Competitive Programming Library

Too bad to be Accepted 2023/2024

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1 Templates

1.1 Setup

1.1.1 IO Manipulation

Input/Output

```
#include <bits/stdc++.h>
freopen("input.txt", "r", stdin);
freopen("output.txt", "w", stdout);

#define fastI0  \
   ios_base::sync_with_stdio(false), cin.tie(nullptr), cout.tie(nullptr);
```

1.1.2 GCC Compiler Optimization (Vectorization)

GCC Opt

```
// Ref: USACO guide
// will make GCC auto-vectorize for loops and optimizes floating points
   better (assumes associativity and turns off denormals).
#pragma GCC optimize ("Ofast")
// can double performance of vectorized code, but causes crashes on old
   machines.
#pragma GCC target ("avx,avx2,fma")

// slows down run time but throws a Runtime Error if an overflow occured
#pragma GCC optimize("trapv")
```

1.2 MOD Template

```
constexpr int MOD = 1e9+7; // must be a prime number
int add(int a, int b) {
   int res = a+b;
   if(res >= MOD) return res -= MOD;
}
```

```
int sub(int a, int b) {
   int res = a-b;
   if(res < 0) return res += MOD;
}
int power(int a, int e) {
   int res = 1;
   while(e) {if(e & 1) res = res * a % MOD; a = a * a % MOD;
   e >>= 1;}
   return res;
}
int inverse(int a) {
   return power(a, MOD-2);
}
int div(int a, int b) {
   return a * inverse(b) % MOD;
}
```

MOD Template

1.3 Macros

Macros

```
#define getBit(n, k) (n >> k)
#define ON(n, idx) (n | (111 << idx))
#define OFF(n, idx) (n & ~(111 << idx))
#define toggle(n, idx) ((n) ^ (111<<(idx)))
#define gray(n) (n ^ (n >> 1))
#define bitCount(x) (__builtin_popcountl1(x))
#define clz(x) (__builtin_clzl1(x))
#define ctz(x) (__builtin_ctzl1(x))
#define uniq(x) x.resize(unique(x.begin(), x.end())-x.begin());

#define angle(a) (atan2((a).imag(), (a).real()))
//#define vec(a, b) ((b)-(a))
#define same(v1, v2) (dp(vec(v1,v2),vec(v1,v2)) < EPS)
#define dotProduct(a, b) ((conj(a)*(b)).real()) // a*b cos(T), if zero -> prep
```

```
#define crossProduct(a, b) ((conj(a)*(b)).imag()) // a*b sin(T), if zero
    -> parallel
//#define length(a) (hypot((a).imag(), (a).real()))
#define normalize(a) ((a)/length(a))
#define rotateO(v, ang) ((v)*exp(point(O,ang)))
#define rotateA(p, ang, about) (rotateO(vec(about,p),ang)+about)
#define reflectO(v, m) (conj((v)/(m))*(m))
#define ceil_i(a, b) (((ll)(a)+(ll)(b-1))/(ll)(b))
#define floor_i(a, b) (a/b)
#define round_i(a, b) ((a+(b/2))/b) // if a>0
#define round_m(a, b) ((a-(b/2))/b) // if a<0
#define round_multiple(n, m) round_i(n,m)*m // round to multiple if
    specified element

const double PI = acos(-1.0);</pre>
```

1.4 Grid Navigation

Grid Nav

```
// knight moves on a chess board
int dx[] = { -2, -1, 1, 2, -2, -1, 1, 2 };
int dy[] = { -1, -2, -2, -1, 1, 2, 2, 1 };

// Grid up, down, right, left (Moves for Chess Rook)
int dx[4] = {1, -1, 0, 0};
int dy[4] = {0, 0, 1, -1};

// Grid cell all neighbours
const int dx[8] = {1, 0, -1, 0, 1, 1, -1, -1}
const int dy[8] = {0, 1, 0, -1, -1, 1, -1, 1};

// Grid Diagonal (Moves for Chess Bishop)
int dx[] = {1, 1, -1, -1};
int dy[] = {1, -1, 1, -1};
```

1.5 Integer 128

```
i128
typedef __int128 i128;
__int128 read() {
   \_int128 x = 0, f = 1;
   char ch = getchar();
   while (ch < '0' || ch > '9') {
       if (ch == '-') f = -1;
       ch = getchar();
   }
   while (ch >= '0' && ch <= '9') {
       x = x * 10 + ch - '0';
       ch = getchar();
   }
   return x * f;
void print(__int128 x) {
   if (x < 0) {
       putchar('-');
       x = -x;
   if (x > 9) print(x / 10);
   putchar(x % 10 + '0');
bool cmp(\_int128 x, \_int128 y) { return x > y; }
```

2 Dynamic Programming

2.1 Some dp patterns

Maximumu/Minimum path cost

```
const int MAX = 21;
int grid[MAX][MAX];
int mem[MAX][MAX];
int n = 20;
bool valid(int r, int c){
  return r >= 0 && r < n && c >= 0 && c < n;</pre>
```

```
int maxPathSum(int r, int c){
   if(!valid(r,c)){
      return 0;
   }

   if(r == n-1 && c == n-1){
      return mem[r][c] = grid[r][c];
   }

   // available moves
   int path1 = maxPathSum(r+1,c);
   int path2 = maxPathSum(r,c+1);

   return grid[r][c] + max(path1,path2);
}
```

add operators between numbers to get max prod/sum

```
// put +, -, between sequence of numbers such that the sum is divisible by
    k, and maximum as possible
const int MAX = 21;
long long mem[MAX][MAX];
const int n = 20;
int k = 4; // example
int v[20];
int fix(int a){
 return (a % k + k) % k;
long long tryAll(int pos, int mod){
   long long &ret = mem[pos][mod];
   if(ret != -1){
       return ret;
   if(pos == n){
       return ret = mod == 0;
   if(tryAll(pos+1,fix(mod + v[pos])) || tryAll(pos+1,fix(mod-v[pos]))){
       return ret = 1;
   return ret = 0;
```

pick choices with no two similar consecutive choices

```
// pick minimum of choinces costs with no two similar consecutive choices
const int choices = 4:
const int n = 20;
int MAX = n;
int mem[MAX][choices];
const int 00 = 1e6+1;
int minCost(int pos, int lastChoice){
   if(pos == n){
       return 0; // invalid move
   int &ret = mem[pos][lastChoice];
   if(ret != -1){
       return ret;
   }
   ret = 00: // want to minimze
   // let choices are 0, 1, 2
   if(lastChoice != 0){
       ret = min(ret, minCost(pos+1,0));
   }
   if(lastChoice != 1){
       ret = min(ret, minCost(pos+1,1));
   if(lastChoice != 2){
       ret = min(ret, minCost(pos+1,2));
   return ret;
```

sum S and max/min Product

```
int maxK;

ll mem[21][101]; // k, and s

// You are given an integer s and an integer k. Find k positive integers a1, a2, ..., ak

// such that their sum is equal to s and their product is the maximal possible. Return their product.
```

