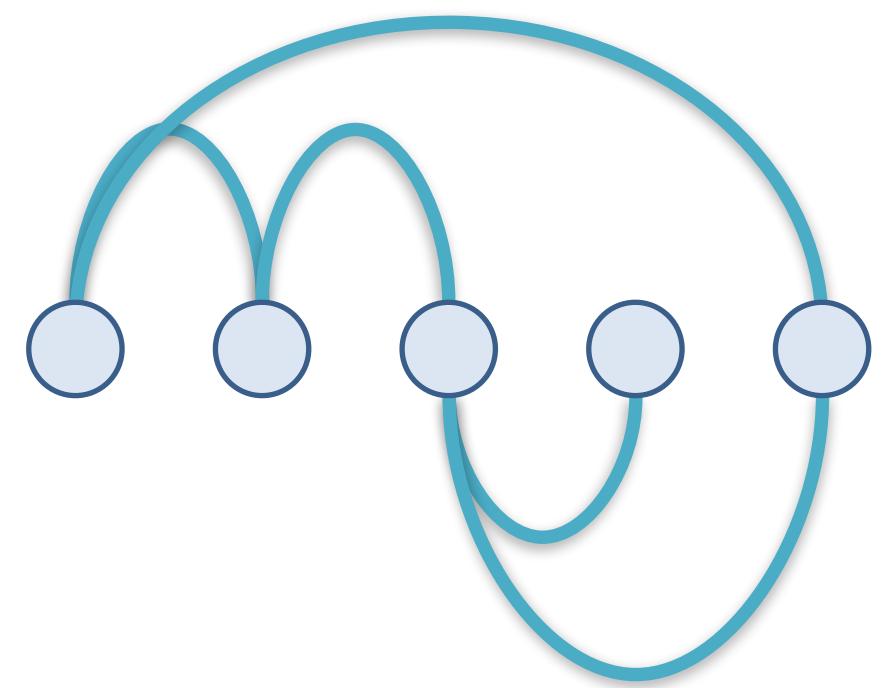


Hybrid Explicit/Matrix

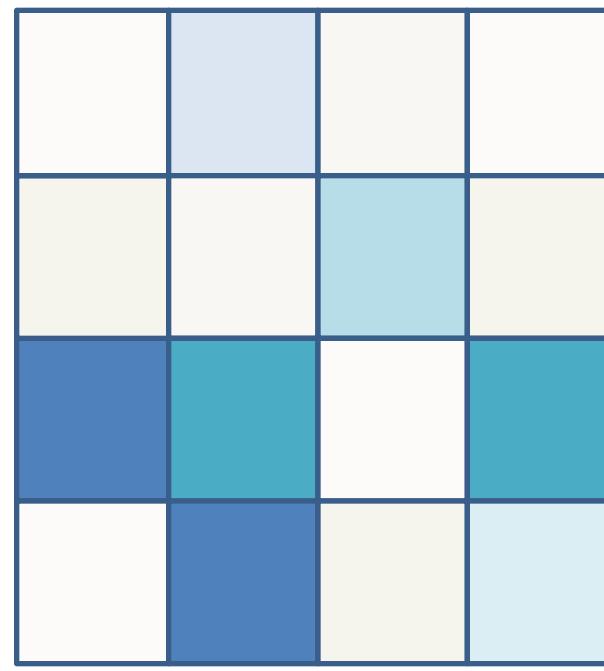


NodeTrix
[Henry et al. 2007]

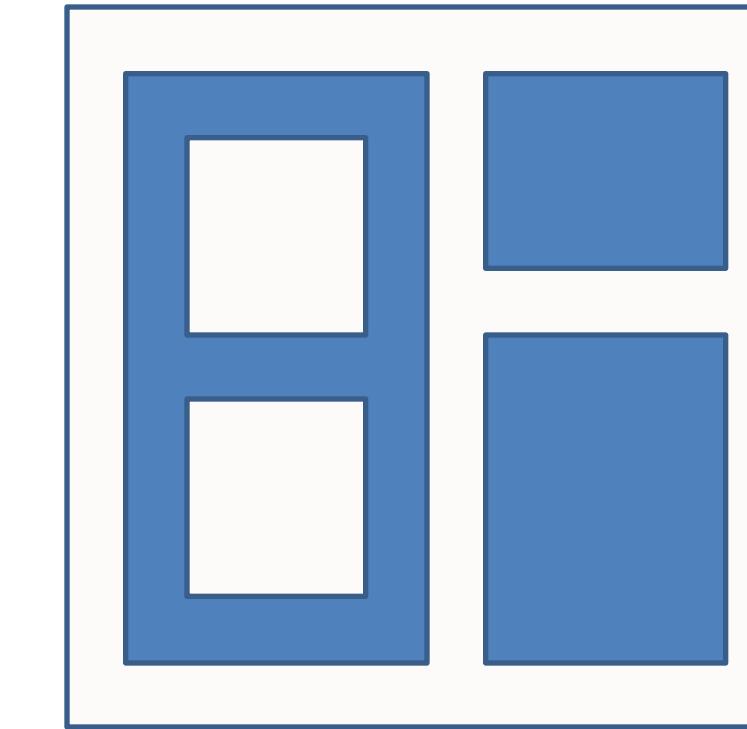
Implicit Layouts



Explicit
(Node-Link)



