

# CS 5010: Programming Design Paradigms

## Fall 2017

### Lecture 7: Data Structures and Algorithms

Acknowledgement: lecture notes inspired by course material prepared by UW  
faculty members Z. Fung and H. Perkins.

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# Administrivia

- No code walk this week (grades for your assignments coming soon)
- Assignment 4 due on Monday, October 23 by 6pm
- Code walkthroughs on Tuesday, October 24 from 10am-9pm, in 401 Terry Ave N:
  - 10am – 5:30pm in Camano classroom
  - 6pm – 10pm in Cypress classroom

# Agenda – Algorithms and Data Structures 1

- Data collections
- List ADT
  - Doubly-linked List
  - Algorithm: Recursion
- Stack ADT
  - Some implementation details
  - Algorithm: backtracking
- Queue ADT
  - Mixing stacks and queues
  - Circular queues
- Trees
  - Binary trees
- Tree Traversals
- Some comments and hints about Assignment 4

Algorithms and Data Structures 1

# DATA COLLECTIONS

# Data Collections?

Collection of chewed gums



Collection of pens



Collection of cassette tapes



Collection of old radios



## What is a data collection?

Shoes collection



Star wars collection



Cars collection



[Pictures credit: <http://www.smosh.com/smash-pit/articles/19-epic-collections-strange-things> ]

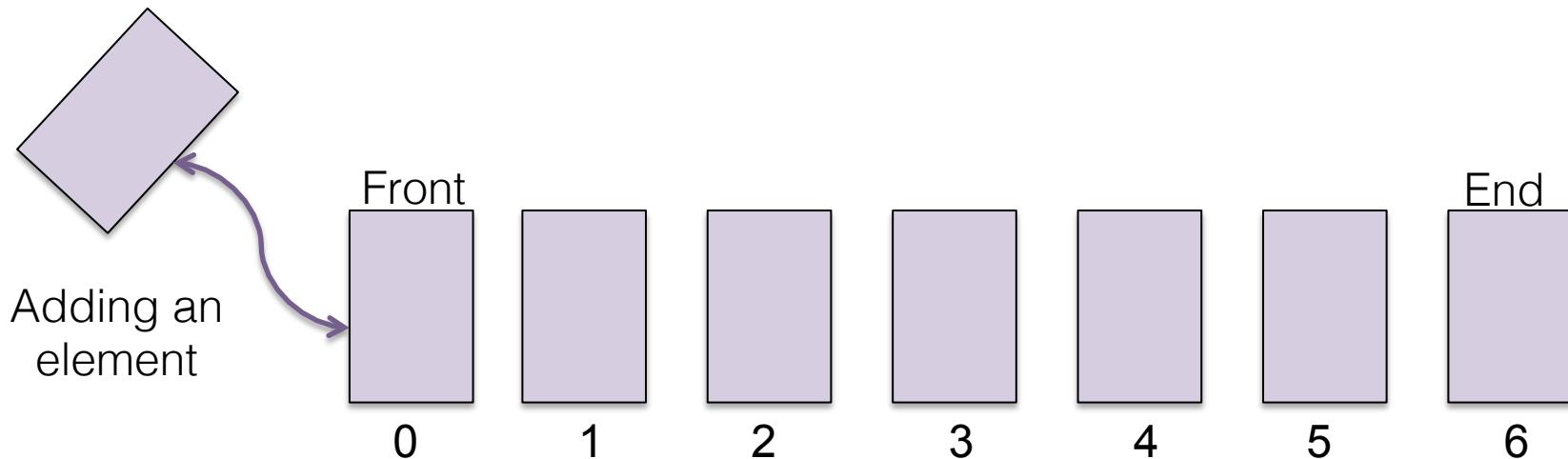
# Data Collections?

- **Data collection** - an object used to store data (think *data structures*)
  - Stored objects called **elements**
  - Some typically operations:
    - `add()`
    - `remove()`
    - `clear()`
    - `size()`
    - `contains()`
- Some examples: `ArrayList`, `LinkedList`, `Stack`, `Queue`, `Maps`, `Sets`, `Trees`

## Why do we need different data collections?

# Example: ArrayList vs. LinkedList

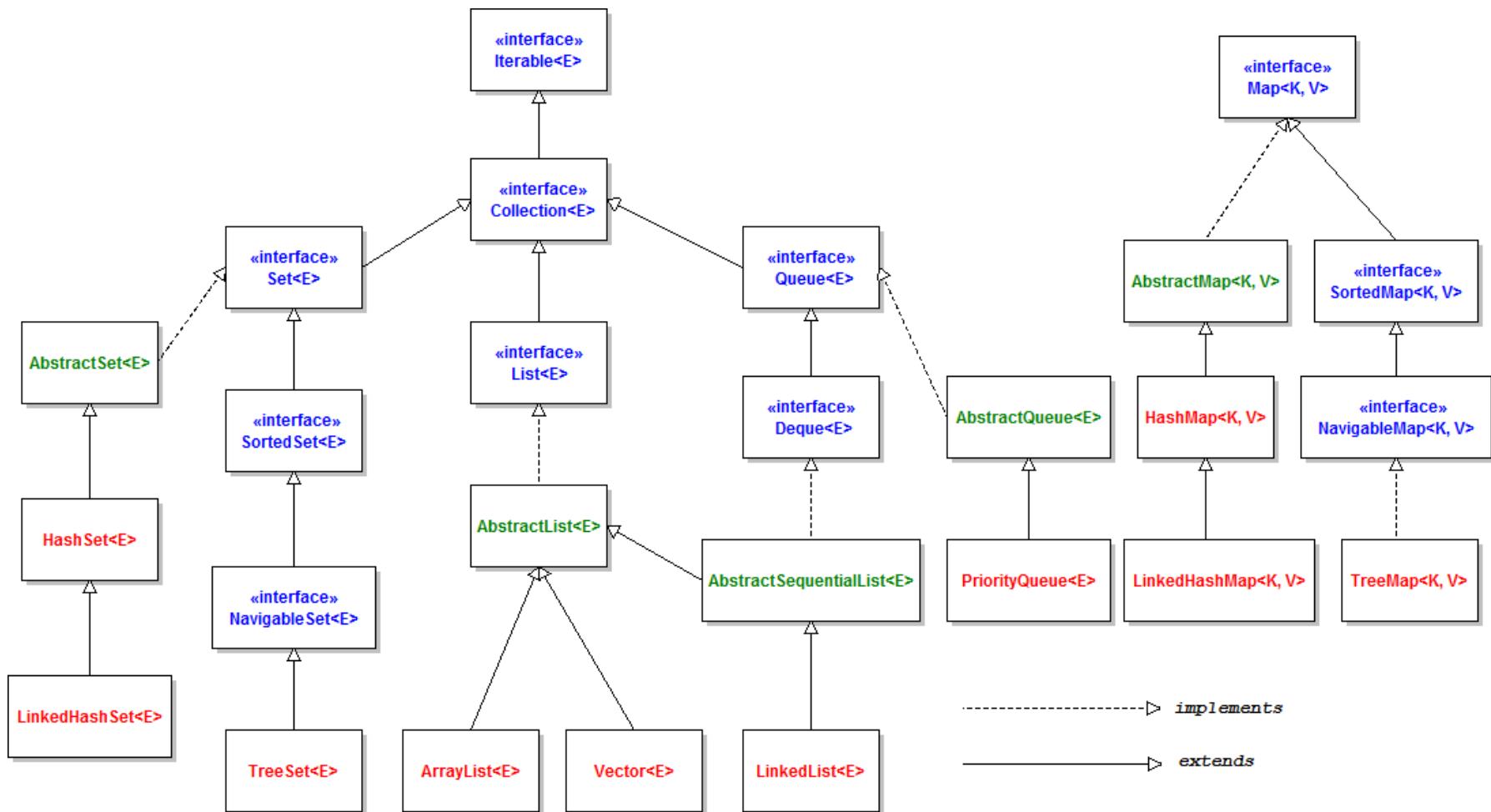
- List - a collection of elements with 0-based indexes
  - Elements can be added to the front, back, or in the middle
  - Can be implemented as an [ArrayList](#) or as a [LinkedList](#)
  - What is the complexity of adding an element to the front of an:
    - [ArrayList](#)?
    - [LinkedList](#)?



