

Intro to ML

March 10, 2020

Data Science CSCI 1951A

Brown University

Instructor: Ellie Pavlick

HTAs: Josh Levin, Diane Mutako, Sol Zitter

Announcements

- This class is going viral! (Funny? No? Too soon?)
 - Not officially, but starting to prep just in case
 - Trial run on Thursday
 - Quizzes and Clickers will remain both valid until further notice
- Questions?

Today

- ML “preliminaries”—terminology, basic building blocks, conceptual background
- The two faces of linear regression
- Training with Stochastic Gradient Descent

Today

- **ML “preliminaries” – terminology, basic building blocks, conceptual background**
- The two faces of linear regression
- Training with Stochastic Gradient Descent

Quick Clicker Q!

How much ML experience have you had?

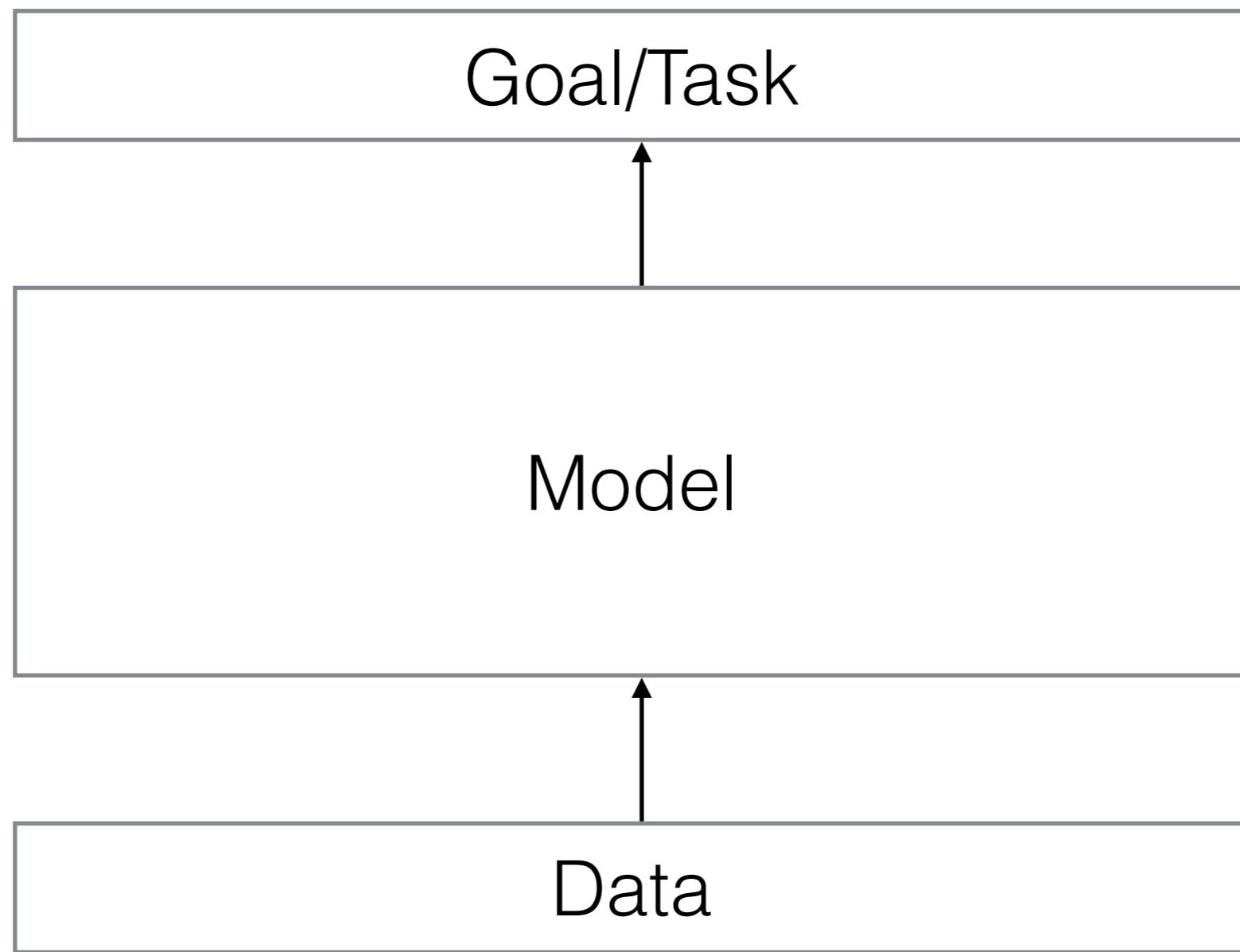
- (a) None at all. I have obviously heard of ML but I've never really dealt with it.
- (b) Small amount of informal experience. I've read articles/blog posts and gotten the gist of how it works.
- (c) Like (b), but I've followed along and coded some models myself
- (d) Comfortable. I've taken an ML class.
- (e) Very comfortable. I've taken an ML class/classes and I've built models myself for research projects or internships.

Quick Clicker Q!

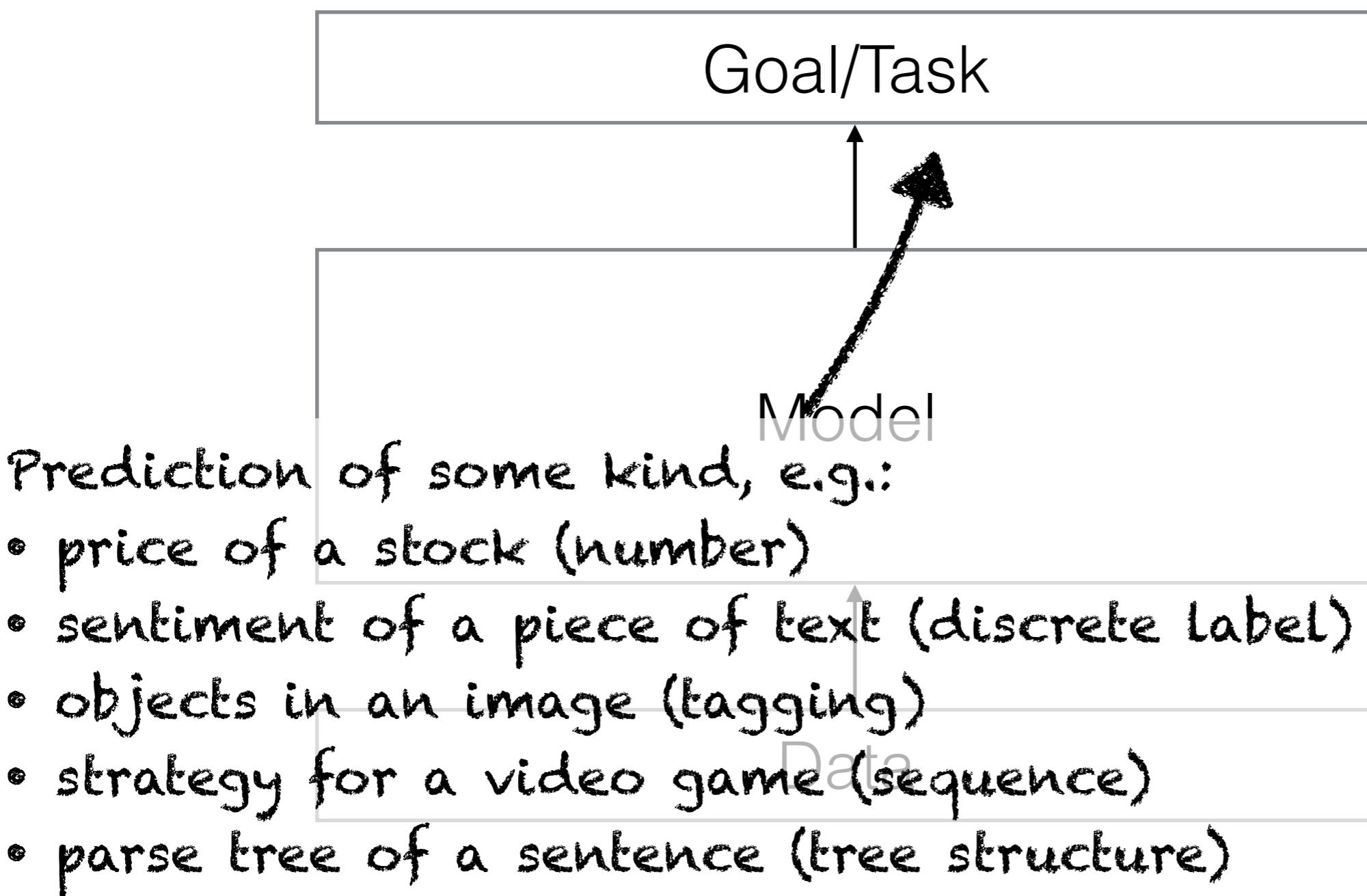
Characterize your knowledge of ML:

- (a) Mostly “conventional” ML
- (b) Mostly deep learning
- (c) Equally comfortable with both
- (d) Not comfortable with either

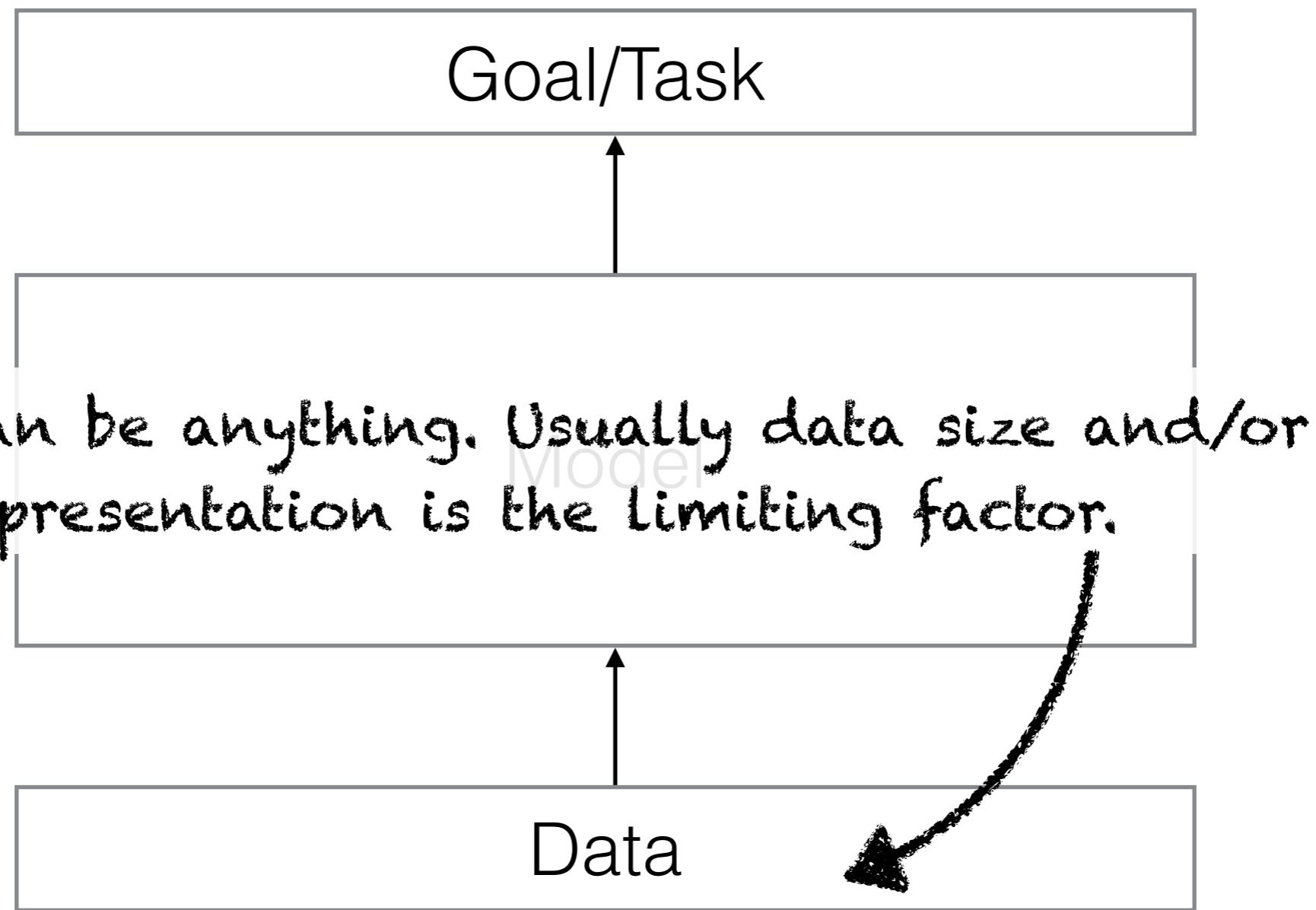
Oversimplified ML



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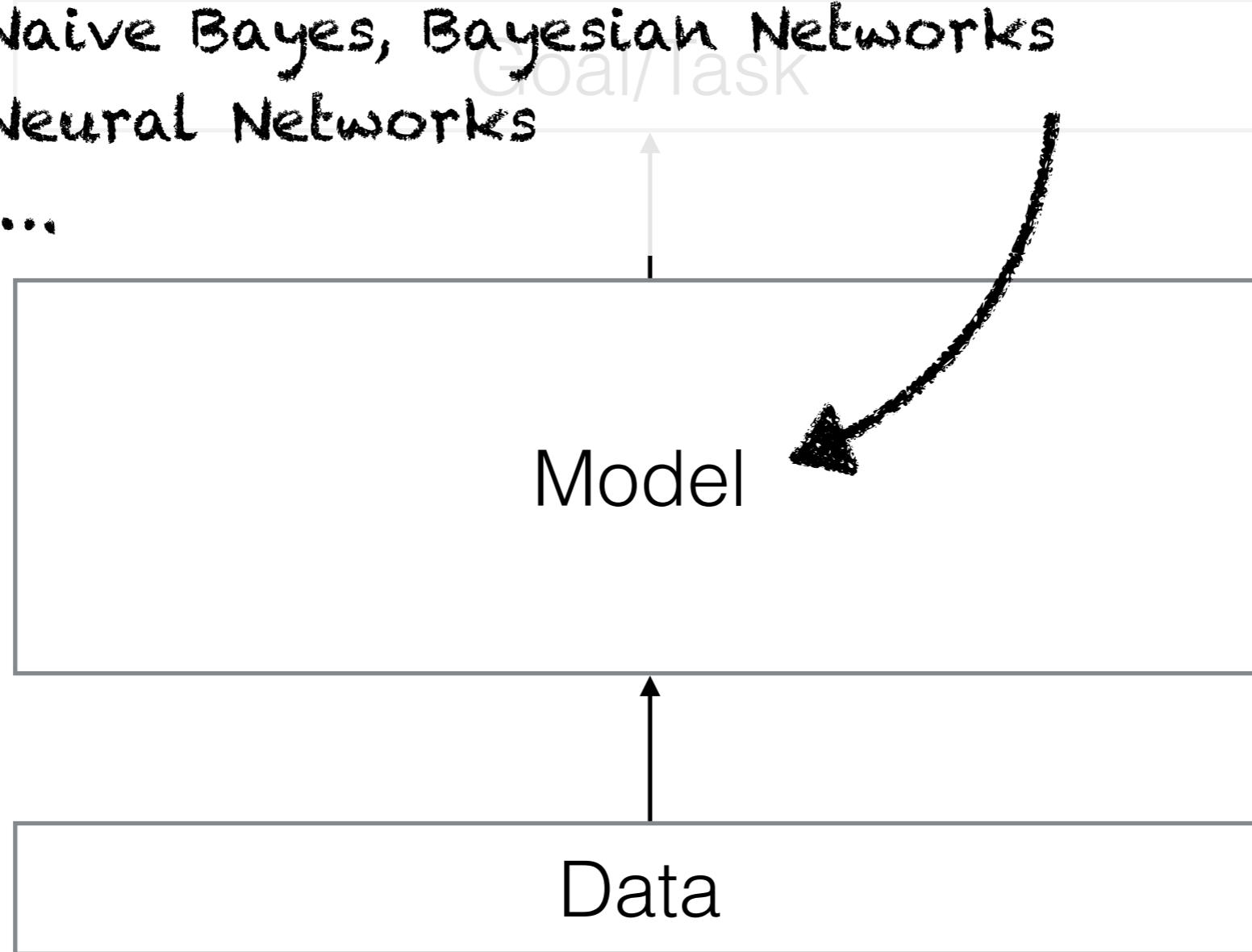
Oversimplified ML



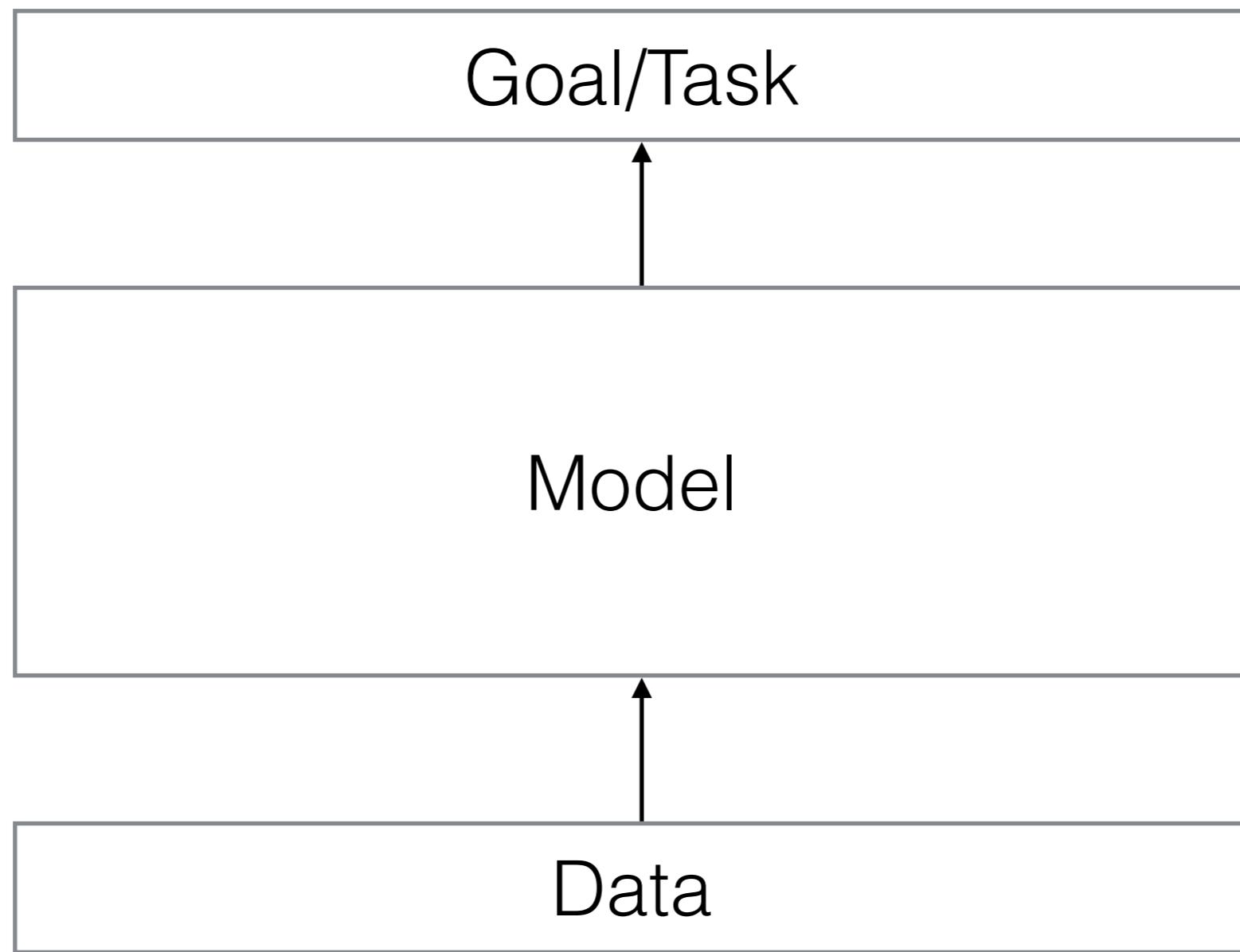
Decisions about how the problem is structured

AND how to estimate parameters

- Linear/logistic regression
- SVMs
- Naive Bayes, Bayesian Networks
- Neural Networks
-



