#### 1

# Assignment 2

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Download all python codes from

https://github.com/CS20BTECH11054/AI1103/blob /main/Assignment\_2/codes/Assignment\_2.py

and latex-tikz codes from

https://github.com/CS20BTECH11054/AI1103/blob/main/Assignment\_2/Assignment\_2.tex

## 1 Problem

(Prob, 5.30) Find the variance of the number obtained on a throw of an unbiased die

## 2 Solution

Let  $X \in \{1, 2, 3, 4, 5, 6\}$ , be the random variable representing outcome of the die. The probability mass function(pmf) can be expressed as

$$p_X(n) = P(X = n) = \begin{cases} \frac{1}{6} & 1 \le n \le 6\\ 0 & otherwise \end{cases}$$
 (2.0.1)

Dandam Variabla(V)	1	2	2	1		6
Random Variable(X)	1		3	4	3	O
Probability	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$

The variance (Var(X)) of this distribution can be found by definition,

$$Var(X) = E(X^{2}) - (E(X))^{2}$$
 (2.0.2)

where,

$$E(X) = \sum_{k=1}^{k=6} k p_X(k)$$
 (2.0.3)

$$E(X) = \frac{1}{6} \sum_{k=1}^{k=6} k$$
 (2.0.4)

We know that, sum of natural numbers from 1 to n is,

$$\sum_{k=1}^{k=n} k = \frac{n(n+1)}{2}$$
 (2.0.5)

By substituting Eq.(2.0.5) in Eq.(2.0.4) we get,

$$E(X) = \frac{1}{6} \times \frac{6 \times 7}{2}$$
 (2.0.6)

$$E(X) = \frac{7}{2} \tag{2.0.7}$$

$$E(X^{2}) = \sum_{k=1}^{k=6} k^{2} p_{X}(k)$$
 (2.0.8)

$$E(X^2) = \frac{1}{6} \sum_{k=1}^{k=6} k^2$$
 (2.0.9)

We know that, sum of squares of natural numbers from 1 to n is,

$$\sum_{k=1}^{k=n} k^2 = \frac{n(n+1)(2n+1)}{6}$$
 (2.0.10)

By substituting the formula from Eq.(2.0.5) in Eq.(2.0.4) and n=6, We get,

$$E(X^2) = \frac{1}{6} \times \frac{6 \times 7 \times 13}{6}$$
 (2.0.11)

$$E(X^2) = \frac{91}{6} \tag{2.0.12}$$

By substituting the formula from Eq.(2.0.10) in Eq.(2.0.9) and n=6, We get,

$$Var(X) = E(X^{2}) - (E(X))^{2}$$
 (2.0.13)

$$Var(X) = \frac{91}{6} - \frac{49}{4}$$
 (2.0.14)

$$Var(X) = \frac{70}{12} \tag{2.0.15}$$

$$Var(X) = 2.9167$$
 (2.0.16)

Therefore, the variance of the number obtained on a throw of an unbiased die is 2.9167.