Algorithms and Data Structures 1

# **JAVA COLLECTIONS**

# Java Collections API



[Pictures credit: <http://www.codejava.net>]

# Java Collections API

- In Java, common data structures implemented in [Java Collections API](#)
  - Part of the `java.util` package
- Interface `Collection<E>`:
  - Extended by four interfaces:
    - `List<E>`
    - `Set<E>`
    - `Queue<E>`
    - `Map<K, V>`
  - Extends interface [Iterable<T>](#)

## Interfaces Iterable<T> and Iterator<E>

- Implementing interface Iterable<T> allows an object to be traversed using the for each loop
- Every object that implements Iterable<T> must provide a method `Iterator iterator()`
- Interface Iterator – an iterator over a collection

```
public interface Iterator<E> {  
    boolean hasNext();  
    E next();  
    void remove();  
}
```
- Iterator `remove()` method – removes the last item returned by method `next()`

# Direct Use of an Iterator<E>

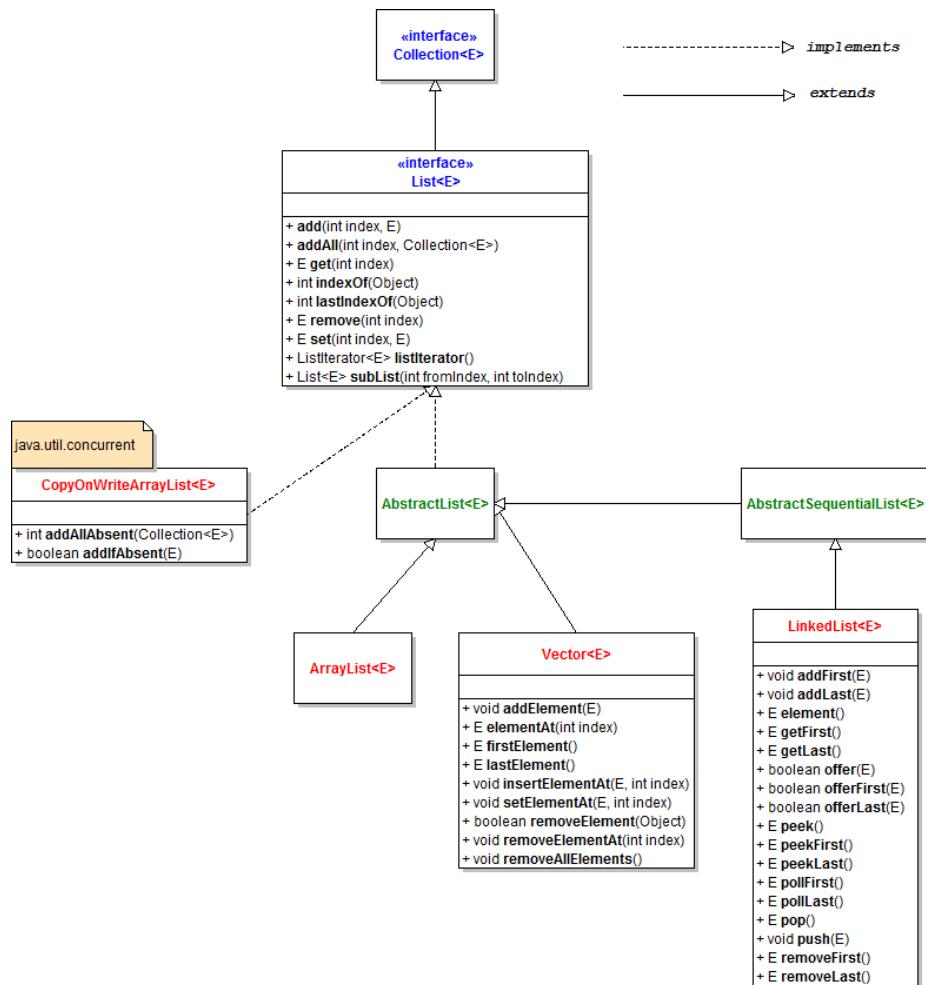
- Interface Iterator – an iterator over a collection

```
public interface Iterator<E> {  
    boolean hasNext();  
    E next();  
    void remove();  
}
```
- Careful when an iterator is used directly (not via a for each loop) → if you make any structural changes to a collection being iterated (add, remove, clear), the iterator is no longer valid (ConcurrentModificationException thrown)

Algorithms and Data Structures 1

# LIST ADT

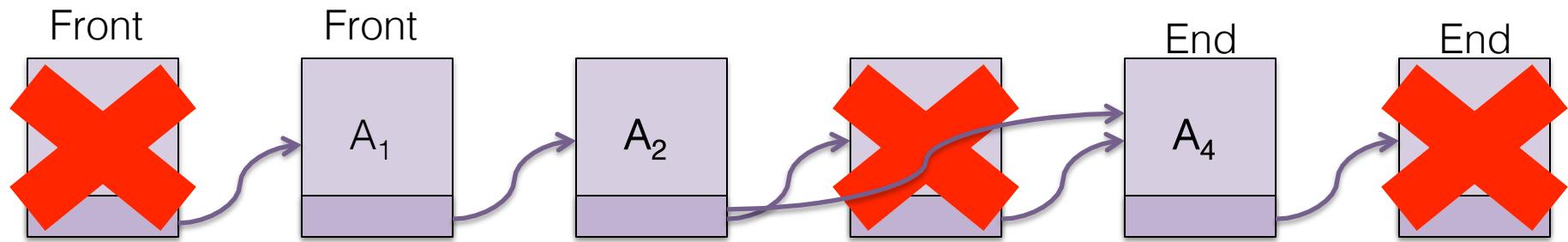
# Java List API



- `List<E>` - the base interface
- **Abstract subclasses:**
  - `AbstractList<E>`
  - `AbstractSequentialList<E>`
- **Concrete classes:**
  - `ArrayList<E>`
  - `LinkedList<E>`
  - `Vector<E>` (legacy collection)
  - `CopyOnWriteArrayList<E>` (class under `java.util.concurrent` package)
- **Main methods:**
  - `E get(int index);`
  - `E set(int index, E newValue);`
  - `Void add(int index, E x);`
  - `Void remove(int index);`
  - `ListIterator<E> listIterator();`

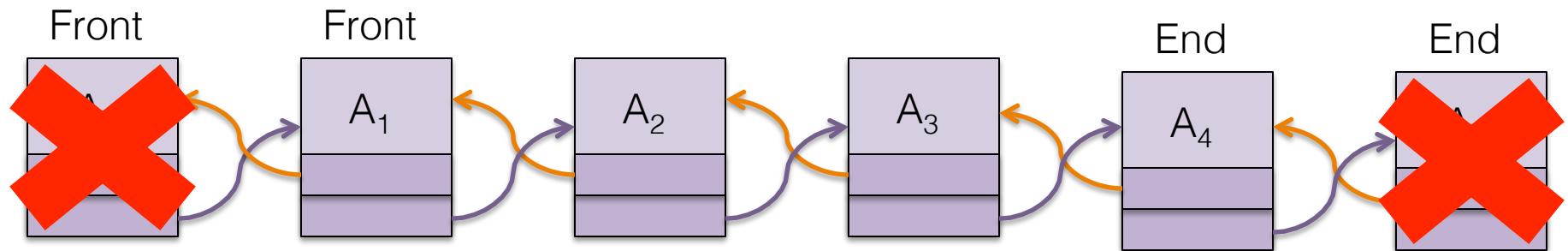
[Pictures credit: <http://www.codejava.net>]

# Example: Removing Elements from a LinkedList



- Remove the first element of the list
- Remove element A<sub>3</sub> from the list
- Remove the last element in the list
- What's the tricky part about removing elements A<sub>3</sub> and A<sub>5</sub>?
- Having to find their predecessors (elements A<sub>2</sub> and A<sub>4</sub>) and updating their link to last node
- Idea: every node maintains the link to its previous and its next node → doubly linked list

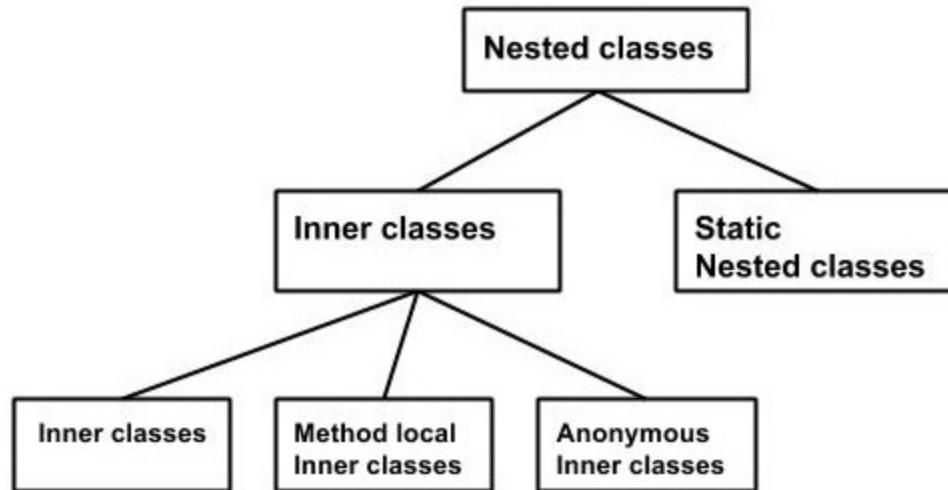
# Doubly LinkedList



- Removing the first element of the list
- Removing the last element of the list

# Implementation of a Doubly LinkedList

- Review – inner and nested classes:

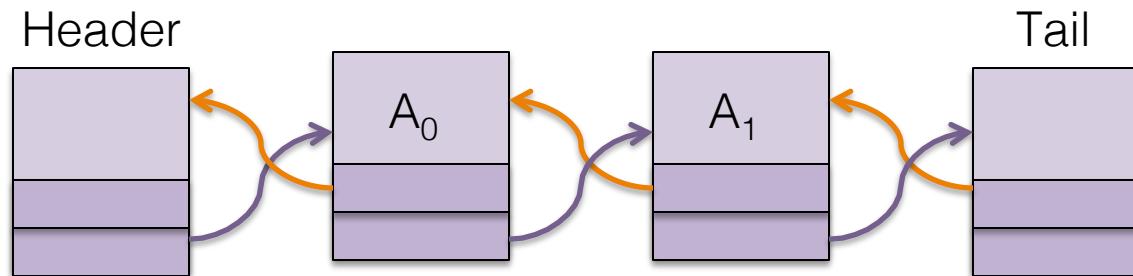


[Pictures credit: [https://www.tutorialspoint.com/java/images/inner\\_classes.jpg](https://www.tutorialspoint.com/java/images/inner_classes.jpg)]

- Java allows us to define a class *within* another class – a nested class
  - Static nested classes
  - Non-static nested classes or inner classes – have access to other members of the enclosing class, even if they are declared private

# Implementation of a Doubly LinkedList

- **Doubly linked list** – need to provide and maintain links to both ends of the list
- Implemented classes:
  - Class MyLinkedList
  - Class Node – private nested class, contains the data and links to previous and next nodes
  - Class LinkedListIterator – private inner class, implementing the interface Iterator
- **Sentinel nodes:**
  - Header and tail nodes, used to logically represent the beginning and the end markers



# Implementation of a Doubly LinkedList: MyLinkedList

```
public class MyLinkedList<E> implements Iterable<E>{
    private int listSize;
    private int modCount = 0;
    private Node<E> beginMarker;
    private Node<E> endMarker;

    public MyLinkedList() {
        doClear();
    }

    public int size() {
        return listSize;
    }

    public boolean isEmpty() {
        return size()==0;
    }

    public boolean add(E x) {
        add(size(), x);
        return true;
    }

    public void add(int index, E x) {
        addBefore(getNode(index, 0, size()), x);
    }
}
```

# Implementation of a Doubly LinkedList: MyLinkedList

```
public E get(int index) {
    return getNode(index).data;
}
public E set(int index, E newVal) {
    Node<E> p = getNode(index);
    E oldVal = p.data;
    p.data = newVal;
    return oldVal;
}
public E remove(int index) {
    return remove(getNode(index));
}
public java.util.Iterator<E> iterator() {
    return new LinkedListIterator();
}
```

# Implementation of a Doubly LinkedList: Node

```
private static class Node<E>{
    public E data;
    public Node<E> prev;
    public Node<E> next;

    public Node(E d, Node<E> p, Node<E> n) {
        data = d;
        prev = p;
        next = n;
    }
}
```

## Implementation of a Doubly LinkedList: clear()

```
public void clear() {
    doClear();
}

private void doClear() {
    listSize = 0;
    modCount++;

    beginMarker = new Node<E>(null, null, null);
    endMarker = new Node<E>(null, beginMarker, null);
    beginMarker.next = endMarker;
}
```

# Implementation of a Doubly LinkedList: addBefore ()

```
/**  
 * Adds an item to this collection, at specified position p.  
 * Items at or after that position are slid one position higher.  
 * @param p Node to add before.  
 * @param x any object.  
 */  
private void addBefore(Node<E> p, AnyType x) {  
    Node<E> newNode = new Node<>(x, p.prev, p);  
    p.prev = newNode;  
    listSize++;  
    modCount++;  
}
```

# Implementation of a Doubly LinkedList: remove()

```
/**  
 * Removes the object contained in Node p.  
 * @param p the Node containing the object.  
 * @return the item that was removed from the collection.  
 */  
private E remove( Node<E> p ) {  
    p.next.prev = p.prev;  
    p.prev.next = p.next;  
    listSize--;  
    modCount++;  
    return p.data;  
}
```

# Implementation of a Doubly LinkedList: getNode()

```
/**  
 * Gets the Node at position index, which must be in range 0  
 * to size()-1.  
 * @param index index to search at.  
 * @return internal node corresponding to index  
 * @throws IndexOutOfBoundsException if index is not between  
 * 0 and size()-1, inclusive.  
 */  
  
private Node<E> getNode(int index) {  
    return getNode(index, 0, size()-1);  
}
```

# Implementation of a Doubly LinkedList: getNode()

```
/**  
 * Gets the Node at position index, which must be in range  
 from lower to upper.  
 * @param index index to search at.  
 * @param lower lowest valid index.  
 * @param upper highest valid index.  
 * @return internal node corresponding to index  
 * @throws IndexOutOfBoundsException if index is not between  
 lower and upper, inclusive.  
 */  
  
private Node<E> getNode(int index, int lower, int upper) {  
    Node<E> p;  
  
    if(index < lower || index > upper)  
        throw new IndexOutOfBoundsException();  
}  
10/18/17
```

# Implementation of a Doubly LinkedList: getNode()

```
if(index < size()/2) {  
    p = beginMarker.next;  
    for(int i = 0; i < index; i++)  
        p = p.next;  
} else {  
    p = endMarker;  
    for(int i = 0; i > index; i--)  
        p = p.prev;  
}  
return p;  
}
```

# Implementation of a Doubly LinkedList: LinkedListIterator()

```
private class LinkedListIterator implements java.util.Iterator<E>{
    private Node<E> current = beginMarker.next;
    private int expectedModCount = modCount;
    private boolean okToRemove = false;

    public boolean hasNext() {
        return current != endMarker;
    }

    public AnyType next() {
        if(modCount != expectedModCount)
            throw new java.util.ConcurrentModificationException();
        if(!hasNext())
            throw new java.util.NoSuchElementException();

        E nextItem = current.data;
        current = current.next;
        okToRemove = true;
        return nextItem;
    }
}
```

# Implementation of a Doubly LinkedList: LinkedListIterator()

```
private class LinkedListIterator implements java.util.Iterator<E>{  
  
    public void remove() {  
        if(modCount != expectedModCount)  
            throw new java.util.ConcurrentModificationException();  
        if(!okToRemove())  
            throw new IllegalStateException();  
  
        MyLinkedList.false.remove(current.prev);  
        expectedModCount++;  
        okToRemove = false;  
    }  
}
```

# Recursion

The image shows a Google search results page for the query "recursion". The search bar contains "recursion". Below it, there are two radio button options: "the web" (selected) and "pages from the UK". A "Web" button with a plus sign and a "Show options..." link are also present. The search results include a "Did you mean: recursion" section. The first result is a link to "Recursion - Wikipedia, the free encyclopedia", which is described as a visual form of recursion known as the Droste effect. It includes a thumbnail image of a woman holding a tray with a smaller version of herself holding the same tray. Below this, another result is shown for "Recursion (computer science) - Wikipedia, the free encyclopedia", describing it as a way of thinking about and solving problems.

recursion

Search:  the web  pages from the UK

**Web**

Did you mean: [recursion](#)

**[Recursion](#)** - Wikipedia, the free encyclopedia

A visual form of **recursion** known as the Droste effect. The woman in this image contains a smaller image of her holding the same ...

[en.wikipedia.org/w/index.php?title=Recursion&oldid=853011111](https://en.wikipedia.org/w/index.php?title=Recursion&oldid=853011111) - Cached - Similar -

**[Recursion \(computer science\)](#)** - Wikipedia, the free encyclopedia

**Recursion** in computer science is a way of thinking about and solving

[Pictures credit: <http://www.telegraph.co.uk/technology/google/6201814/Google-easter-eggs-15-best-hidden-jokes.html>]

# Recursion

- **Recursion** – an operation defined in terms of itself
  - Solving a problem recursively means solving smaller occurrences of the same problem
- **Recursive programming** – an object consists of methods that call themselves to solve some problem
- Can you think of some examples of recursions and recursive programs?

# Recursive Algorithm

- Every recursive algorithm consists of:
  - **Base case** – at least one simple occurrence of the problem that can be answered directly
  - **Recursive case** - more complex occurrence that cannot be directly answered, but can be described in terms of smaller occurrences of the same problem
- A crucial part of recursive programming is identifying these cases
- What were base cases for our Fibonacci problem in Assignment 1?
- Why are we now talking about recursion???

