# Competitive Programming Library

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# 1 Dynamic Programming

# 1.1 Some dp patterns

### Maximumu/Minimum path cost

```
const int MAX = 21;
int grid[MAX][MAX];
int mem[MAX][MAX];
int n = 20;
bool valid(int r, int c){
 return r >= 0 \&\& r < n \&\& c >= 0 \&\& c < n:
int maxPathSum(int r, int c){
   if(!valid(r,c)){
       return 0:
   }
   if(r == n-1 \&\& c == n-1){
       return mem[r][c] = grid[r][c];
   // available moves
   int path1 = maxPathSum(r+1,c);
   int path2 = maxPathSum(r,c+1);
   return grid[r][c] + max(path1,path2);
}
```

# add operators between numbers to get max prod/sum

```
// put +, -, between sequence of numbers such that the sum is divisible by
    k, and maximum as possible
const int MAX = 21;
long long mem[MAX][MAX];
const int n = 20;
int k = 4; // example
int v[20];
int fix(int a){
    return (a % k + k) % k;
}
long long tryAll(int pos, int mod){
```

```
long long &ret = mem[pos][mod];
if(ret != -1){
    return ret;
}
if(pos == n){
    return ret = mod == 0;
}
if(tryAll(pos+1,fix(mod + v[pos])) || tryAll(pos+1,fix(mod-v[pos]))){
    return ret = 1;
}
return ret = 0;
}
```

### pick choices with no two similar consecutive choices

```
// pick minimum of choinces costs with no two similar consecutive choices
const int choices = 4;
const int n = 20;
int MAX = n;
int mem[MAX][choices];
const int 00 = 1e6+1;
int minCost(int pos, int lastChoice){
   if(pos == n){
       return 0; // invalid move
   int &ret = mem[pos][lastChoice];
   if(ret != -1){
       return ret;
   }
   ret = 00; // want to minimze
   // let choices are 0, 1, 2
   if(lastChoice != 0){
       ret = min(ret, minCost(pos+1,0));
   }
   if(lastChoice != 1){
       ret = min(ret, minCost(pos+1,1));
   if(lastChoice != 2){
       ret = min(ret, minCost(pos+1,2));
   }
```

```
return ret;
}
```

# sum S and max/min Product

```
int maxK;
11 mem[21][101]; // k, and s
// You are given an integer s and an integer k. Find k positive integers
    a1, a2, ..., ak
// such that their sum is equal to s and their product is the maximal
   possible. Return their product.
11 maxProd(int k, int rem)
if(k == maxK){
 // base case
 if(rem == 0)
  return 1;
 return 0;
 }
if(rem == 0) // invalid case
 return 0;
11 &ret = mem[k][rem];
 if(ret != -1)
 return ret;
 ret = 0;
for (int i = 1; i <= rem; ++i) {</pre>
 ll sol = maxProd(k+1, rem - i) * i;
 ret = max(ret, sol);
 }
 return ret;
```

# 2 Bit Manipulation

# 3 Algorithms

### 3.1 MO

# MO Algorithm

```
// MO
           -> O(N+Q SQRT(N)) <= 10^5
const int N = 1e5+5, M = 1e5+5;
int n, m;
int nums[N], q_ans[M];
struct query {
   int idx, block_idx, l, r;
   query() = default;
   query(int _1, int _r, int _idx) {
       idx = _idx;
       r = _r - 1;
       1 = _1 - 1;
       block_idx = _l / sqrt(n);
   }
   bool operator <(const query & y) const {</pre>
       if(y.block_idx == block_idx) return r < y.r;</pre>
       return block_idx < y.block_idx;</pre>
};
int freq[N], ans;
void add(int idx) {
   freq[nums[idx]]++;
   if (freq[nums[idx]] == 2) ans++;
}
void remove(int idx) {
   freq[nums[idx]]--;
   if (freq[nums[idx]] == 1) ans--;
}
cin >> n >> m;
for (int i = 0; i < n; ++i) cin >> nums[i];
```

```
vector<query> Query(m);
for (int i = 0; i < m; ++i) {
    int l, r; cin >> l >> r;
    Query[i] = query(l, r, i);
}

sort(Query.begin(), Query.end());
int l0 = 1, r0 = 0;
for (int i = 0; i < m; ++i) {
    while (l0 < Query[i].l) remove(l0++);
    while (l0 > Query[i].l) add(--l0);
    while (r0 < Query[i].r) add(++r0);
    while (r0 > Query[i].r) remove(r0--);
    q_ans[Query[i].idx] = ans;
}
for (int i = 0; i < m; ++i) {
    cout << q_ans[i] << '\n';
}</pre>
```

