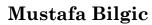
#### CS 581 – ADVANCED ARTIFICIAL INTELLIGENCE

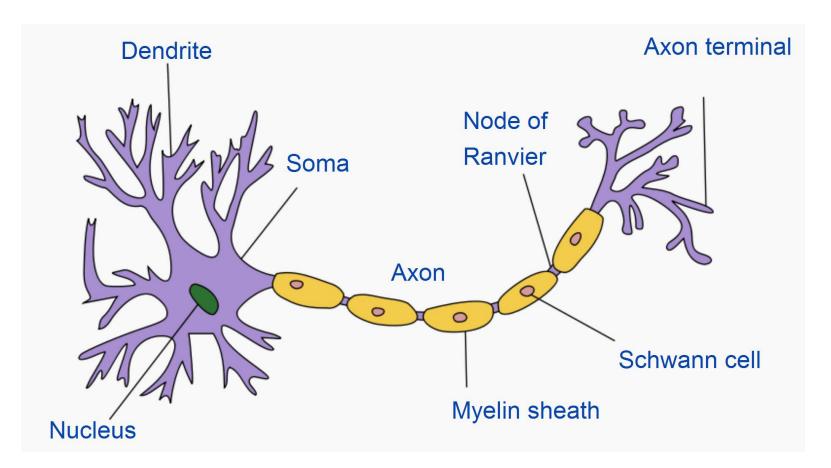
**TOPIC: NEURAL NETWORKS** 





http://www.cs.iit.edu/~mbilgic

## NEURON



By Quasar Jarosz at English Wikipedia, CC BY-SA 3.0, <a href="https://commons.wikimedia.org/w/index.php?curid=7616130">https://commons.wikimedia.org/w/index.php?curid=7616130</a>

#### NEURON

- Neurons can have multiple dendrites and at most one axon
- Typical connections are from an axon of a neuron to dendrites of other neurons
- Synaptic signals are received through dendrites and somas;
  signals are transmitted through axons
- Signals can excite or inhibit the receiving neuron
- A neuron fires when the excitement is above a threshold
- Note: these are general statements and simplifications, and there are many exceptions!

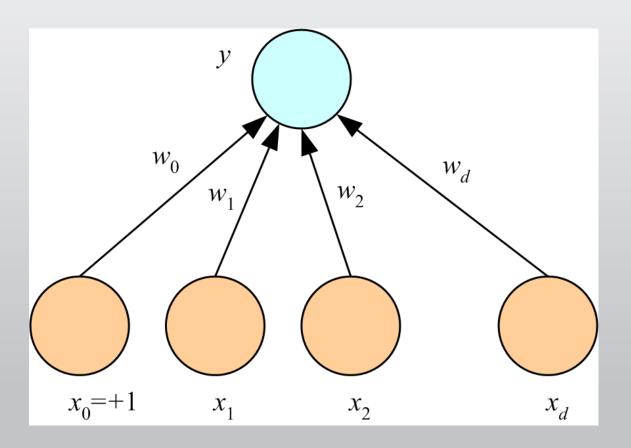
#### ARTIFICIAL NEURAL NETWORKS

- Artificial neural networks are *inspired* by real neurons
- 1943 One of the first neural computational models was proposed by McCulloch and Pitts
- 1958 Perceptron
- 1975 Backpropagation

#### WHAT AN ARTIFICIAL NEURON DOES

- Takes a weighted sum of its inputs (~signals it receives through its dendrites)
  - $w_0 + \sum_{i=1}^k w_i x_i$
  - Assume that there is always a constant input 1, that is,  $x_0 = 1$ . Then,
  - $\sum_{i=0}^k w_i x_i$
- Passes this sum through its activation function (~output at its axon)
  - $f(\sum_{i=0}^k w_i x_i)$

## PERCEPTRON



$$y = sign(w_0 + \sum w_i x_i)$$

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## **EXAMPLES**

- Logical AND
- Logical OR
- Logical XOR
- See OneNote and Notebook

#### SIMPLE MULTILAYER NETWORK FOR XOR

- $\bullet XOR(A,B) = (A \land \neg B) \lor (\neg A \land B)$
- One perceptron for  $(A \land \neg B)$
- One perceptron for  $(\neg A \land B)$
- One perceptron for combining the outputs, through OR, of the two previous perceptrons
- See Notebook