Defining an ML problem



MACHINE LEARNING

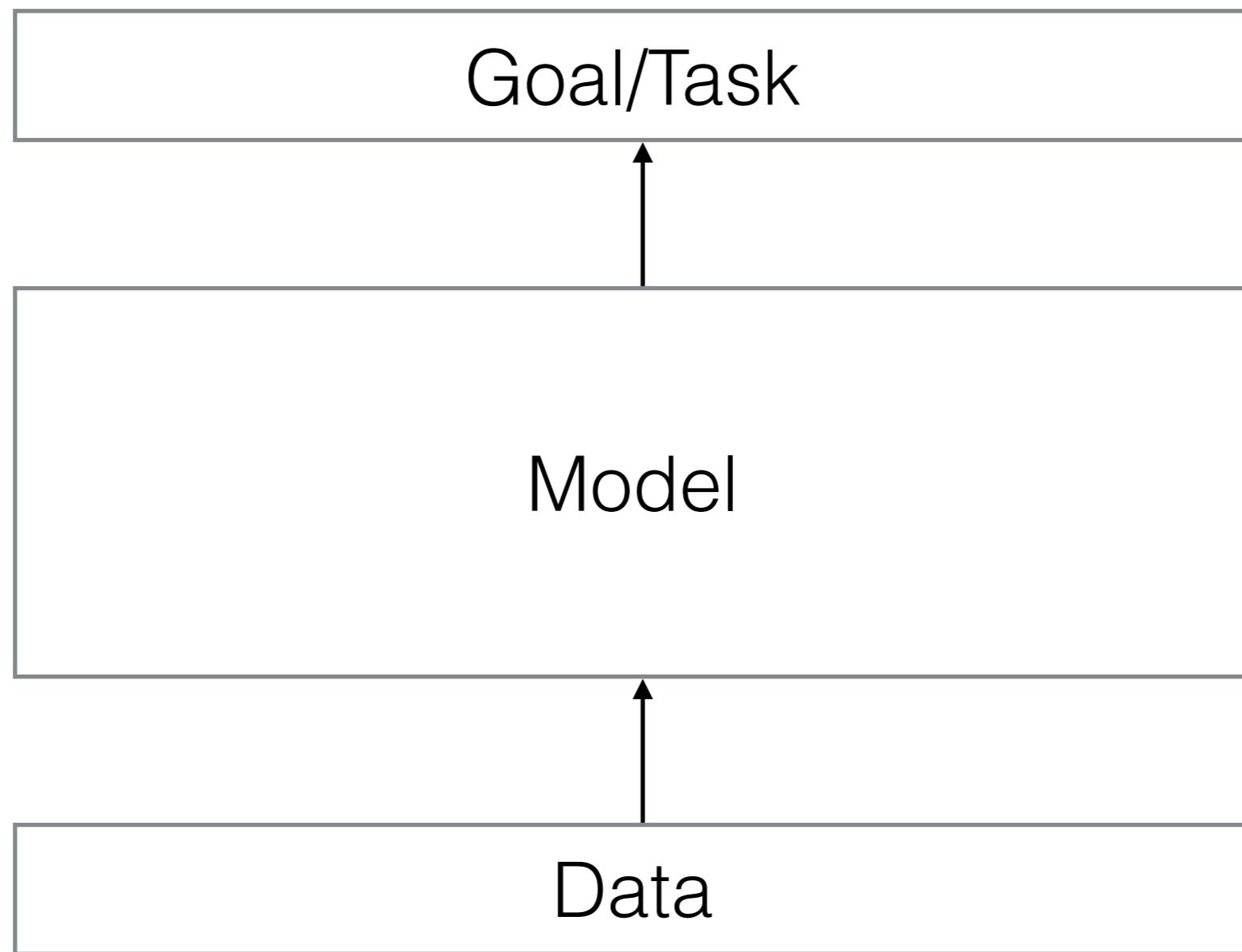


https://youtu.be/bq2_wSsDwkQ?t=682

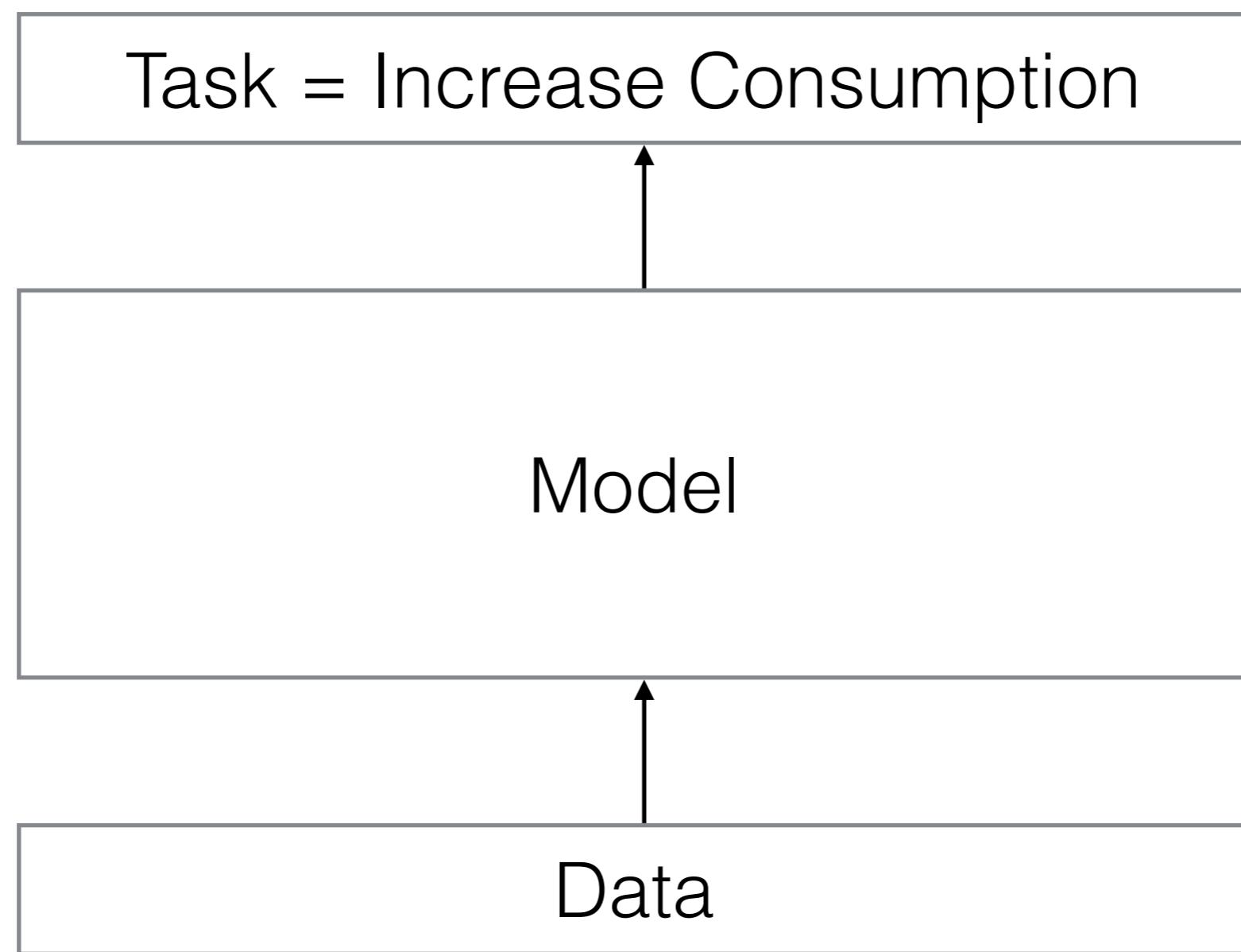
MACHINE LEARNING



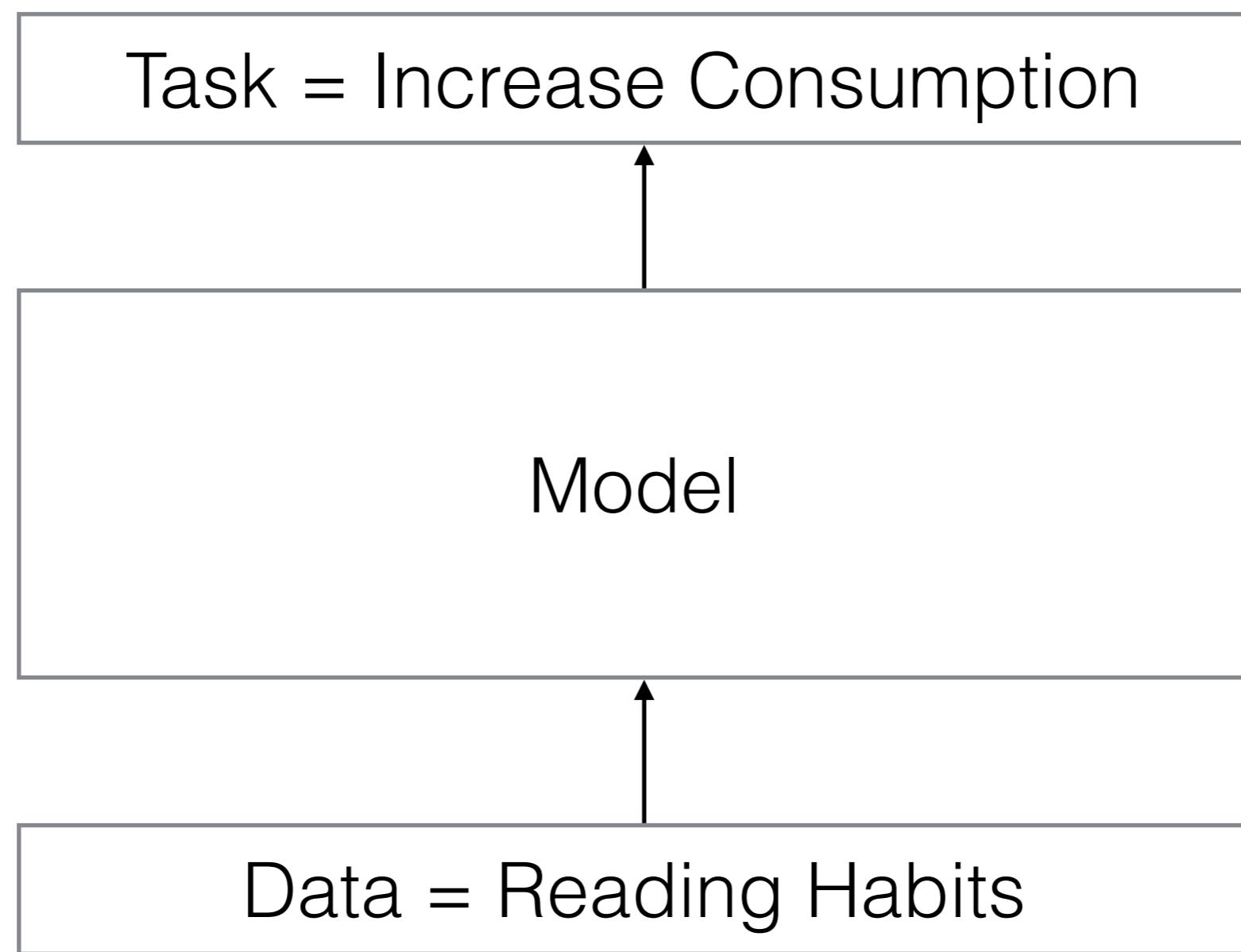
Defining an ML problem



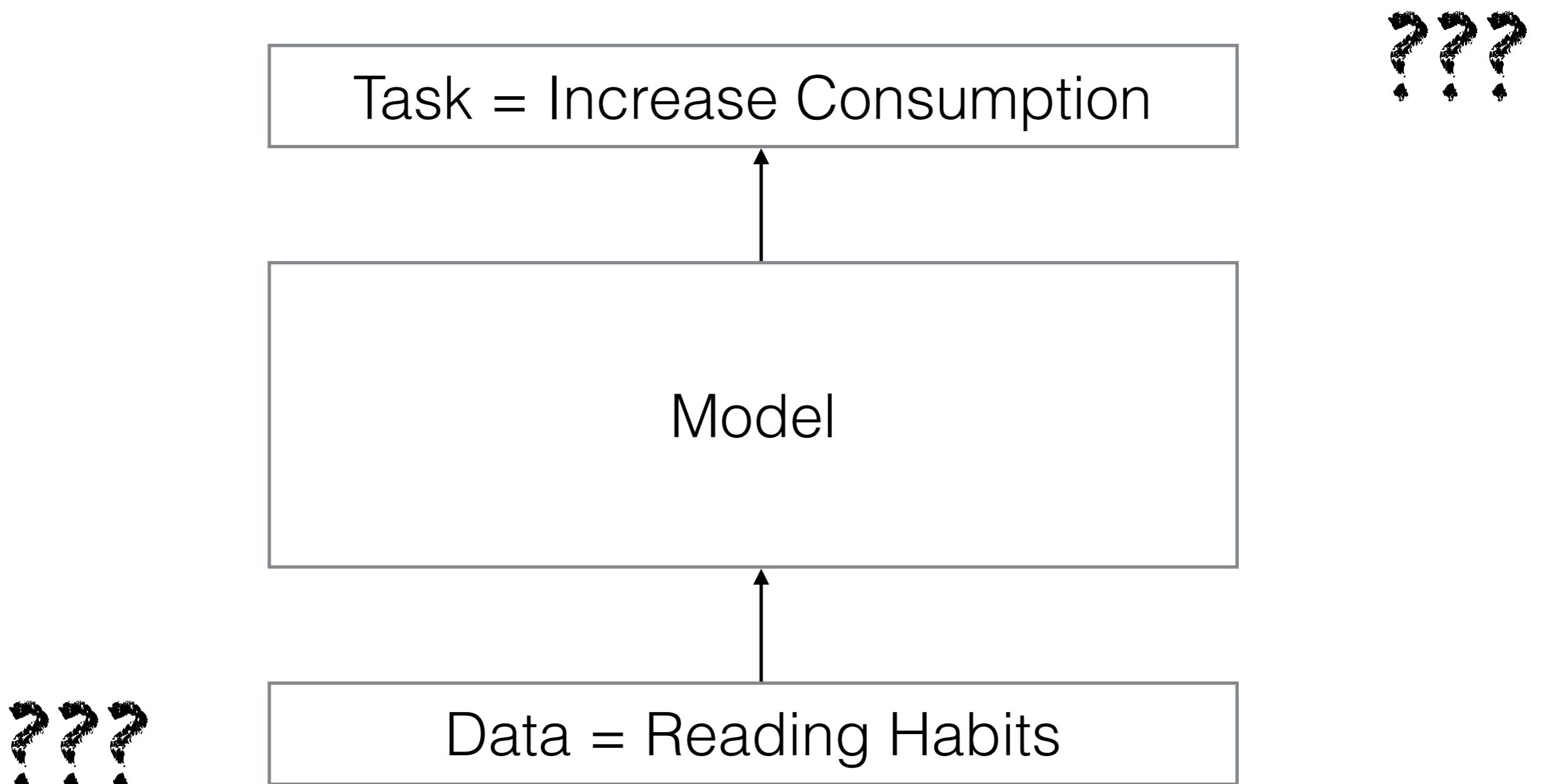
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Defining an ML problem



Defining an ML problem



Defining an ML problem

- What is “machine learnable”?

Defining an ML problem

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Defining an ML problem

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Defining an ML problem

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Defining an ML problem

- What is “machine learnable”?
- ~~Like... basically everything, right? WRONG!!~~ (kind of)
- Input features need to be concrete and representable. Definition of “success” needs to be quantifiable (and, right now, usually differentiable).

Defining an ML problem

Objective/Loss Function = ???

~~Task = Increase Consumption~~

Model

Data = Reading Habits

Defining an ML problem

Objective/Loss Function = ???

~~Task — Increase Consumption~~

Model

~~Data — Reading Habits~~

Features = ???

Defining an ML problem

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Prediction Target

- Goal = Increase consumption of “content” NOS for your ~~clickbait farm~~ pulitzer-prize worthy publication

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Clicker Question!

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- Time spent on site (avg. per user/total)
- Number of users
- Number of articles read (need to define “read”)
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- Prediction target: $y - \hat{y}$
 - Difference between predicted and true value
 - Squared difference between predicted and true value
- Objective/Loss function
 - Time spent reading
 - Number of articles read
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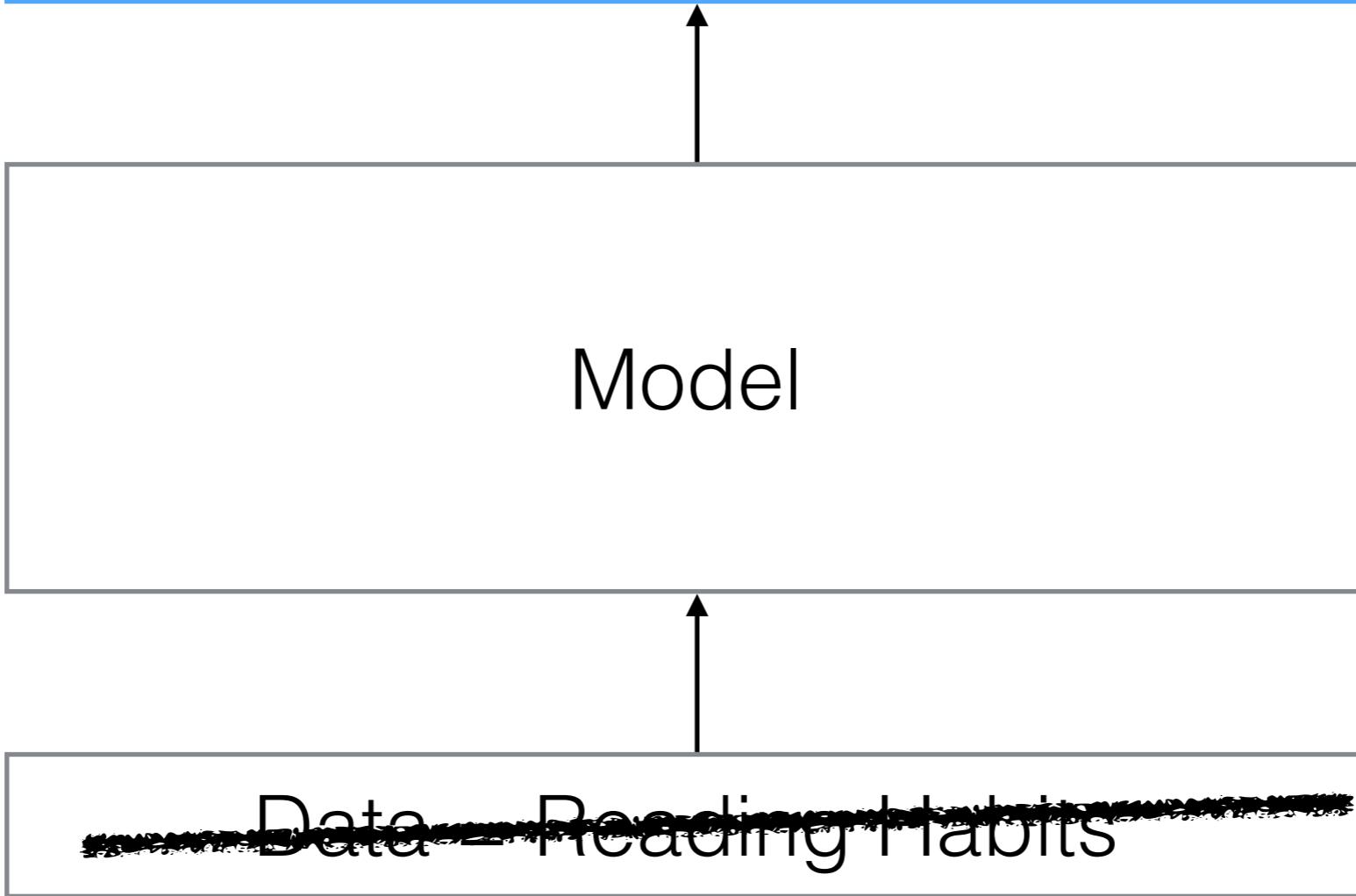
Model

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Defining an ML problem

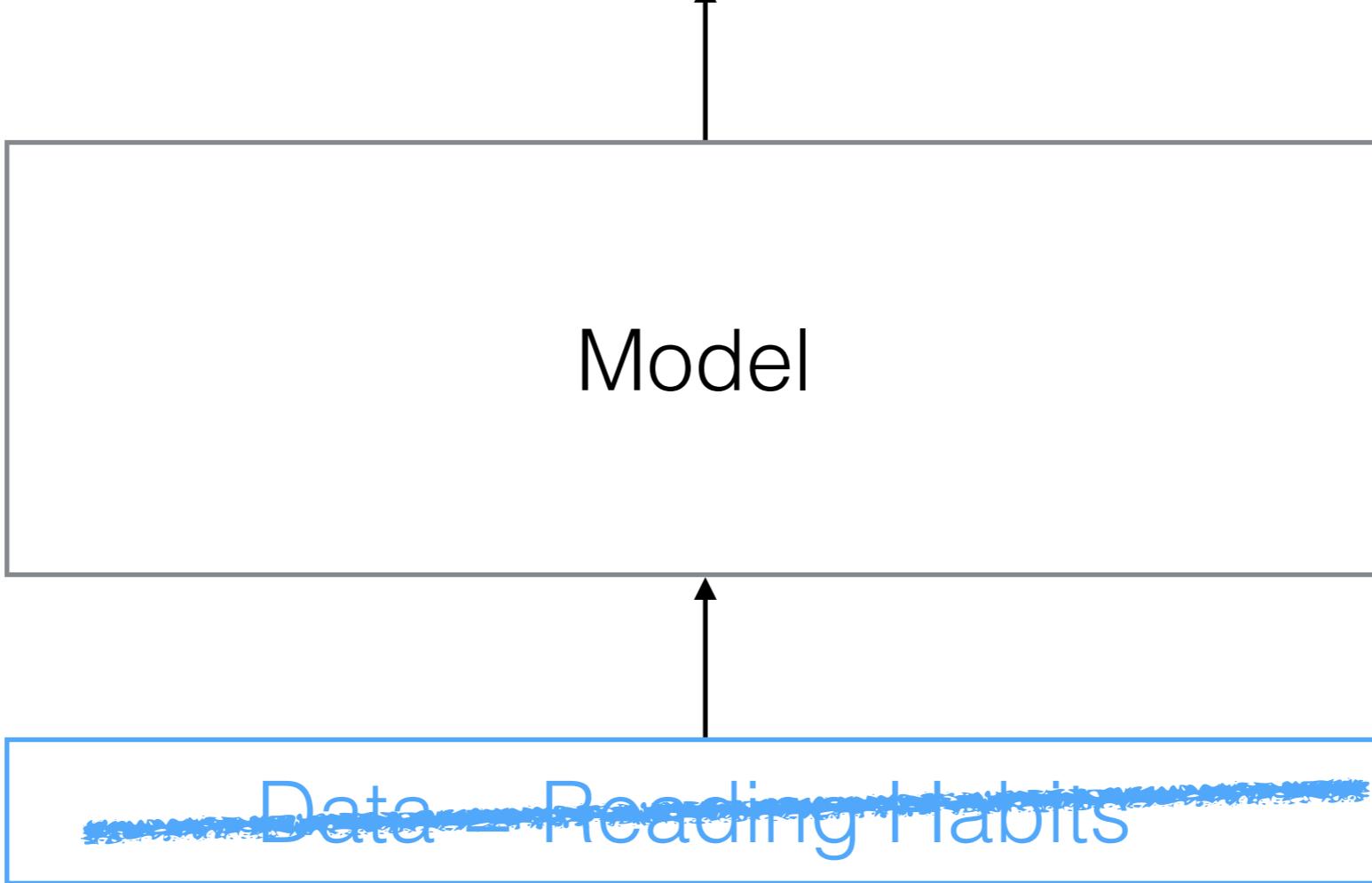
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Defining an ML problem

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Features = ???

Features

- Data = Reading habits collected via ~~unauthorized ever present cookies and remote control of webcam~~ user-consented GDPR-compliant data usage agreements

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 - Article topic
- Features
 - Recency (minutes since release)
 - Words in title/snippet
 - Presence of photo
 - Reading level
 - Fonts/layouts
 - User location
 - Topics of articles the user has read previously
 - Number of likes
 - ...

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Features

- Recency: Float
- Words in title: String
- Presence of photo: Boolean
- Reading level: Integer

Features

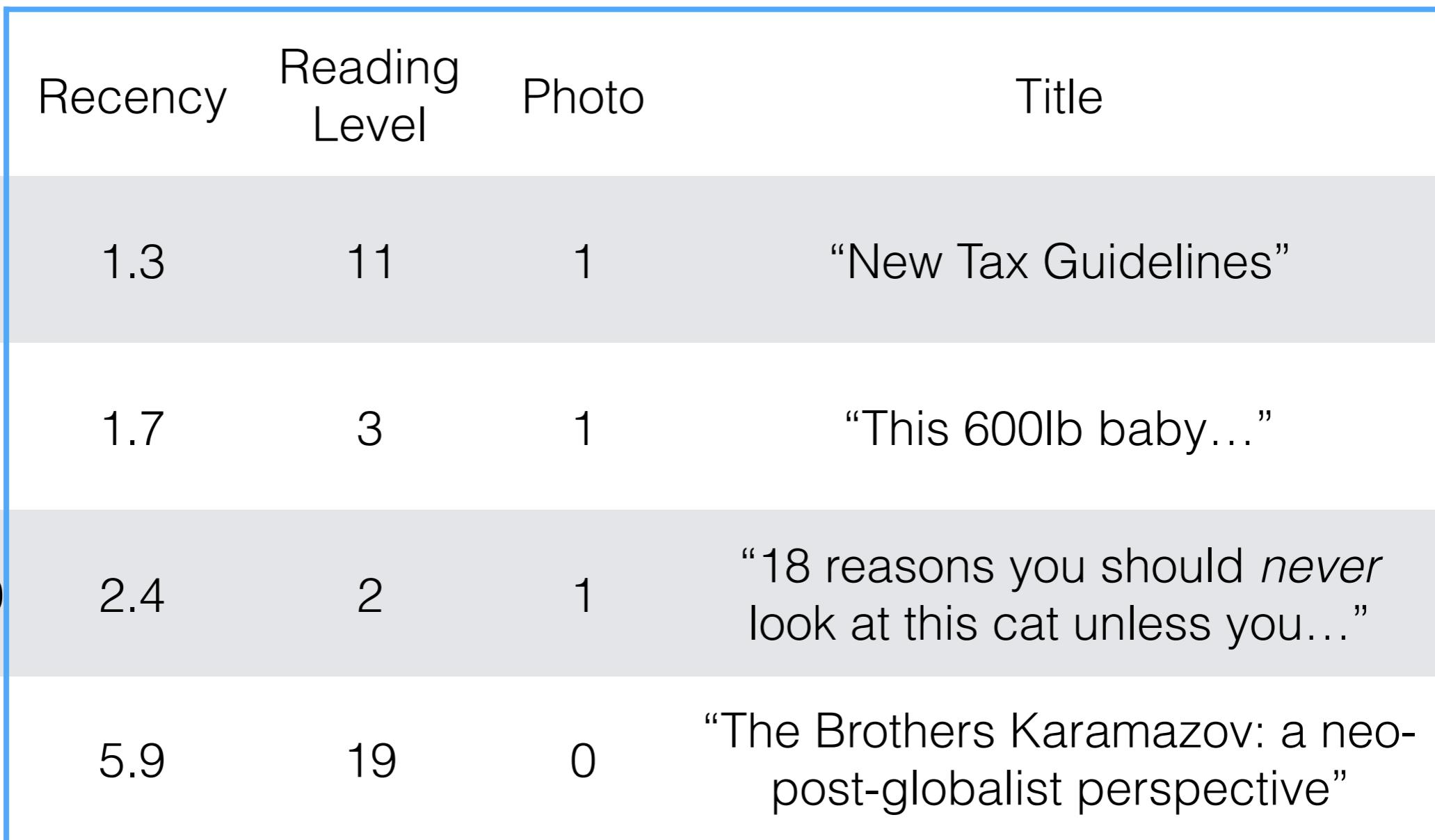
Clicks	Recency	Reading Level	Photo	Title
10	1.3	11	1	“New Tax Guidelines”
1000	1.7	3	1	“This 600lb baby...”
1000000	2.4	2	1	“18 reasons you should <i>never</i> look at this cat unless you...”
1	5.9	19	0	“The Brothers Karamazov: a neo-post-globalist perspective”

Features

4

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Features



A blue 'X' mark is positioned above the table's header row.

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Features

numeric features – defined for (nearly) every row

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boolean features – 0 or 1 ("dummy" variables)

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strings = boolean features – 0 or 1 ("dummy" variables)

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1000	1.7	3	1	0	0	1	1	...
1000000	2.4	2	1	0	0	1	1	...
1	5.9	19	0	0	0	0	0	...

Features

“sparse features” – 0 for most rows

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Clicker Question!

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For the problem set up, how many features will there be? I.e. how many columns in our X matrix, (not including Y)?

Y: happiness

X1: day of week ("monday", "tuesday", ... "sunday")

X2: bank account balance (real value)

X3: breakfast (yes, no)

X4: whether you have found your inner peace
(yes, no)

X5: words from last week's worth of tweets
(assuming tweets are at most 15 words long and
there are 100K words in the English vocabulary)

(a) 112,000

(b) 5

(c) 27

(d) 110,000

Clicker Question!

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Y: happiness

X1: day of week ("monday", "tuesday", ... "sunday") 7

X2: bank account balance (real value) 1

X3: breakfast (yes, no) 1

X4: whether you have found your inner peace 1
(yes, no)

X5: words from last week's worth of tweets 100,000
(assuming tweets are at most 15 words long and
there are 100K words in the English vocabulary)

(a) 100,012

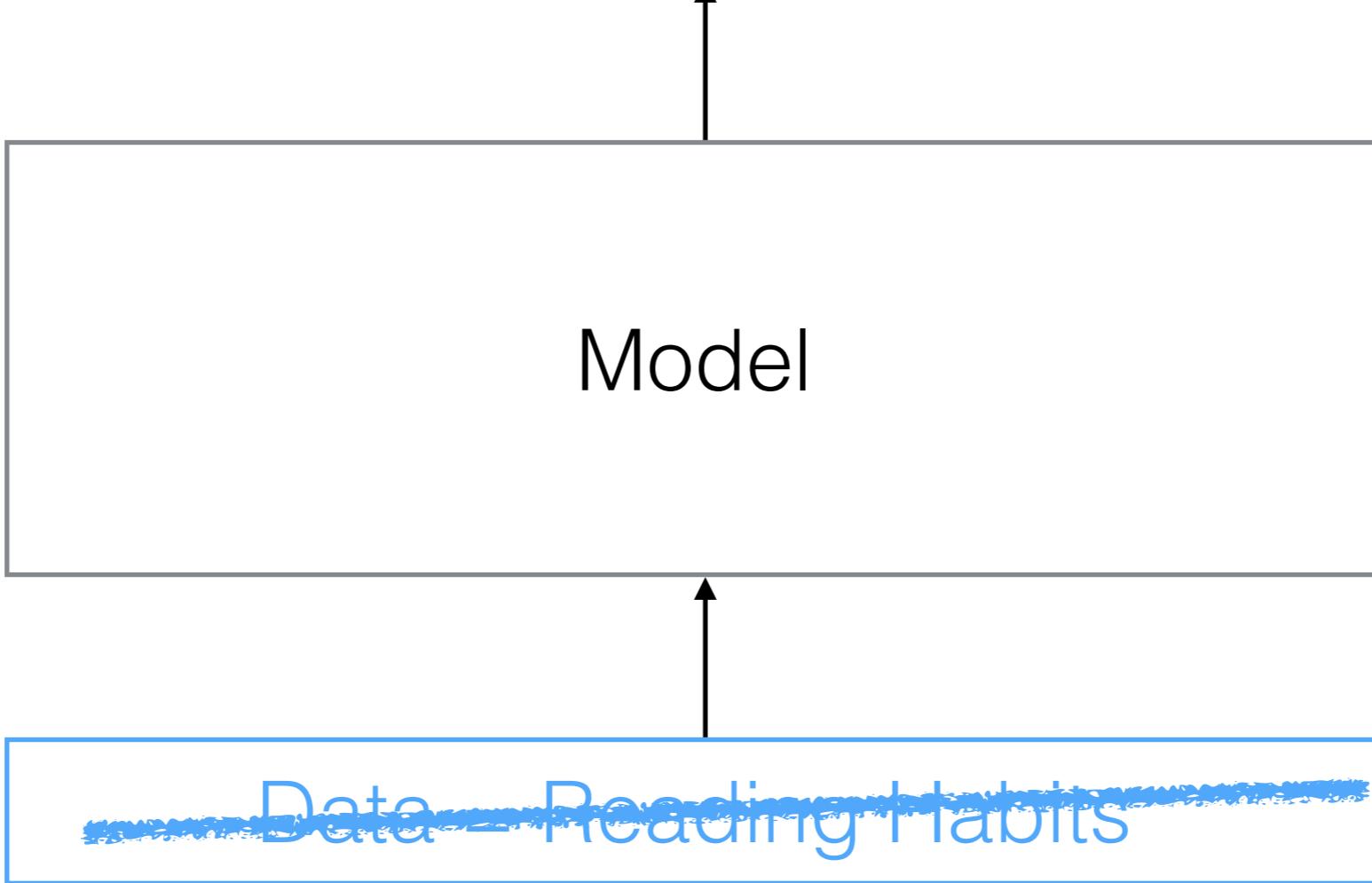
(b) 5

(c) 27

(d) 100,010

Defining an ML problem

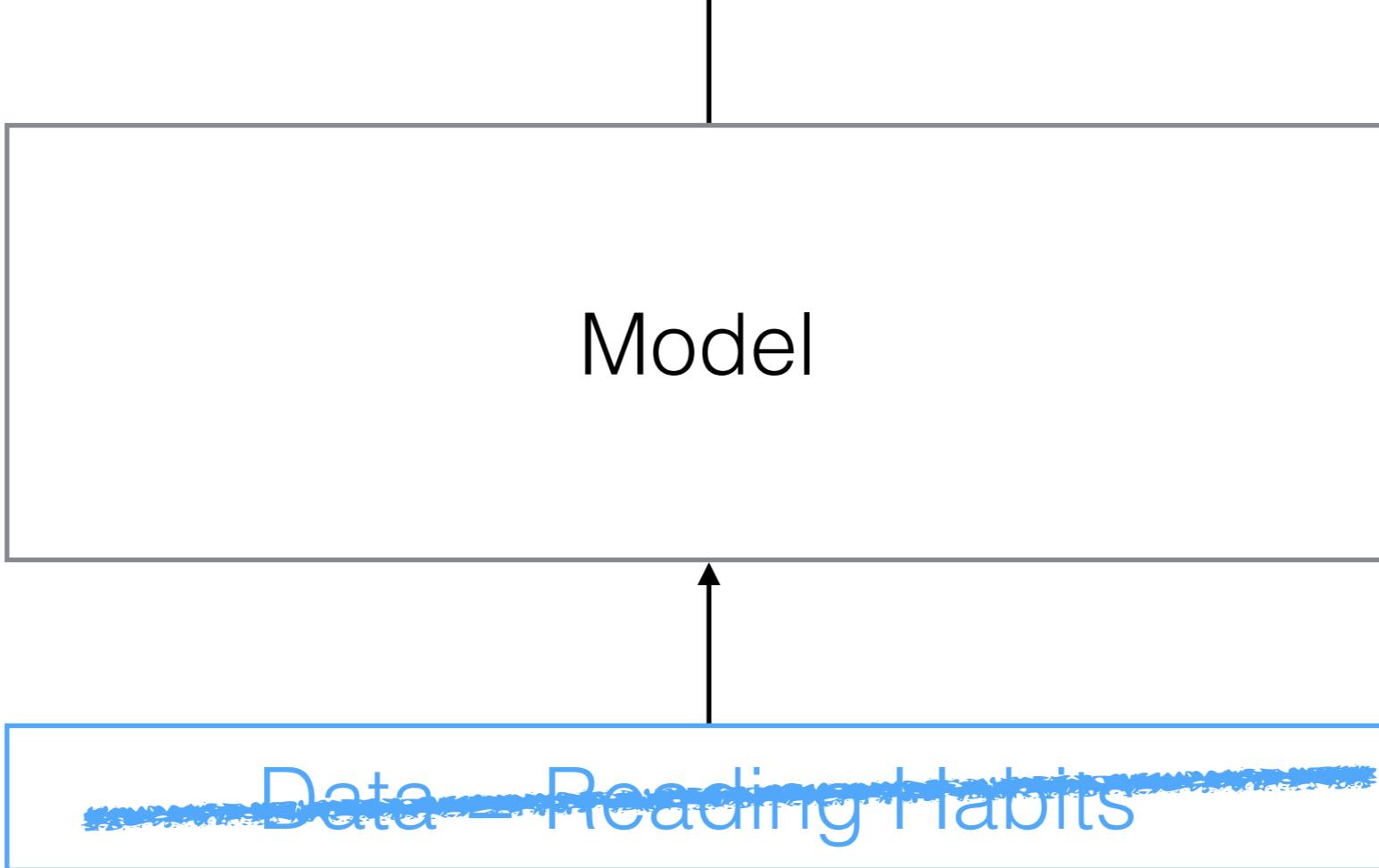
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~~Task — Increase Consumption~~



Features = ???