# Recursive Data Structures

- **Recursive data structure** - a data structure partially composed of smaller or simpler instances of the same data structure
- Is linked list a recursive data structure?
- Let's see - a linked list is either
  - Null (base case)
  - A node whose next field references a list

# Example: Printing Values in a Linked List

```
public static void printList (Node nodeToPrint) {  
    if (nodeToPrint == null)  
        return;  
    else {  
        System.out.println(nodeToPrint.data);  
        print (nodeToPrint.next);  
    }  
}
```

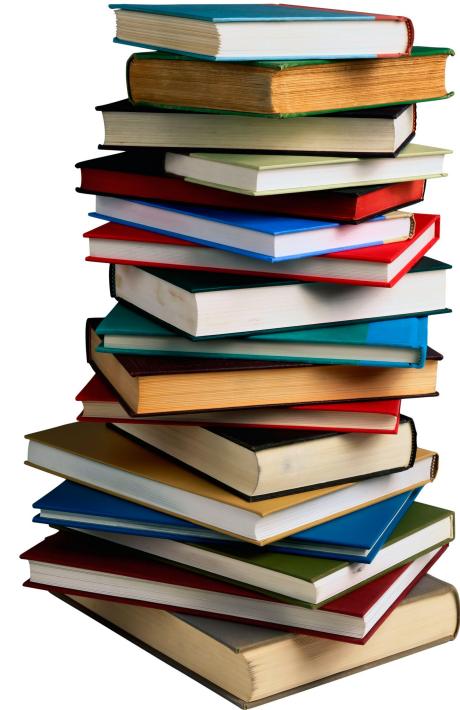
- Similar problems: print in the reverse order, sum elements of the list,...
- Careful – this is a tail recursion
  - Tail recursions are not bad, but they do consume the stack

Algorithms and Data Structures 1

# STACK ADT

# Stacks

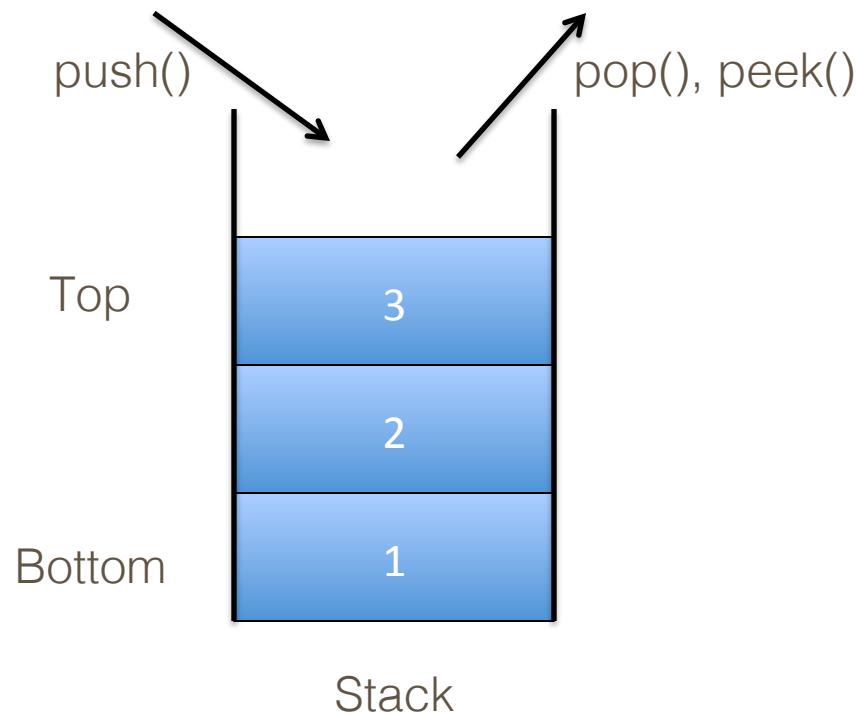
- Some of my favorite stacks:



[Pictures credit: <https://rukminim1.flixcart.com/image/1408/1408/stacking-toy>, <http://battellemedia.com/wp-content/uploads/2014/08/National-Pancake-Day-at-IHOP.jpg>, [http://all4desktop.com/data\\_images/original/4245681-book.jpg](http://all4desktop.com/data_images/original/4245681-book.jpg)]

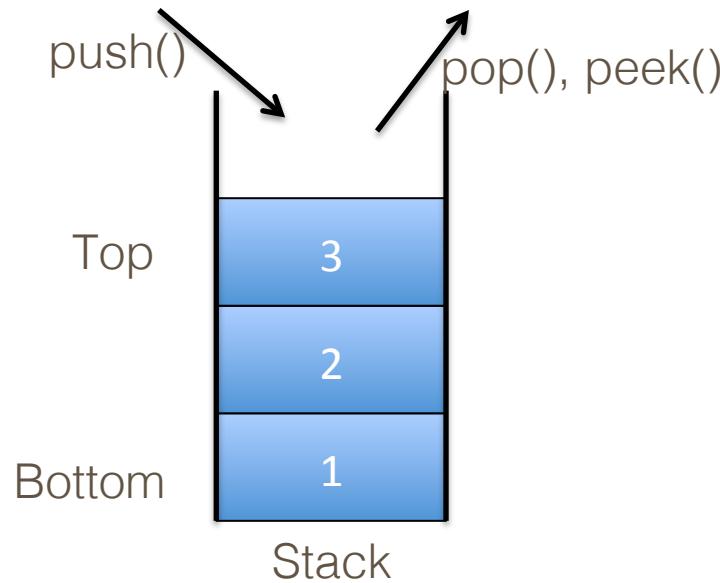
# What is a Stack?

- **Stack** – a data collection that retrieves elements in the LIFO order (last-in-first-out)



- Is there another way to think about a stack?

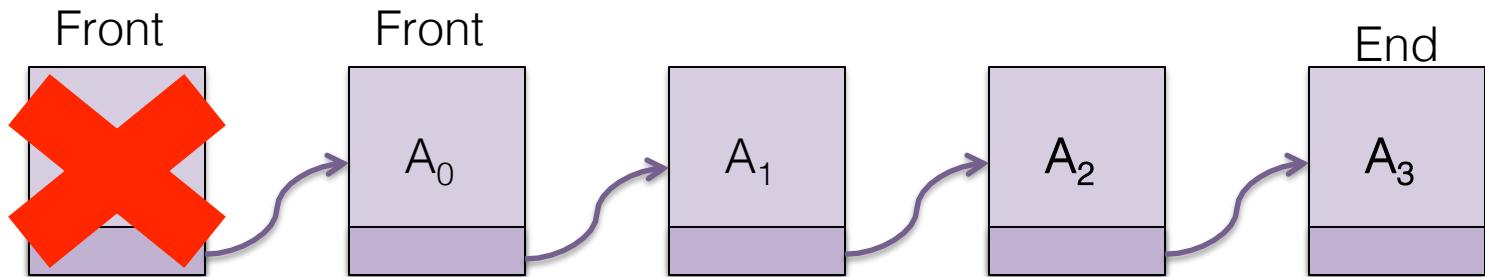
# What is a Stack?



- Is there another way to think about a stack?
- **Stack** – a constrained data collection where clients are limited to use only limited optimized methods (`pop`, `push`, `peek`)
- **Stack** – a list with restriction that insertions and deletions can be performed in only one position, the end of the list, called **the top**

# Implementations of a Stack

- **Stack** – a list with restriction that insertions and deletions can be performed in only one position, the end of the list, called **the top**
- Since a stack is a list, any list implementation will do:
  - Example: linked list implementation
    - push ()
    - peek () / top ()
    - pop ()



# Java Class Stack

Stack <E> ( )	Object constructor – constructs a new stack with elements of type E
push (value)	Places given value on top of the stack
pop ()	Removes top value from the stack, and returns it. Throws EmptyStackException if the stack is empty.
peek ()	Returns top value from the stack without removing it. Throws EmptyStackException if the stack is empty.
size ()	Returns the number of elements on the stack.
isEmpty ()	Returns true if the stack is empty.

- Example:

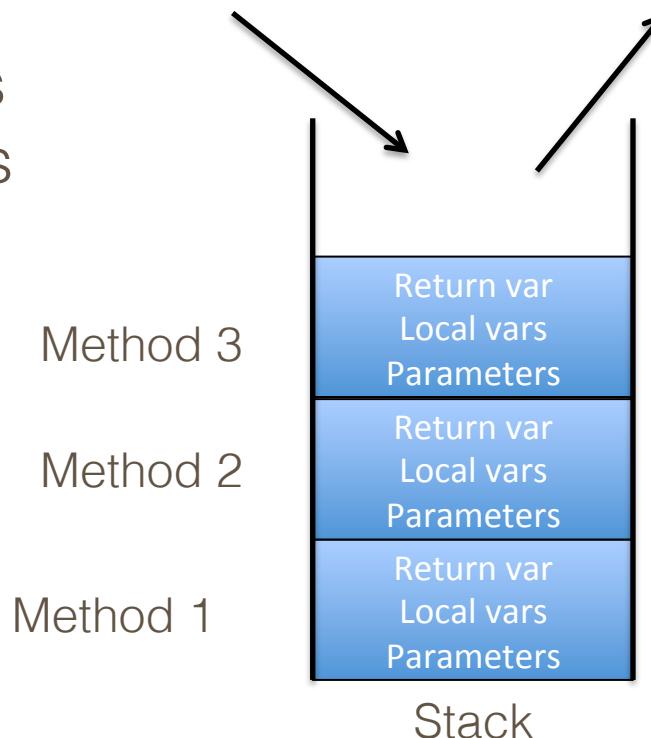
```
Stack<String> s = new Stack<String>();  
s.push("Hello");  
s.push("PDP");  
s.push("Fall 2017"); //bottom ["Hello", "PDP", "Fall 2017"] top  
System.out.println(s.pop()); //Fall 2017
```

# Applications of a Stack

- Programming languages and compilers:
  - Method calls (*call=push, return=pop*)
  - Compilers (parsers)
- Matching up related pairs of things:
  - Find out whether a string is a palindrome
  - Examine a file to see if its braces { } match
  - Convert "infix" expressions to pre/postfix
- Sophisticated algorithms:
  - Searching through a maze with "backtracking"

# Example: Methods Call

- In some system whenever there is a method call, some information about the current state of the system needs to be stored before the control is transferred to a new method:
  - Parameters
  - Local variables
  - Return address



# Example: Postfix Expressions

- Suppose you are using a calculator to compute the total cost of your groceries
  - Add the costs of individual items
  - Multiply by 1.1 to account for local sales tax
- The natural way to do this with a calculator:  
$$5.5 + 4.5 + 7 + 8 * 1.1$$
- What is the expected result?
  - 27.5 (expected value)
  - 25.8
- That depends on how “smart” is your calculator!