Matrix



Implicit

Explicit vs. Implicit Tree Vis

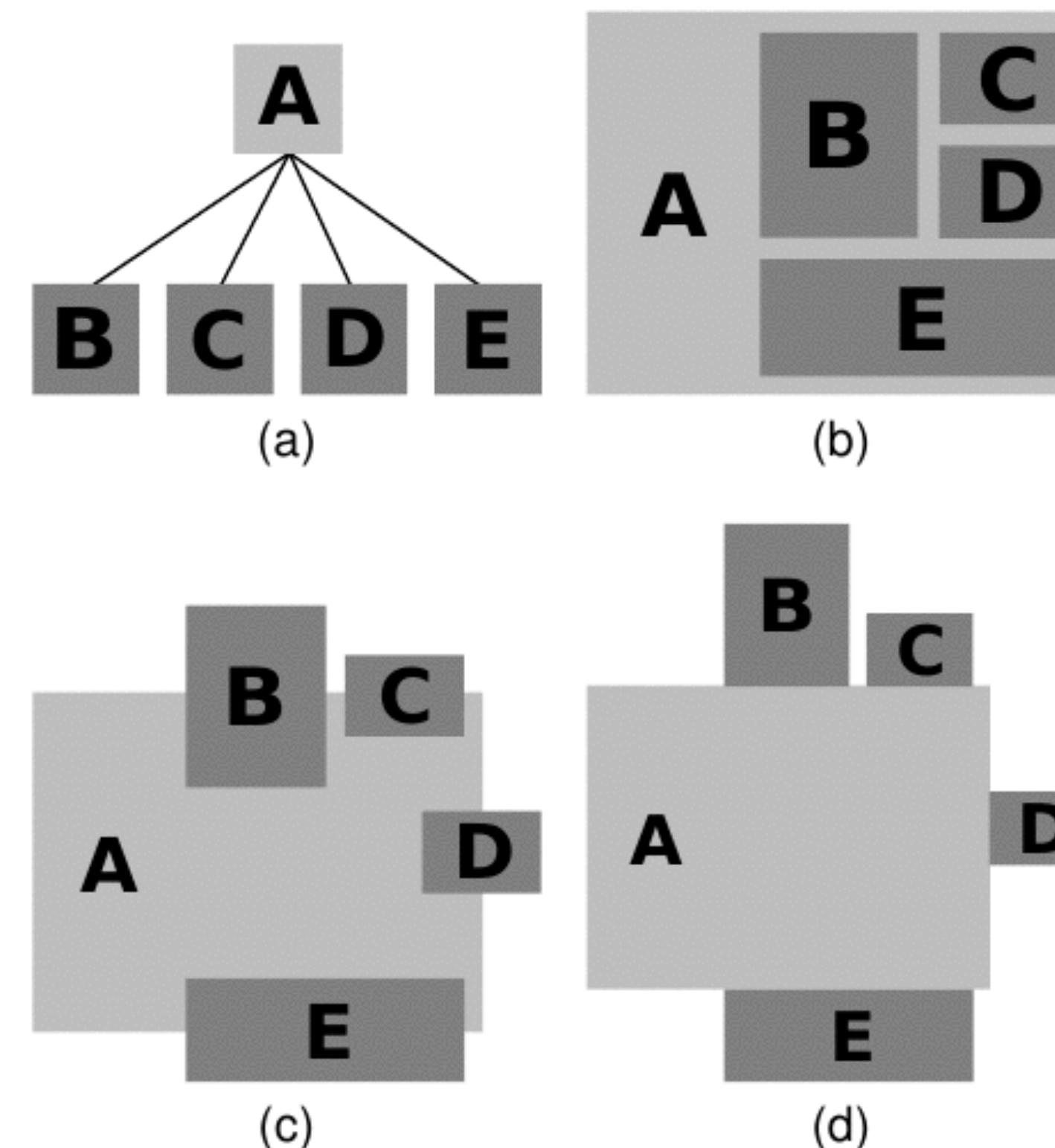