Defining an ML problem

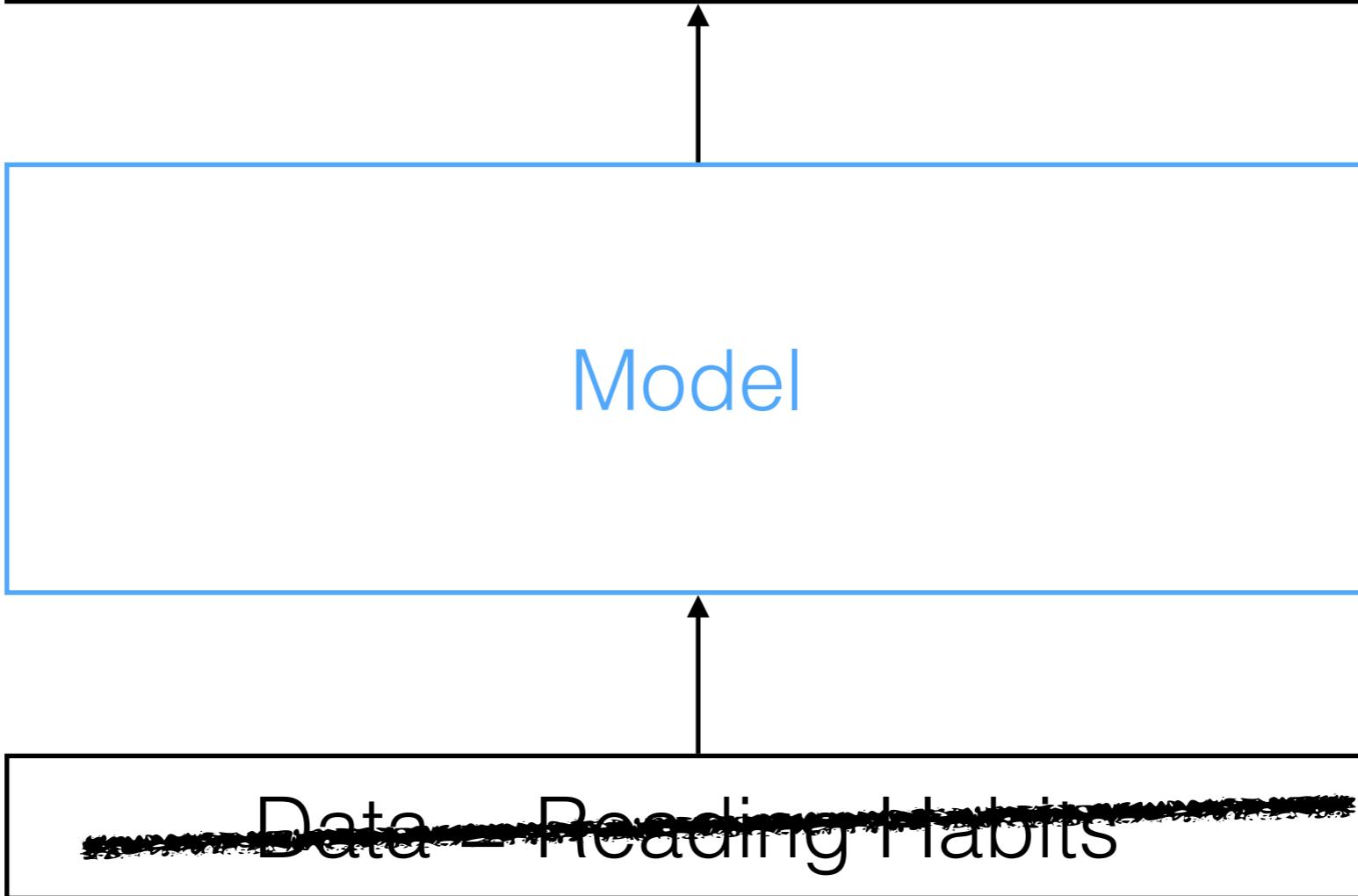
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Features = {Recency:float, ReadingLevel:Int,
Photo:Bool, Title_New:Bool, Title_Tax:Bool, ...}

Defining an ML problem

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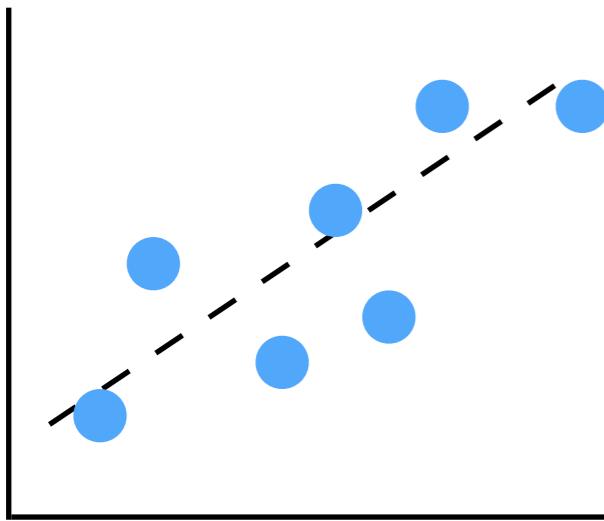
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Photo:Bool, Title_New:Bool, Title_Tax:Bool, ...}

Model

ML = Function Approximation

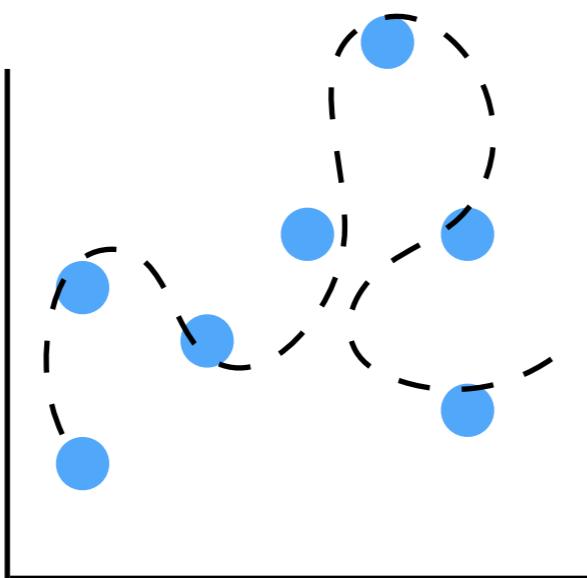
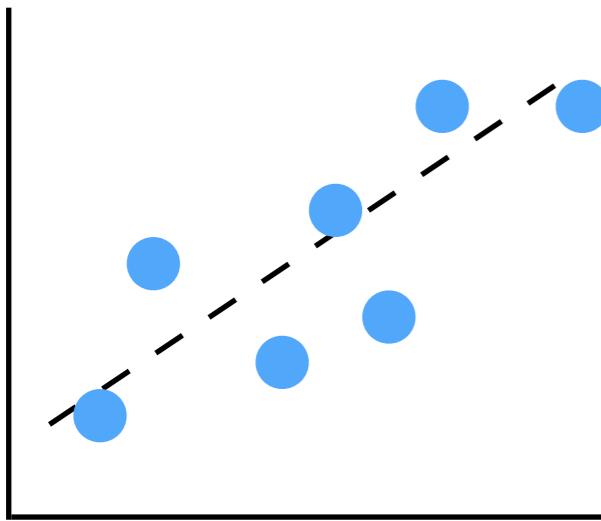
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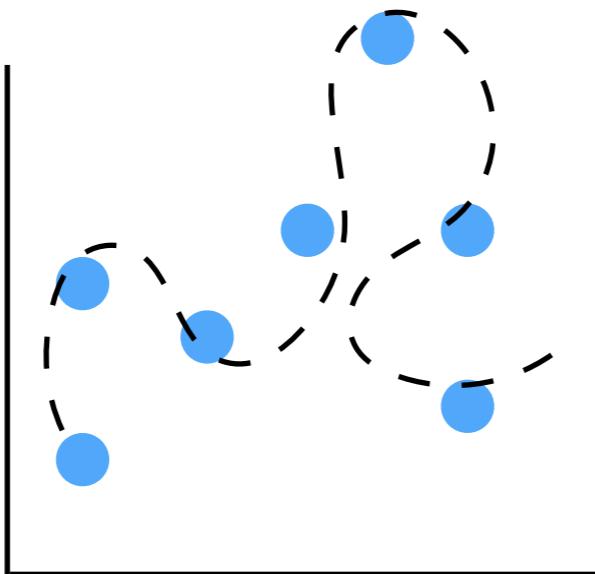
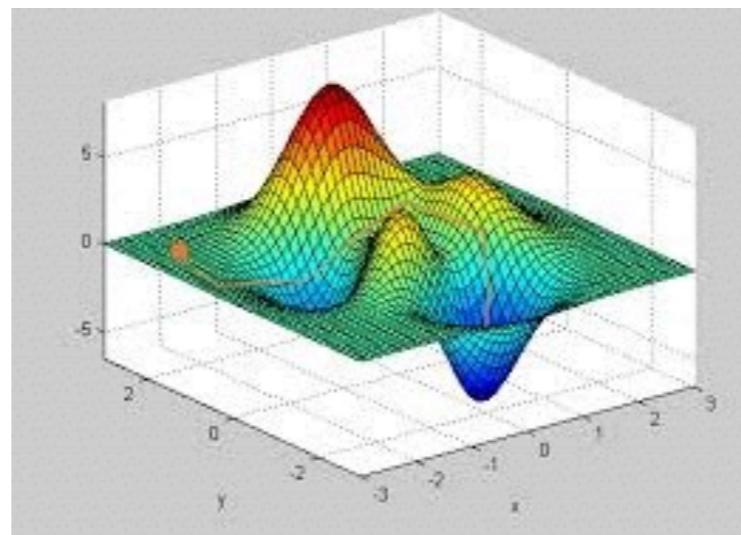
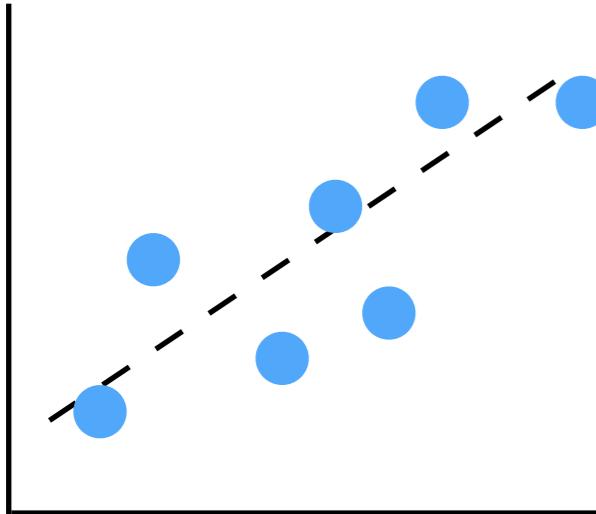
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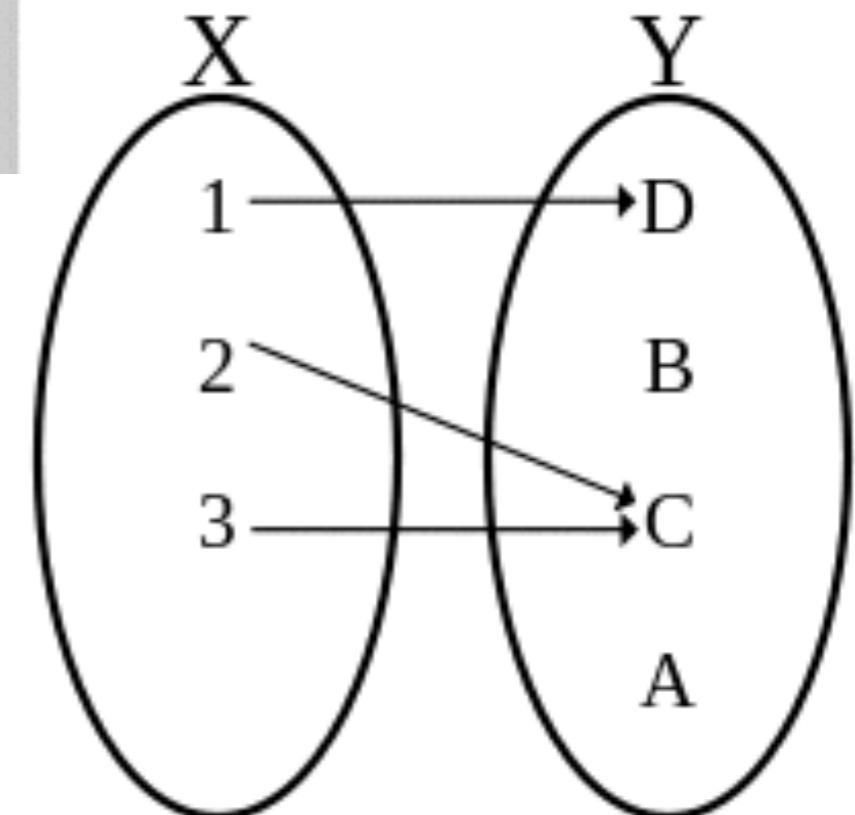
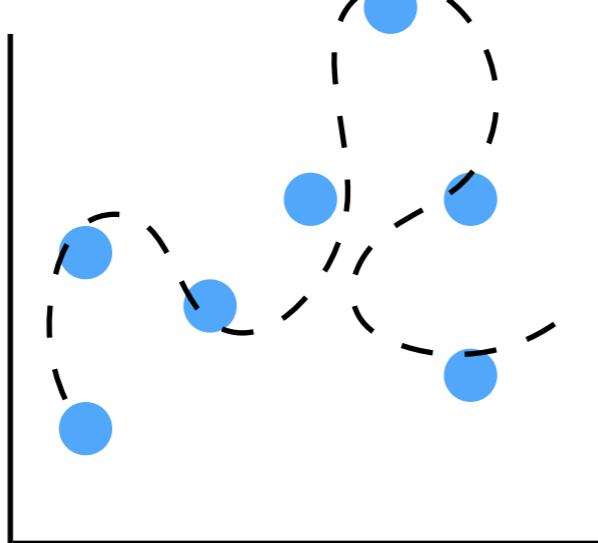
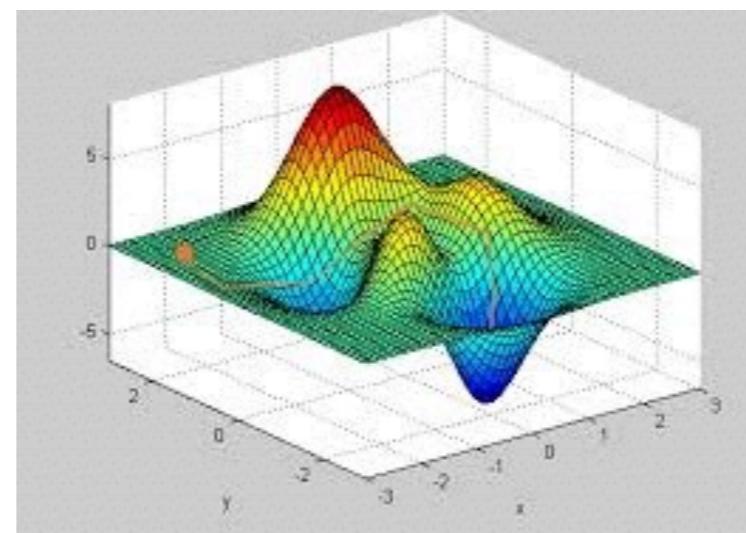
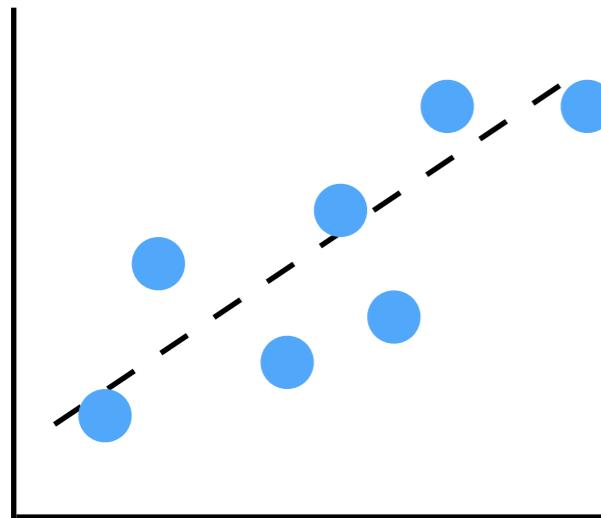
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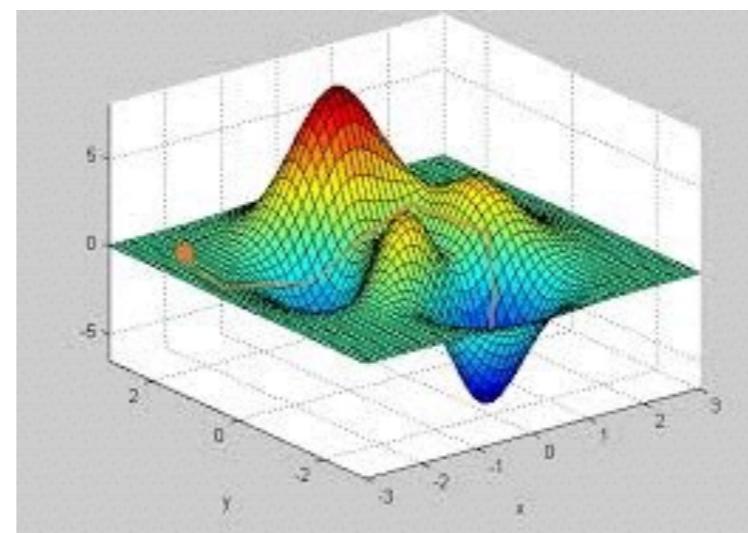
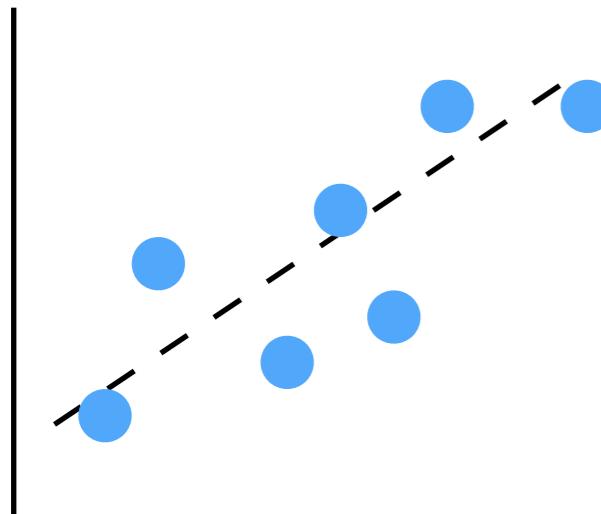
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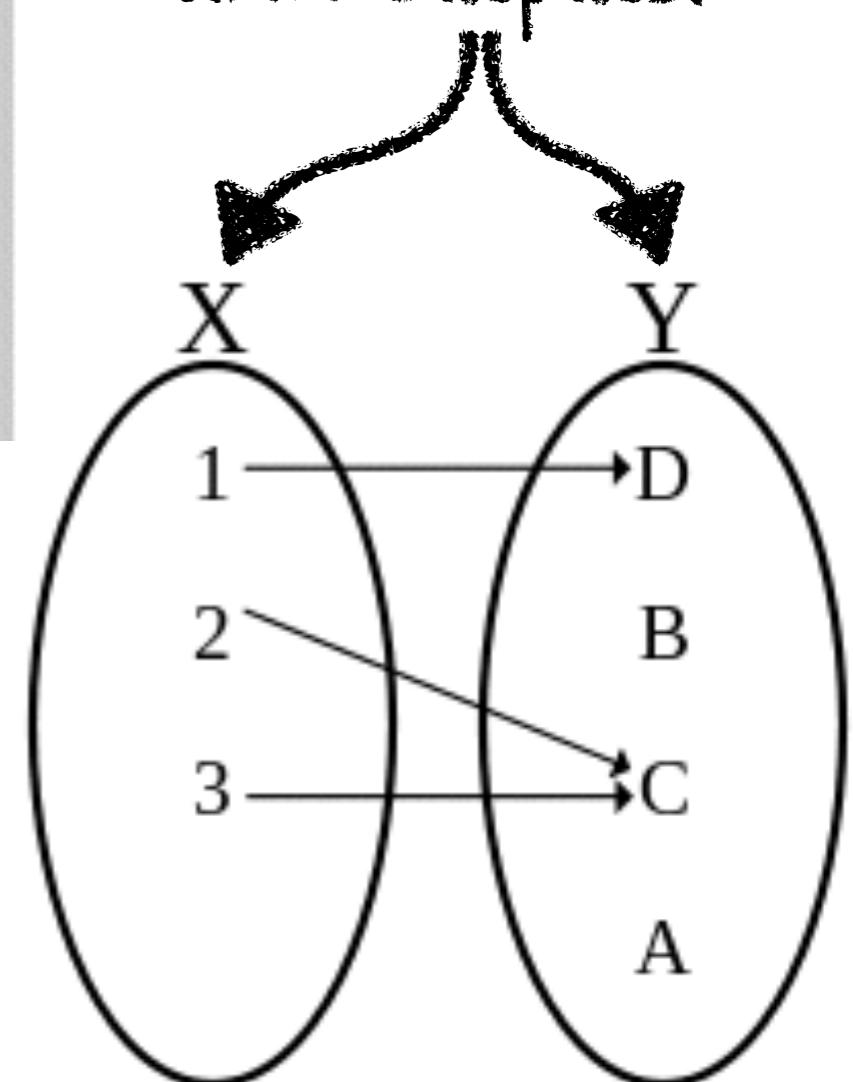
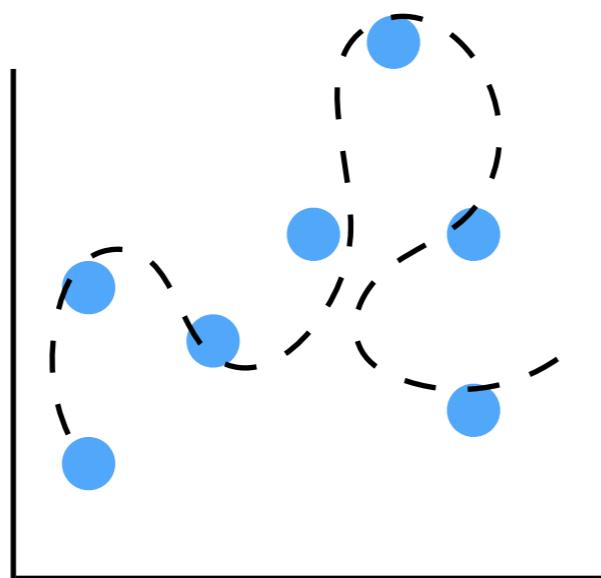


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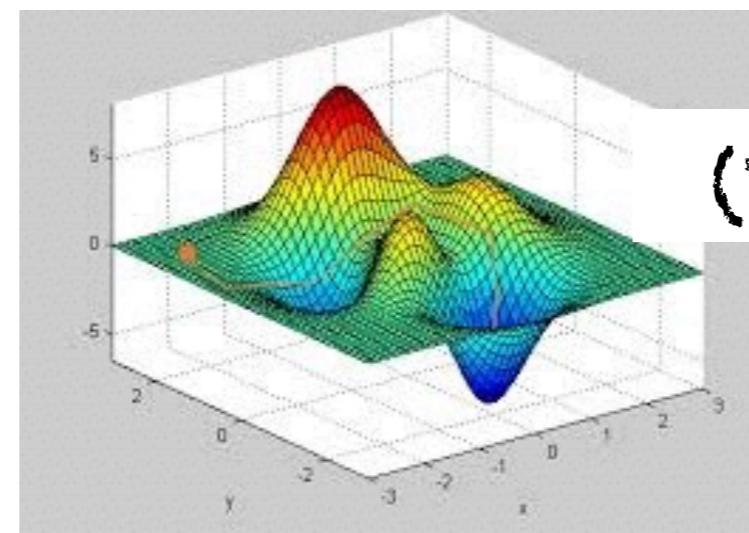
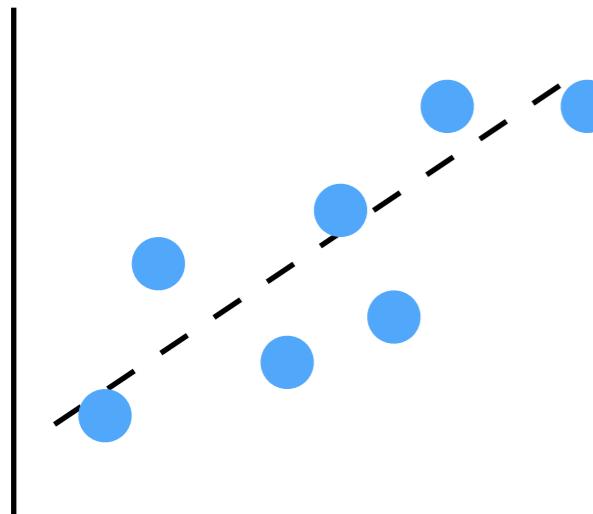


You define inputs
and outputs.