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```
11 maxProd(int k, int rem)
if(k == maxK){
 // base case
 if(rem == 0)
  return 1;
 return 0;
}
if(rem == 0) // invalid case
 return 0;
11 &ret = mem[k][rem];
if(ret != -1)
 return ret;
ret = 0;
for (int i = 1; i <= rem; ++i) {</pre>
 ll sol = maxProd(k+1, rem - i) * i;
 ret = max(ret, sol);
}
return ret;
}
```

2.2 DP solutions

2.2.1 Max Subarray sum (Kadane's Algorithm)

$Max\ Subarray\ sum$

```
int maxSubarraySum(vector<int>& arr, int len) {
   int ans = INT_MIN, cur = 0;

for (int i = 0; i < len; i++) {
    cur = cur + arr[i];
   if (ans < cur)
       ans = cur;

   if (cur < 0)</pre>
```

```
cur = 0;
}
return ans;
```

2.2.2 Maximum Subarray Alternating Sum

Maximum Subarray Alternating Sum

```
/* REF: GeeksForGeeks
Input: arr[] = \{-4, -10, 3, 5\}
Output: 9
Explanation: Subarray {arr[0], arr[2]} = {-4, -10, 3}. Therefore, the sum
     of this subarray is 9.
int maxSubarraySumALT(vector<int>& a, int len) {
   int ans = INT_MIN, cur = 0;
   for (int i = 0; i < len; i++) {</pre>
       if (i % 2 == 0)
           cur = max(cur + a[i], a[i]);
           cur = max(cur - a[i], -a[i]);
       ans = max(ans, cur);
   }
   cur = 0;
   for (int i = 0; i < len; i++) {</pre>
       if (i % 2 == 1)
           cur = max(cur + a[i], a[i]);
       else
           cur = max(cur - a[i], -a[i]);
       ans = max(ans, cur);
   }
   return ans;
```

sums to x

Count distinct

```
/*
For example, if the coins are \{2,3,5\} and the desired sum is 9, there
    are 3 ways:
2+2+5
3+3+3
2+2+2+3
*/
int n, x;
cin >> n >> x;
vector<int> coins(n);
read(coins);
vector dp(x + 1, 0);
dp[0] = 1;
for (int i = 0; i < n; ++i) {</pre>
for (int j = coins[i]; j <= x; ++j) {</pre>
 dp[j] = add(dp[j], dp[j - coins[i]]);
}
}
cout << dp[x] << el;
```

Min absolute difference between 2 elements from (L, R) (DP 2.2.4Ranges)

Min absolute difference

```
const int N = 1e4 + 1;
int dp[N][N];
int n;
cin >> n;
vector<int> a(n);
read(a);
```

```
Count number of DISTINCT ordered ways to produce coins for (int i = 0; i < n; ++i) dp[i][i] = 1e6; // INF, you can't take the
                                                                         element with it self
                                                                     for (int i = 1; i < n; ++i) dp[i - 1][i] = abs(a[i] - a[i - 1]);
                                                                     for (int len = 3; len <= n; ++len) {</pre>
                                                                     for (int l = 0, r = len - 1; r < n; ++1, ++r) {
                                                                      dp[1][r] = min(dp[1][r - 1], dp[1 + 1][r]);
                                                                      dp[1][r] = min(dp[1][r], abs(a[1] - a[r]));
                                                                     int q;
                                                                     cin >> q;
                                                                     while (q--) {
                                                                     int 1, r;
                                                                     cin >> 1 >> r;
                                                                     --1, --r;
                                                                     cout << dp[l][r] << el;
```

2.2.5 Longest common subsequence between 2 Strings

$$dp[i][j] = \begin{cases} max(dp[i-1][j], dp[i][j-1]) & \text{if } A_i \neq B_j \\ dp[i-1][j-1] + 1 & \text{if } A_i = B_j \end{cases}$$

LIS 2 Strings

```
// REF: USACO guide
int longestCommonSubsequence(string a, string b) {
int dp[a.size()][b.size()];
for (int i = 0; i < a.size(); i++) { fill(dp[i], dp[i] + b.size(), 0); }</pre>
for (int i = 0; i < a.size(); i++) {</pre>
 if (a[i] == b[0]) dp[i][0] = 1;
 if (i != 0) dp[i][0] = max(dp[i][0], dp[i - 1][0]);
for (int i = 0; i < b.size(); i++) {</pre>
 if (a[0] == b[i]) dp[0][i] = 1;
 if (i != 0) dp[0][i] = max(dp[0][i], dp[0][i - 1]);
for (int i = 1; i < a.size(); i++) {</pre>
for (int j = 1; j < b.size(); j++) {</pre>
```

```
if (a[i] == b[j]) {
   dp[i][j] = dp[i - 1][j - 1] + 1;
   } else {
   dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
   }
}
return dp[a.size() - 1][b.size() - 1];
}
```

3 Bit Manipulation

3.1 Subset Operations

count subsets with give sum

```
int countDistinctSubsetsWithSum(vector<int>& arr, int n, int k) {
    // Count distinct subsets of array arr that sum up to k
    vector<int> dp(k + 1, 0);
    dp[0] = 1;
    for (int i = 0; i < n; ++i) {
        for (int j = k; j >= arr[i]; --j) {
            dp[j] += dp[j - arr[i]];
        }
    }
    return dp[k]; // Number of distinct subsets with sum k
}
```

max xor of any subset of elements in the array

```
int maximalSubsetXOR(vector<int>& arr, int n) {
    // Find the maximum XOR of any subset of elements in array arr
    int maxXor = 0;
    for (int mask = 0; mask < (1 << n); ++mask) {
        int xorSum = 0;
        for (int i = 0; i < n; ++i) {
            if (mask & (1 << i)) {
                  xorSum ^= arr[i];
            }
        }
}</pre>
```