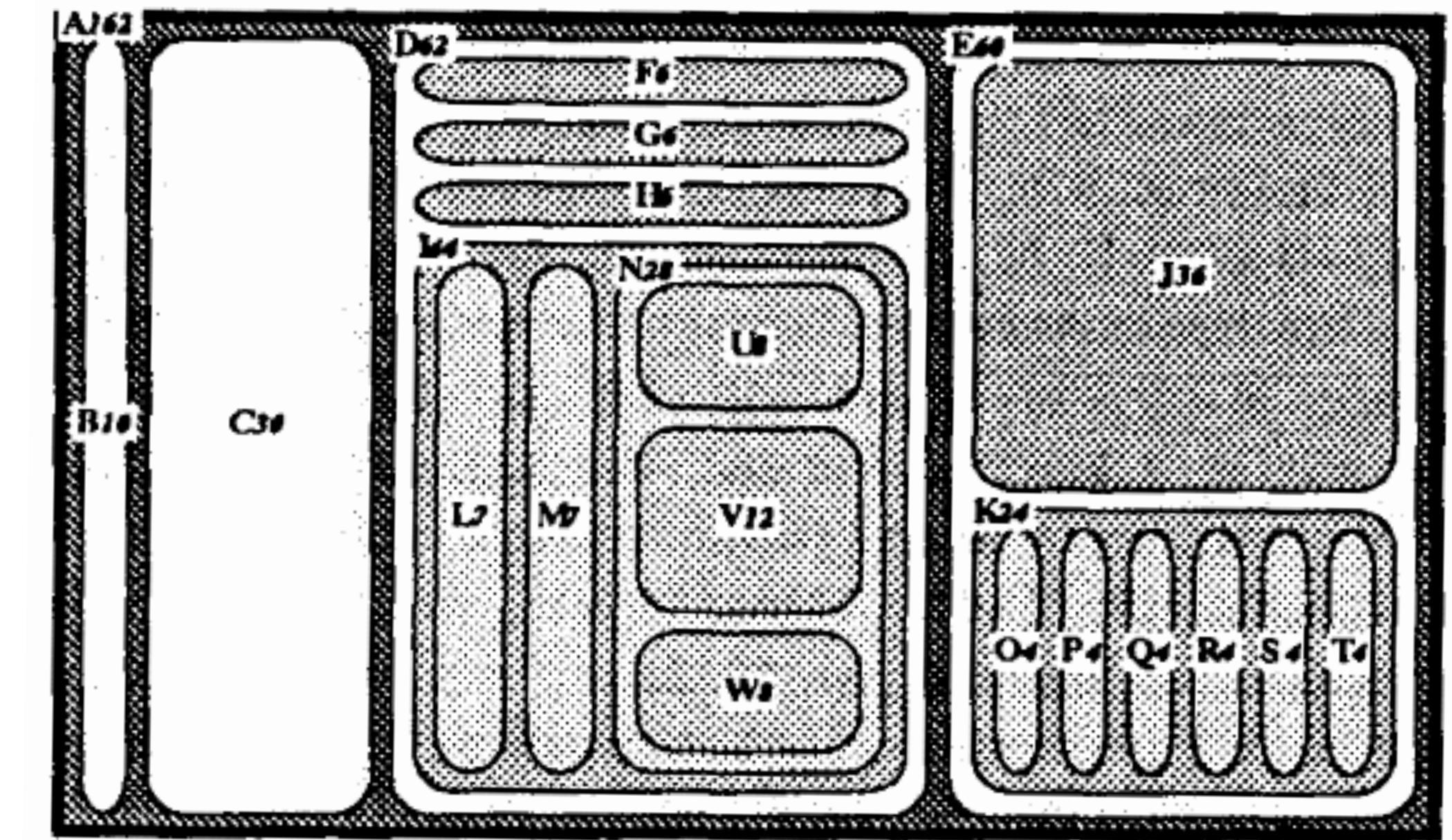
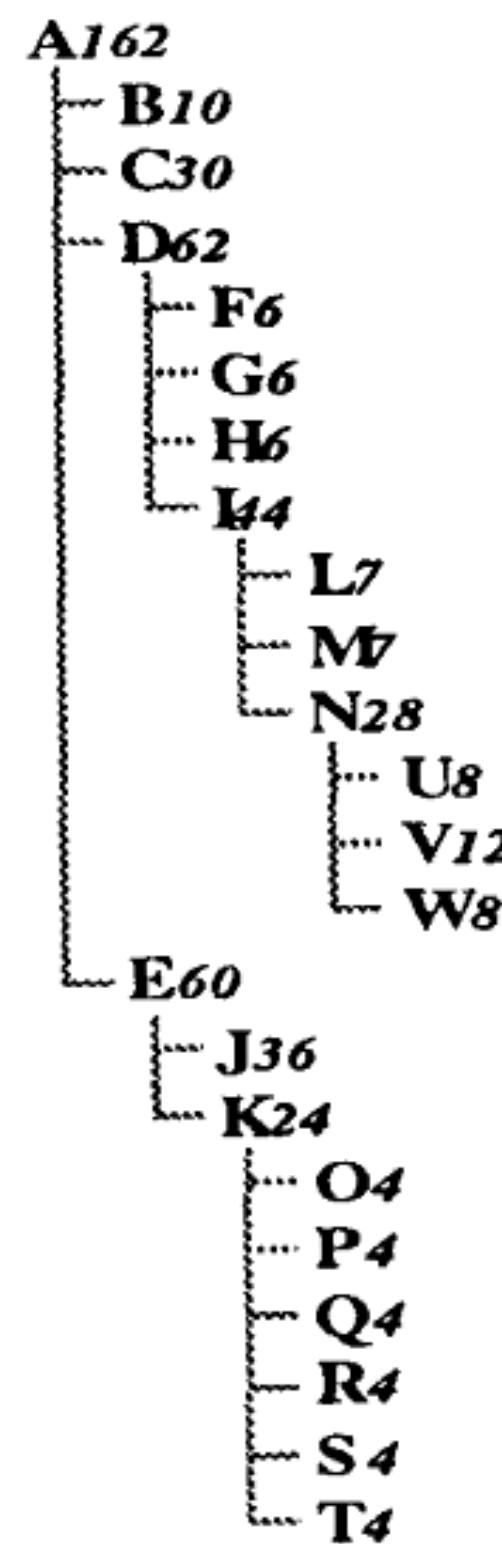
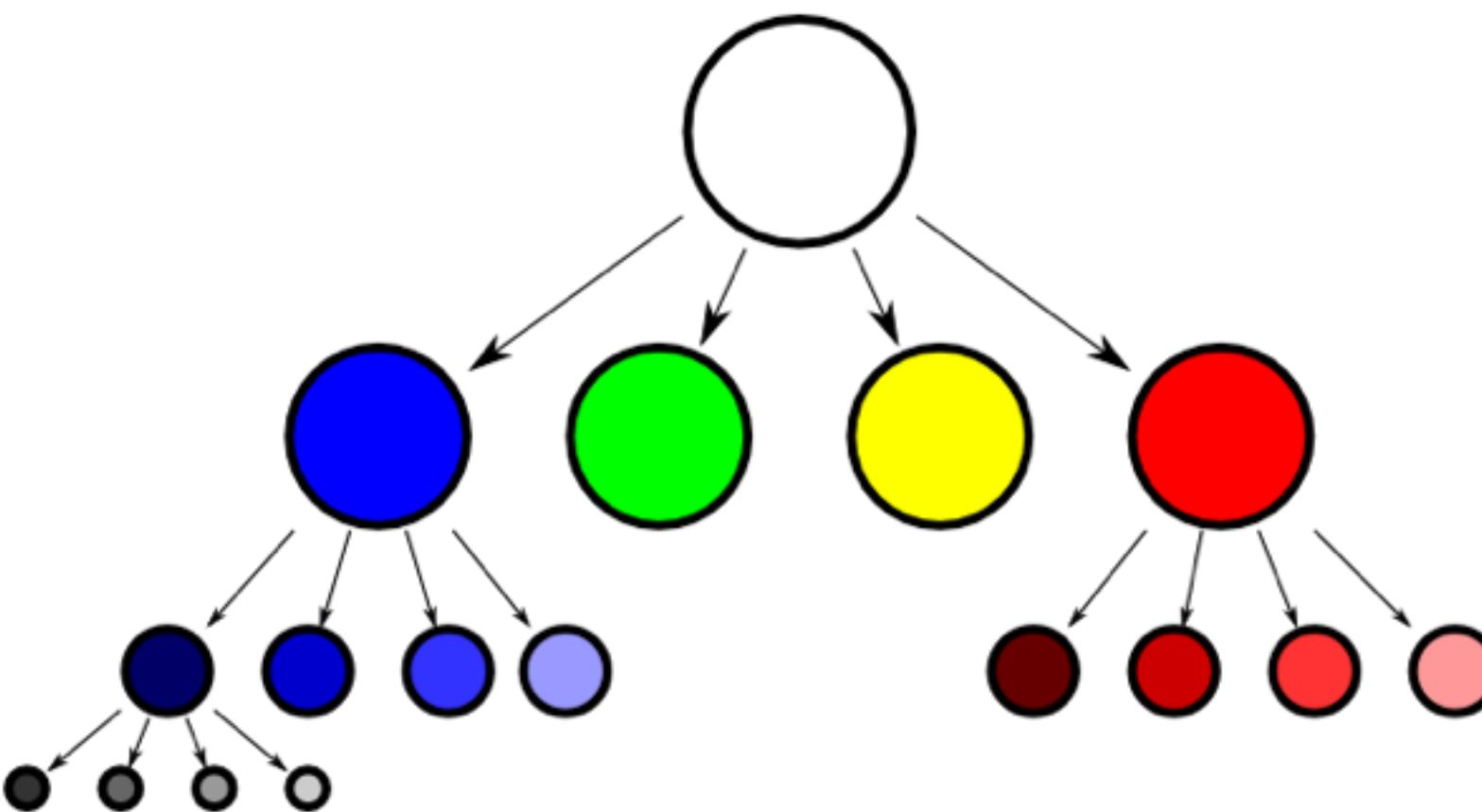