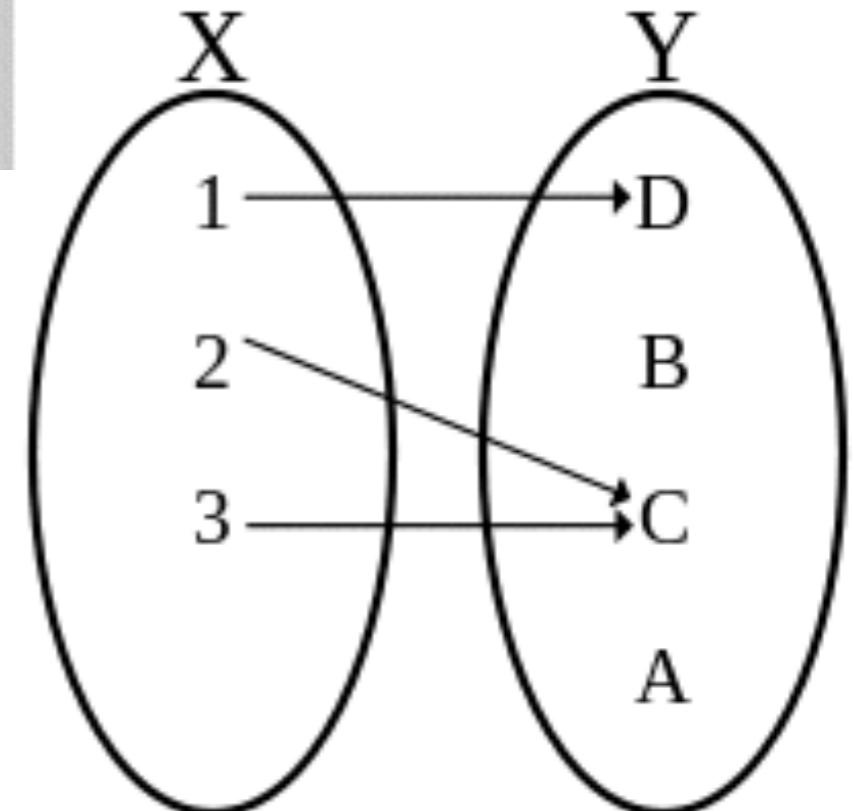
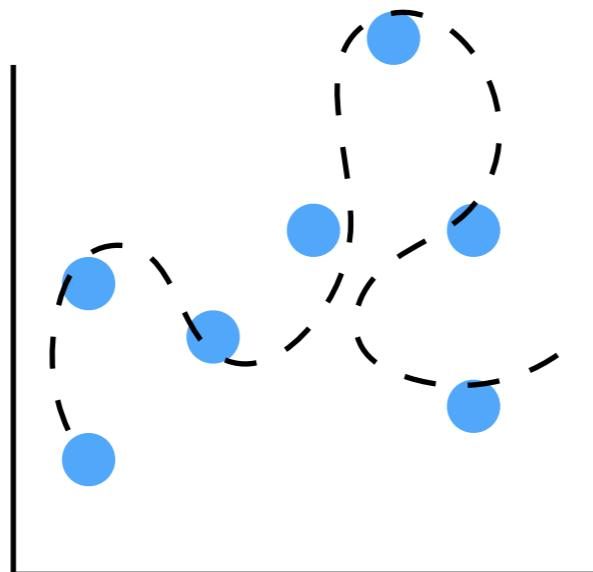


Model

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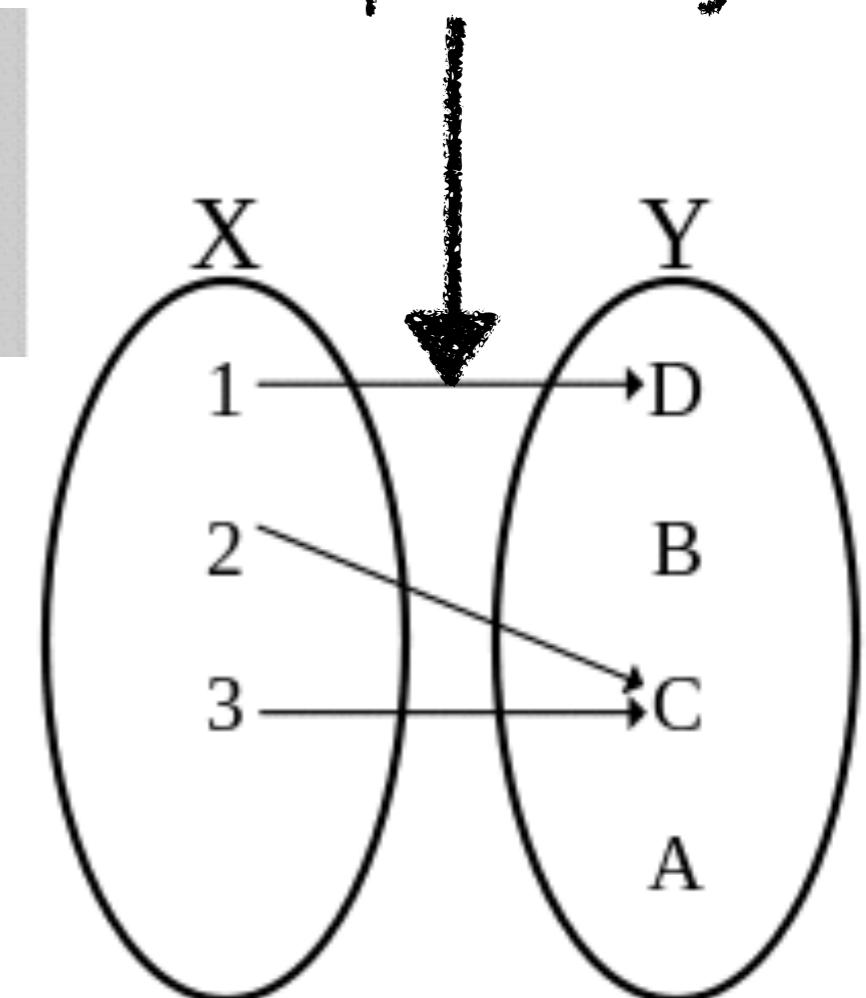
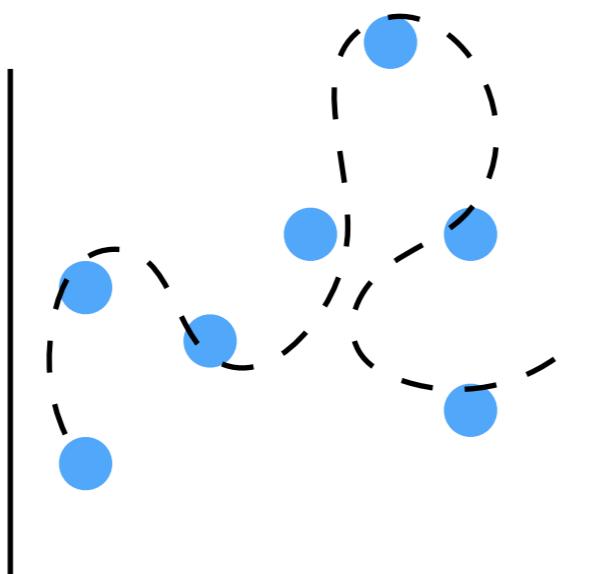
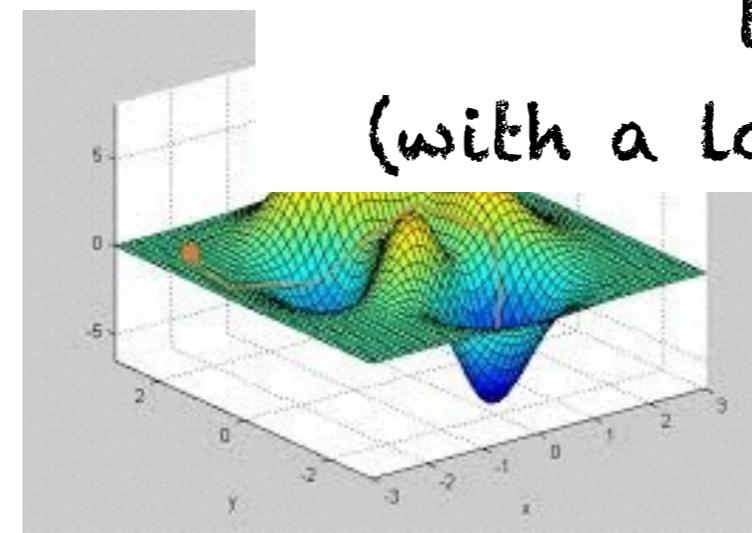
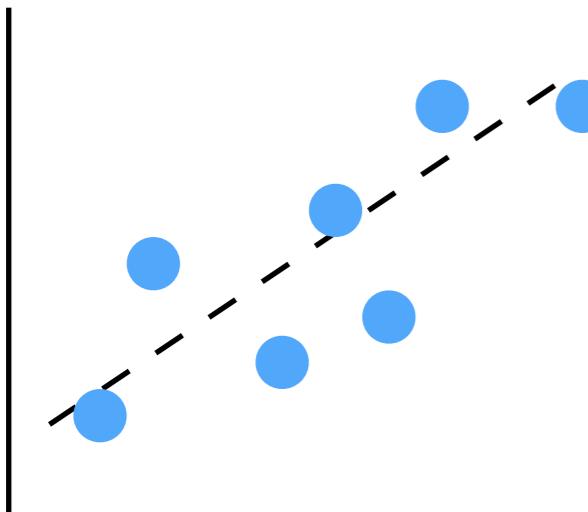
You define inputs
and outputs.
(The really hard part)



Model

ML = Function

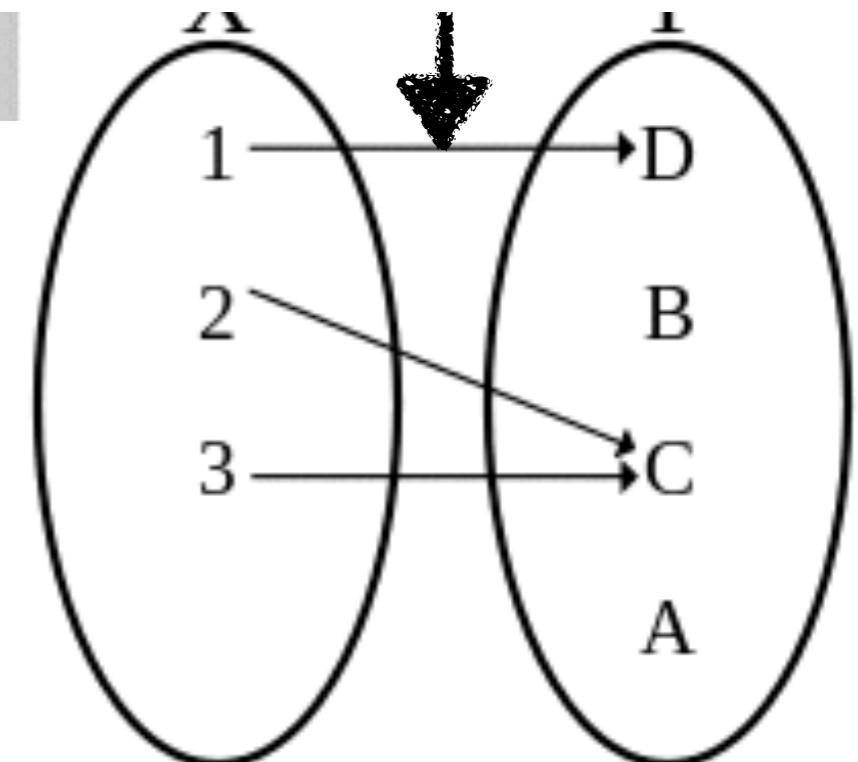
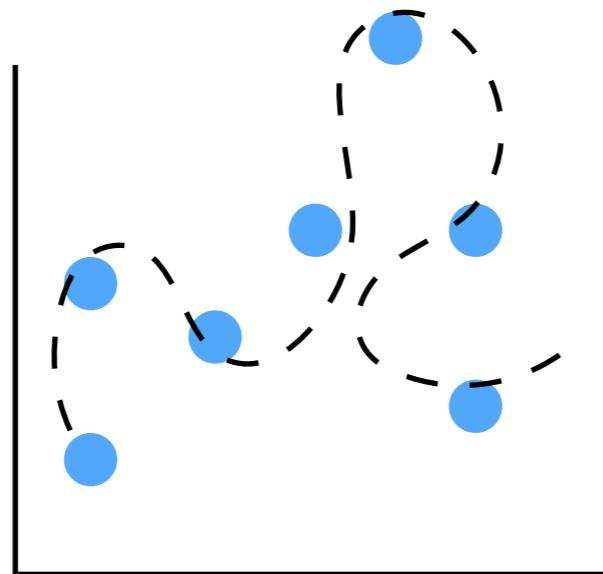
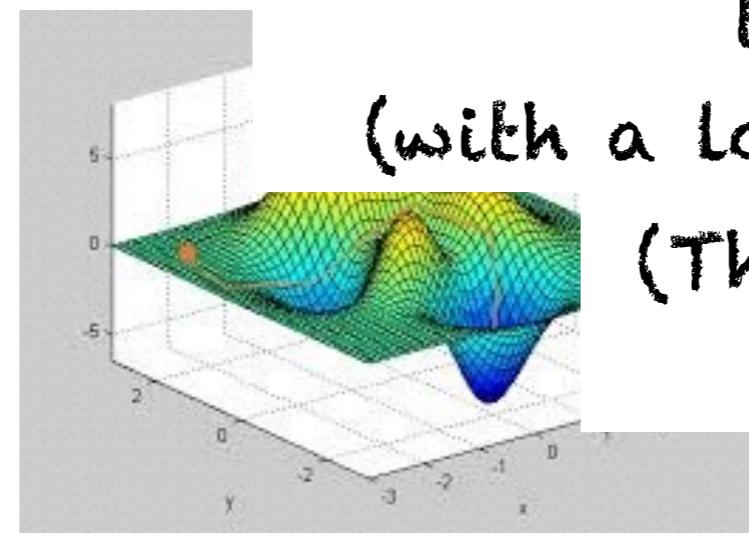
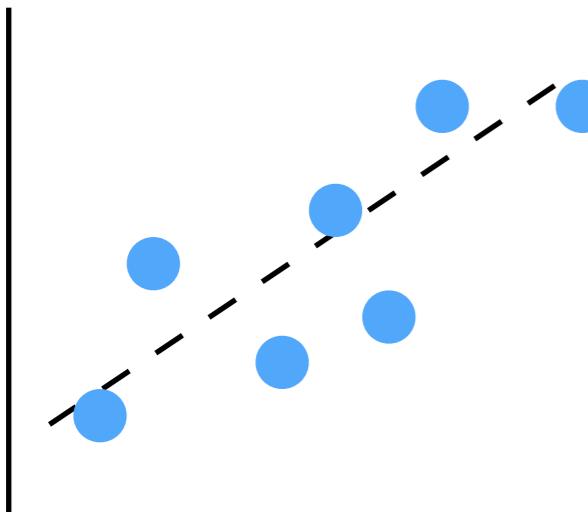
The machine will (ideally) learn
the function
(with a lot of help from you)



Model

ML = Function

The machine will (ideally) learn
the function
(with a lot of help from you)
(The part that gets the
most attention.)



Model

#1

- Make assumptions about the problem domain.

Model

#1

- Make assumptions about the problem domain.
- How is the data generated?

Model

#1

- Make assumptions about the problem domain.
- How is the data generated?
- How is the decision-making procedure structured?

Model

#1

- Make assumptions about the problem domain.
- How is the data generated?
- How is the decision-making procedure structured?
- What types of dependencies exist?

Model

#1

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- How is the data generated?
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- What types of dependencies exist?
- Trending buzzword: “inductive biases”

Model

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- How is the decision-making procedure structured?
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- Trending buzzword: “inductive biases”

#2

- How to train the model?

Model

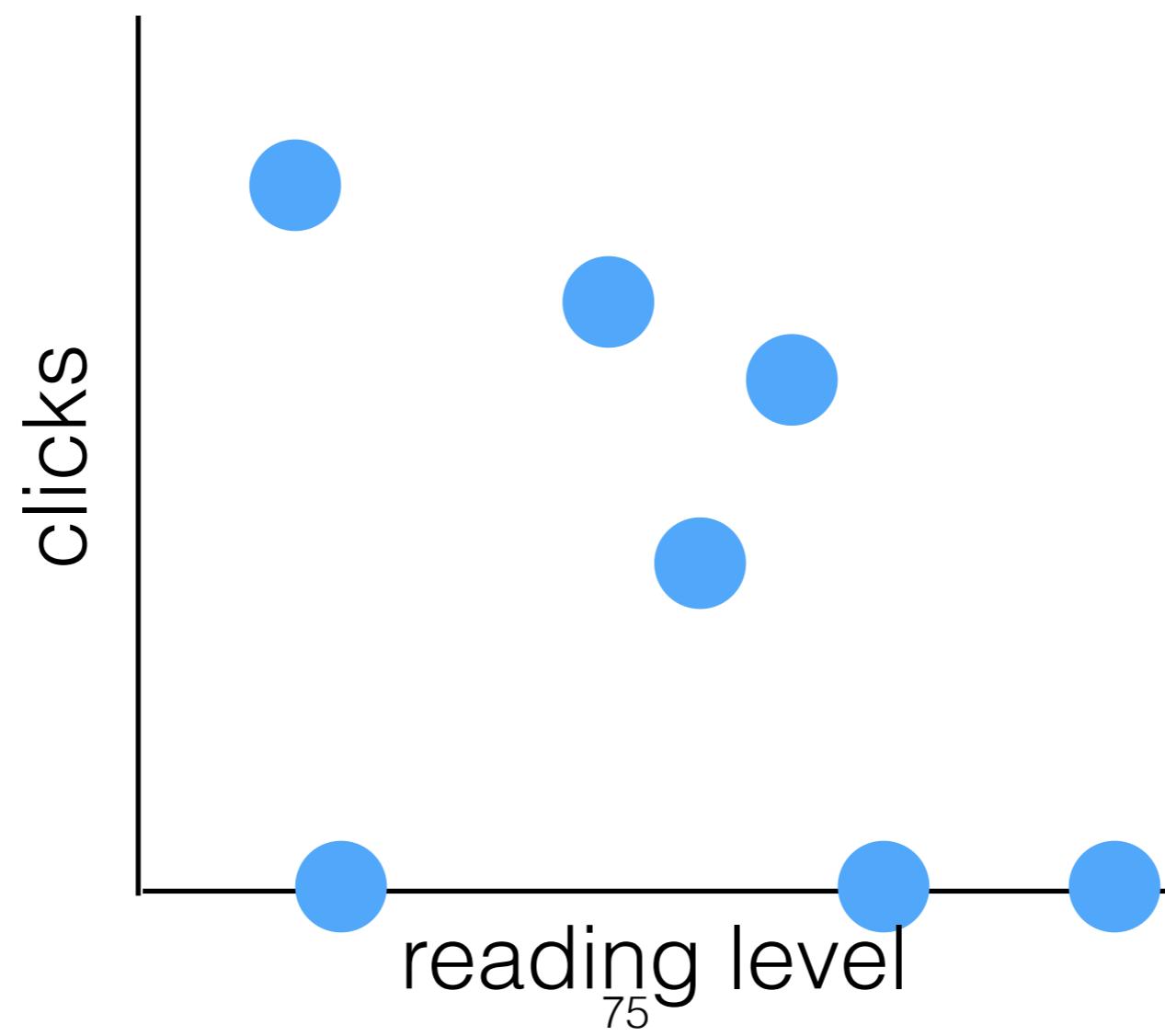
#1

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- What types of dependencies exist?
- Trending buzzword: “inductive biases”

#2

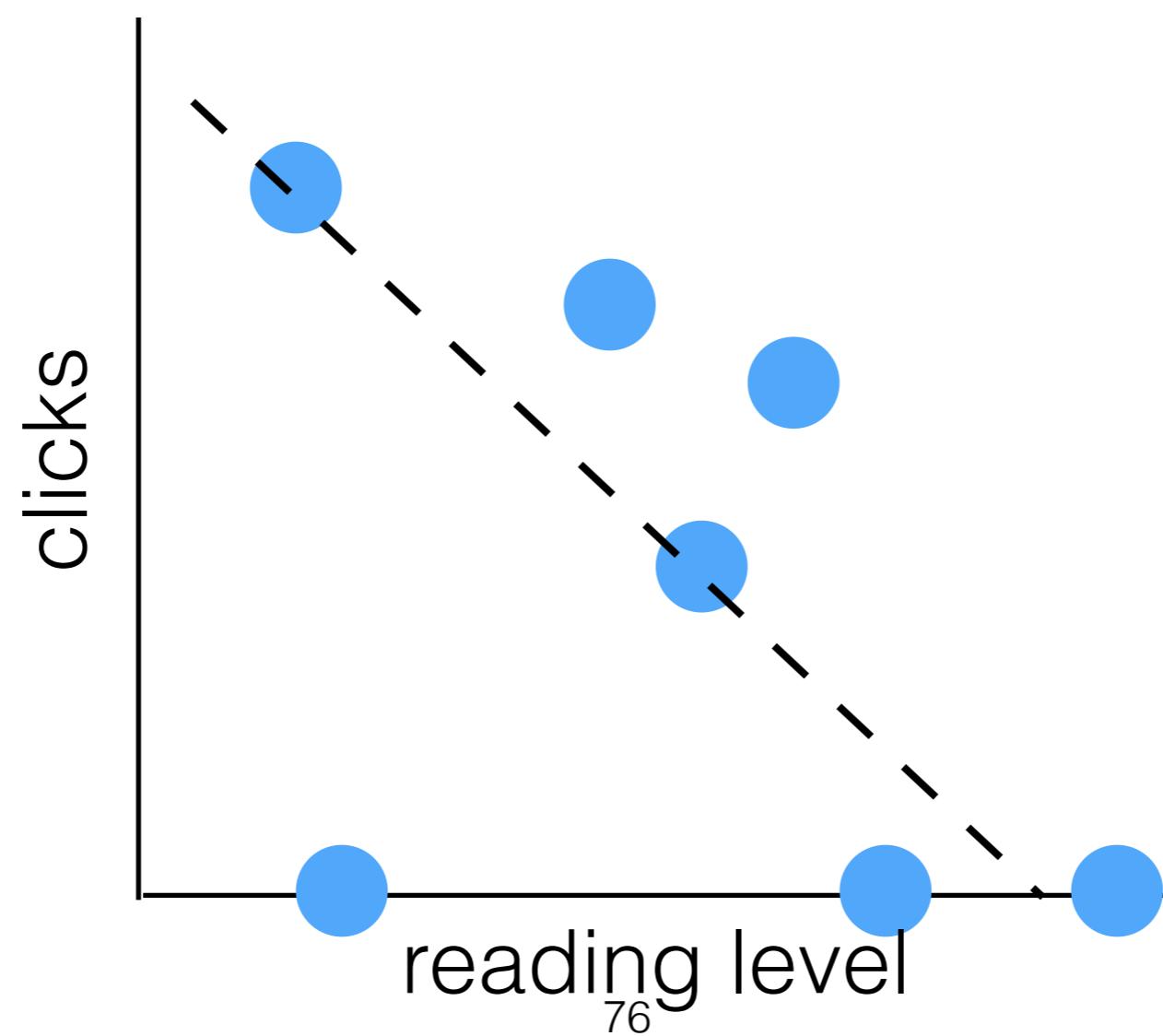
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Model



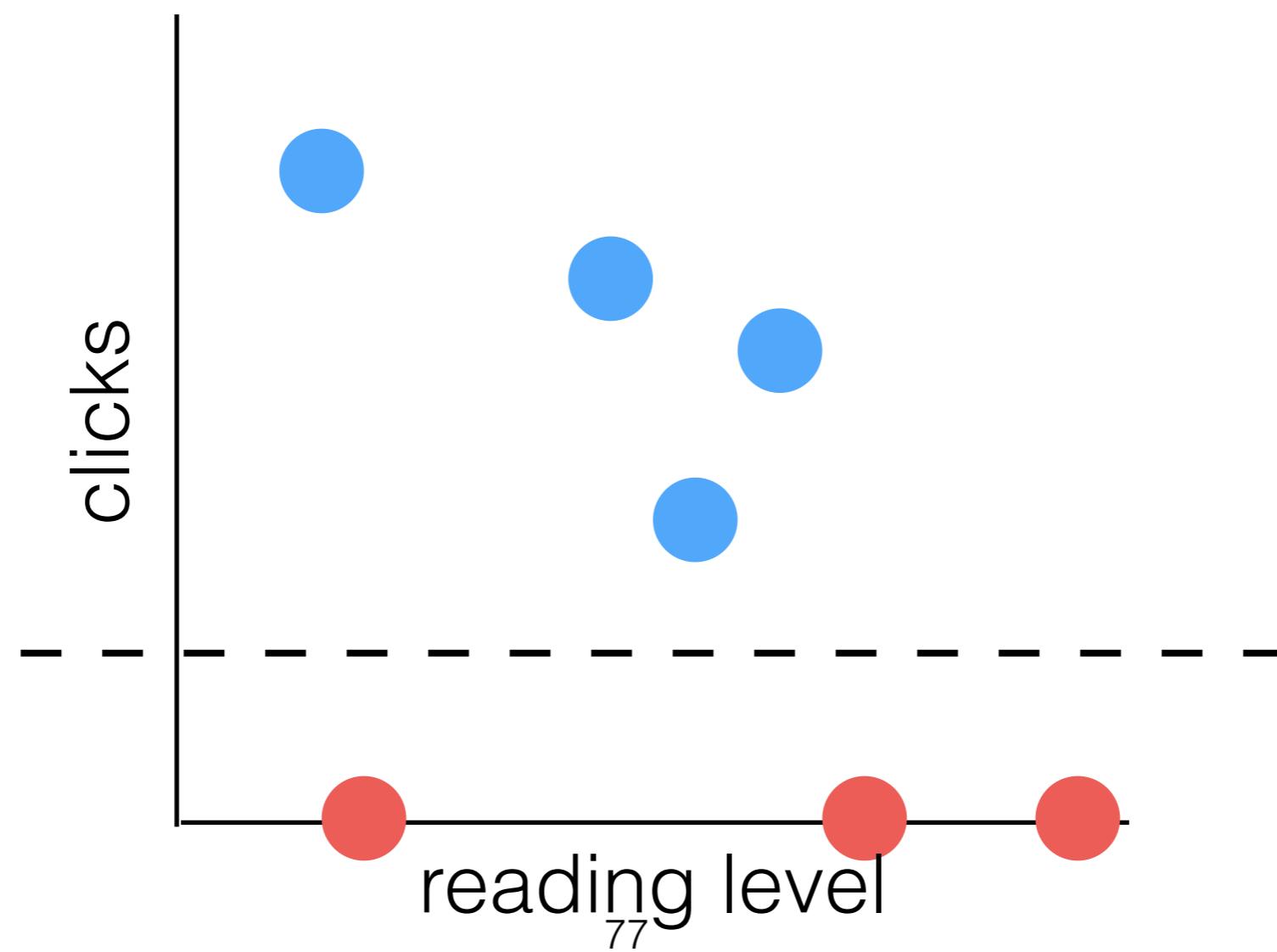
Model

Regression: continuous (infinite) output
 $f(\text{reading level}) = \# \text{ of clicks}$



