1

AI1103 Assignment-1

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Download all python codes from

https://github.com/CS20BTECH11062/AI1103/tree/ main/Assignment-1/codes

and latex-tikz codes from

https://github.com/CS20BTECH11062/AI1103/tree/ main/Assignment-1/Assignment-1.tex

QUESTION(Prob 1.4)

Suppose that 90 % of people are right handed. What is the probability that at most 6 of a random sample of 10 people are right handed?

SOLUTION

Given that 90 % of the population is 'right' handed and since being 'right' handed and being 'left' handed are mutually exclusive,

- Probability of 'right' handed = $Pr(R) = \frac{9}{10}$ Probability of 'left' handed = $Pr(L) = \frac{1}{10}$

One can use binomial distribution to find out the probability that more that 6 people are 'right' handed.

Let M be a variable representing number of people who are 'right' handed in a given sample.

So M has a binomial distribution:

$$\Pr\left(M = k\right) = \binom{n}{k} \times (l)^{n-k} \times (r)^{k} \tag{0.0.1}$$

Where

- n = Total number of people = 10
- 1 = Probability that a person is 'left' handed =
- $r = Probability that a person is 'right' handed = \frac{9}{10}$

So.

$$\Pr\left(M = k\right) = \binom{n}{k} \times \left(\frac{1}{10}\right)^{n-k} \times \left(\frac{9}{10}\right)^{k} \tag{0.0.2}$$

Pr(at most 6 are right handed) = Pr
$$(M = 0)$$

+ Pr $(M = 1)$ + Pr $(M = 2)$ + Pr $(M = 3)$
+ Pr $(M = 4)$ + Pr $(M = 5)$ + Pr $(M = 6)$
$$\implies Pr (0 \le M \le 6) = 1 - Pr (7 \le M \le 10)$$
 $(0.0.3)$
(Since $\sum_{k=0}^{10} Pr (M = k) = 1$)

$$\implies 1 - \Pr(7 \le M \le 10) = 1 - \sum_{k=7}^{10} \Pr(M = k)$$
(0.0.4)

From (0.0.2) we get,

$$\implies 1 - \sum_{k=7}^{10} {10 \choose k} \times \left(\frac{1}{10}\right)^{10-k} \times \left(\frac{9}{10}\right)^k \qquad (0.0.5)$$

$$\implies 1 - {10 \choose 7} \times \left(\frac{1}{10}\right)^3 \times \left(\frac{9}{10}\right)^7 - {10 \choose 8} \times \left(\frac{1}{10}\right)^2 \times \left(\frac{9}{10}\right)^8 \\ - {10 \choose 9} \times \left(\frac{1}{10}\right)^1 \times \left(\frac{9}{10}\right)^9 - {10 \choose 10} \times \left(\frac{1}{10}\right)^0 \times \left(\frac{9}{10}\right)^{10}$$
(0.0.6)

$$\implies$$
 Pr $(0 \le M \le 6) = \frac{7996999}{625000000} = 0.012795198$

Thus probability 6 the that most 'right' handed is 0.012795198 people are