# 4 Data Structures

# 4.1 Strings

#define MAX\_CHAR 26

## 4.1.1 Trie (Prefix Tree)

## $Basic\ Implementation$

```
struct TrieNode {
   TrieNode *pTrieNode[MAX_CHAR]{};
   bool isWord;
   TrieNode() {
       isWord = false;
       fill(pTrieNode, pTrieNode + 26, (TrieNode *) NULL);
   }
   virtual ~TrieNode() = default;
};
class Trie {
private:
   TrieNode *root;
public:
   Trie() {
       root = new TrieNode();
   }
   virtual ~Trie() = default;
   TrieNode *getTrieNode() {
       return this->root;
   }
   void insert(const string &word) {
       TrieNode *current = root;
       for (char c: word) {
           int i = c - 'a';
          if (current->pTrieNode[i] == nullptr)
              current->pTrieNode[i] = new TrieNode();
           current = current->pTrieNode[i];
```

```
current->isWord = true;
   }
   bool search(const string &word) {
       TrieNode *current = root;
       int ch = 0:
       for (char c: word) {
          ch = c - 'a';
          if (current->pTrieNode[ch] == nullptr)
              return false:
          current = current->pTrieNode[ch];
       }
       return current->isWord;
   }
   bool startsWith(const string &prefix) {
       TrieNode *current = root;
       int ch = 0;
       for (char c: prefix) {
          ch = c - 'a';
          if (current->pTrieNode[ch] == nullptr)
              return false;
          current = current->pTrieNode[ch];
       return true;
   }
};
```

# 4.2 Range Queries

### 4.2.1 Segment Tree

### Basic Implementation

```
struct Node {
    long long val;
};

struct SegTree {
private:
    const Node NEUTRAL = {INT_MIN};
```

```
static Node merge(const Node& x1, const Node& x2) {
       return {x1.val + x2.val};
   }
   void set(const int& idx, const int& val, int x, int lx, int rx) {
       if (rx - lx == 1) return void(values[x].val = val):
       int mid = (rx + lx) / 2;
       if (idx < mid)</pre>
           set(idx, val, 2 * x + 1, lx, mid);
       else
           set(idx, val, 2 * x + 2, mid, rx);
       values[x] = merge(values[2 * x + 1], values[2 * x + 2]);
   }
   Node query(const int& 1, const int& r, int x, int lx, int rx) {
       if (lx >= r || l >= rx) return NEUTRAL;
       if (lx >= 1 && rx <= r) return values[x];</pre>
       int mid = (rx + lx) / 2;
       return merge(query(1, r, 2 * x + 1, 1x, mid), query(1, r, 2 * x + 1
           2, mid, rx));
   }
   void build(vector<int> &a, int x, int lx, int rx) {
       if (rx - 1x == 1) {
           if (lx < a.size()) {</pre>
              values[x] = single(a[lx]);
          }
           return;
       int m = (1x + rx) / 2;
       build(a, 2 * x + 1, lx, m);
       build(a, 2 * x + 2, m, rx);
       values[x] = merge(values[2 * x + 1], values[2 * x + 2]);
   }
public:
   int size{};
   vector<Node> values;
   void build(vector<int> &a) {
```

```
build(a, 0, 0, size);
}

void init(int _size) {
    size = 1;
    while (size < _size) size *= 2;
    values.assign(2 * size, NEUTRAL);
}

void set(int idx, int val) {
    set(idx, val, 0, 0, size);
}

Node query(const int& 1, const int& r) {
    return query(1, r, 0, 0, size);
}
};</pre>
```