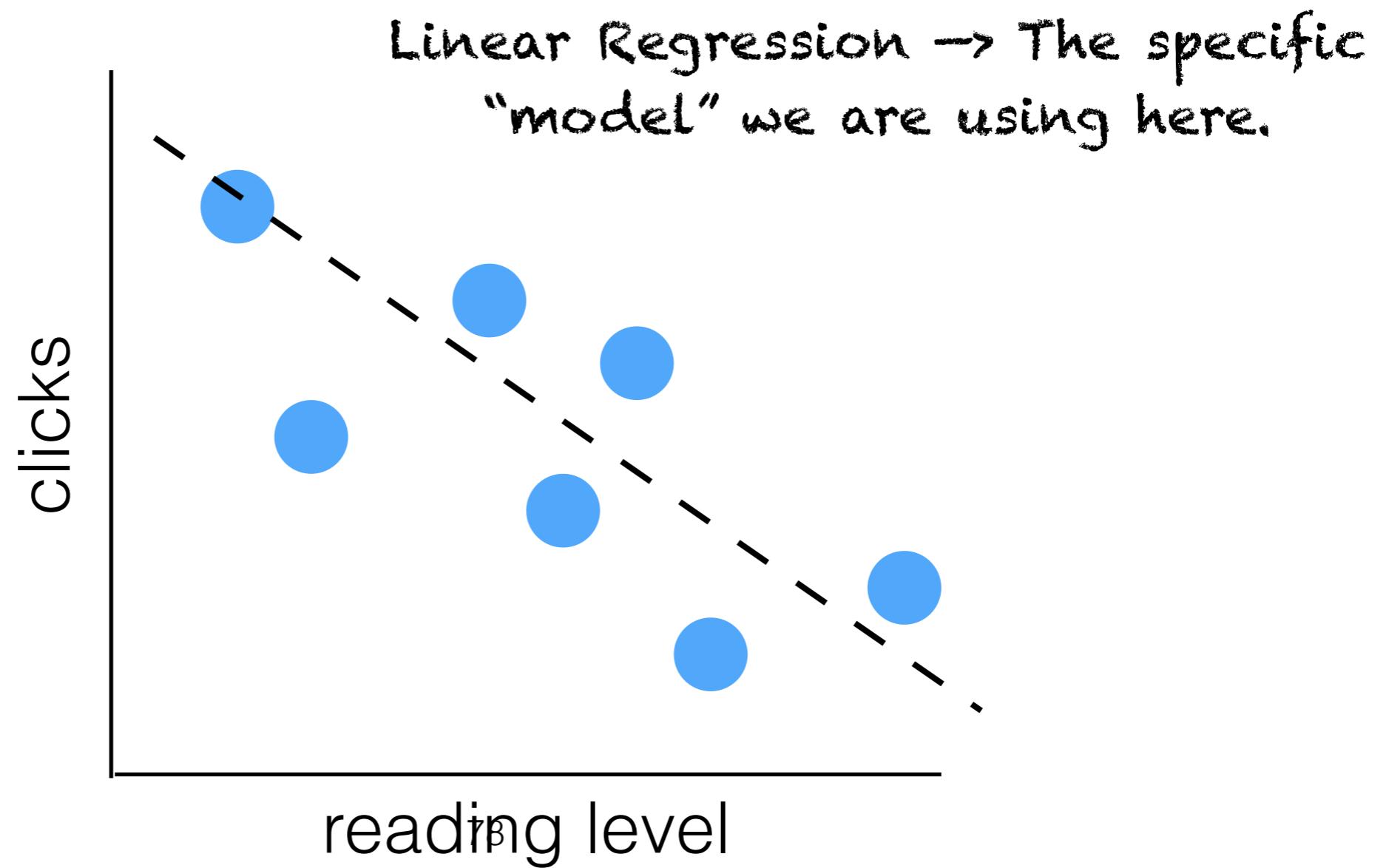
Model

Classification: discrete (finite) output
 $f(\text{reading level}) = \{\text{clicked}, \text{not clicked}\}$



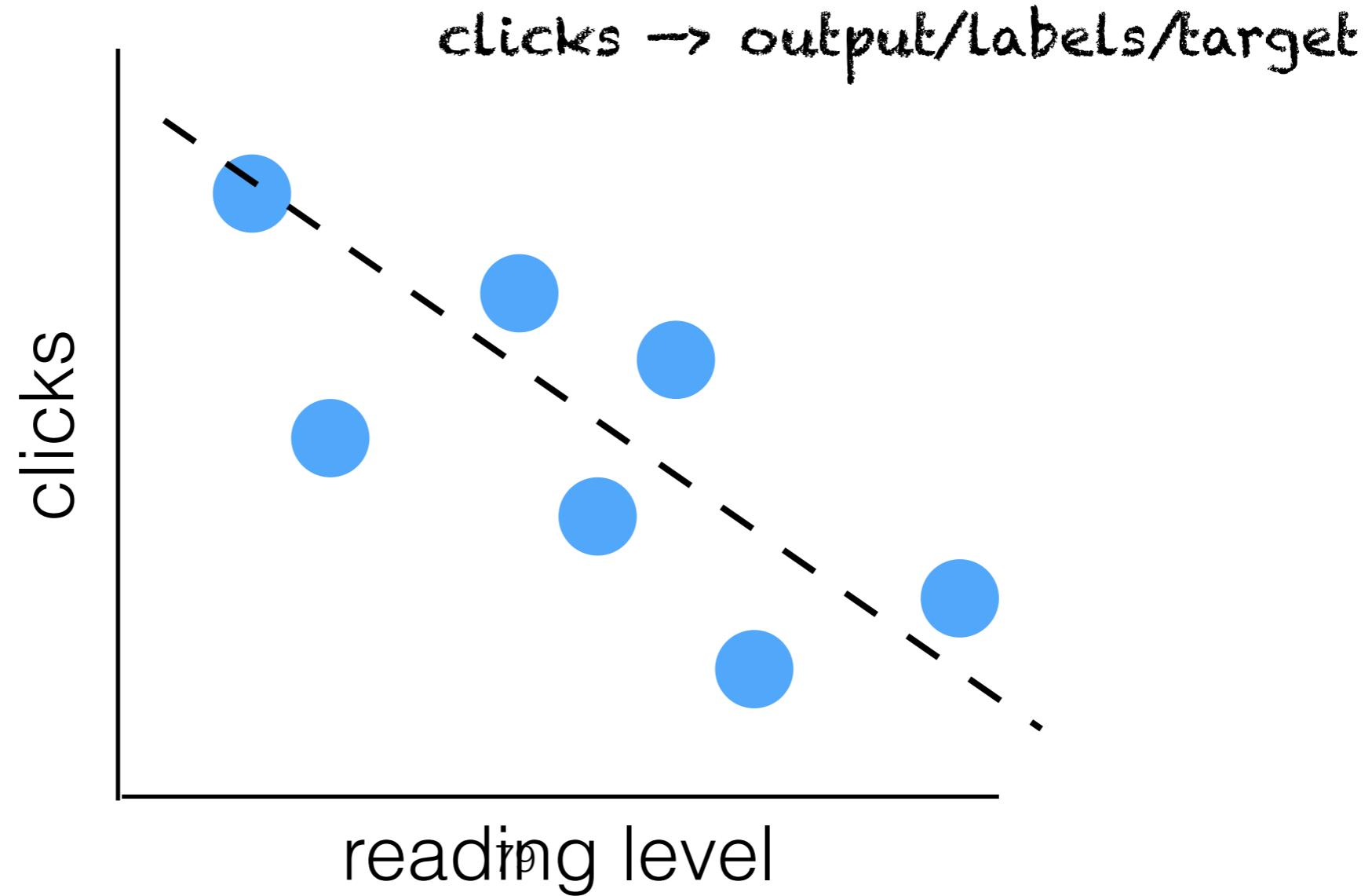
Model

clicks = m(reading_level) + b



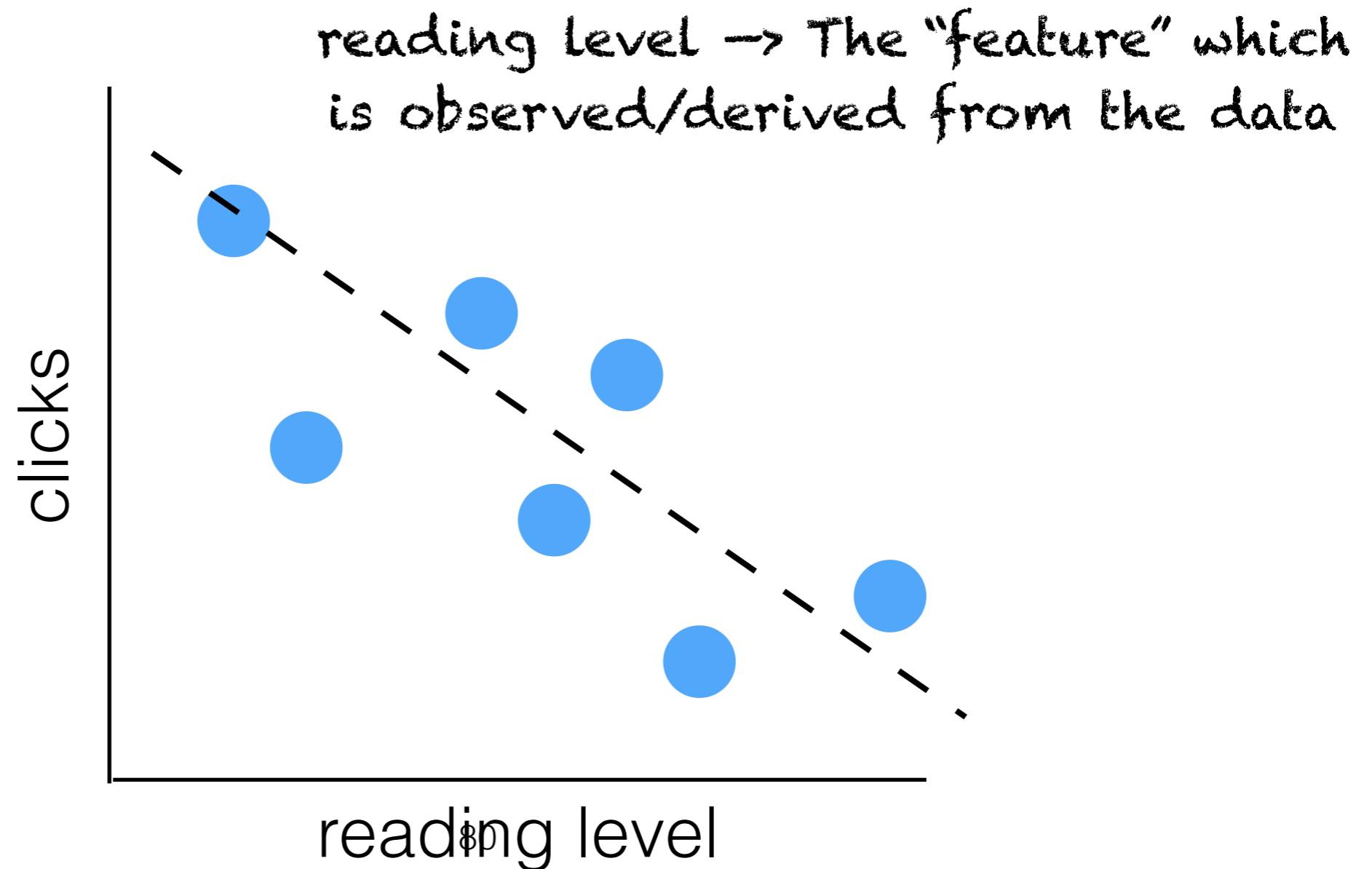
Model

$$\text{clicks} = m(\text{reading_level}) + b$$



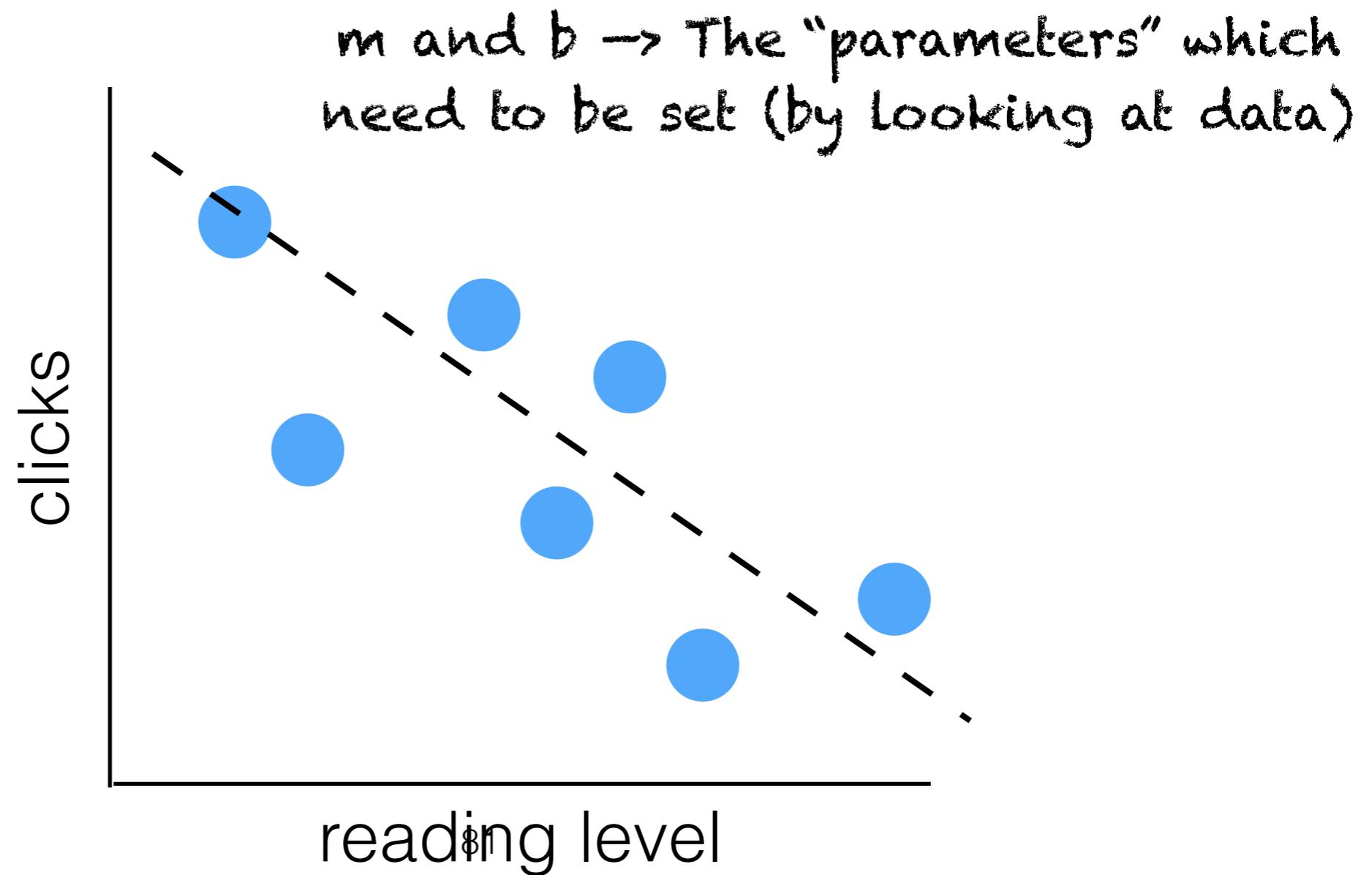
Model

$$\text{clicks} = m(\text{reading_level}) + b$$



Model

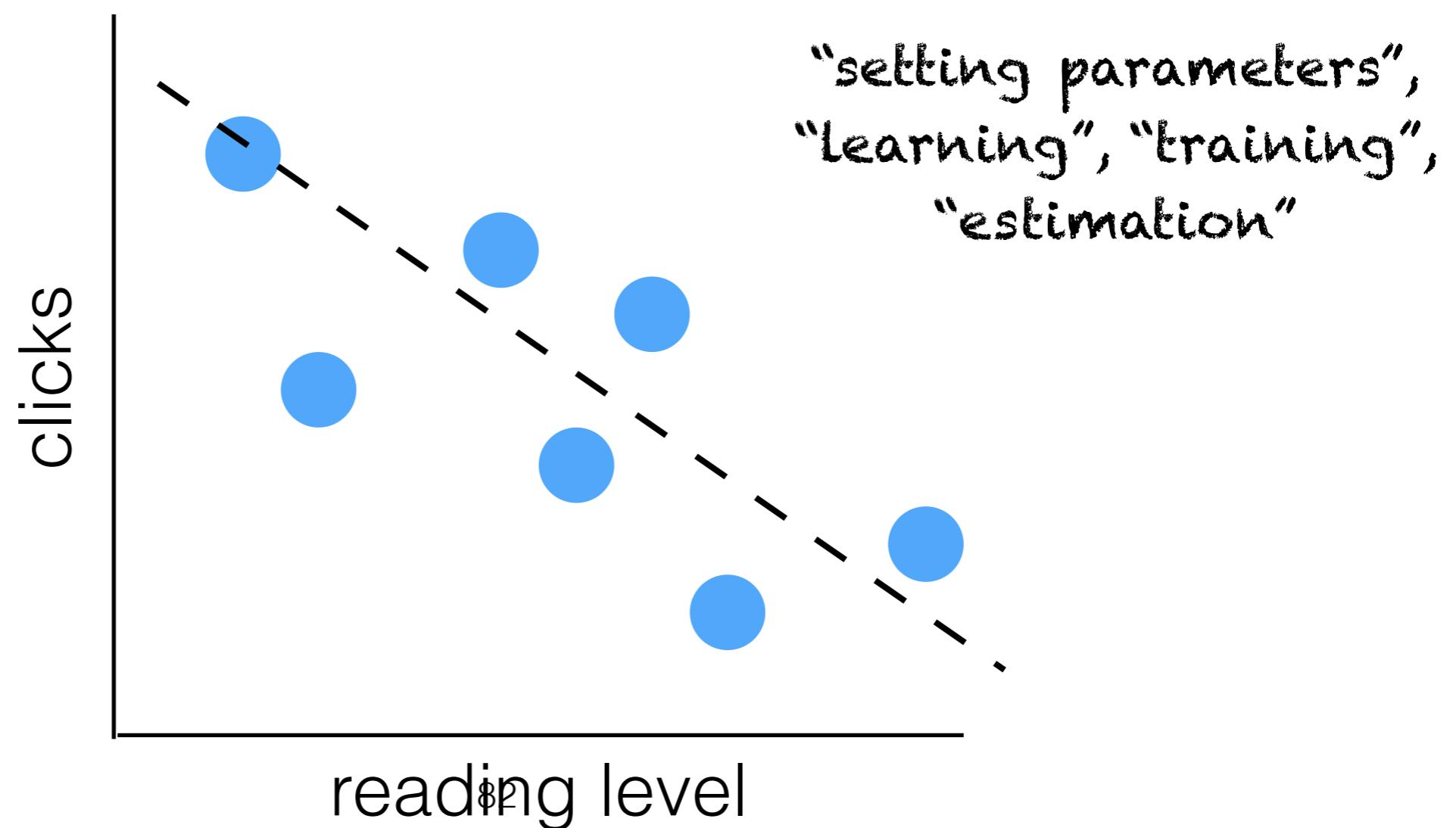
$$\text{clicks} = m(\text{reading_level}) + b$$



Model

`clicks = m(reading_level) + b`

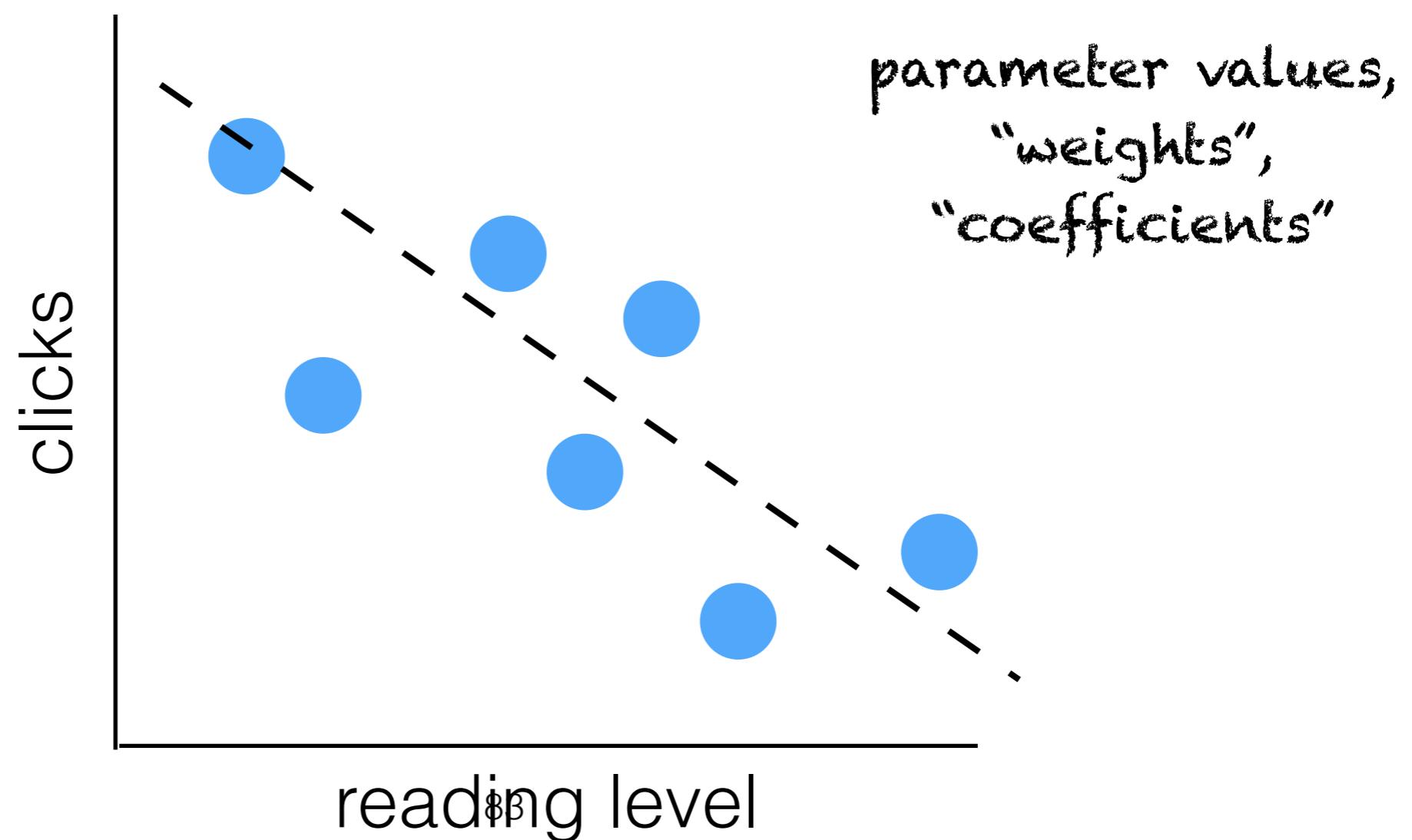
`m = cov(rl, c) / var(rl)`



Model

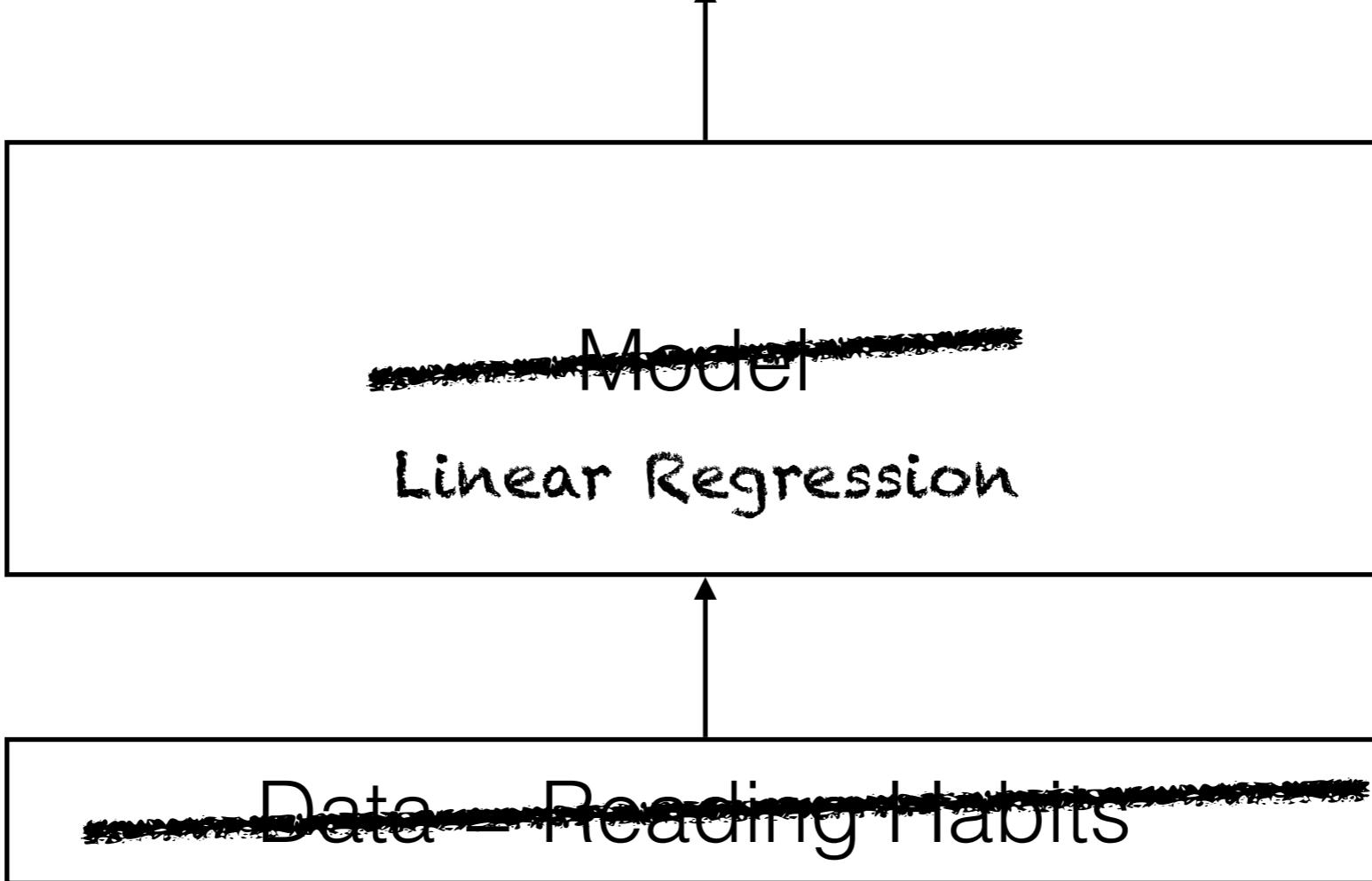
$$\text{clicks} = m(\text{reading_level}) + b$$