```
maxXor = max(maxXor, xorSum);
}
return maxXor;
```

min xor of any subset

```
int minimumSubsetXOR(vector<int>& arr, int n) {
    // Find the minimum XOR of any pair of elements in array arr
    int minSubsetXor = INT_MAX;
    for (int mask = 0; mask < (1 << n); ++mask) {
        int xorSum = 0;
        for (int i = 0; i < n; ++i) {
            if (mask & (1 << i)) {
                xorSum ^= arr[i];
            }
        }
        minSubsetXor = min(minSubsetXor, xorSum);
    }
    return minSubsetXor;
}</pre>
```

$subset\ generation$

```
void subsetGeneration(int x, int n) {
    // Generate all non-empty subsets of a set represented by an integer x
    for (int subset = x; subset > 0; subset = (subset - 1) & x) {
        // Process subset
        cout << subset << endl;
    }
}</pre>
```

check if subset of elements in the array sum up to k

```
void subsetSumCheck(vector<int>& arr, int n, int k) {
    // Check if a subset of elements in array arr sums up to k
    for (int subset = 0; subset < (1 << n); ++subset) {
        int sum = 0;
        for (int i = 0; i < n; ++i) {
            if (subset & (1 << i)) {</pre>
```

```
sum += arr[i];
}

if (sum == k) {
    // Found subset with sum k
    cout << "Subset with sum " << k << ": " << subset << endl;
}
}</pre>
```

max subset sum mod m

```
int subsetWithMaxSumModuloM(vector<int>& arr, int n, int m) {
   // Find the maximum subset sum modulo m
   vector<int> dp(m, -1);
   dp[0] = 0;
   int currentMod = 0;
   for (int i = 0; i < n; ++i) {
       currentMod = (currentMod + arr[i]) % m;
       for (int j = 0; j < m; ++j) {
          if (dp[j] != -1) {
              dp[(j + currentMod) % m] = max(dp[(j + currentMod) % m], dp
                  [j] + arr[i]);
          }
       }
       dp[currentMod] = max(dp[currentMod], arr[i]);
   }
   return dp[0]; // Maximum subset sum modulo m
```

iterate over all supersets represented by x

4 Algorithms

4.1 MO

MO Algorithm

```
// MO
           -> O(N+Q SQRT(N)) <= 10^5
const int N = 1e5+5, M = 1e5+5;
int n, m;
int nums[N], q_ans[M];
struct query {
   int idx, block_idx, l, r;
   query() = default;
   query(int _1, int _r, int _idx) {
       idx = _idx;
       r = _r - 1;
       1 = _1 - 1;
       block_idx = _1 / sqrt(n);
   bool operator <(const query & y) const {</pre>
       if(y.block_idx == block_idx) return r < y.r;</pre>
       return block_idx < y.block_idx;</pre>
   }
};
int freq[N], ans;
void add(int idx) {
   freq[nums[idx]]++;
   if (freq[nums[idx]] == 2) ans++;
void remove(int idx) {
   freq[nums[idx]]--;
   if (freq[nums[idx]] == 1) ans--;
cin >> n >> m;
for (int i = 0; i < n; ++i) cin >> nums[i];
```

```
vector<query> Query(m);
for (int i = 0; i < m; ++i) {</pre>
   int 1, r; cin >> 1 >> r;
   Query[i] = query(1, r, i);
}
sort(Query.begin(), Query.end());
int 10 = 1, r0 = 0;
for (int i = 0; i < m; ++i) {
   while (10 < Query[i].1) remove(10++);</pre>
   while (10 > Query[i].1) add(--10);
   while (r0 < Query[i].r) add(++r0);
   while (r0 > Query[i].r) remove(r0--);
   q_ans[Query[i].idx] = ans;
}
for (int i = 0; i < m; ++i) {
    cout << q_ans[i] << '\n';
}
```

4.2 Intervals

4.2.1 Prefix Sum (L, R) intervals

Prefix Sum (L, R) intervals

```
// NOTE: works fine with small n or with large memory
int main() {
   int n, k;
   cin >> n >> k;

   vector<int>> a(n + 1);
   vector<vector<int>> rangesPrefix(n + 1, vector<int>(n + 1, 0));
   for (int i = 1; i <= n; ++i)
        cin >> a[i];

   int l = 1, r = 1, sum = 0;
   // validate your intervals
   // here the intervals are the ones that have a sum of k
   while (r <= n) {
        sum += a[r];
   }
}</pre>
```

```
while (sum > k) {
       sum -= a[1];
       ++1;
   }
   while (1 \le r \&\& a[1] == 0) {
       if (sum != k)
           break;
       rangesPrefix[r][1]++;
       ++1;
   }
   if (sum == k) {
       rangesPrefix[r][1]++;
    ++r;
}
// prefix sum the columns
for (int i = 1; i <= n; ++i) {
   for (int j = n - 1; j \ge 0; --j) {
       rangesPrefix[i][j] += rangesPrefix[i][j + 1];
   }
}
// prefix sum the rows
for (int i = 0; i <= n; ++i) {
   for (int j = 1; j <= n; ++j) {
       rangesPrefix[j][i] += rangesPrefix[j - 1][i];
   }
}
int q; cin >> q;
while (q--) {
   // answer the number of intervals (X, Y) X <= Y that are included
        between L. R
    cout << rangesPrefix[r][l] - rangesPrefix[l - 1][l] << el;</pre>
```

```
}
```

4.2.2 Find subarrays intervals that sum to K Using Map

Find subarray intervals that sum to K Using Map

```
int n, k;
cin >> n >> k;
vector < int > a(n + 1);
vector<pair<int, int>> rng;
for (int i = 1; i <= n; ++i)
    cin >> a[i];
map<int, set<int>> prev;
int currSum = 0;
for (int i = 1; i <= n; ++i) {
    currSum += a[i];
   if (currSum == k) {
       rng.push_back({1, i});
   if (prev.find(currSum - k) != prev.end()) {
       for (auto &j : prev[currSum - k]) {
           rng.push_back(\{j + 1, i\});
       }
    prev[currSum].insert(i);
```

4.3 Ad-hoc

4.3.1 Find duplicate

Find duplicate using XOR

```
int findDuplicate(int arr[] , int n)
{
   int answer=0;
    //XOR all the elements with 0
```