# Example: Postfix Expressions

- The natural way to do this with a calculator:

$$5.5 + 4.5 + 7 + 8 * 1.1$$

- What if we represent the given expression in the **postfix** or **Reverse Polish notation**:

$$5.5 \ 1.1 * \ 4.5 \ 1.1 * + \ 7 \ 1.1 * + \ 8 \ 1.1 * +$$

- The easiest way to implement this is with a stack:

$$(5.5 * 1.1) + (4.5 * 1.1) + (7 * 1.1) + (8 * 1.1)$$

# Backtracking

- **Backtracking** – an algorithmic approach that finds solution(s) by trying partial solutions, and abandoning them as soon as they are no longer suitable
- A "brute force" algorithmic method
  - All possible solutions paths explored
  - Often implemented recursively
- Some applications:
  - Finding all permutations of a set of values
  - Parsers
  - Different games: sudoku, anagrams, crosswords, word jumbles, 8 queens

# Backtracking Strategies

- When solving a backtracking problem, we often ask:
  - What are the "choices" in this problem?
    - What is the "base case"?
    - How do I know when I'm out of choices?
  - How do I "make" a choice?
    - Do I need to create additional variables to remember my choices?
    - Do I need to modify the values of existing variables?
  - How do I explore the rest of the choices?
    - Do I need to remove the made choice from the list of choices?
  - Once I'm done exploring, what should I do?
  - How do I "un-make" a choice?

# Backtracking Algorithm

A general pseudo-code algorithm for backtracking problems:

Explore(choices):

If there are no more choices to make:  
stop

Else:

Choose C.

Explore the remaining choices.

Un-choose C, if necessary. (backtrack!)

- Why are we talking about backtracking now?
  - Many backtracking problems can be implemented using a stack!

# Example: Maze



[Pictures credit: <https://d1f28u9l1tudce.cloudfront.net/inside-culvers/tyf-story-corn-maze.jpg>]

[Example credit: Zorah Fung, University of Washington]

# Example: Class Maze

- Let's assume that we have class `Maze` with the following methods:

Method/Constructor	Description
<code>public Maze(String text)</code>	construct a given maze
<code>public int getHeight(), getWidth()</code>	get maze dimensions
<code>public boolean isExplored(int r, int c)</code> <code>public void setExplored(int r, int c)</code>	get/set whether you have visited a location
<code>public void isWall(int r, int c)</code>	whether given location is blocked by a wall
<code>public void mark(int r, int c)</code> <code>public void isMarked(int r, int c)</code>	whether given location is marked in a path
<code>public String toString()</code>	text display of maze

[Example credit: Zorah Fung, University of Washington]

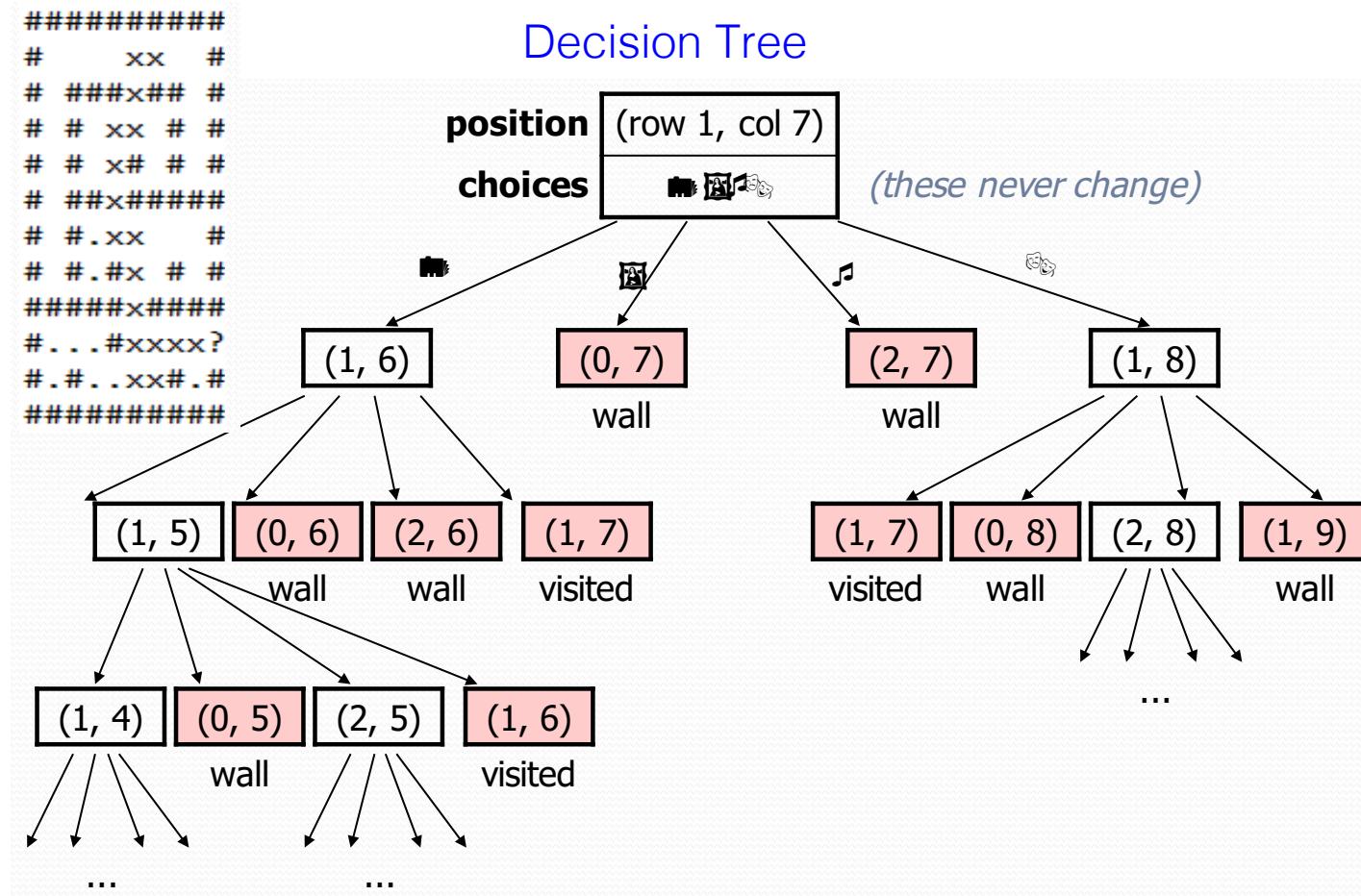
# Example: Solving the Maze

- Write a method `solveMaze` that accepts as parameters:
  - A maze
  - A starting row/columnand tries to find a path in out of the maze starting from that position
- If you find a solution:
  - Your code should **stop** exploring
  - You should **mark** the path out of the maze on your way back out of the recursion, using backtracking
  - (As you explore the maze, squares you set as 'explored' will be printed with a dot, and squares you 'mark' will display an X)

```
#####
#   xx  #
# ####x## #
# # xx # #
# # x# # #
# ##x######
# .xx      #
# .#x # #
#####x#####
#...#xxxx?
#.#. .xx#.#
##########
```

[Example credit: Zorah Fung, University of Washington]

# Example: Solving the Maze



[Picture credit: Zorah Fung]

What are our choices in this problem?

Algorithms and Data Structures 1

# QUEUE ADT

# My Least Favorite Queues



[Pictures credit: <http://airport.blog.ajc.com>, <https://s1.cdn.autoevolution.com/images/news/the-longest-traffic-jam-in-history-12-days-62-mile-long-47237-7.jpg>]

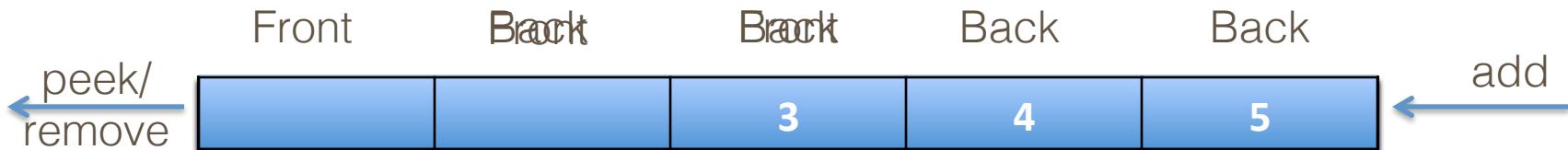
# What is a Queue?