$m = -2.4$



Defining an ML problem

Objective/Loss Function = squared difference
between predicted total number of clicks and
actual total number of clicks
~~Task — Increase Consumption~~



Features = {Recency:float, ReadingLevel:Int,
Photo:Bool, Title_New:Bool, Title_Tax:Bool, ...}

Defining an ML problem

Objective/Loss Function = squared difference between predicted total number of clicks and actual total number of clicks

Linear Regression

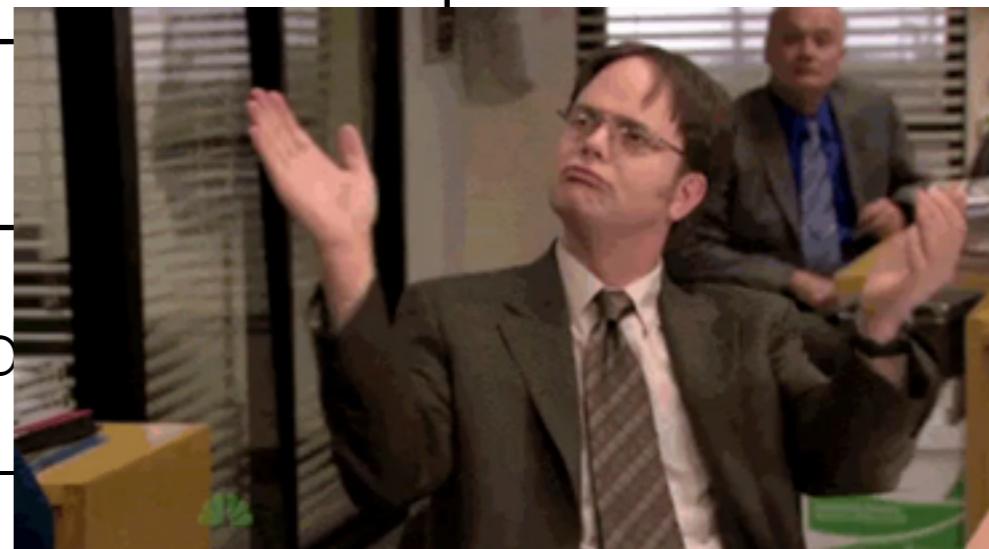
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Defining an ML problem

Objective/Loss Function = squared difference between predicted total number of clicks and actual total number of clicks

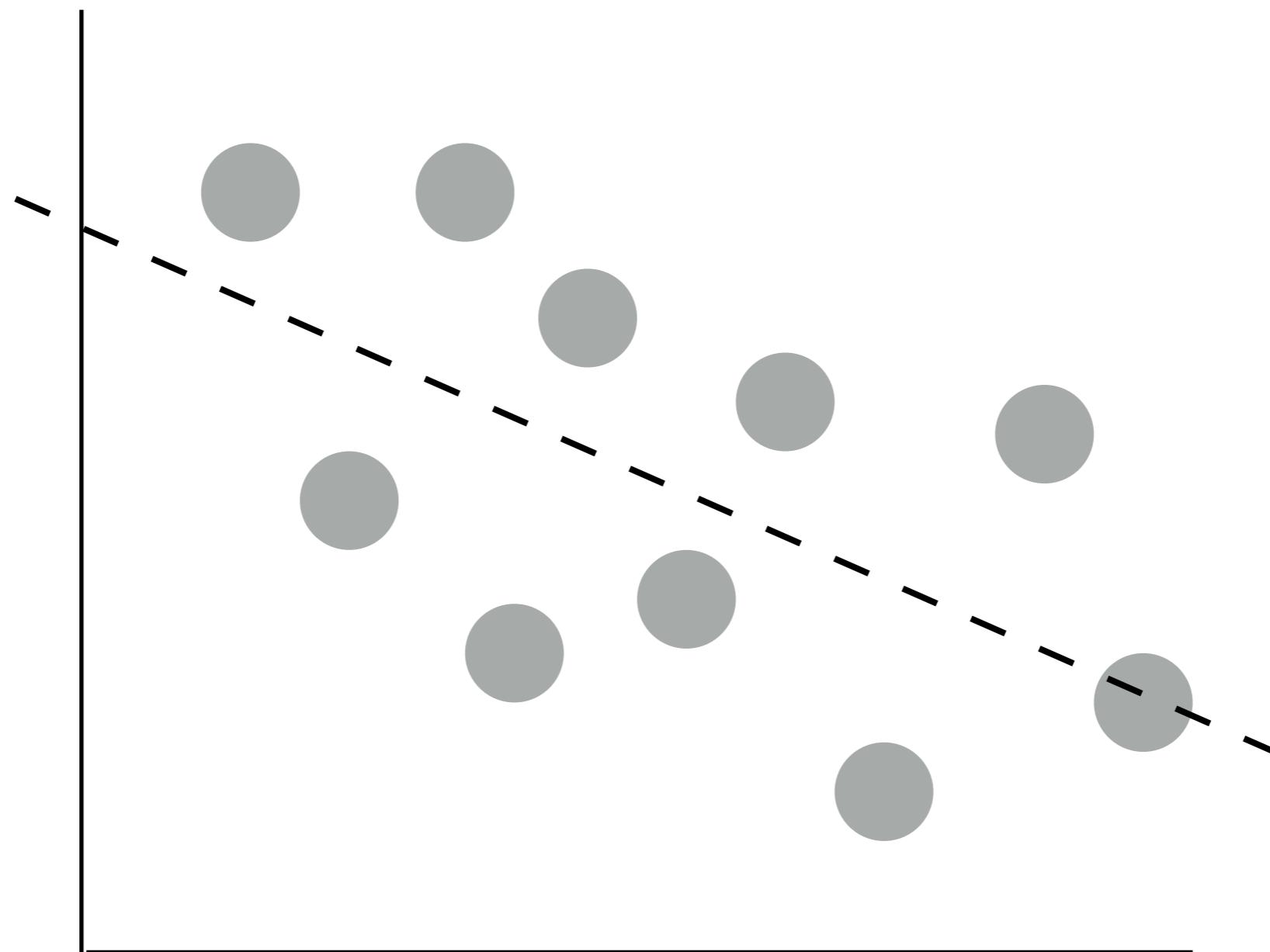
Soooo...how do I know if my model is good?

Linear Regression

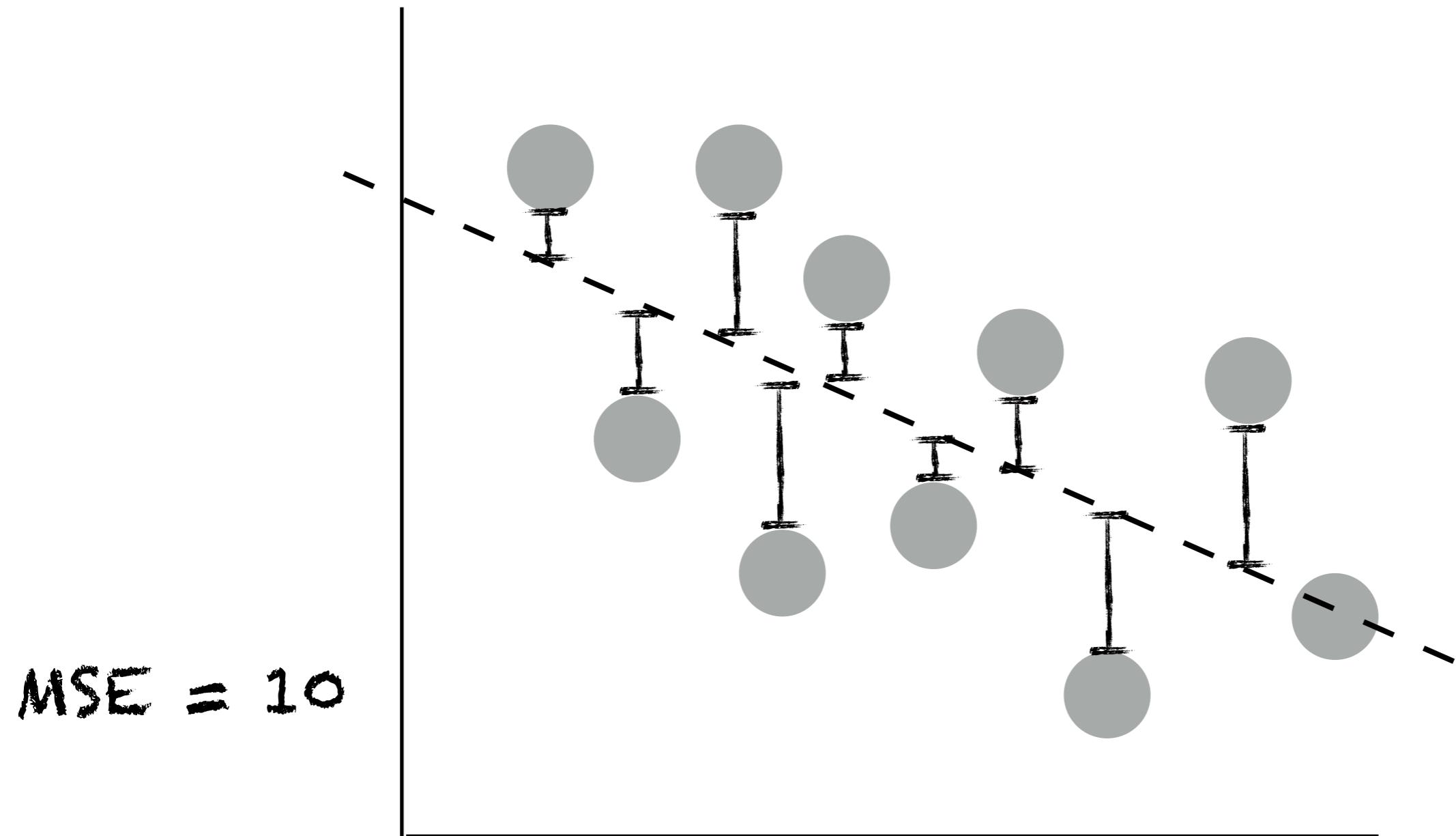
Features = {Recency:float, Read Photo:Bool, Title_New:Bool, Title_



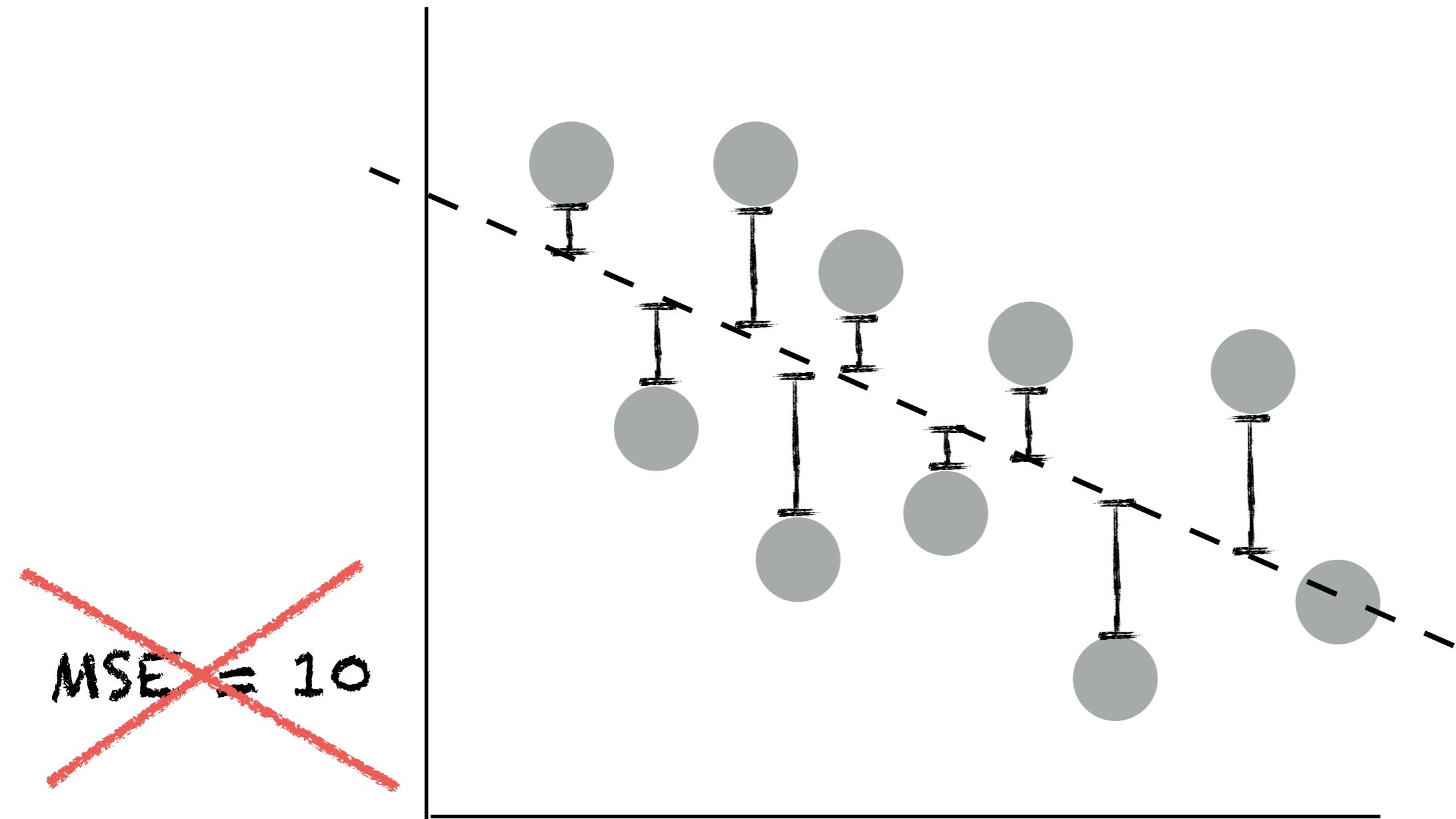
Train/Test Splits



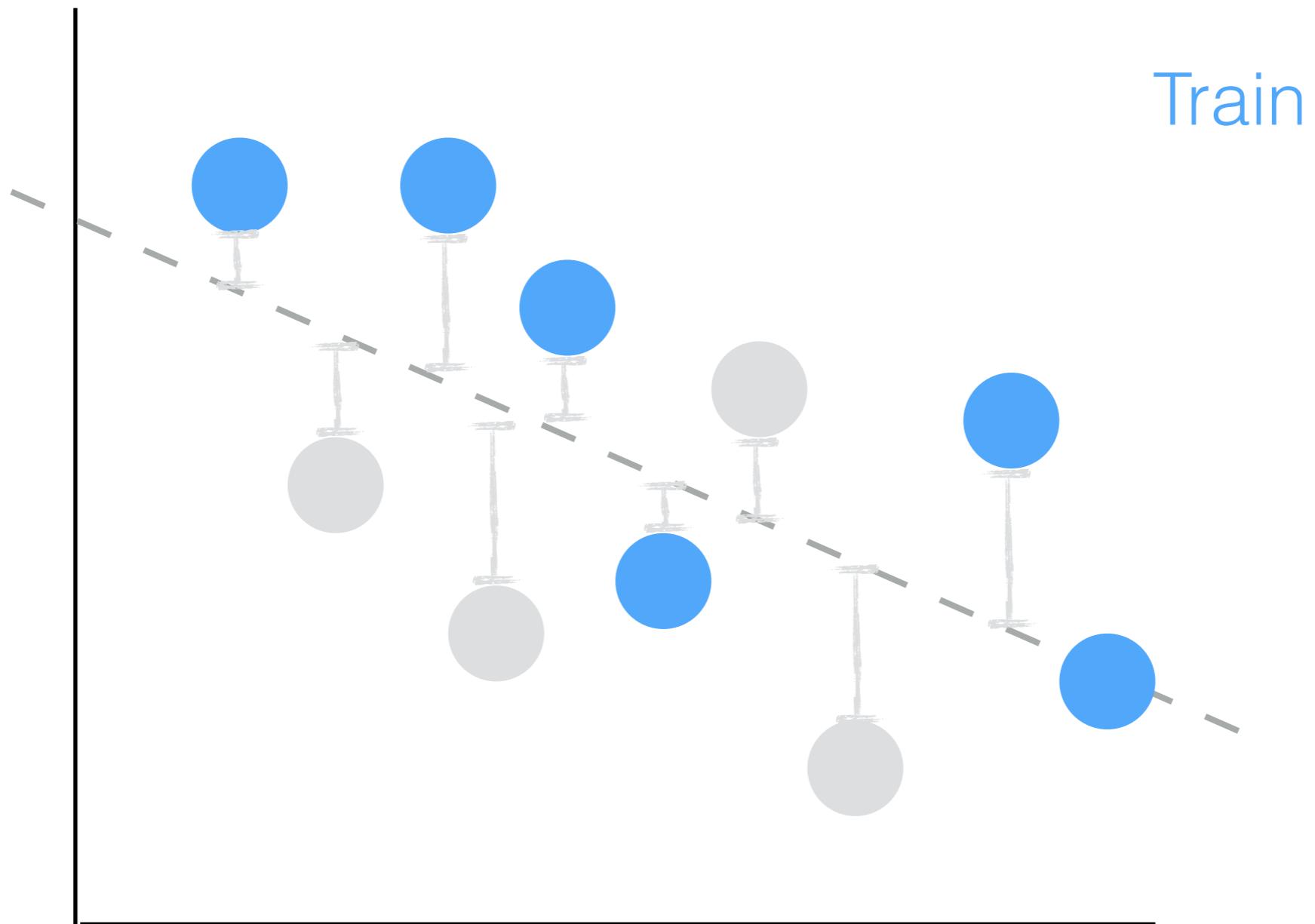
Train/Test Splits



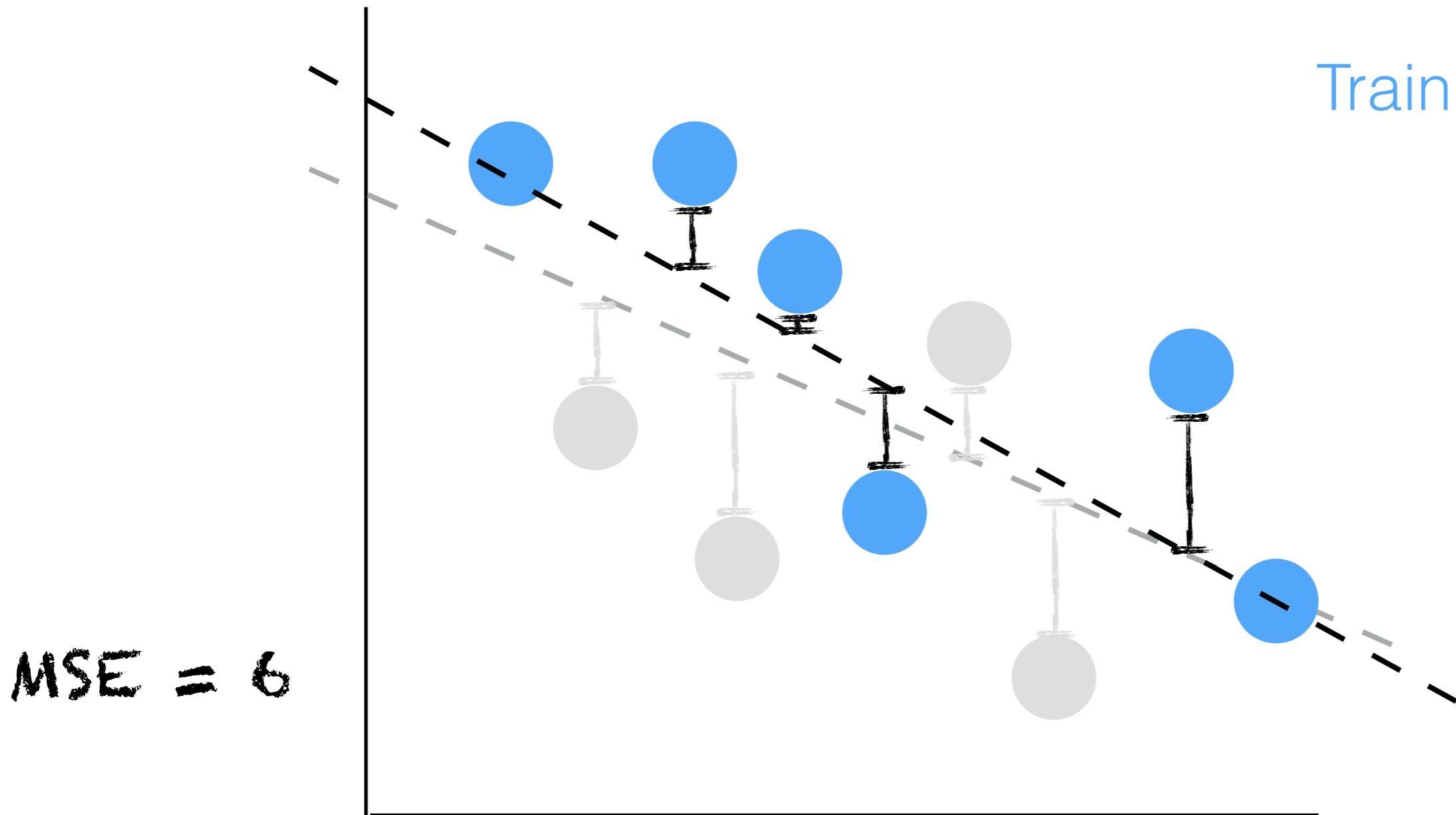
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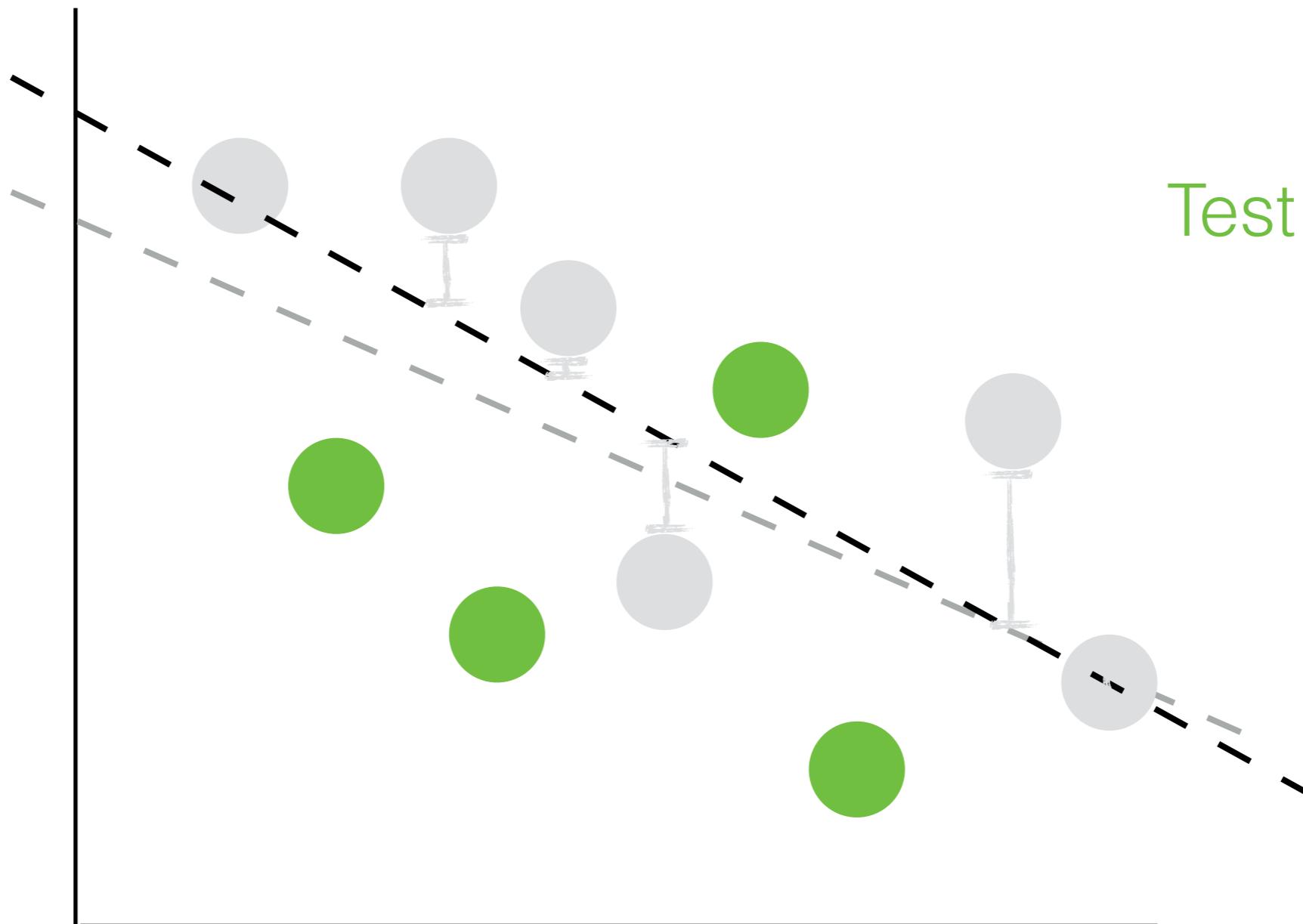
Train/Test Splits



Train/Test Splits



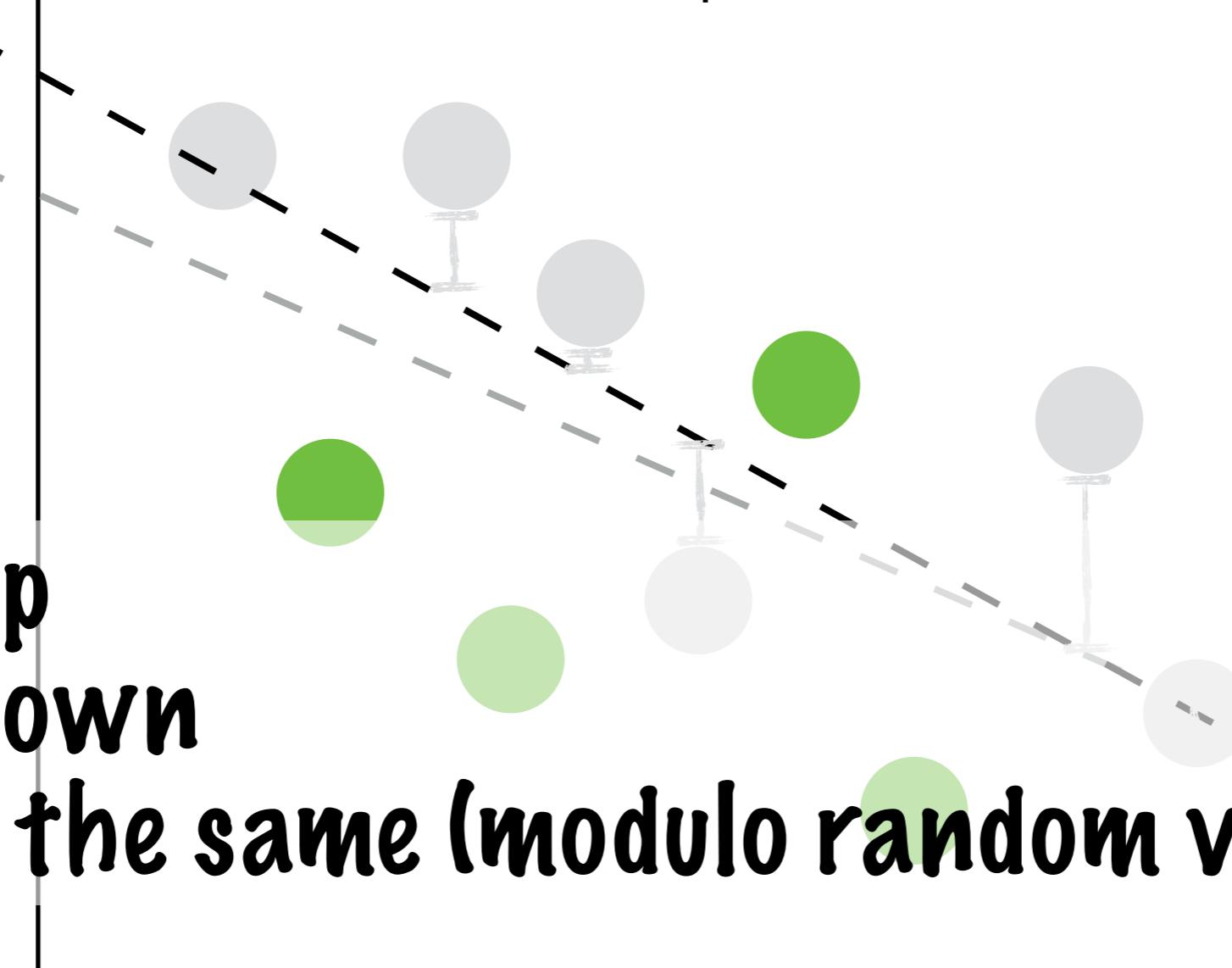
Train/Test Splits



Clicker Question!