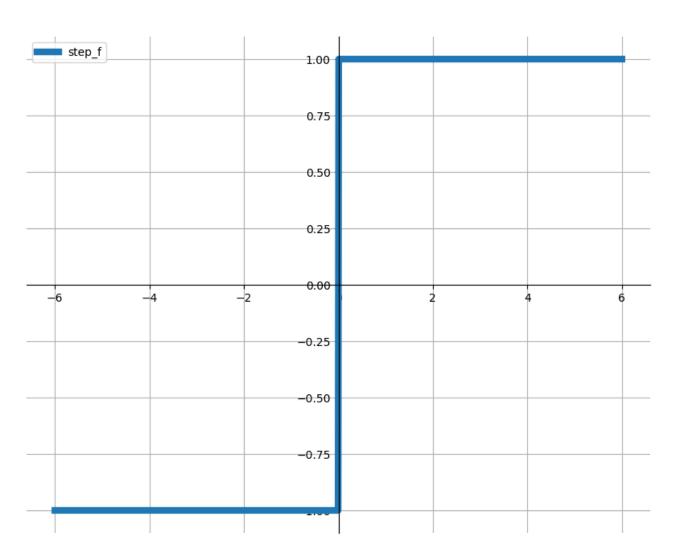
#### VARIOUS ACTIVATION FUNCTIONS

- Identity function
- Bipolar step function
- Binary sigmoid
- Bipolar sigmoid
- Hyperbolic tangent

#### BIPOLAR STEP FUNCTION

- $of(\sum_{i=0}^k w_i x_i) = sign(\sum_{i=0}^k w_i x_i)$
- Returns either +1 or -1 (except right on the decision boundary)
- Useful for both hidden layers and output layer
- However, its discontinuous and it is problematic for learning algorithms that require taking its derivative

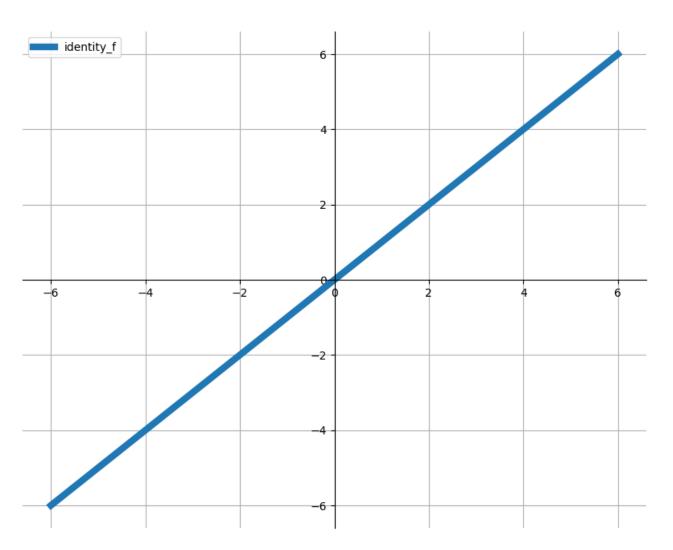
## BIPOLAR STEP FUNCTION



#### **IDENTITY FUNCTION**

- $of(\sum_{i=0}^k w_i x_i) = \sum_{i=0}^k w_i x_i$
- Typically used for the output neurons, when the task is regression
- The identity function should not be used in the hidden layers
  - Linear combination of linear functions is another linear function, and hence using the identity function in the hidden layers do not increase representative power of the neural network