- **Queue** – a data collection that retrieves elements in the FIFO order (first in, first out)
  - Elements are stored in order of insertion, but don't have indexes
    - Client can only:
      - Add to the end of the queue,
      - Examine/remove the front of the queue
- Basic queue operations:
  - **Add** (enqueue) - add an element to the back of the queue
  - **Peek** - examine the front element
  - **Remove** (dequeue) - remove the front element



# Implementations of Queues

- Like stack, queue can be seen as a list with restriction, and can be implemented as a list:
- Example: [ArrayList implementation](#)
  - Initially, queue only has elements 1 and 2
  - Add another element, 3, to the queue
  - Add another element, 4, to the queue
  - Add another element, 5, to the queue
  - Remove an element from the queue
  - Remove an element from the queue



What happens when we remove two more elements from the queue?

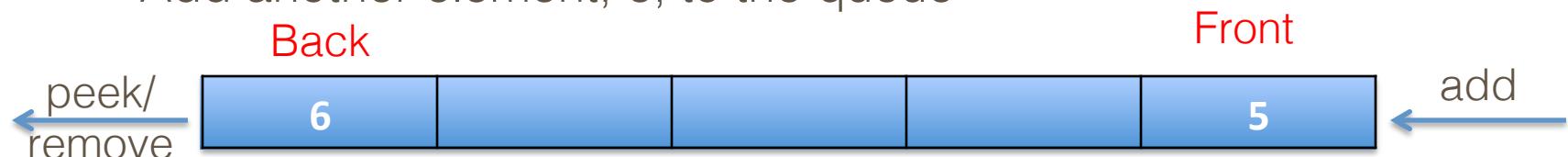
# Implementations of Queues

- What happens when we remove two more elements from the queue?



- Approach – circular array implementation - whenever front or back get to the end of the array, allow them to wrap around to the beginning
- Example:

- Add another element, 6, to the queue

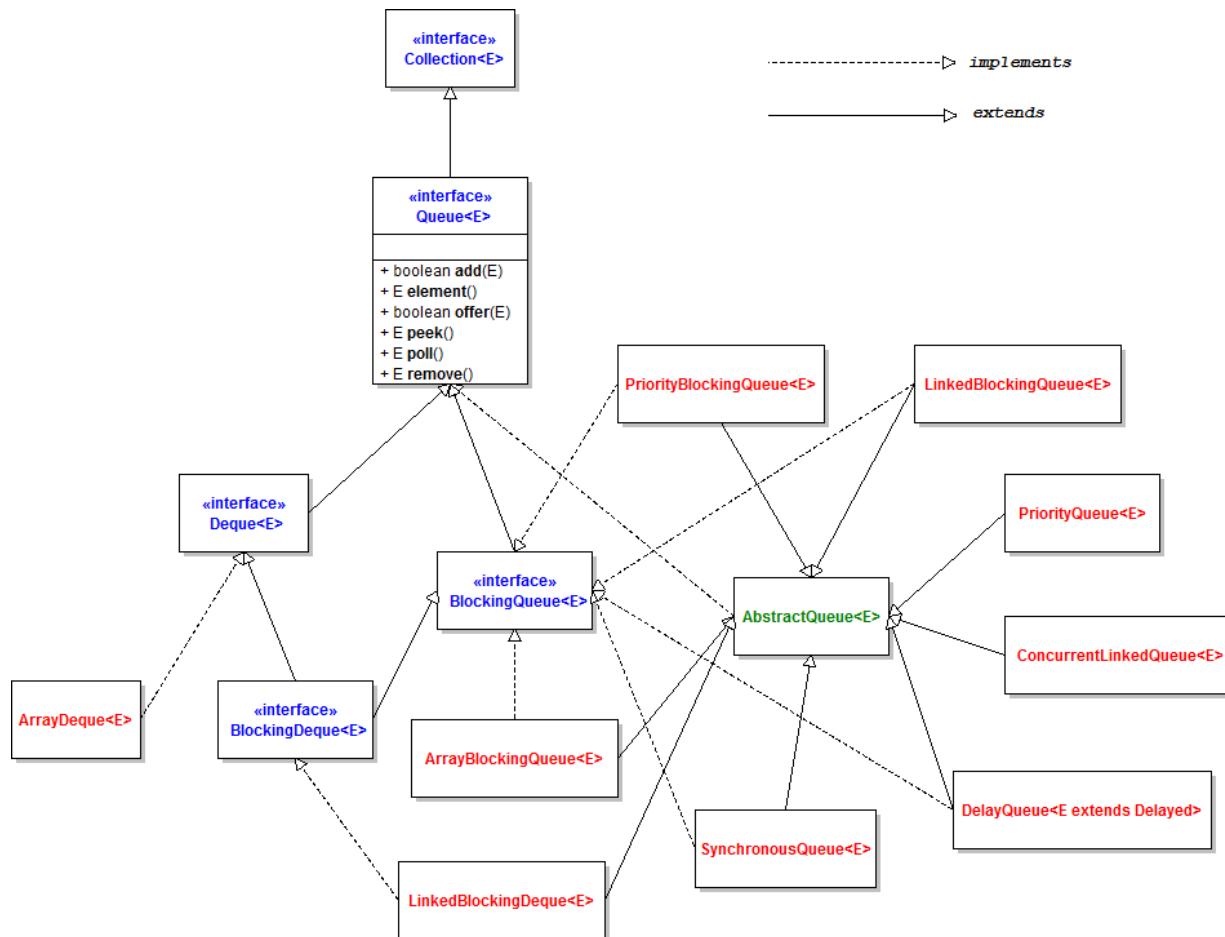


- What is the front and what is the back of the queue now?

# Applications of Queues

- Operating systems:
  - Queue of print jobs to send to the printer
  - Queue of programs / processes to be run
  - Queue of network data packets to send
- Programming:
  - Modeling a line of customers or clients
  - Storing a queue of computations to be performed in order
- Real world examples:
  - People waiting in some line
  - ???

# Class Diagram of the Queue API



[Pictures credit: <http://www.codejava.net/java-core/collections/class-diagram-of-queue-api>]

# Java Interface Queue

<code>add (value)</code>	places given value at back of queue
<code>remove ()</code>	removes value from front of queue and returns it; throws a <code>NoSuchElementException</code> if queue is empty
<code>peek ()</code>	returns front value from queue without removing it; r eturns <code>null</code> if queue is empty
<code>size ()</code>	returns number of elements in queue
<code>isEmpty ()</code>	returns <code>true</code> if queue has no elements

- Example:

```
Queue<Integer> myQueue = new LinkedList<Integer>();  
myQueue.add(10);  
myQueue.add(18);  
myQueue.add(2017); // front [10, 18, 2017] back  
System.out.println(myQueue.remove()); // 10
```

# Mixing Queues and Stacks

- We often mix stacks and queues to achieve certain effects
- Example: Reverse the order of the elements of a queue

```
Queue<Integer> q = new LinkedList<Integer>();  
q.add(1);  
q.add(2);  
q.add(3); // [1, 2, 3]  
Stack<Integer> s = new Stack<Integer>();  
while (!q.isEmpty()) {  
    s.push(q.remove()); } // Q -> S  
while (!s.isEmpty()) {  
    q.add(s.pop()); } // S -> Q  
System.out.println(q); // [3, 2, 1]
```

Algorithms and Data Structures 1

# TREES

# Trees



[Pictures credit: <https://static1.squarespace.com/>]

# Trees

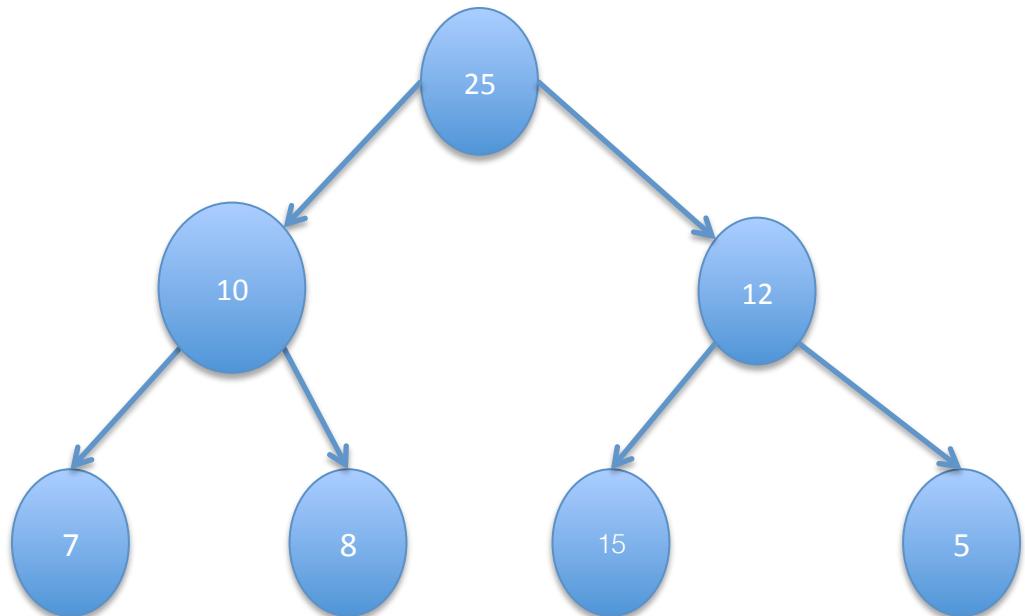
- Tree - a directed, acyclic structure of linked nodes
    - Directed - one-way links between nodes
    - Acyclic - no path wraps back around to the same node twice
  - Can be defined recursively:
    - A tree is either:
      - Empty(null), or
      - A root node that contains:
        - Data
        - A left subtree
        - A right subtree
- (The left and/or right subtree could be empty)