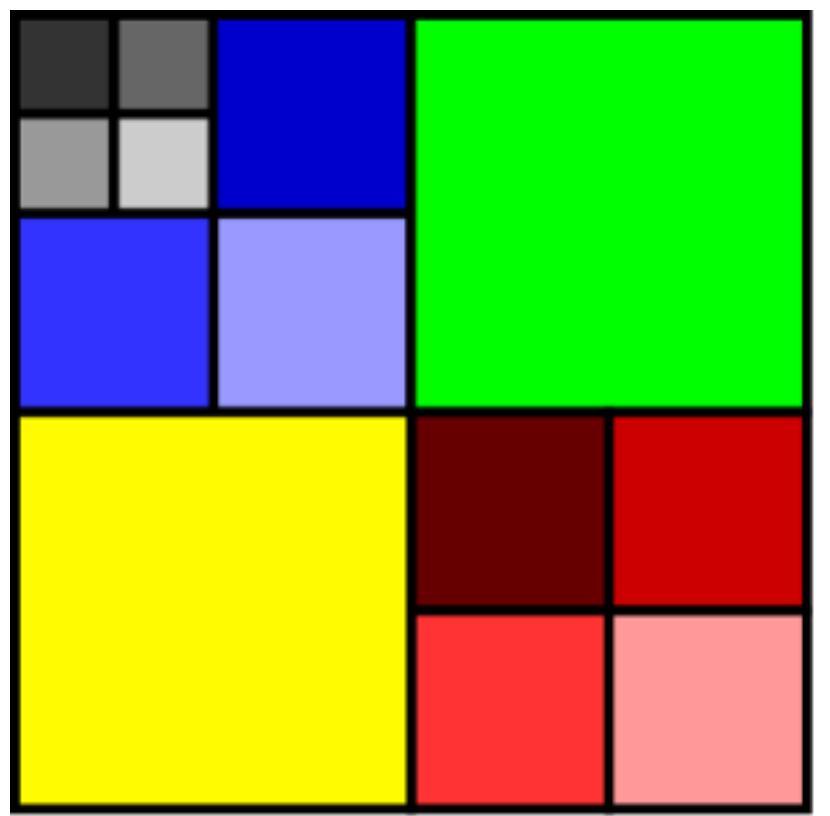
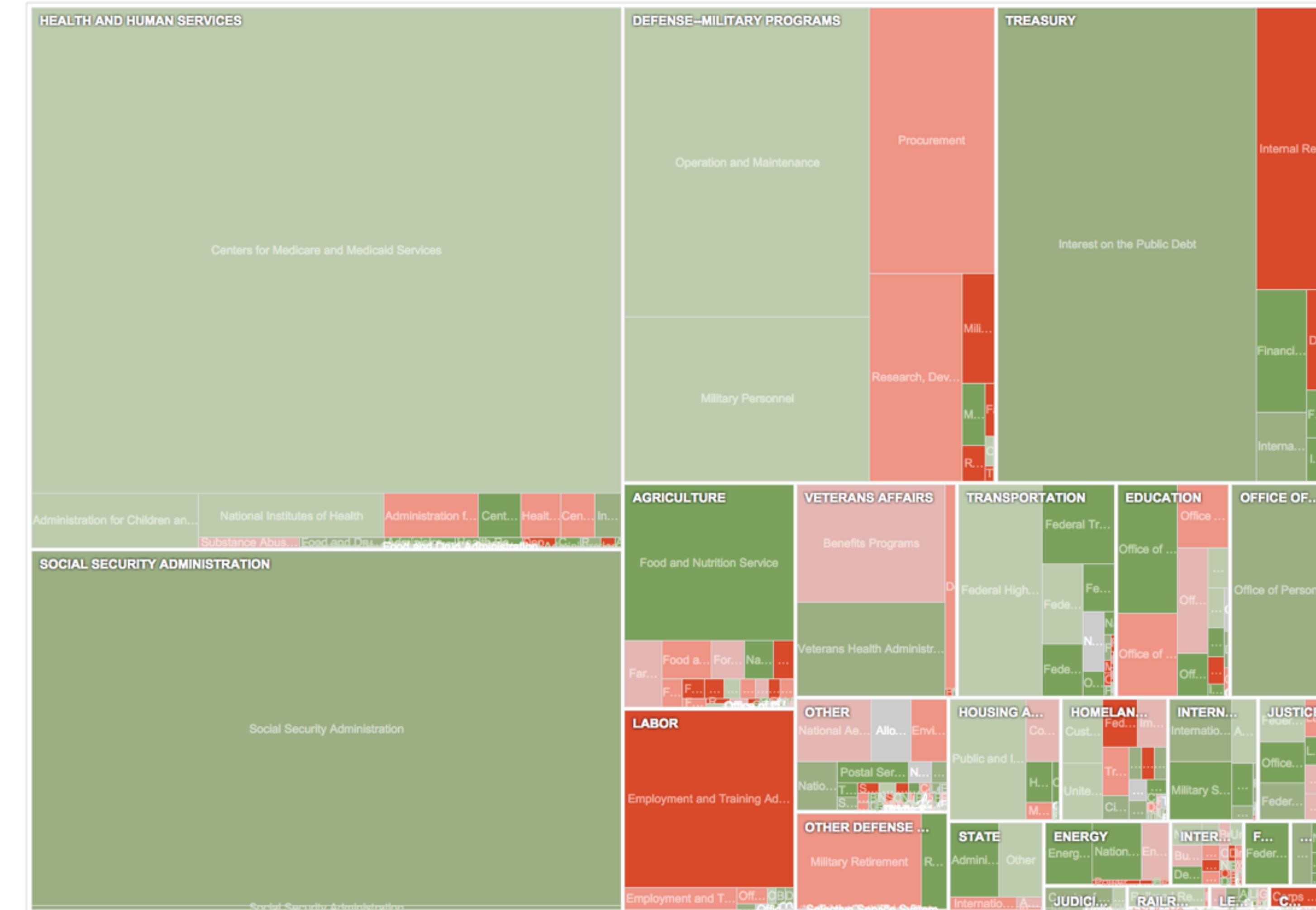