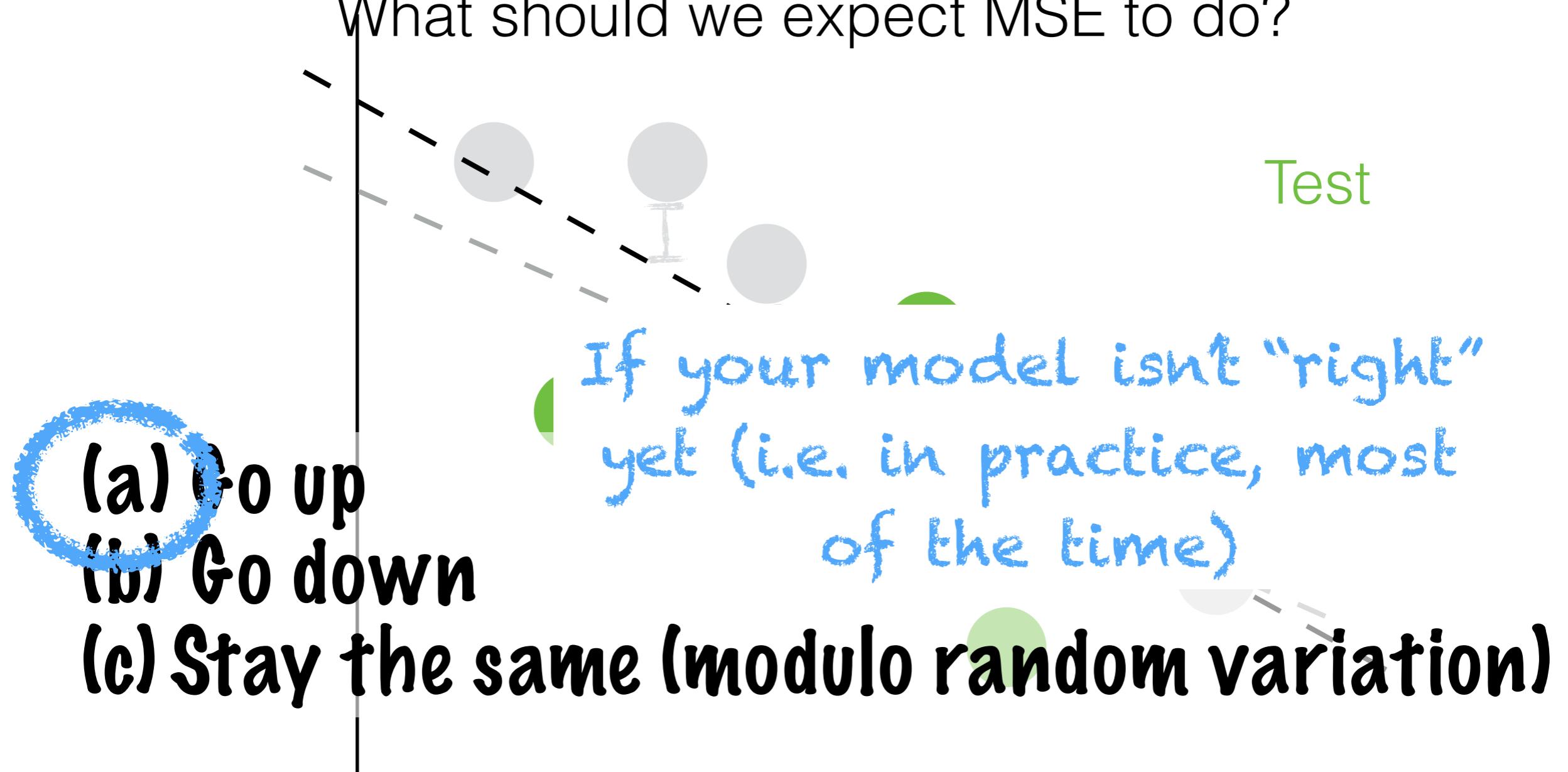
Clicker Question!

What should we expect MSE to do?

- 
- (a) Go up
(b) Go down
(c) Stay the same (modulo random variation)

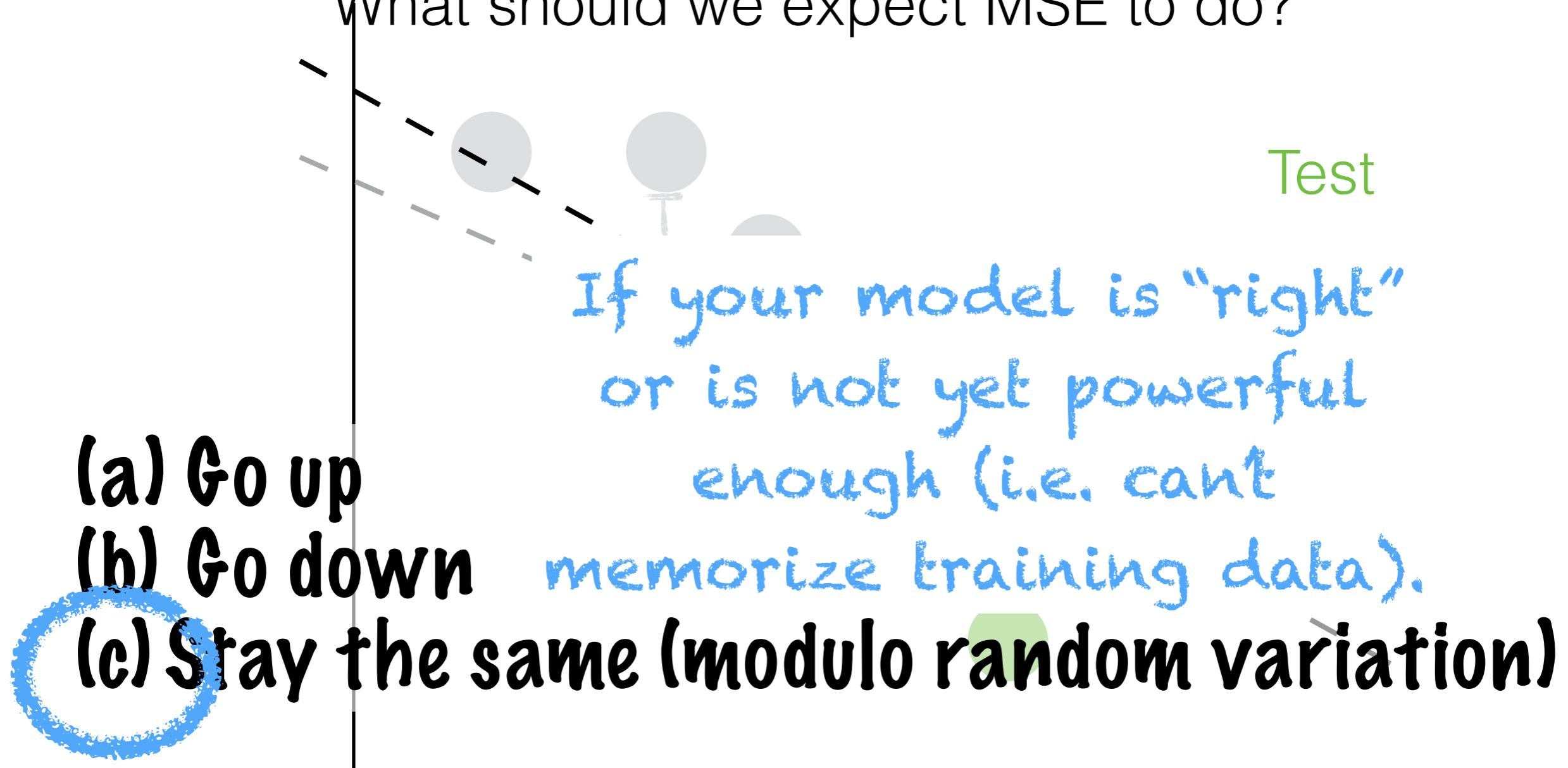
Clicker Question!

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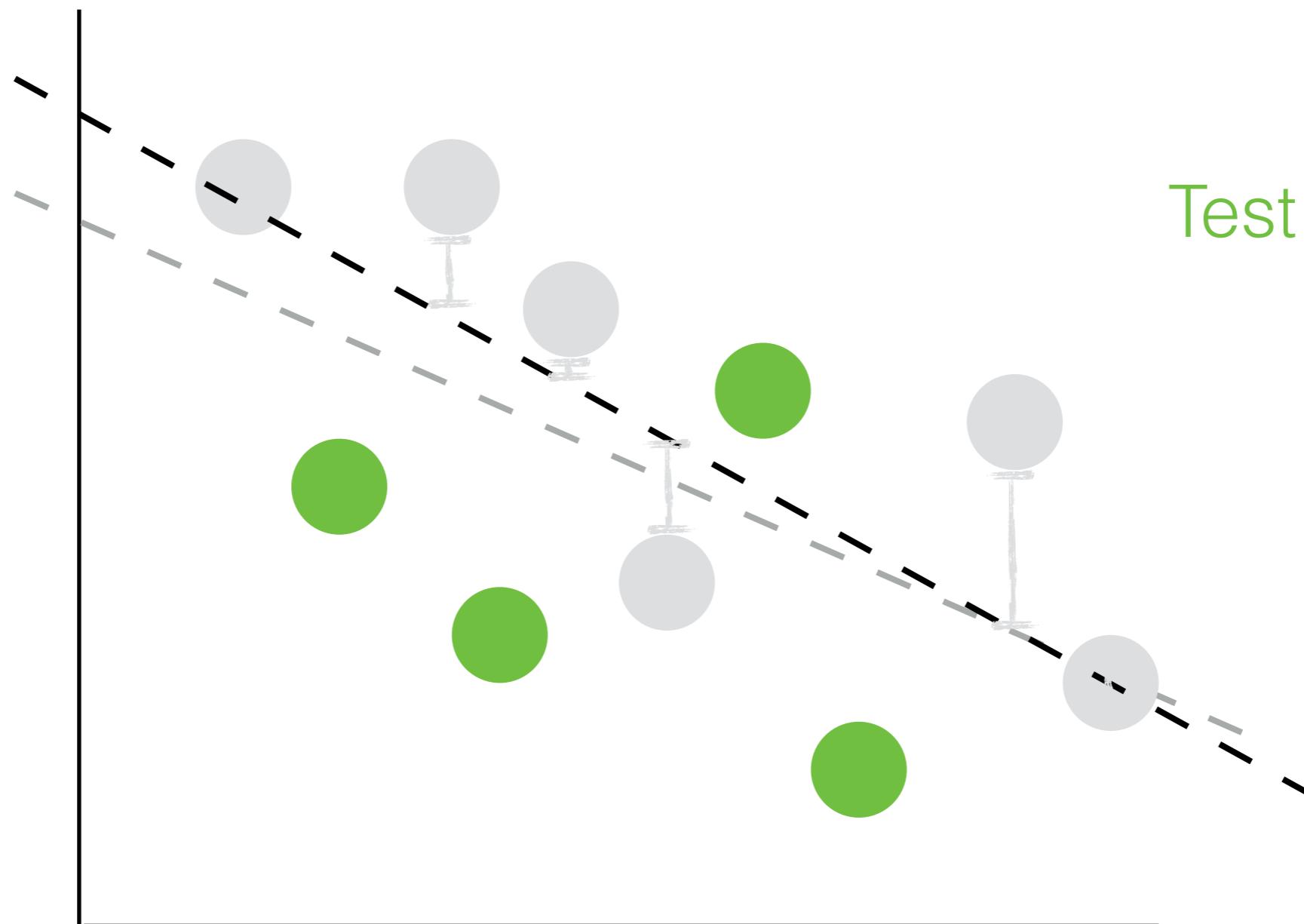


Clicker Question!

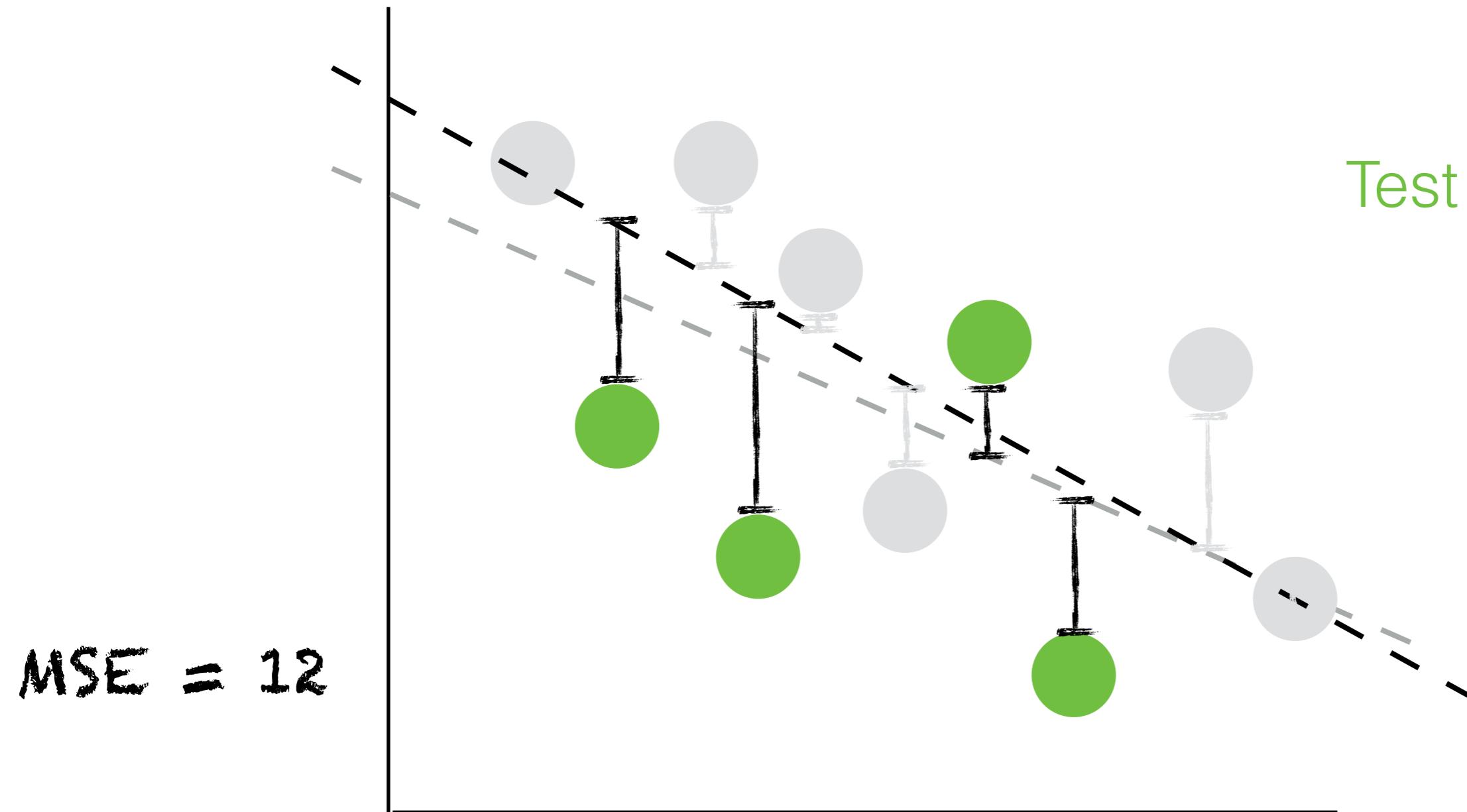
What should we expect MSE to do?



Train/Test Splits

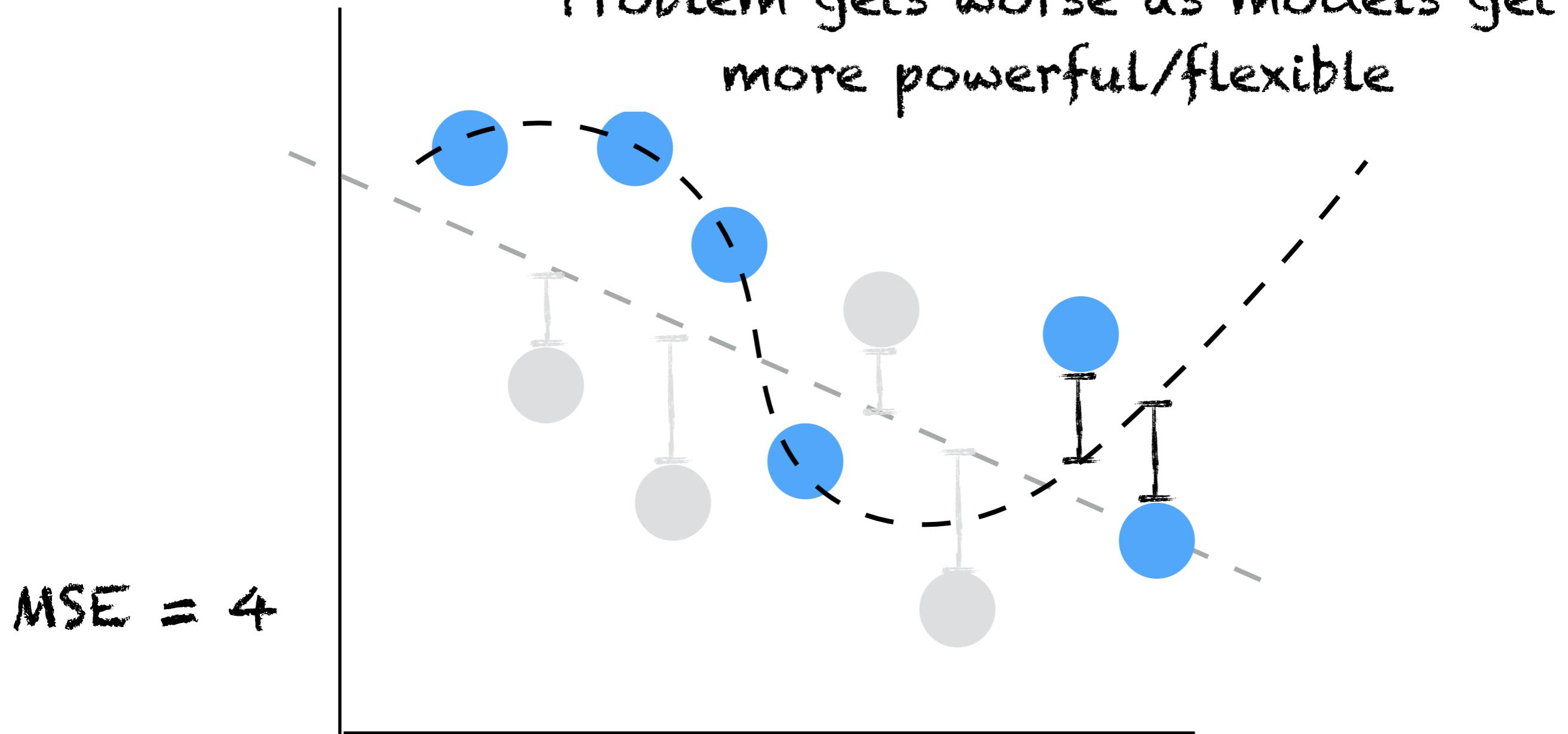


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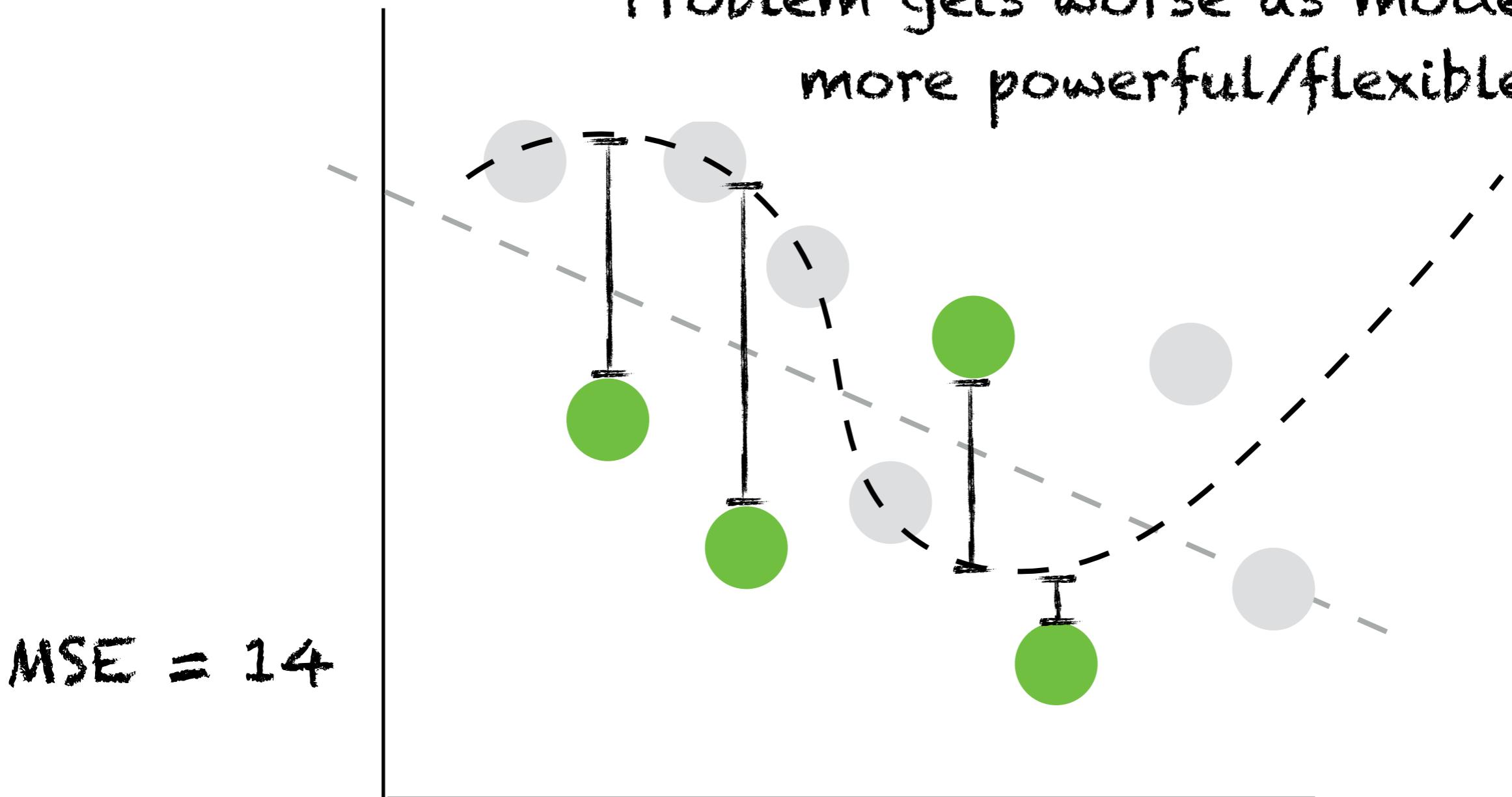
Train/Test Splits

Problem gets worse as models get
more powerful/flexible



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Today

- ML “preliminaries”—terminology, basic building blocks, conceptual background
- **The two faces of linear regression**
- Training with Stochastic Gradient Descent

Regression Analysis in Stats

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Regression Analysis in Stats

Make claims about whether there is a meaningful relationship between X and Y

(Often causal and relevant)

A “residual” form of relationship relevant to other models

Avoid overfitting by preferring simple models; avoid overclaiming by accounting for “degrees of freedom” when computing p values

Regression in ML

Given X, predict Y; deploy a model to make predictions for new inputs

But! These are the same model.

These differences are “in general”/“by convention”, not anything fundamental.

Avoid overfitting through regularization; avoid overclaiming by maintaining train/test splits and reporting test performance

Regression Analysis in Stats

- Make claims about whether there is a meaningful relationship between X and Y
- (Often) interested in causation: focus on controls and
- A “for form” for relationship and/or practically relevant effect size
- Avoid overfitting by preferring simple models; avoid overclaiming by accounting for “degrees of freedom” when computing p values

Different scientific communities with different goals.

Regression in ML

- Given X, predict Y; deploy a model to make predictions for new inputs
- Focused on prediction accuracy: exploiting

performance on a (held out) test set

- Avoid overfitting through regularization; avoid overclaiming by maintaining train/test splits and reporting test performance

Regression Analysis in Stats

- Make claims about whether there is a meaningful relationship between X and Y

- (Often causal and)

- A “research” for related relevance

- Avoid overfitting by preferring simple models; avoid overclaiming by accounting for “degrees of freedom” when computing p values

Regression in ML

- Given X, predict Y; deploy a model to make predictions for new inputs

Different scientific communities with different goals.

(and different software packages :))

`<- R, stats_models, STATA`

`sklearn, matlab, pytorch ->`

- Avoid overfitting through regularization; avoid overclaiming by maintaining train/test splits and reporting test performance

Regression Analysis in Stats

- Make claims about whether there is a meaningful relationship between X and Y
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preferring
id
counting
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In the limit, I think these goals are the same. Even if we care about prediction (and we want to do it using as few models as possible), shouldn't we get the best performance by modeling the “true” underlying process?

Isn't it the case that correct explanatory/causal models necessarily make right predictions, but not vice-versa?



formal relationships, relevant effects



preferring
id
counting
dom”
values



Avoid overfitting through regularization; avoid overclaiming by maintaining train/test splits and reporting test performance

Counter argument: You can get perfect* predictive performance with the wrong model. We were extremely good at predicting whether objects would fall or float long before we knew about gravity.