```
for(int i=0; i<n; i++){
    answer=answer^arr[i];
}
    //XOR all the elements with no from 1 to n
    // i.e answer^0 = answer
for(int i=1; i<n; i++){
    answer=answer^i;
}
return answer;</pre>
```

4.4 Sorting Algorithms

4.4.1 Radix Sort

Radix Sort

```
// O(n + b), where n is the number of elements and b is the base of the
    number system
// A function to do counting sort of arr[] according to the digit
    represented by exp.
void countingSort(vector<int>& arr, int exp) {
   int n = arr.size();
   vector<int> output(n); // output array
   int count[10] = {0};
   // Store count of occurrences in count[]
   for (int i = 0; i < n; i++)</pre>
       count[(arr[i] / exp) % 10]++;
   // Change count[i] so that count[i] now contains the actual
   // position of this digit in output[]
   for (int i = 1; i < 10; i++)</pre>
       count[i] += count[i - 1];
   // Build the output array
   for (int i = n - 1; i >= 0; i--) {
       output[count[(arr[i] / exp) % 10] - 1] = arr[i];
       count[(arr[i] / exp) % 10]--;
   }
   // Copy the output array to arr[], so that arr now
```

4.4.2 Counting Sort

Counting Sort

```
// O(N+M), where N and M are the size of inputArray[] and countArray[]
// The main function that sorts arr[] of size n using Counting Sort
void countingSort(vector<int>& arr) {
   int maxElement = *max_element(arr.begin(), arr.end());
   int minElement = *min_element(arr.begin(), arr.end());
   int range = maxElement - minElement + 1;
   vector<int> count(range), output(arr.size());
   for (int i = 0; i < arr.size(); i++)</pre>
       count[arr[i] - minElement]++;
   for (int i = 1; i < count.size(); i++)</pre>
       count[i] += count[i - 1];
   for (int i = arr.size() - 1; i >= 0; i--) {
       output[count[arr[i] - minElement] - 1] = arr[i];
       count[arr[i] - minElement]--;
   }
   for (int i = 0; i < arr.size(); i++)</pre>
       arr[i] = output[i];
}
```

5 Data Structures

5.1 Strings

5.1.1 Trie (Prefix Tree)

Basic Implementation

```
#define MAX_CHAR 26
struct TrieNode {
   TrieNode *pTrieNode[MAX_CHAR]{};
   bool isWord;
   TrieNode() {
       isWord = false;
       fill(pTrieNode, pTrieNode + 26, (TrieNode *) NULL);
   }
   virtual ~TrieNode() = default;
};
class Trie {
private:
   TrieNode *root;
public:
   Trie() {
       root = new TrieNode();
   }
   virtual ~Trie() = default;
   TrieNode *getTrieNode() {
       return this->root;
   }
   void insert(const string &word) {
       TrieNode *current = root;
       for (char c: word) {
           int i = c - 'a';
           if (current->pTrieNode[i] == nullptr)
```

```
current->pTrieNode[i] = new TrieNode();
           current = current->pTrieNode[i];
       current->isWord = true;
   }
   bool search(const string &word) {
       TrieNode *current = root;
       int ch = 0;
       for (char c: word) {
           ch = c - 'a';
          if (current->pTrieNode[ch] == nullptr)
              return false;
           current = current->pTrieNode[ch];
       return current->isWord;
   }
   bool startsWith(const string &prefix) {
       TrieNode *current = root;
       int ch = 0;
       for (char c: prefix) {
           ch = c - 'a';
           if (current->pTrieNode[ch] == nullptr)
              return false;
           current = current->pTrieNode[ch];
       }
       return true;
};
```

5.2 Range Queries

5.2.1 Segment Tree

Basic Implementation

```
struct Node {
    long long val;
};
struct SegTree {
```

```
private:
   const Node NEUTRAL = {INT_MIN};
   static Node merge(const Node& x1, const Node& x2) {
       return {x1.val + x2.val}:
   }
   void set(const int& idx, const int& val, int x, int lx, int rx) {
       if (rx - lx == 1) return void(values[x].val = val);
       int mid = (rx + lx) / 2;
       if (idx < mid)</pre>
           set(idx, val, 2 * x + 1, lx, mid);
       else
           set(idx, val, 2 * x + 2, mid, rx);
       values[x] = merge(values[2 * x + 1], values[2 * x + 2]);
   }
   Node query(const int& 1, const int& r, int x, int lx, int rx) {
       if (lx >= r || l >= rx) return NEUTRAL;
       if (lx >= 1 && rx <= r) return values[x];</pre>
       int mid = (rx + lx) / 2:
       return merge(query(1, r, 2 * x + 1, 1x, mid), query(1, r, 2 * x + 1
           2, mid, rx));
   void build(vector<int> &a, int x, int lx, int rx) {
       if (rx - lx == 1) {
           if (lx < a.size()) {</pre>
              values[x].val = a[lx];
           }
           return;
       int m = (1x + rx) / 2;
       build(a, 2 * x + 1, 1x, m);
       build(a, 2 * x + 2, m, rx);
       values[x] = merge(values[2 * x + 1], values[2 * x + 2]);
   }
    void assign_range(int 1, int r, int node, int lx, int rx, int time,
        int val) {
```

```
if (lx > r || l > rx) return;
       if (lx >= 1 && rx <= r) {
          lazy[node] = {time, val};
           return;
       }
       int mid = (1x+rx) / 2;
       assign_range(1, r, 2*node+1, lx, mid, time, val);
       assign_range(l, r, 2*node+2, mid+1, rx, time, val);
   }
   pair<int, int> point_query(int lx, int rx, int node, int idx) {
       if(rx == lx) return lazy[node];
       int mid = (1x+rx) / 2;
       if(idx <= mid) {</pre>
           auto x = point_query(lx, mid, 2*node+1, idx);
           if(x.first > lazy[node].first) return x;
           return lazy[node];
       }
       auto x = point_query(mid+1, rx, 2*node+2, idx);
       if(x.first > lazy[node].first) return x;
       return lazy[node];
   }
public:
   int size{};
   vector<Node> values;
   void build(vector<int> &a) {
       build(a, 0, 0, size);
   }
   void init(int _size) {
       size = 1;
       while (size < _size) size *= 2;</pre>
       values.assign(2 * size, NEUTRAL);
   }
   void set(int idx, int val) {
       set(idx, val, 0, 0, size);
   }
   Node query(const int& 1, const int& r) {
```