# Trees Terminology

- **Node** - an object containing a data value and left/right children
- **Root** - topmost node of a tree
- **Subtree** – a smaller tree of nodes on the left or right of the current node
- **Parent** - a node above the left and right subtrees, that both subtrees are connected to
- **Child** - a root of each subtree
- **Sibling** - a node with a common parent
- **Leaf** - a node that has no children
- **Branch** - any internal node; neither the root nor a leaf
- **Level** or **depth** - length of the path from a root to a given node
- **Height** - length of the longest path from the root to any node

# Trees Terminology Example

- **Nodes:** {25, 10 ,12, 7, 8, 15, 5}
- **Root:** 25
- **Subtrees:** {10, 7, 8} and {12, 15, 5}
- **Parents:** 10 → {7, 8}, 12 → {15, 5}, 25→ {10, 12}
- **Children:** {10, 12, 7, 8, 15, 5}
- **Siblings:** {7, 8}, {15, 5} and {10, 12}
- **Leaves:** {7, 8, 15, 5}
- **Height:** 3



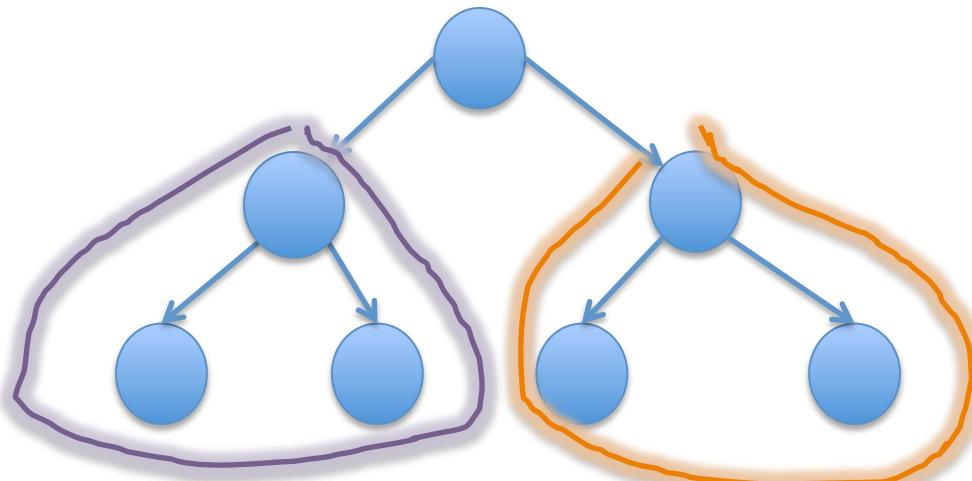
# Implementation of Trees

- Idea: each node in the tree keeps track of:
  - Its data
  - Links to all of its children
- Problem: The number of children per node is not known in advance, and may vary significantly
- Approach: Keep a children of each node in a linked list of tree nodes

```
class TreeNode {  
    Object element;  
    TreeNode firstChild;  
    TreeNode nextSibling;  
}
```

# Binary Trees

- **Binary tree** – a tree in which no node can have more than two children



# Binary Tree Implementation

- A basic `BinaryNode` object stores:
  - Data,
  - Link to the left child
  - Link to the right child
- Multiple nodes can be linked together into a larger tree

```
class BinaryNode{  
    //Friendly data; accessible by other package routines  
    Object element;  
    BinaryNode left;  
    BinaryNode right;  
}
```

# Example: Class StringTreeNode

```
StringTreeNode class
// An StringTreeNode object is one node in a binary tree of String
    public class StringTreeNode{
        public String data; // data stored at this node
        Public StringTreeNode left; // reference to left subtree
        Public StringTreeNode right; // reference to right subtree

        // Constructs a leaf node with the given data
        Public StringTreeNode(String data){
            this(data, null, null);
        }

        // Constructs a branch node with the given data and links
        Public StringTreeNode(String data, StringTreeNode left, StringTreeNode right) {
            this.data = data;
            this.left = left;
            this.right = right;
        }
    }
```

# Example: Class StringTree

```
// An StringTree object represents an entire binary tree of
String.

public class StringTree{
    private StringTreeNode root;
    //some methods
}
```

- Observations:
  - We can only talk to the StringTree, not to the node objects inside the tree
  - Methods of the StringTree create and manipulate the nodes, their data and links between them

Algorithms and Data Structures 1

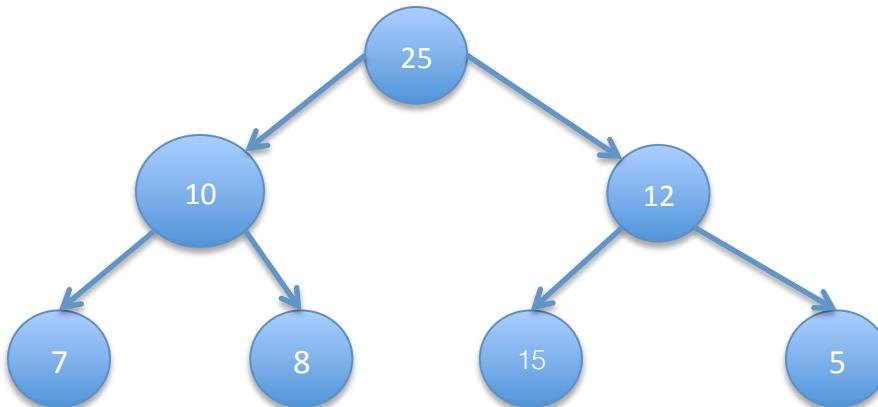
# TREE TRAVERSALS

# Tree Traversals

- Tree traversal - an examination of the elements of a tree
  - Used in many tree algorithms and methods
- Common orderings for traversals:
  - Pre-order – process root node, then its left/right subtrees
  - In-order – process left subtree, then root node, then right subtree
  - Post-order – process left/right subtrees, then root node

# Tree Traversals Example

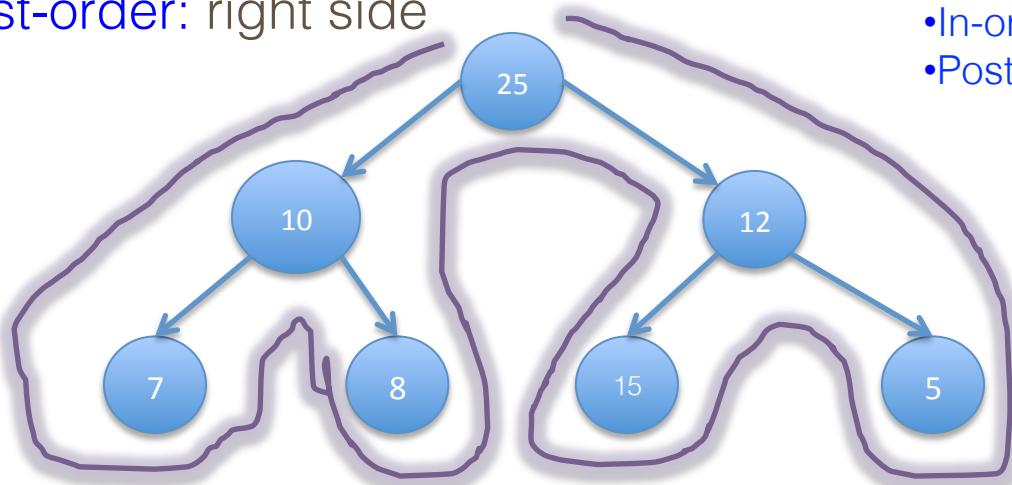
- Common orderings for traversals:
  - **Pre-order** – process root node, then its left/right subtrees
  - **In-order** – process left subtree, then root node, then right subtree
  - **Post-order** – process left/right subtrees, then root node



- Pre-order: 25 10 7 8 12 15 5
- In-order: 7 10 8 25 15 12 5
- Post-order: 7 8 10 15 5 12 25