# **IDENTITY FUNCTION**



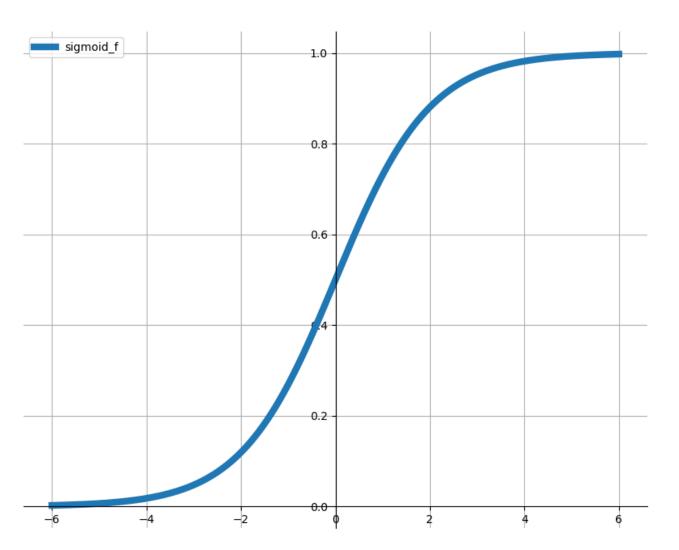
#### BINARY SIGMOID

$$of(\sum_{i=0}^{k} w_i x_i) = \frac{1}{1 + e^{-\sum_{i=0}^{k} w_i x_i}}$$



- This is the logistic function that we used
  - Except, notice the minus sign in front of the sum
    - This is only a convention and does not change much
- The output of the binary sigmoid is between 0 and 1
  - Useful for output layer when the task is classification
  - The output can be interpreted as a probability

## BINARY SIGMOID



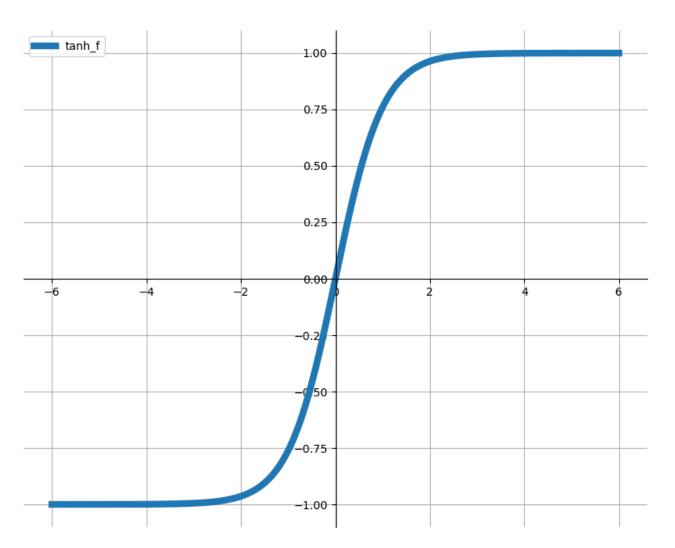
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#### HYPERBOLIC TANGENT

$$\frac{e^{5}-5}{e^{5}+e^{-5}}$$

- $f\left(\sum_{i=0}^{k} w_i x_i\right) = \frac{e^{\sum_{i=0}^{k} w_i x_i e^{-\sum_{i=0}^{k} w_i x_i}}}{e^{\sum_{i=0}^{k} w_i x_i + e^{-\sum_{i=0}^{k} w_i x_i}}}$
- The output of tanh is between -1 and +1
  - Useful for output layer when the task is classification
  - Useful for both hidden and output layers