```
return query(1, r, 0, 0, size);
};
```

5.2.2 Lazy Propegation

Lazy Propegation

```
struct SegTree {
private:
   void propegate(int lx, int rx, int node) {
       if(!lazy[node]) return;
       if(lx != rx) {
           lazy[2*node+1] = lazy[node];
           lazy[2*node+2] = lazy[node];
       values[node] = lazy[node] * (rx - lx + 1);
       lazy[node] = 0;
   }
   // assign val in range [1, r]
   void update_range(int 1, int r, int node, int lx, int rx, int val,
       bool f) {
       propegate(lx, rx, node);
       if (1x > r \mid | 1 > rx) return:
       if (lx >= 1 && rx <= r) {
           lazy[node] = val;
          propegate(lx, rx, node);
           return;
       }
       int mid = (lx+rx) / 2;
       update_range(l, r, 2*node+1, lx, mid, val, f);
       update_range(l, r, 2*node+2, mid+1, rx, val, f);
       values[node] = values[2*node+1] + values[2*node+2];
   }
   // get sum in range [1, r]
   int range_query(int 1, int r, int lx, int rx, int node) {
       propegate(lx, rx, node);
       if (lx > r \mid | l > rx) return 0;
       if (lx >= 1 && rx <= r) return values[node];</pre>
```

```
int mid = (1x+rx) / 2;
       return range_query(1, r, lx, mid, 2*node+1) + range_query(1, r, mid
           +1, rx, 2*node+2);
   }
public:
   int size{};
   vector<int> values, lazy;
   void init(int _size) {
       size = 1;
       while (size < _size) size *= 2;</pre>
       values.assign(2 * size, 0);
       lazy.assign(2 * size, 0);
   }
   void update_range(int 1, int r, int v, bool f) {
       update_range(1, r, 0, 0, size-1, v, f);
   }
   int range_query(int 1, int r) {
       return range_query(1, r, 0, size-1, 0);
   }
};
```

5.2.3 Fenwick Tree

Fenwick Tree

```
struct Fenwick {
    // One Based
    vector<int> tree;

explicit Fenwick(int n) {tree.assign(n + 5, {});}

// Computes the prefix sum from [1, i], O(log(n))
int query(int i) {
    int res = 0;
    while (i > 0) {
        res += tree[i];
        i &= ~(i & -i);
    }
}
```

```
return res;
   }
   int query(int 1, int r) {
       return query(r) - query(1-1);
   }
   // Get the value at index i
   int get(int i) {
       return query(i, i);
   }
   // Add 'v' to index 'i', O(log(n))
   void update(int i, int v) {
       while (i < tree.size()) {</pre>
           tree[i] += v;
           i += (i & -i);
       }
   }
   // Update range, Point query
   // To get(k) do prefix sum [1, k] and in insert update_range(i, i, a[i
       1)
   void update_range(int 1, int r, int v) {
       update(1, v);
       update(r+1, -v);
   }
};
```

5.2.4 Fenwick UpdateRange

$BIT\ UpdateRange$

```
struct BITUpdateRange {
private:
   int n;
   vector<int> B1, B2;

  void add(vector<int> &b, int idx, int x) {
     while (idx <= n) {
        b[idx] += x;
        idx += idx & -idx;
   }</pre>
```

```
}
   int sum(vector<int> &b, int idx) {
       int total = 0;
       while (idx > 0) {
          total += b[idx];
           idx &= (idx & -idx);
       }
       return total;
   }
   int prefix(int idx) {
       return sum(B1, idx) * idx - sum(B2, idx);
   }
public:
   explicit BITUpdateRange(int n) : n(n) {
       B1.assign(n + 1, {});
       B2.assign(n + 1, {});
   }
   void update(int 1, int r, int x) {
       add(B1, 1, x);
       add(B1, r + 1, -x);
       add(B2, 1, x * (1 - 1));
       add(B2, r + 1, -x * r);
   }
   int query(int i) {
       return prefix(i) - prefix(i - 1);
   }
   int query(int 1, int r) {
       return prefix(r) - prefix(l - 1);
   }
};
```

5.2.5 2D BIT

2D BIT

```
struct BIT2D {
   int n, m;
```

```
vector<vector<int>> bit;
   BIT2D(int n, int m) : n(n), m(m) {
       bit.assign(n + 2, vector<int>(m + 2));
   }
   void update(int x, int y, int val) {
       for (; x <= n; x += x & -x) {
           for (int i = y; i <= m; i += i & -i) {
              bit[x][i] += val;
       }
   }
   int prefix(int x, int y) {
       int res = 0;
       for (; x > 0; x &= (x & -x)) {
          for (int i = y; i > 0; i &= (i & -i)) {
              res += bit[x][i];
       }
       return res;
   }
   int query(int sx, int sy, int ex, int ey) {
       int ans = 0;
       ans += prefix(ex, ey);
       ans -= prefix(ex, sy - 1);
       ans -= prefix(sx - 1, ey);
       ans += prefix(sx - 1, sy - 1);
       return ans;
   }
};
```

5.2.6 Sparse Table

Impl with the index

```
// storing the index also
struct SNode {
   int val;
   int index;
};
```

```
class SparseTable {
private:
   vector<vector<SNode>> table;
   function<SNode(const SNode&, const SNode&)> merge;
   static SNode StaticMerge(const SNode& a, const SNode& b) {
       return a.val < b.val ? a : b;</pre>
   }
public:
   explicit SparseTable(const vector<int>& arr, const function<SNode(</pre>
       const SNode&, const SNode&)>& mergeFunc = StaticMerge) {
       int n = static_cast<int>(arr.size());
       int log_n = static_cast<int>(log2(n)) + 1;
       this->merge = mergeFunc;
       table.resize(n, vector<SNode>(log_n));
       for (int i = 0; i < n; i++) {</pre>
           table[i][0] = {arr[i], i};
       }
       for (int j = 1; (1 << j) <= n; j++) {
           for (int i = 0; i + (1 << j) <= n; i++) {
               table[i][j] = mergeFunc(table[i][j - 1], table[i + (1 << (j
                   - 1))][j - 1]);
           }
   SNode query(int left, int right) {
       int j = static_cast<int>(log2(right - left + 1));
       return merge(table[left][j], table[right - (1 << j) + 1][j]);</pre>
   }
   // query in O(log(n)) if its could't apply to Sparse Table directly
   T query_log(int 1, int r){
     int len = r - 1 + 1;
     T ans:
     for(int i = 0; 1 <= r; i++){</pre>
         if (len & (1 << i)){
             ans = merge(ans, table[i][1]);
```