#### 4.2.2 Fenwick Tree

#### Fenwick Tree

```
struct Fenwick {
   // One Based
   vector<int> tree;
   explicit Fenwick(int n) {tree.assign(n + 5, {});}
   // Computes the prefix sum from [1, i], O(\log(n))
   int query(int i) {
       int res = 0;
       while (i > 0) {
           res += tree[i];
           i &= ~(i & -i);
       }
       return res;
   }
   int query(int 1, int r) {
       return query(r) - query(l-1);
   }
   // Get the value at index i
```

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```
int get(int i) {
    return query(i, i);
}

// Add 'v' to index 'i', O(log(n))
void update(int i, int v) {
    while (i < tree.size()) {
        tree[i] += v;
        i += (i & -i);
    }
};</pre>
```

# 4.2.3 Sparse Table

### 4.3 Ordered Set

### Ordered Set

# 5 Counting Principles

### 5.1 nCr

$$C(n,k) = \frac{n!}{(n-k)!k!} = \frac{n*(n-1)*(n-2)*...*(n-k+1)}{k!}$$

#### 5.1.1 Fast nCr

$$C(n,k) = \frac{n * (n-1) * (n-2) * \dots * (n-k+1)}{1 * 2 * 3 * \dots * k} = \prod_{i=0}^{k-1} \frac{n-i}{i+1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1}$$

#### Fast nCr

```
int nCr(const int& n, const int& r) {
   double res = 1;
   for (int i = 1; i <= r; ++i)
      res = res * (n - r + i) / i;
   return (int)(res + 0.01);
}</pre>
```

# 6 Graph Theory

# 6.1 Shortest Path algorithms

# 6.2 Dijkstra Algorithm

### Dijkstra Implementation

```
#define INF (1e18) // for int defined as 11
int n, m;
vector<vector<pair<int, int>>> adj;
vector<int> cost;
vector<int> parent;
void dijkstra(int startNode = 1) {
   priority_queue<pair<11, int>, vector<pair<11, int>>, greater<>> pq;
   cost[startNode] = 0;
   pq.emplace(0, startNode);
   while (!pq.empty()) {
       int u = pq.top().second;
       11 d = pq.top().first;
       pq.pop();
       if (d > cost[u]) continue:
       for (auto &p: adj[u]) {
          int v = p.first;
          int w = p.second;
          if (cost[v] > cost[u] + w) {
              cost[v] = cost[u] + w;
              parent[v] = u;
              pq.emplace(cost[v], v);
          }
       }
   }
}
void run_test_case(int testNum) {
   cin >> n >> m;
   adj.assign(n + 1, {});
```

```
cost.assign(n + 1, INF);
parent.assign(n + 1, -1);
while (m--) {
    // Read Edges
}
dijkstra();
if (cost[n] == INF) {
    cout << -1 << el; // not connected {Depends on you use case}</pre>
    return:
}
stack<int> ans;
for (int v = n; v != -1; v = parent[v]) ans.push(v);
while (!ans.empty()) { // printing the path
    cout << ans.top() << ' ';</pre>
    ans.pop();
}
cout << el;</pre>
```

# 6.3 Floyd Warshal Algorithm

## $Floyd Warshal\ Implementation$

```
int main() {
   int n, m; cin >> n >> m;
   vector <vector <int>> adj(n + 1, vector <int>> (n + 1, 2e9));
   for (int i = 0; i < n; i++) adj[i][i] = 0;

while(m--) {
    int u, v, w;
   cin >> u >> v >> w;
    adj[u][v] = min(adj[u][v], w);
   adj[v][u] = min(adj[v][u], w);
}

for (int mid = 1; mid <= n; mid++) {
    for (int start = 1; start <= n; start++) {</pre>
```

# 6.4 Bellman Ford Algorithm

### BellmanFord Implementation

```
vector <vector <pair<int, int>>> &adj
vector <long long> BellmanFord(int src) {
   int n = (int)adj.size();
   vector <long long> dist(n, 2e18);
   dist[src] = 0:
   for (int it = 0; it < n-1; it++) {</pre>
       bool in = false;
       for (int i = 0; i < n; i++) { // iterate on the edges
           for (auto &[j, w] : adj[i]) {
              if (dist[j] > dist[i] + w) {
                  in = true;
                  dist[j] = dist[i] + w;
           }
       if (!in) return dist;
   for (int i = 0; i < n; i++) {</pre>
       for (auto &[j, w] : adj[i]) {
           if (dist[j] > dist[i] + w) { //negative cycle
              return vector <long long> (n, -1); // or any flag
   }
```