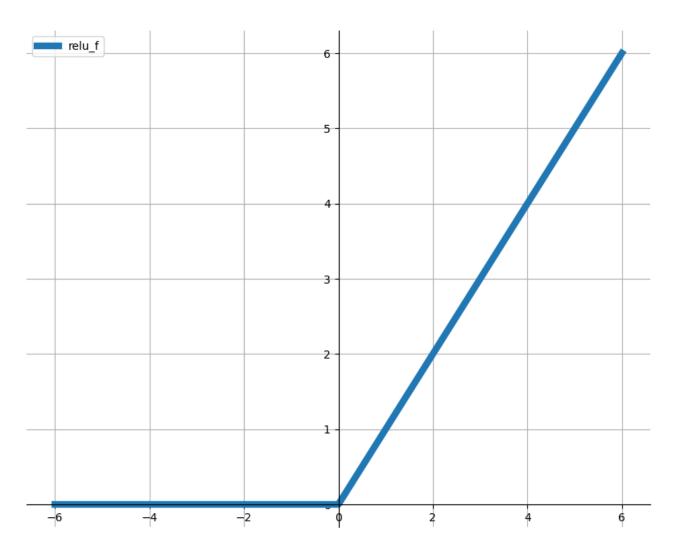
# HYPERBOLIC TANGENT



#### RELU

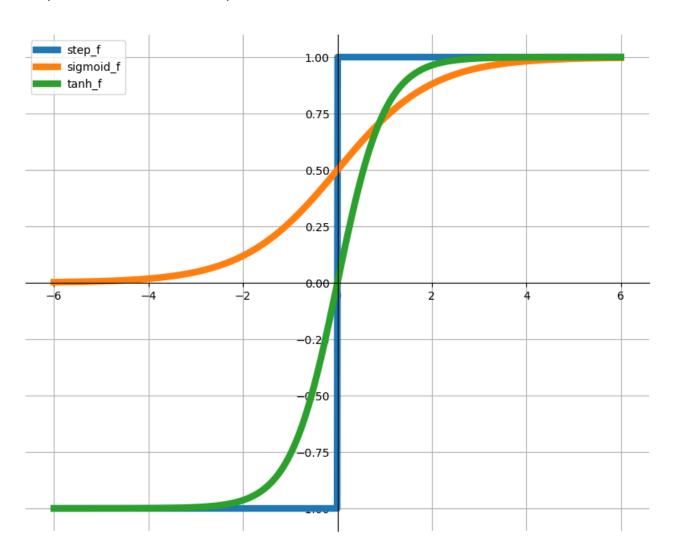
- $of(\sum_{i=0}^{k} w_i x_i) = \sum_{i=0}^{k} w_i x_i \text{ if } \sum_{i=0}^{k} w_i x_i > 0;$ 
  - 0 otherwise
- Typically used for hidden layers, especially for computer vision tasks

# RELU



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# STEP, SIGMOID, TANH



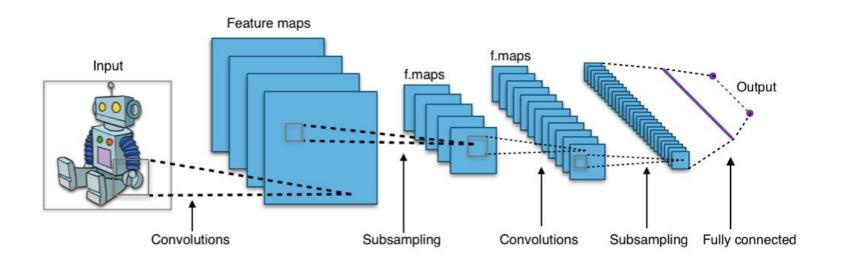
#### DEEP LEARNING

- o Several hidden layers Syuchire
  - Millions of parameters
- Big data, big computation
- o If a neural network with a single hidden layer is a universal approximator, why go deep?
  - "Why and When Can Deep -- but Not Shallow -- Networks Avoid the Curse of Dimensionality: a Review" <a href="https://arxiv.org/abs/1611.00740">https://arxiv.org/abs/1611.00740</a>

#### EXAMPLE DL NETWORK ARCHITECTURES

- Convolutional neural networks (CNN)
- Recurrent neural networks (RNN)
  - Long Short-Term Memory networks (LSTM)

## CONVOLUTIONAL NEURAL NETWORKS



https://commons.wikimedia.org/wiki/File:Typical cnn.png

#### CONVOLUTION

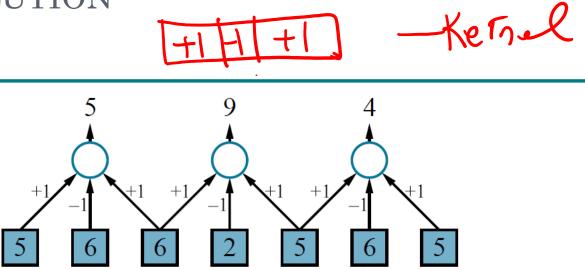


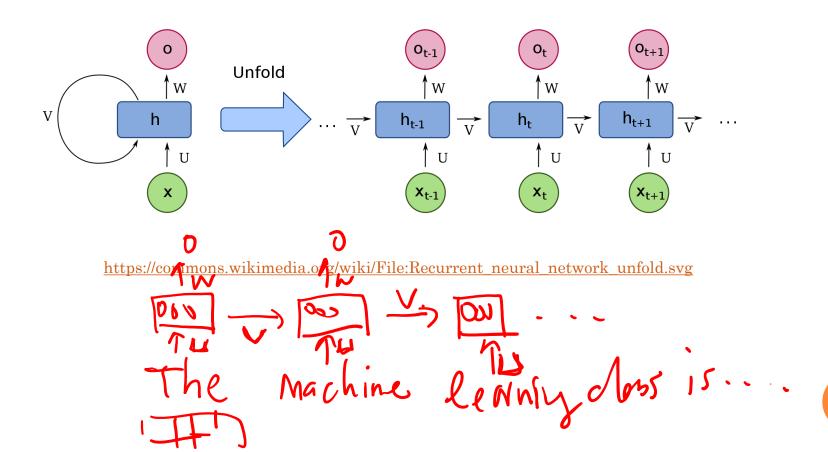
Figure 21.4 An example of a one-dimensional convolution operation with a kernel of size l=3 and a stride s=2. The peak response is centered on the darker (lower intensity) input pixel. The results would usually be fed through a nonlinear activation function (not shown) before going to the next hidden layer.