```
l+= (1 << i);
}
}

int main(void) {
  int n;
  cin >> n;
  vector<int> arr(n);
  for (auto& element : arr) cin >> element;

SparseTable minSt(arr, [](const SNode& a, const SNode& b) -> SNode {
    return a.val < b.val ? a : b;
});

SparseTable maxSt(arr, [](const SNode& a, const SNode& b) -> SNode {
    return a.val > b.val ? a : b;
});
}
```

5.3 Ordered Set

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;

template < typename T >
    using ordered_set = tree < T, null_type, less < T >, rb_tree_tag,
        tree_order_statistics_node_update >;

void erase_set(ordered_set & os, int v) {
        // Number of elements less than v
        int rank = os.order_of_key(v);

        auto it = os.find_by_order(rank);
        os.erase(it);
}
```

Ordered Set

Counting Principles

6.1nCr

$$C(n,k) = \frac{n!}{(n-k)!k!} = \frac{n*(n-1)*(n-2)*...*(n-k+1)}{k!}$$

6.1.1 Fast nCr

Fast nCr

```
int nCr(const int& n, const int& r) {
   double res = 1;
   for (int i = 1; i <= r; ++i)
       res = res * (n - r + i) / i;
   return (int)(res + 0.01);
}
```

Method 1: Pascal's Triangle (Dynamic Programming) - $\mathcal{O}(n^2)$

nCk using dp

```
// REF: USACO guide
/** Creturn nCk mod p using dynamic programming */
int binomial(int n, int k, int p) {
// dp[i][j] stores iCj
vector<vector<int>> dp(n + 1, vector<int>(k + 1, 0));
// base cases described above
for (int i = 0; i <= n; i++) {</pre>
  * i choose 0 is always 1 since there is exactly one way
```

```
* to choose O elements from a set of i elements
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  * (don't choose anything)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dp[i][0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  * i choose i is always 1 since there is exactly one way
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  * to choose i elements from a set of i elements
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * (choose every element in the set)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (i <= k) { dp[i][i] = 1; }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int i = 0; i <= n; i++) {</pre>
C(n,k) = \frac{n*(n-1)*(n-2)*\dots*(n-k+1)}{1*2*3*\dots*k} = \prod_{i=0}^{k-1} \frac{n-i}{i+1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ uses the recurrence relation above } \frac{1}{1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{-1} / \text{ use } \frac{1}{1} = \prod_{i=0}^{k-1} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return dp[n][k]; // returns nCk modulo p
```

6.1.3 Method 2: Factorial Definition (Modular Inverses) - O(n + $\log MOD$

nCk using Modular Inverses

```
// REF: USACO guide
const int MAXN = 1e6;
long long fac[MAXN + 1];
long long inv[MAXN + 1];
/** @return x^n modulo m in O(log p) time. */
long long exp(long long x, long long n, long long m) {
x \%= m; // note: m * m must be less than 2^63 to avoid ll overflow
long long res = 1;
while (n > 0) {
 if (n % 2 == 1) { res = res * x % m; }
```

```
x = x * x % m;
 n /= 2:
return res;
/** Precomputes n! from 0 to MAXN. */
void factorial(long long p) {
fac[0] = 1;
for (int i = 1; i <= MAXN; i++) { fac[i] = fac[i - 1] * i % p; }</pre>
/**
* Precomputes all modular inverse factorials
* from 0 to MAXN in O(n + log p) time
void inverses(long long p) {
inv[MAXN] = exp(fac[MAXN], p - 2, p);
for (int i = MAXN; i >= 1; i--) { inv[i - 1] = inv[i] * i % p; }
}
/** @return nCr mod p */
long long choose(long long n, long long r, long long p) {
return fac[n] * inv[r] % p * inv[n - r] % p;
int main() {
factorial();
inverses();
int n;
 cin >> n;
 for (int i = 0; i < n; i++) {</pre>
 int a, b;
 cin >> a >> b;
 cout << choose(a, b) << '\n';</pre>
}
}
```

7 Graph Theory

7.1 Shortest Path algorithms

7.1.1 Dijkstra Algorithm

$Dijkstra\ Implementation$

```
#define INF (1e18) // for int defined as 11
int n, m;
vector<vector<pair<int, int>>> adj;
vector<int> cost;
vector<int> parent;
void dijkstra(int startNode = 1) {
   priority_queue<pair<11, int>, vector<pair<11, int>>, greater<>> pq;
   cost[startNode] = 0;
   pq.emplace(0, startNode);
   while (!pq.empty()) {
       int u = pq.top().second;
       11 d = pq.top().first;
       pq.pop();
       if (d > cost[u]) continue;
       for (auto &p: adj[u]) {
          int v = p.first;
          int w = p.second;
           if (cost[v] > cost[u] + w) {
              cost[v] = cost[u] + w;
              parent[v] = u;
              pq.emplace(cost[v], v);
void run_test_case(int testNum) {
   cin >> n >> m;
   adj.assign(n + 1, {});
```

```
cost.assign(n + 1, INF);
parent.assign(n + 1, -1);
while (m--) {
    // Read Edges
}
dijkstra();
if (cost[n] == INF) {
    cout << -1 << el; // not connected {Depends on you use case}</pre>
    return;
}
stack<int> ans;
for (int v = n; v != -1; v = parent[v]) ans.push(v);
while (!ans.empty()) { // printing the path
    cout << ans.top() << ' ';</pre>
    ans.pop();
}
cout << el;</pre>
```

7.1.2 Floyd Warshal Algorithm

$FloydWarshal\ Implementation$

```
int main() {
    int n, m; cin >> n >> m;
    vector <vector <int>> adj(n + 1, vector <int>> (n + 1, 2e9));
    for (int i = 0; i < n; i++) adj[i][i] = 0;

while(m--) {
        int u, v, w;
        cin >> u >> v >> w;
        adj[u][v] = min(adj[u][v], w);
        adj[v][u] = min(adj[v][u], w);
    }

for (int mid = 1; mid <= n; mid++) {
        for (int start = 1; start <= n; start++) {
            for (int end = 1; end <= n; end++) {</pre>
```