```
return dist;
}
```

# 6.5 Cycle Detection

### 6.5.1 DFS Implementation

# $DFS\ Implementation$

```
// return true with number of nodes in the cycle, either odd cycle or even
bool cycle_detection(unordered_map<int, vector<int>>> &graph, int source,
    int par, unordered_map<int,bool> vis, int c){
    if(vis[source]) return true;

    vis[source] = true;

    for(int v: graph[source]){
        if(v != par){
            c++;
            if(dfs(graph,v, source, vis, c)) return true;
        }
    }
    return false;
}
```

### 6.5.2 Another way for undirected graphs

## Another way for undirected graphs

```
// this is true only for undirected graphs
bool dfs1(int cur, int par) {
   bool ret = false;
   vis[cur] = true;
   for (auto &i : adj[cur]) {
      if (!vis[i]) ret|=dfs1(i, cur);
      else if (par != i) ret = true;
   }
   return ret;
}
```

### 6.5.3 General Way

## General Way

```
// general algorithm
vector <bool> cyc;
bool dfs(int cur, int par) {
   bool ret = false;
   vis[cur] = cyc[cur] = true;
   for (auto &i : adj[cur]) {
      if (par == i) continue;
      if (!vis[i]) ret|=dfs(i, cur);
      else if (cyc[i]) ret = true;
   }
   cyc[cur] = false;
   return ret;
}
```

### 6.5.4 DSU Implementation

### DSU Implementation

```
#include <iostream>
#include <vector>
class UnionFind {
public:
   UnionFind(int n) {
       parent.resize(n);
       rank.resize(n, 0);
       for (int i = 0; i < n; ++i) {</pre>
           parent[i] = i;
   }
   int find(int u) {
       if (parent[u] != u) {
           parent[u] = find(parent[u]);
       }
       return parent[u];
   }
   void unionSets(int u, int v) {
```

```
int rootU = find(u);
       int rootV = find(v);
       if (rootU != rootV) {
           if (rank[rootU] > rank[rootV]) {
              parent[rootV] = rootU;
           } else if (rank[rootU] < rank[rootV]) {</pre>
              parent[rootU] = rootV;
           } else {
              parent[rootV] = rootU;
              ++rank[rootU];
       }
   }
private:
   std::vector<int> parent;
   std::vector<int> rank;
};
bool detectCycle(const std::vector<std::pair<int, int>>& edges, int n) {
   UnionFind uf(n);
   for (const auto& edge : edges) {
       int u = edge.first;
       int v = edge.second;
       if (uf.find(u) == uf.find(v)) {
           return true;
       uf.unionSets(u, v);
   }
   return false;
int main() {
   std::vector<std::pair<int, int>> edges = { {0, 1}, {1, 2}, {2, 3}, {3,
        0} };
   int n = 4; // Number of vertices
   if (detectCycle(edges, n)) {
       std::cout << "Cycle detected" << std::endl;</pre>
   } else {
```

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```
std::cout << "No cycle detected" << std::endl;
}
return 0;</pre>
```

# 7 Techniques

# 7.1 Coordinate Compression

```
void coordinate_compress(vector<int> &x, int start=0, int
    step=1) {
    set unique(x.begin(), x.end());
    map<int, int> valPos;

    int idx=0;
    for (auto i: unique) {
      valPos[i] = start + idx * step;
      ++idx;
    }
    for(auto &i: x) i = valPos[i];
}
```

Coordinate Compression

# 8 Templates

# 8.1 MOD Template

```
constexpr int MOD = 1e9+7; // must be a prime number
int add(int a, int b) {
    int res = a+b;
    if(res >= MOD) return res -= MOD;
}
int sub(int a, int b) {
    int res = a-b;
    if(res < 0) return res += MOD;</pre>
}
int power(int a, int e) {
    int res = 1;
    while(e) {if(e & 1) res = res * a % MOD; a = a * a % MOD;
    e >>= 1;}
    return res;
}
int inverse(int a) {
    return power(a, MOD-2);
}
int div(int a, int b) {
    return a * inverse(b) % MOD;
}
```

MOD Template