Explanatory/causal models are hard! We might never get there. Maybe empirically accurate predictions should lead, and theory/explanation will follow?

Avoid overfitting by preferring simple models; avoid overclaiming by accounting for “degrees of freedom” when computing p values



Avoid regularizing overtraining tests



Today

- ML “preliminaries”—terminology, basic building blocks, conceptual background
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Model

#1

- Make assumptions about the problem domain.
- How is the data generated?
- How is the decision-making procedure structured?
- What types of dependencies exist?
- Trending buzzword: “inductive biases”

#2

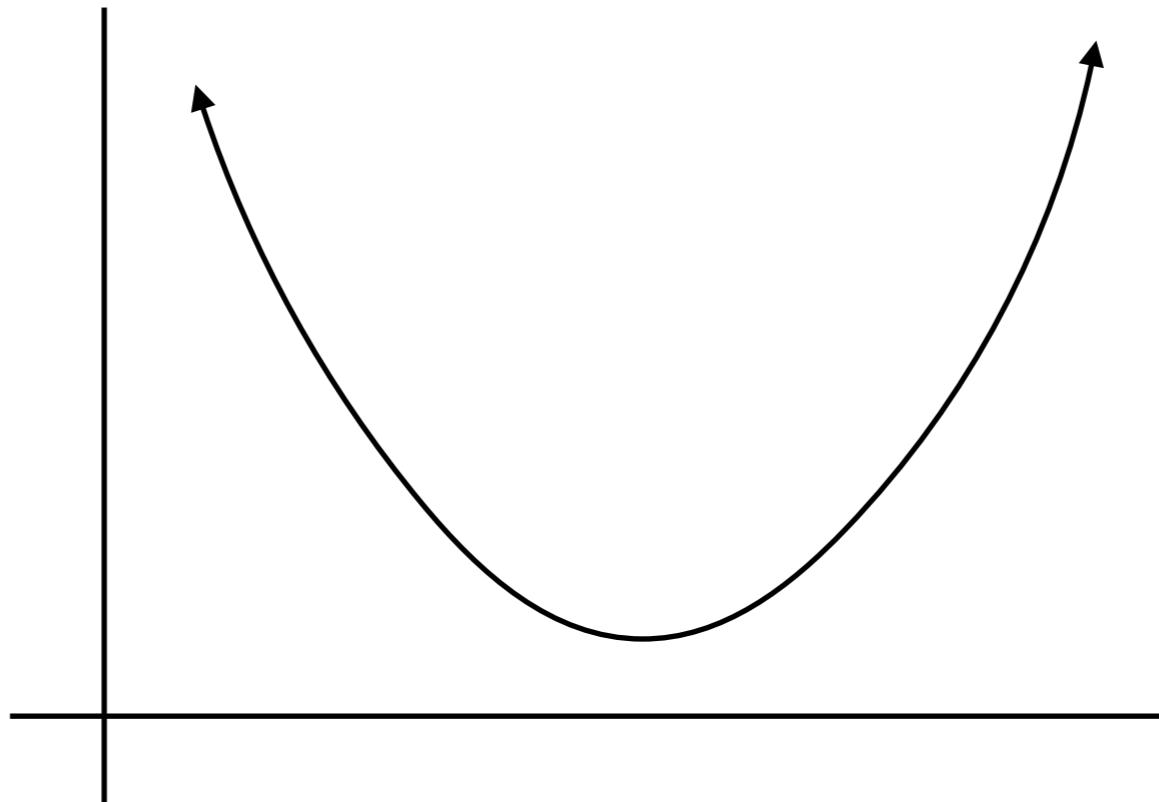
- How to train the model?

Training with Gradient Descent

$$\text{minimize} \quad \sum_{i=1}^n (Y_i - \hat{Y})^2$$

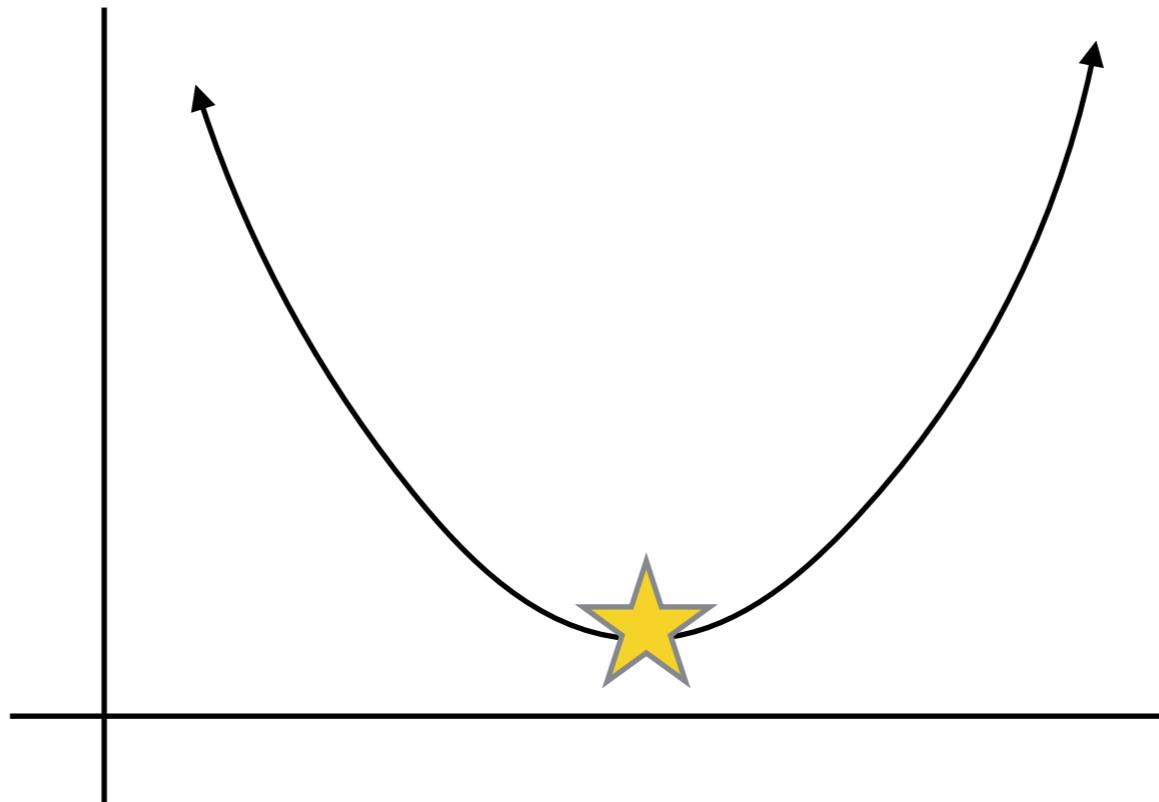
Training with Gradient Descent

minimize $\sum_{i=1}^n (Y_i - \hat{Y})^2$



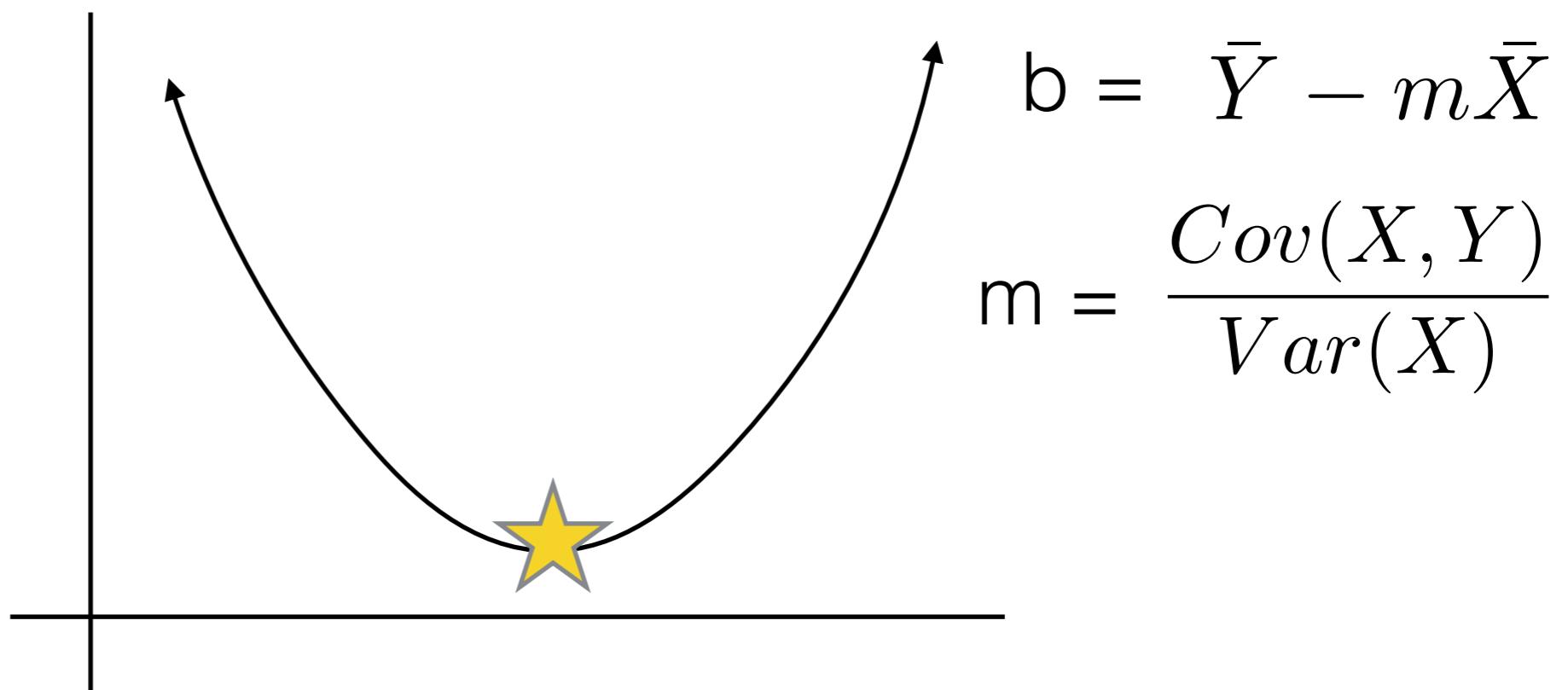
Training with Gradient Descent

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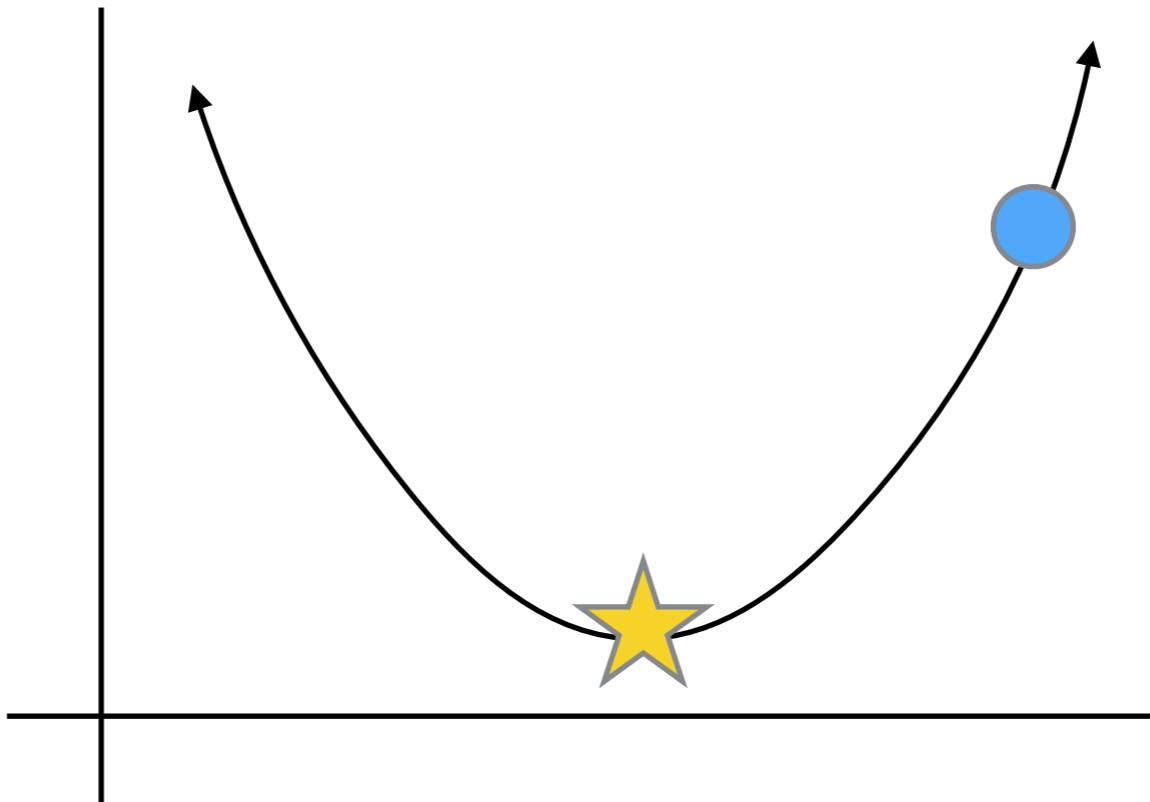
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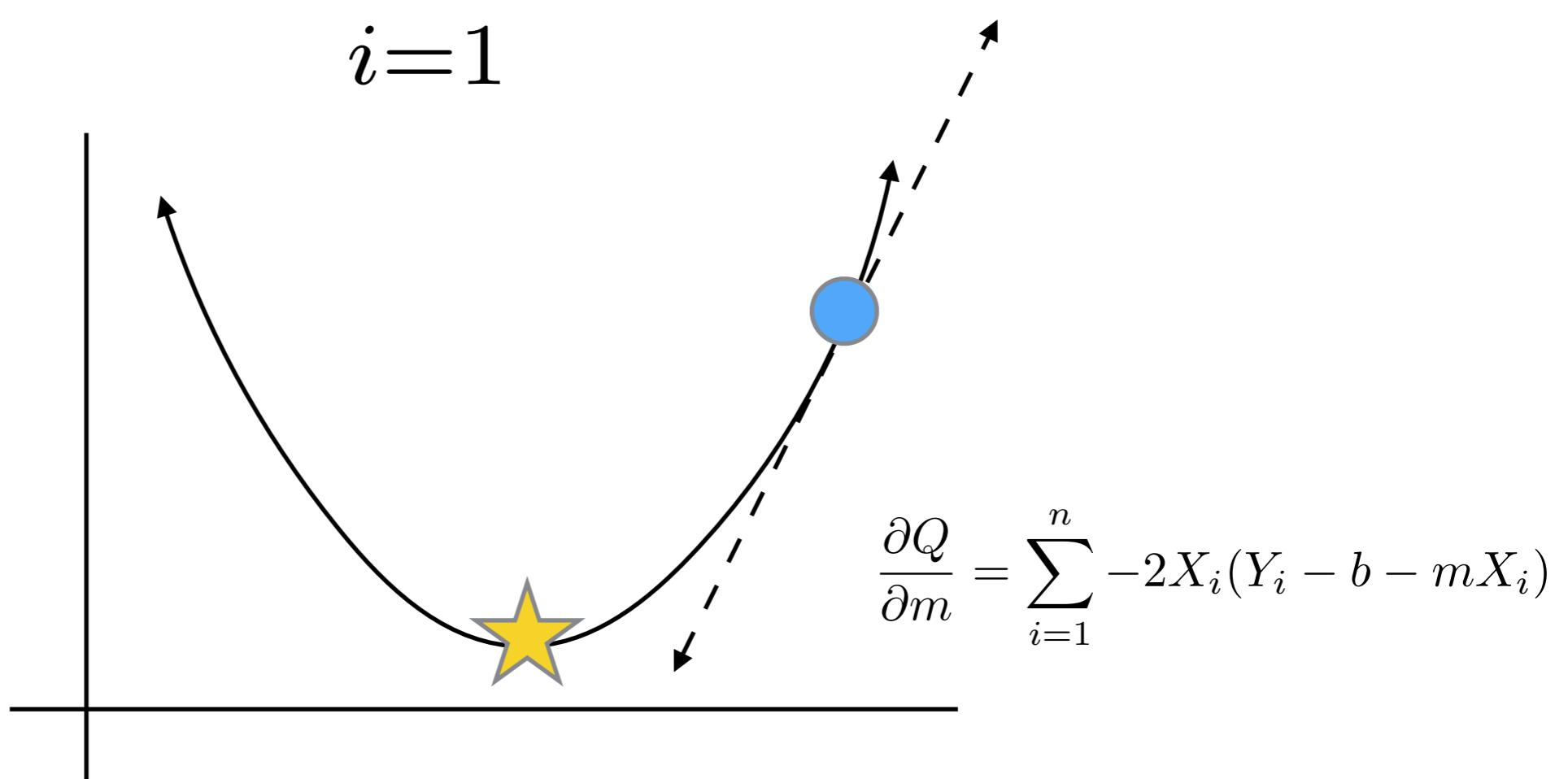
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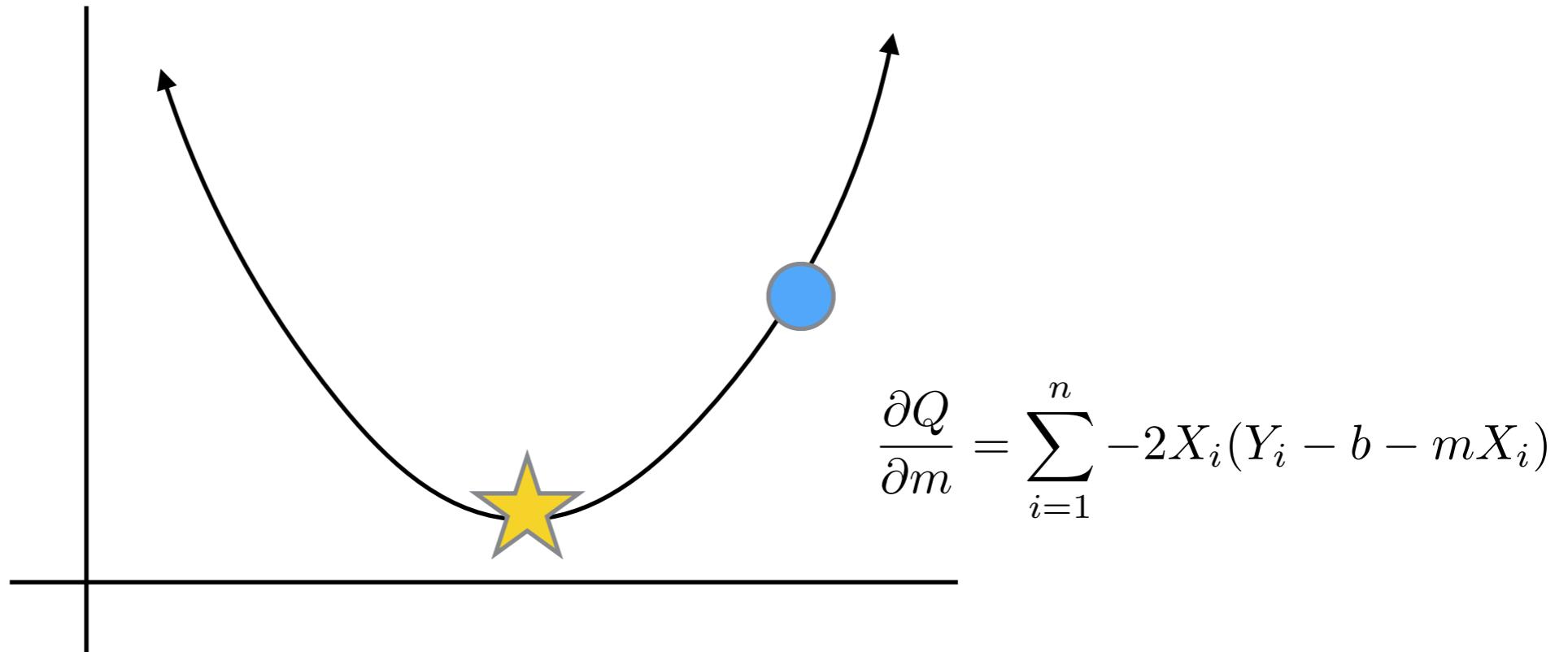
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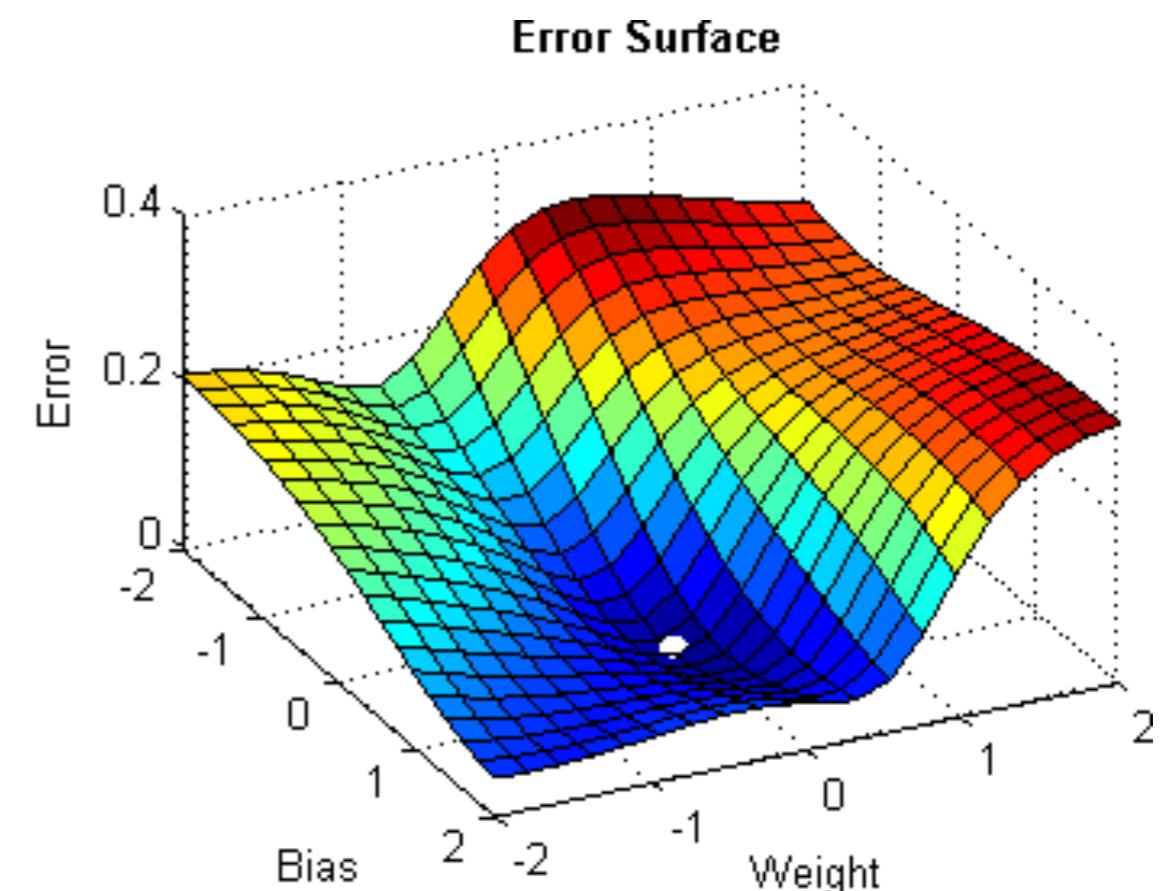
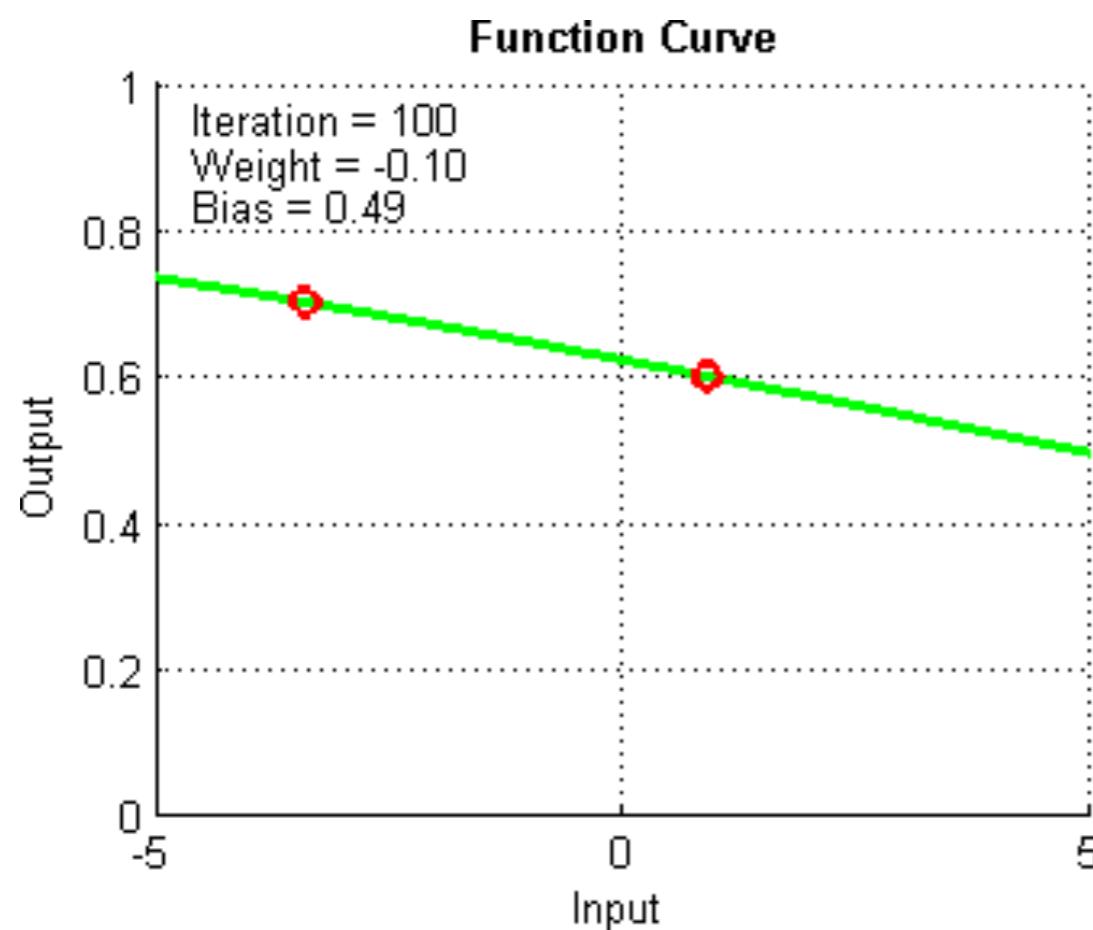


Training with Gradient Descent

minimize $\sum_{i=1}^n (Y_i - \hat{Y})^2$



Training with Gradient Descent



Training with Gradient Descent

Helpful equations for following along in the jupyter notebook

$$Q = \sum_{i=1}^n (Y_i - (mX_i + b))^2$$

$$\frac{\partial Q}{\partial b} = \sum_{i=1}^n -2(Y_i - mX_i - b) = 0$$

$$\frac{\partial Q}{\partial m} = \sum_{i=1}^n -2X_i(Y_i - b - mX_i) = 0$$

$$m = \frac{Cov(X, Y)}{Var(X)} \quad b = \bar{Y} - m\bar{X}$$