7.1.3 Bellman Ford Algorithm

BellmanFord Implementation

```
vector <vector <pair<int, int>>> &adj
vector <long long> BellmanFord(int src) {
   int n = (int)adj.size();
   vector <long long> dist(n, 2e18);
   dist[src] = 0;
   for (int it = 0; it < n-1; it++) {</pre>
       bool in = false;
       for (int i = 0; i < n; i++) { // iterate on the edges</pre>
           for (auto &[j, w] : adj[i]) {
              if (dist[j] > dist[i] + w) {
                  in = true;
                  dist[j] = dist[i] + w;
              }
           }
       }
       if (!in) return dist;
   }
   for (int i = 0; i < n; i++) {</pre>
       for (auto &[j, w] : adj[i]) {
           if (dist[j] > dist[i] + w) { //negative cycle
              return vector <long long> (n, -1); // or any flag
       }
   }
   return dist;
```

7.2 Cycle Detection

7.2.1 DFS Implementation

DFS Implementation

```
// return true with number of nodes in the cycle, either odd cycle or even
bool cycle_detection(unordered_map<int, vector<int>> &graph, int source,
    int par, unordered_map<int,bool> vis, int c){
    if(vis[source]) return true;

    vis[source] = true;

    for(int v: graph[source]){
        if(v != par){
            c++;
            if(dfs(graph,v, source, vis, c)) return true;
        }
    }
    return false;
}
```

7.2.2 Another way for undirected graphs

Another way for undirected graphs

```
// this is true only for undirected graphs
bool dfs1(int cur, int par) {
   bool ret = false;
   vis[cur] = true;
   for (auto &i : adj[cur]) {
      if (!vis[i]) ret|=dfs1(i, cur);
      else if (par != i) ret = true;
   }
   return ret;
}
```

7.2.3 General Way

General Way

```
// general algorithm
vector <bool> cyc;
bool dfs(int cur, int par) {
   bool ret = false;
   vis[cur] = cyc[cur] = true;
   for (auto &i : adj[cur]) {
      if (par == i) continue;
      if (!vis[i]) ret|=dfs(i, cur);
      else if (cyc[i]) ret = true;
   }
   cyc[cur] = false;
   return ret;
}
```

7.2.4 DSU Implementation

DSU Implementation

```
#include <iostream>
#include <vector>
class UnionFind {
public:
   UnionFind(int n) {
       parent.resize(n);
       rank.resize(n, 0);
       for (int i = 0; i < n; ++i) {</pre>
           parent[i] = i;
       }
   }
   int find(int u) {
       if (parent[u] != u) {
           parent[u] = find(parent[u]);
       }
       return parent[u];
   }
   void unionSets(int u, int v) {
```

```
int rootU = find(u);
       int rootV = find(v);
       if (rootU != rootV) {
           if (rank[rootU] > rank[rootV]) {
              parent[rootV] = rootU;
           } else if (rank[rootU] < rank[rootV]) {</pre>
              parent[rootU] = rootV;
           } else {
              parent[rootV] = rootU;
              ++rank[rootU];
          }
   }
private:
   std::vector<int> parent;
   std::vector<int> rank;
};
bool detectCycle(const std::vector<std::pair<int, int>>& edges, int n) {
   UnionFind uf(n);
   for (const auto& edge : edges) {
       int u = edge.first;
       int v = edge.second;
       if (uf.find(u) == uf.find(v)) {
           return true;
       }
       uf.unionSets(u, v);
   }
   return false;
int main() {
   std::vector<std::pair<int, int>> edges = { {0, 1}, {1, 2}, {2, 3}, {3,
        0} }:
   int n = 4; // Number of vertices
   if (detectCycle(edges, n)) {
       std::cout << "Cycle detected" << std::endl;</pre>
   } else {
```

```
std::cout << "No cycle detected" << std::endl;
}
return 0;</pre>
```

7.3 Algorithms

7.3.1 Heavy Light Decomposition

Basic HLD Impl

```
struct Node {
   int val;
};
const Node nullNode = {0};
const int N = 2e5 + 5, S = 1 << 19;
int n, q;
int val[N];
int sz[N], par[N], dep[N], id[N], top[N];
vector<int> adj[N];
Node st[S];
Node merge(const Node& a, const Node& b) {
   return {a.val + b.val};
void update(int idx, Node val) {
   st[idx += n] = val;
   for (idx /= 2; idx; idx /= 2) st[idx] = merge(st[idx * 2], st[idx * 2]
       + 1]);
Node query(int lo, int hi) {
   Node ra = nullNode, rb = nullNode;
   for (lo += n, hi += n + 1; lo < hi; lo /= 2, hi /= 2) {
       if (lo & 1) ra = merge(ra, st[lo++]);
       if (hi & 1) rb = merge(st[--hi], rb);
```

```
}
   return merge(ra, rb);
}
int dfs_size(const int& node, const int& parent) {
   sz[node] = 1;
   par[node] = parent;
   for (const int& ch : adj[node]) {
       if (ch == parent) continue;
       dep[ch] = dep[node] + 1;
       par[ch] = node;
       sz[node] += dfs_size(ch, node);
   }
   return sz[node];
}
int curId = 0;
void dfs_hld(const int& cur, const int& parent, const int& curTop) {
   id[cur] = curId++;
   top[cur] = curTop;
   update(id[cur], {val[cur]});
   int heavyChild = -1, heavyMax = -1;
   for (const int& ch : adj[cur]) {
       if (ch == parent) continue;
       if (sz[ch] > heavyMax) {
          heavyMax = sz[ch];
           heavyChild = ch;
       }
   }
   if (heavyChild == -1) return;
   dfs_hld(heavyChild, cur, curTop);
   for (int ch : adj[cur]) {
       if (ch == parent || ch == heavyChild) continue;
       dfs_hld(ch, cur, ch);
   }
}
Node path(int u, int v) {
   Node ans = nullNode;
```

```
while (top[u] != top[v]) {
       if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
       ans = merge(ans, query(id[top[u]], id[u]));
       u = par[top[u]];
   }
   if (dep[u] > dep[v]) swap(u, v);
   ans = merge(ans, query(id[u], id[v]));
   return ans;
void init() {
   for (int i = 0; i < S; i++) st[i] = nullNode;</pre>
   dfs_size(1, 1);
   dfs_hld(1, 1, 1);
int main() {
   cin >> n >> q;
   for (int i = 1; i <= n; i++) cin >> val[i];
   int a, b;
   for (int i = 2; i <= n; i++) {
       cin >> a >> b;
       adj[a].pb(b);
       adj[b].pb(a);
   }
   init(); // <----- DON'T FORGET TO CALL THIS FUNCTION</pre>
   int type;
   while (q--) {
       cin >> type;
       if (type == 1) {
           cin >> a >> b;
           val[a] = b;
           update(id[a], {val[a]});
       }
       else {
           cin >> a;
           cout << path(1, a).val << el;</pre>
   }
```