Fig. 2. (a) Explicit, node-link layout, (b) Implicit layout by inclusion, (c) Implicit Layout by overlap, (d) Implicit layout by adjacency.

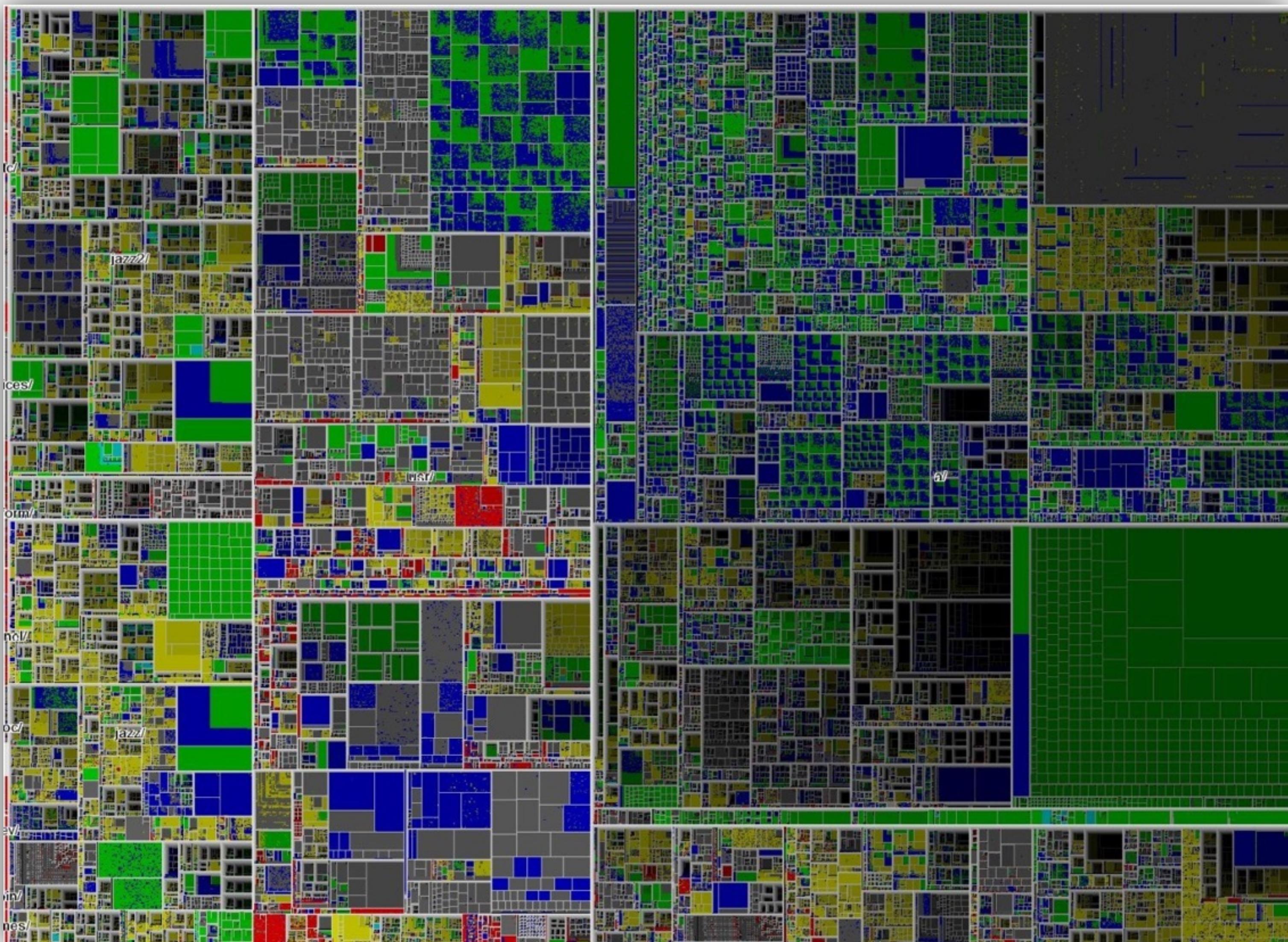
Tree Maps



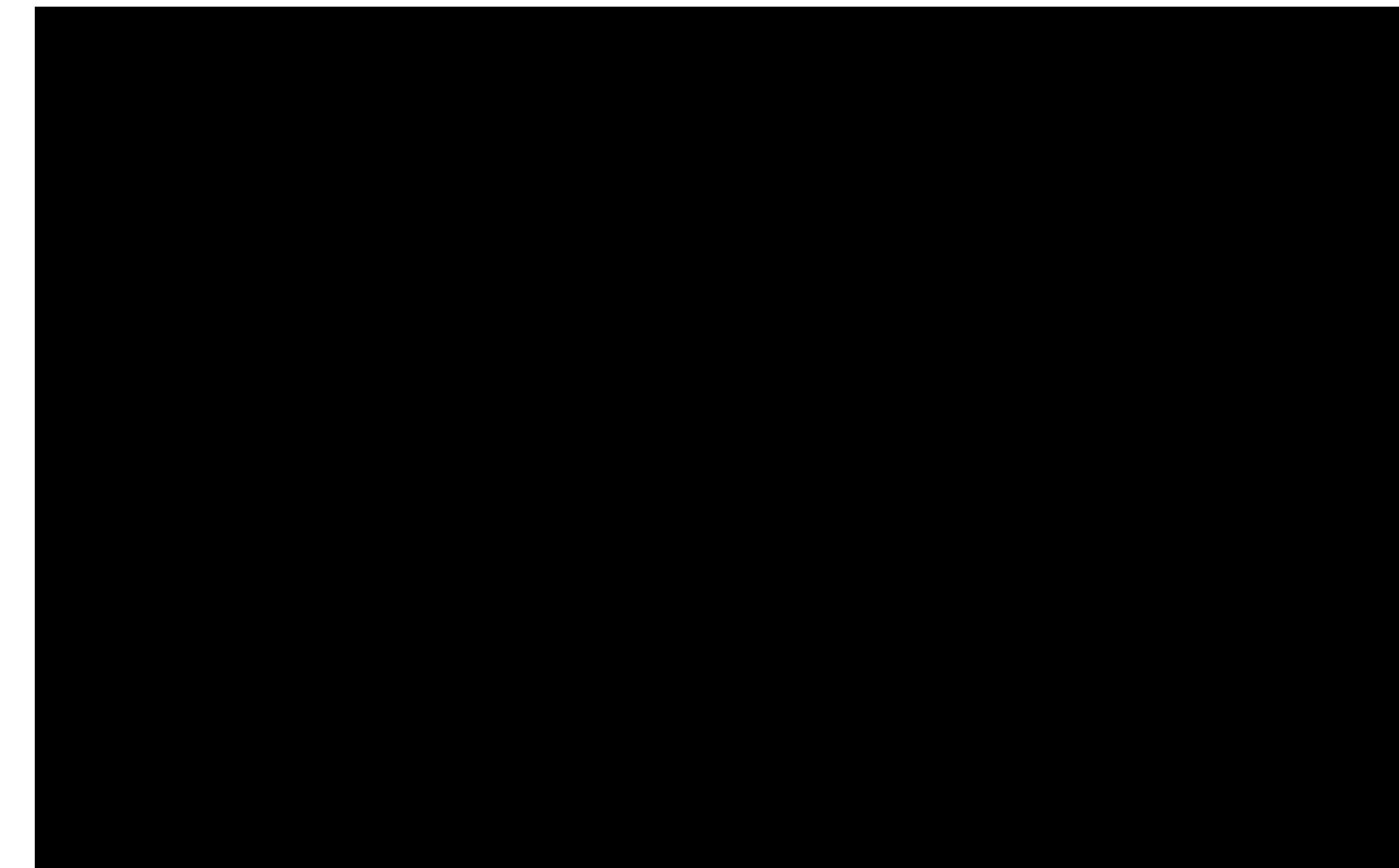
Zoomable Treemap



Example: Interactive TreeMap of a Million Items



Sunburst: Radial Layout



[Sunburst by John Stasko, Implementation in Caleydo by Christian Partl]

Tree Visualization Reference

How to cite this site?
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treevis.net - A Visual Bibliography of Tree Visualization 2.0 by Hans-Jörg Schulz

v.21-OCT-2014

Dimensionality Representation Alignment Fulltext Search Techniques Shown: 277

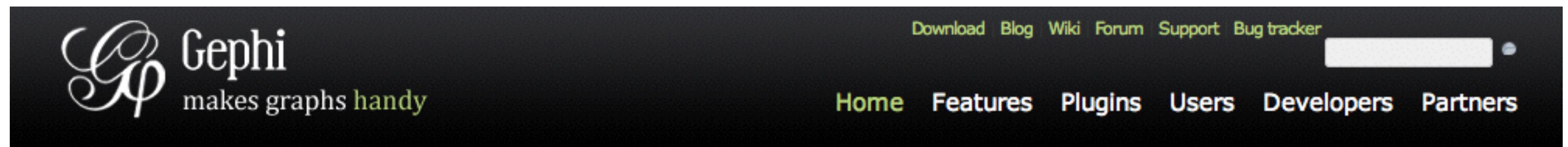
All All All All All

The image displays a collection of 100 tree visualization examples arranged in a 10x10 grid. Each example is represented by a small thumbnail image showing a different type of tree diagram or visualization. The examples include various representations such as radial trees, hierarchical trees, sunburst charts, treemaps, and network-like structures. The visualizations are color-coded and often show complex data relationships.

Graph Tools & Applications

Gephi

<http://gephi.org>



The Open Graph Viz Platform

Gephi is a visualization and exploration [platform](#) for all kinds of networks and complex systems, dynamic and hierarchical graphs.

Runs on Windows, Linux and Mac OS X. Gephi is open-source and free.

[Learn More on Gephi Platform »](#)