Figure from <a href="http://aima.cs.berkeley.edu/figures.pdf">http://aima.cs.berkeley.edu/figures.pdf</a>

#### POOLING

- Aggregates a set of adjacent units
- Like convolution, has a kernel size and a stride size
- Unlike convolution, weights are fixed (not learned)
- Examples
  - Average pooling
  - Max pooling

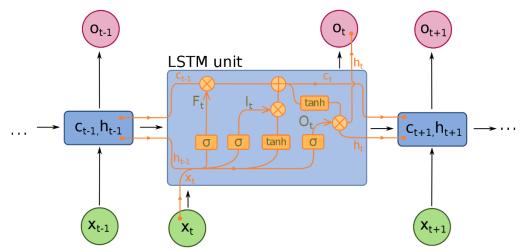
#### RECURRENT NEURAL NETWORKS



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## LONG SHORT-TERM MEMORY (LSTM)

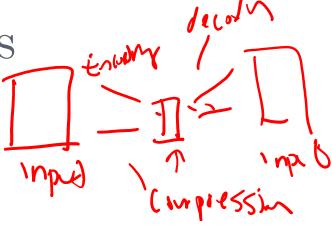
- A specialized RNN
- Works better than vanilla RNN for "remembering" long sequences
- Has additional units
  - Cell, forget gate, input gate, output gate



https://commons.wikimedia.org/wiki/File:Long Short-Term Memory.svg

OTHER NETWORKS/CONCEPTS

- Autoencoder
  - Input and output are the same
- Deep autoregressive model
  - Predict an element of the data using the other elements
- Generative adversarial networks (GAN)
  - A pair of generator and discriminator networks



#### LEARNING THE WEIGHTS

- Define an error (loss) function
- Take its derivative with respect to the weights
- Perform gradient descent

## SOME ERROR/LOSS FUNCTIONS

- Classification: log-loss, cross entropy, negative
  CLL
  - $-(1-t) \times ln(1-y) t \times ln(y) = -$
  - *t*: the true target value (0/1)
  - y: probability of class 1
- Regression: squared error
  - $\frac{1}{2}(t-y)^2$
  - *t*: the true target value
  - *y*: the predicted value

## BACKPROPAGATION ALGORITHM

• See OneNote

# DERIVATIVES OF THE ACTIVATION FUNCTIONS

- $\circ$  f is the activation function, h is the weighted sum of the incoming signals
- $\circ$   $f(h(x)) \equiv \text{binary sigmoid}$

• 
$$\frac{\partial f(h(x))}{\partial x} = f(h(x)) \times (1 - f(h(x))) \times \frac{\partial h(x)}{\partial x}$$

 $\circ$   $f(h(x)) \equiv \tanh$ 

• 
$$\frac{\partial f(h(x))}{\partial x} = (1 + f(h(x))) \times (1 - f(h(x))) \times \frac{\partial h(x)}{\partial x}$$

See OneNote

#### **OVERFITTING**

- Neural networks are powerful tools
- Even with a single hidden layer, they are "universal approximators", i.e., they can approximate arbitrary functions arbitrarily close
- Therefore, it is very easy to overfit them
- To prevent overfitting, utilize
  - Domain knowledge
  - Shared parameters
  - Validation data
  - Regularization
  - Dropout

#### SOME LIBRARIES

#### Scikit-learn

- <a href="https://scikit-learn.org/stable/modules/neural\_networks\_supervised.h">https://scikit-learn.org/stable/modules/neural\_networks\_supervised.h</a>
  <a href="mailto:tml">tml</a>
- Only MLP; no GPU support

#### Keras

• <a href="https://keras.io/">https://keras.io/</a>

#### Tensorflow

https://www.tensorflow.org/

#### PyTorch

https://pytorch.org/