# Tree Traversals Trick

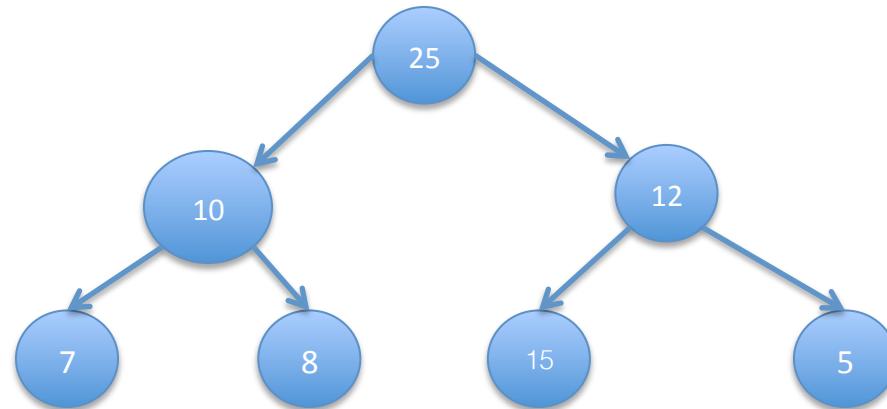
- To quickly generate a traversal, trace a path around the tree
- As you pass a node on the proper side, process it:
  - Pre-order: left side
  - In-order: bottom
  - Post-order: right side



- Pre-order: 25 10 7 8 12 15 5
- In-order: 7 10 8 25 15 12 5
- Post-order: 7 8 10 15 5 12 25

# Example: Printing a Tree

- Assume we have some class IntTree
- Add a method `print` to the `IntTree` class that prints the elements of the tree, such that
  - Elements of a tree are separated by spaces
  - A node's left and right subtree should be printed before it
- Example: `tree.print(); //7 8 10 15 5 12 25`



# Example: Printing a Tree

```
// An IntTree object represents an entire binary tree of ints
public class IntTree{
    private IntTreeNode overallRoot; // null for an empty tree ...
    public void print() {
        print(overallRoot);
        System.out.println(); // end the line of output
    }
    private void print(IntTreeNode root) {
        // (base case is implicitly to do nothing on null)
        if (root != null) {
            // recursive case: print left, right, center
            print(overallRoot.left);
            print(overallRoot.right);
            System.out.print(overallRoot.data + " ");
        }
    }
}
```

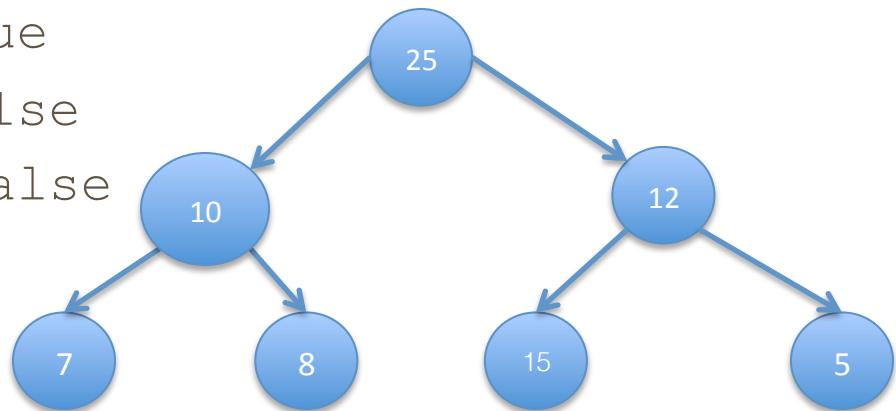
# Template for Tree Methods

- Tree methods are often implemented recursively with a public/private pair
  - The private version accepts the root node to process

```
public class IntTree {  
    private IntTreeNode overallRoot;  
  
    ...  
    public type name(parameters) {  
        name(overallRoot, parameters);  
    }  
    private type name(IntTreeNode root, parameters) {  
        ...  
    }  
}
```

## Example: contains ()

- Add a method `contains` to the `IntTree` class that searches the tree for a given integer, returning `true` if it is found.
- Example: If an `IntTree` variable `tree` referred to the tree below, the following calls would have these results:
  - `tree.contains(25) → true`
  - `tree.contains(12) → true`
  - `tree.contains(4) → false`
  - `tree.contains(77) → false`



## Example: contains()

```
// Returns whether this tree contains the given integer
public boolean contains(int value) {
    return contains(overallRoot, value);
}

private boolean contains(IntTreeNode node, int value) {
    if (node == null) {
        return false; // base case: not found here
    } else if (node.data == value) {
        return true; // base case: found here
    } else {
        // recursive case: search left/right subtrees
        return contains(node.left, value) || contains(node.right,
               value);
    }
}
```

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## **ASSIGNMENT 4 – COMMENTS AND HINTS**

# Assignment 4 – Background

- **Halloween Trick-or-treating:**
  - Kids walk from a house to a house, asking for a trick or a treat
  - Different houses give out different kinds of treats (candy)
  - Kids have very particular preferences what kinds of candy would they like to get
  - Kids also have historical knowledge about the type of candy given out in different households

# Assignment 4

- Your Assignment:
  - Given:
    - Historical knowledge about the neighborhood
    - A list of desired candy for every child
  - Find a way to traverse a neighborhood to get all the candy from the list

# Assumptions and Simplifications

- Only one neighborhood, with four kinds of houses:
  - Mansions
  - Detached homes
  - Duplexes
  - Townhomes
- Houses give out four different sizes of candy:
  - Super size
  - King size
  - Regular size (default)
  - Fun size

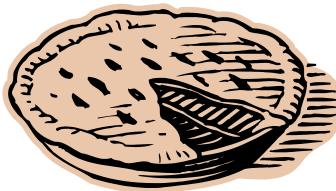
# Assumptions and Simplifications

- Houses give out ten different kinds of candy:
  - Twix
  - Snickers
  - Mars
  - Kit Kat
  - Whoopers
  - Milky Way
  - Toblerone
  - Crunch
  - Baby Ruth
  - Almond Joy
- And not other kind and size of candy

# Assumptions and Simplifications

- Desired list of candy:
  - Case-insensitive
  - Ordered
- Historical knowledge about households:
  - Specifics which household gives out which size and kind of candy

# How Do You Implement This?



- **Classic slogans:**
  - Do one thing well
  - Minimize coupling, maximize cohesion
  - Isolate operations/abstractions in modules
  - Hide implementation details
- **Idea:** abstract class Candy, inherited by a concrete candy class for every candy type

# Where do the Operations Go?

- Pure “object-oriented” style
  - Really, really, really smart candy objects
  - Each candy object knows how to perform every operation on itself

```
public class TwixCandy extends Candy{  
    public TwixCandy(...);  
    public typeCheck(...);  
    public print();  
    public prettyPrint(...);  
    ...  
}
```

# Critique

- This is nicely encapsulated – all details about a TwixCandy are hidden in that class
- But it is poor modularity
- What happens if we want to add some new operation on a candy?
  - Have to modify every concrete candy class ☹
- Worse: the details of any particular operation (e.g., type checking, print) are scattered across all candy classes

# Modularity Issues

- Smart objects make sense if the set of operations is relatively fixed, but we expect to need flexibility to add new kinds of objects
- Example: graphics system
  - Operations: draw, move, iconify, highlight
  - Objects: textbox, scrollbar, canvas, menu, dialog box, window, plus new objects defined as the system evolves

# Visitor Pattern

- Idea: package each operation (print, pretty print, maximize candy) in a separate visitor class
- Create exactly one instance of each visitor class
  - Sometimes called a “function object”
  - Contains all of the methods for that particular operation, one for each kind of an object
- Include a generic “accept visitor” method in every class
- To perform an operation, pass the appropriate “visitor object” around during a traversal

# Avoiding instanceof

- We'd like to avoid huge if-elseif nests in the visitor to discover the node types

```
void checkTypes(Candy c) {  
    if (c instanceof TwixCandy) { ... }  
    else if (c instanceof MarsCandy) { ... }  
    else if (c instanceof KitKatCandy) { ... }  
  
    ...  
}
```

# Visitor Double Dispatch

- Idea: include a “visit” method for every type object in each Visitor

```
void visit(TwixCandy);  
void visit(MarsCandy);  
etc.
```
- Include an `accept(Visitor v)` method in every class
- When **Visitor v** is passed to an **object**, the **object's** accept method calls **v.visit(this)**
  - Selects correct Visitor method for this node
  - “Double dispatch”

# Visitor Interface

- Every separate Visitor implements this interface

```
interface Visitor {  
    // overload visit for every object type  
    public void visit(TwixCandy c);  
    public void visit(MarsCandy c);  
    public void visit(KitKatCandy c);  
    ...  
}
```

# Accept Method in Each Class

- Every class overrides accept(Visitor)
- Example

```
public class TwixCandy extends Candy{  
    ...  
    // accept a visit from a Visitor object v  
    public void accept(Visitor v) {  
        v.visit(this);  
    }  
    ...  
}
```

- Key points
  - Visitor object passed as a parameter to TwixCandy
  - TwixCandy calls visitor's visit method, which dispatches to visit(TwixCandy) automatically – i.e., the correct method in the visitor object for this kind of node

# Encapsulation

- A visitor object often needs to be able to access state in the objects
  - .∴ May need to expose more object's state than we might have done otherwise
    - i.e., lots of public fields in objects
  - Overall a good tradeoff – better modularity (plus, the objects are relatively simple data objects anyway – not hiding much of anything)

## Your Questions



[Meme credit: imgflip.com]

# References and Reading Material

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