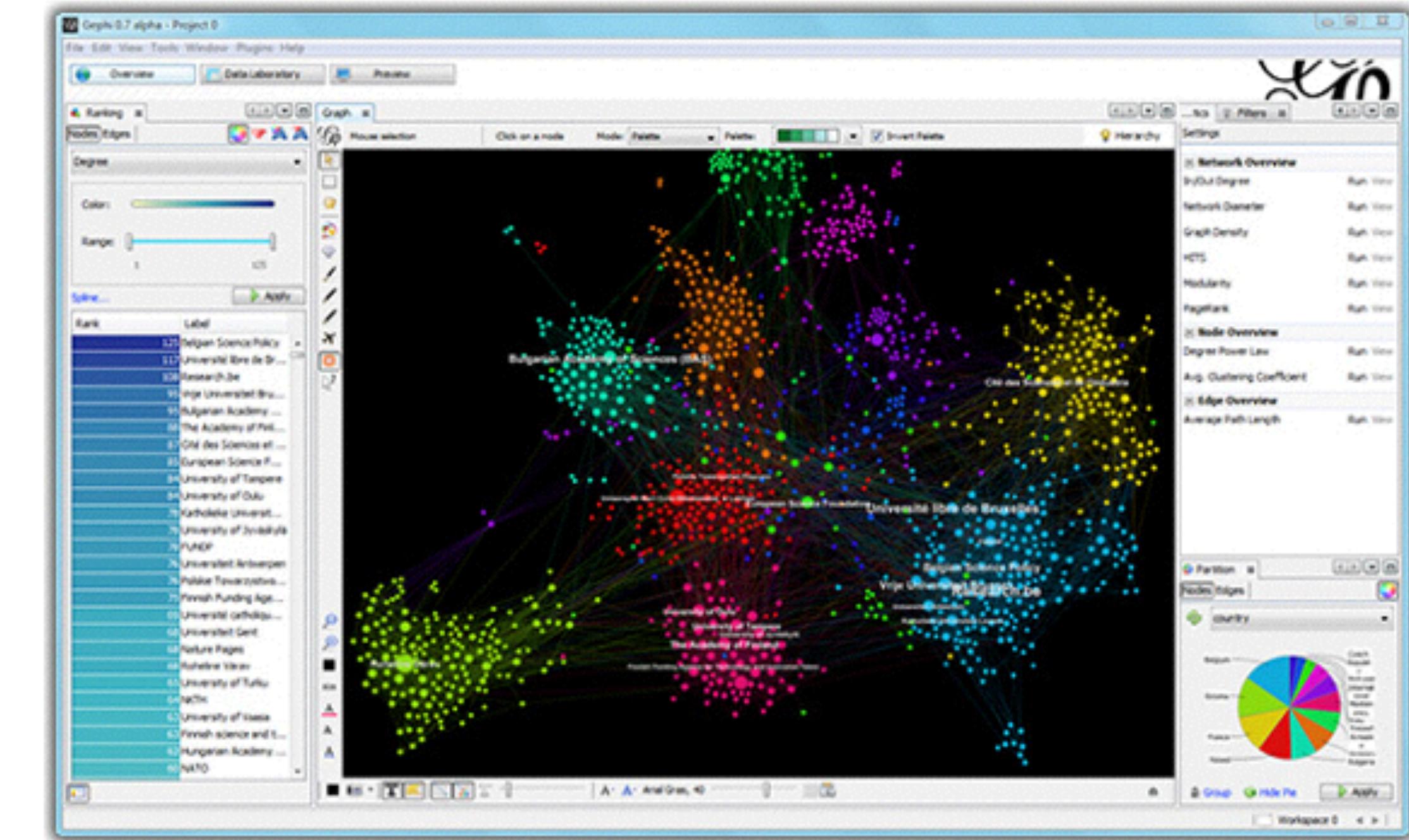


Download FREE
Gephi 0.7 alpha

[Release Notes](#) | [System Requirements](#)

► [Features](#)
► [Quick start](#)

► [Screenshots](#)
► [Videos](#)



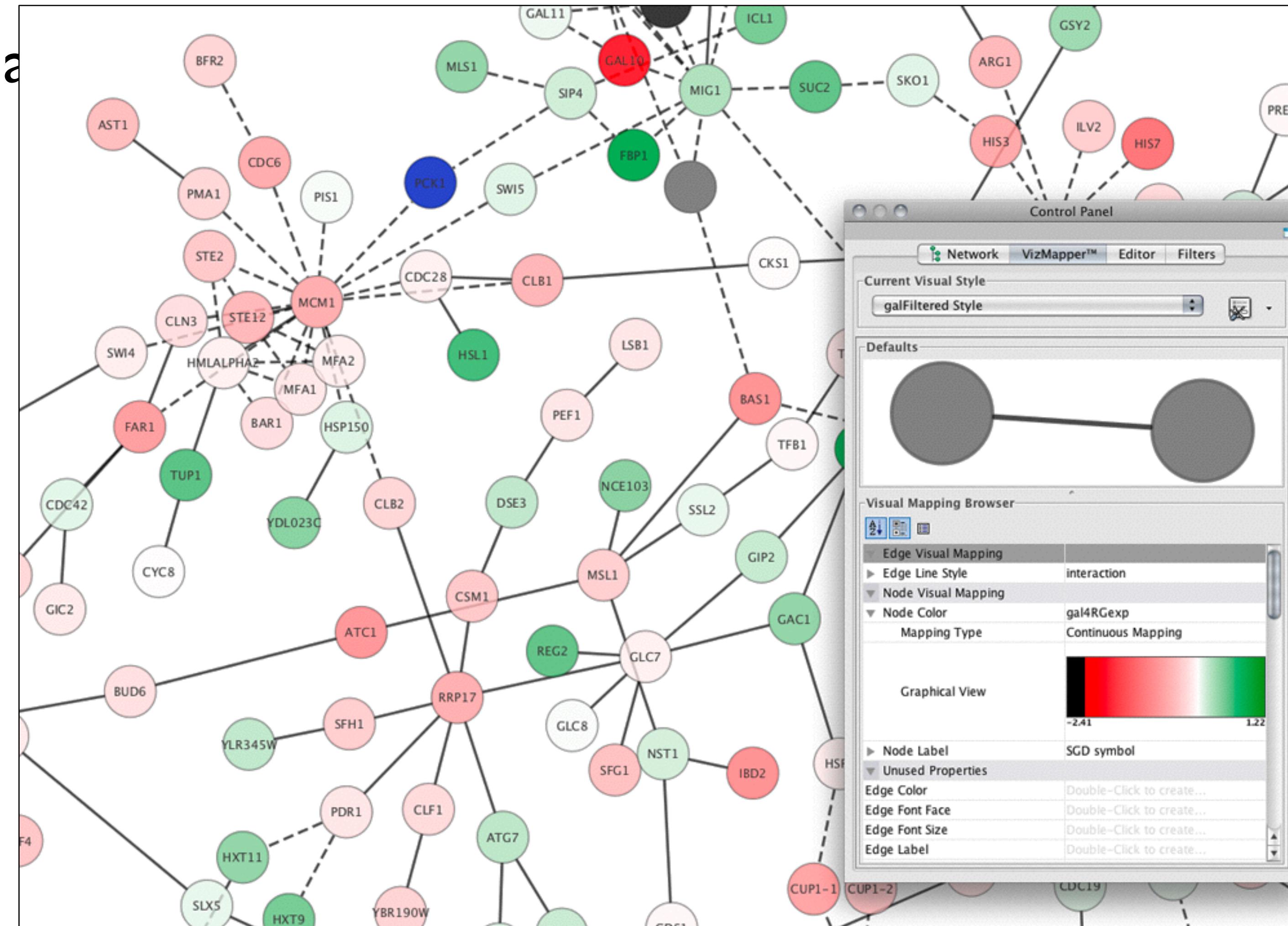
Gephi has been accepted again for Google Summer of Code! The program is the best way for students around the world to start contributing to an open-source project. Students, apply now for Gephi proposals. Come to the GSOC forum section and say Hi! to this topic.

[Learn More »](#)

Cytoscape

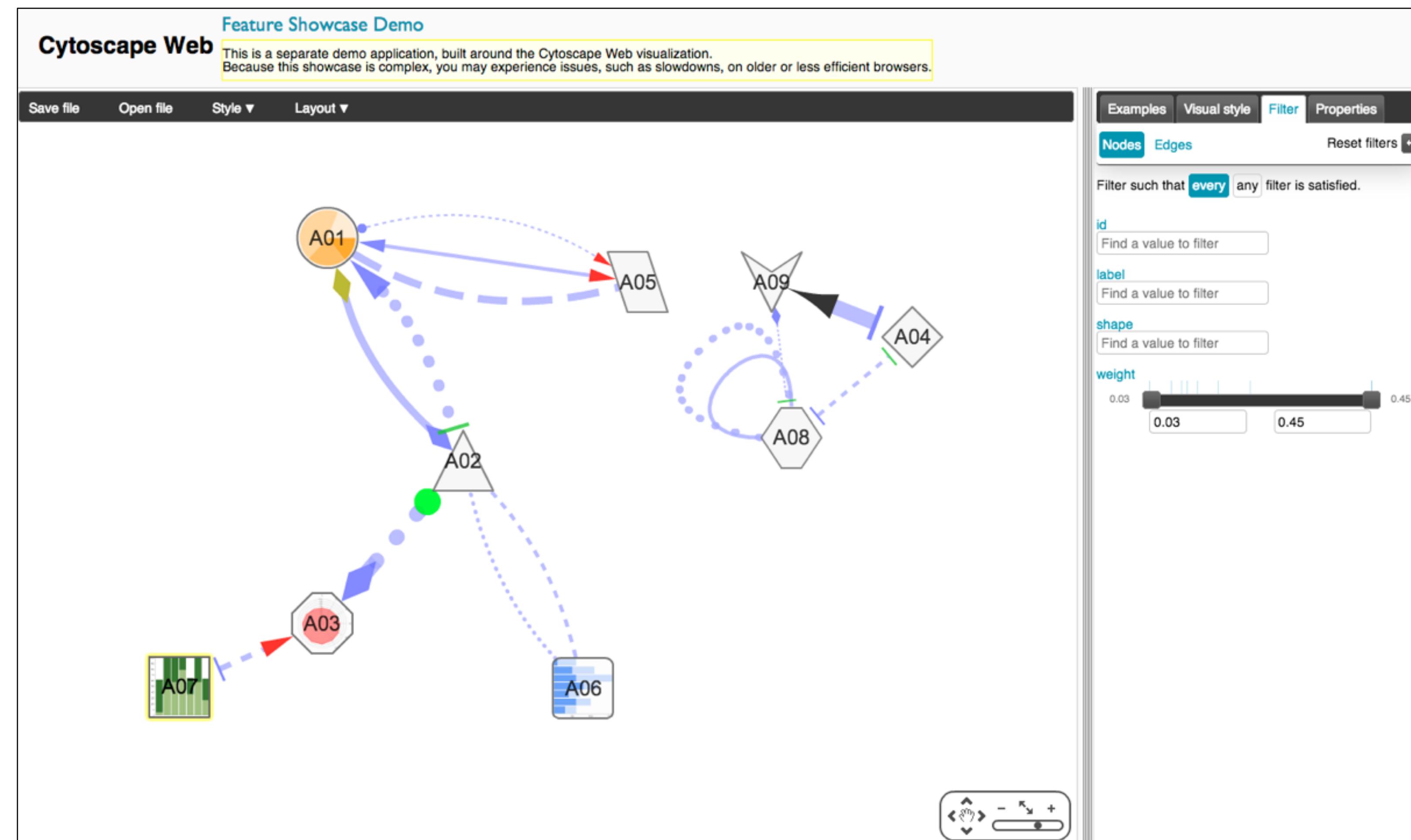
<http://www.cytoscape.org/>

Open source plat-



Cytoscape Web

<http://cytoscapeweb.cytoscape.org/>



NetworkX

<https://networkx.github.io/>

NetworkX

[NetworkX Home](#) | [Documentation](#) | [Download](#) | [Developer \(Github\)](#)

High-productivity software for complex networks

NetworkX is a Python language software package for the creation, manipulation, and study of the structure, dynamics, and functions of complex networks.

[Documentation](#)
all documentation

[Examples](#)
using the library

[Features](#)

- Python language data structures for graphs, digraphs, and multigraphs.
- Nodes can be "anything" (e.g. text, images, XML records)
- Edges can hold arbitrary data (e.g. weights, time-series)
- Generators for classic graphs, random graphs, and synthetic networks
- Standard graph algorithms
- Network structure and analysis measures
- Open source [BSD license](#)
- Well tested: more than 1800 unit tests, >90% code coverage
- Additional benefits from Python: fast prototyping, easy to teach, multi-platform



[Reference](#)
all functions and methods

Versions

1.8.1 - 4 August 2013
[downloads](#) | [docs](#) | [pdf](#)

Development

1.9dev
[github](#) | [docs](#) | [pdf](#)
[build](#) passing
[coverage](#) 83%

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