7.3.2 Heavy Light Decomposition with lazy SegTree

Basic HLD Impl

```
struct Node {
   int val;
};
const Node nullNode = {0};
const int N = 2e5 + 5, S = 1 << 19;
int n, q;
int val[N];
int sz[N], par[N], dep[N], id[N], top[N];
vector<int> adj[N];
Node st[S];
int lazy[S];
Node merge(const Node& a, const Node& b) {
   return {a.val + b.val};
}
void push(int idx, int 1, int r) {
   if (lazy[idx] != 0) {
       st[idx].val += lazy[idx] * (r - l + 1);
       if (1 != r) {
           lazy[idx * 2] += lazy[idx];
           lazy[idx * 2 + 1] += lazy[idx];
       lazy[idx] = 0;
   }
}
void update_range(int lo, int hi, int l, int r, int idx, int value) {
   push(idx, l, r);
   if (lo > r || hi < 1) return;
   if (lo <= 1 && r <= hi) {
       lazy[idx] += value;
       push(idx, l, r);
       return;
   }
```

```
int mid = (1 + r) / 2:
   update_range(lo, hi, l, mid, idx * 2, value);
   update_range(lo, hi, mid + 1, r, idx * 2 + 1, value);
   st[idx] = merge(st[idx * 2], st[idx * 2 + 1]);
void update(int idx, Node val) {
   update_range(idx, idx, 0, n - 1, 1, val.val);
void update_range(int lo, int hi, int value) {
   update_range(lo, hi, 0, n - 1, 1, value);
Node query(int lo, int hi, int l, int r, int idx) {
   push(idx, l, r);
   if (lo > r || hi < 1) return nullNode;</pre>
   if (lo <= 1 && r <= hi) return st[idx];</pre>
   int mid = (1 + r) / 2;
   return merge(query(lo, hi, l, mid, idx * 2), query(lo, hi, mid + 1, r,
        idx * 2 + 1));
Node query(int lo, int hi) {
   return query(lo, hi, 0, n - 1, 1);
int dfs_size(const int& node, const int& parent) {
   sz[node] = 1;
   par[node] = parent;
   for (const int& ch : adj[node]) {
       if (ch == parent) continue;
       dep[ch] = dep[node] + 1;
       par[ch] = node;
       sz[node] += dfs_size(ch, node);
   }
   return sz[node];
int curId = 0;
void dfs_hld(const int& cur, const int& parent, const int& curTop) {
   id[cur] = curId++:
   top[cur] = curTop;
```

```
update(id[cur], {val[cur]});
   int heavyChild = -1, heavyMax = -1;
   for (const int& ch : adj[cur]) {
       if (ch == parent) continue;
       if (sz[ch] > heavyMax) {
           heavyMax = sz[ch];
           heavyChild = ch;
       }
   }
   if (heavyChild == -1) return;
   dfs_hld(heavyChild, cur, curTop);
   for (int ch : adj[cur]) {
       if (ch == parent || ch == heavyChild) continue;
       dfs_hld(ch, cur, ch);
}
int get(int u) {
   return query(id[u], id[u]).val;
}
void path(int u, int v, int val) {
   // Node ans = nullNode;
   while (top[u] != top[v]) {
       if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
       // ans = merge(ans, query(id[top[u]], id[u]));
       update_range(id[top[u]], id[u], val);
       u = par[top[u]];
   }
   if (dep[u] > dep[v]) swap(u, v);
   // ans = merge(ans, query(id[u], id[v]));
   update_range(id[u], id[v], val);
    // return ans;
}
void init() {
   for (int i = 0; i < S; i++) st[i] = nullNode;</pre>
   memset(lazy, 0, sizeof(lazy));
   dfs_size(1, 1);
   dfs_hld(1, 1, 1);
```

```
int main(void) {
   cin >> n >> q;
   for (int i = 1; i <= n; i++) val[i] = 0;</pre>
   int a. b:
   for (int i = 2; i <= n; i++) {</pre>
       cin >> a >> b;
       adj[a].push_back(b);
       adj[b].push_back(a);
   }
   init(); // <----- DON'T FORGET TO CALL THIS FUNCTION
   int v;
   while (q--) {
       cin >> a >> b >> v;
       path(a, b, v);
   }
   for (int i = 1; i <= n; i++) {
       cout << get(i) << " ";
   }
   cout << el;</pre>
```

7.3.3 LCA functions using Binary Lifting

LCA functions using Binary Lifting

```
const int N = 2e5 + 15, M = 23;
int ancestors[N][M], depth[N], parent[N], val[N];
vector<vector<int>> adj;
//int tin[N], tout[N], timer;

void dfs_LCA(const int &node, const int &par) {
    // tin[node] = timer++;
    parent[node] = par;
    ancestors[node][0] = par;
    depth[node] = depth[par] + 1;

    for (int i = 1; i < M; i++) {
        int p = ancestors[node][i - 1];
        ancestors[node][i] = ancestors[p][i - 1];
    }
}</pre>
```

```
}
   for (const int &v: adj[node]) {
       if (v == par) continue;
       dfs_LCA(v, node);
   }
     tout[node] = timer++;
//bool is_ancestor(int u, int v) {
     return tin[u] <= tin[v] && tout[u] >= tout[v];
//}
int findKth(int u, int k) {
   if (depth[u] <= k) return -1;</pre>
   for (int i = M - 1; i >= 0; i--) {
       if (k & (1 << i)) {
           u = ancestors[u][i];
   }
   return u;
}
int getLCA(int u, int v) {
   if (depth[u] < depth[v])</pre>
       swap(u, v);
   u = findKth(u, depth[u] - depth[v]);
   if (u == v) return u;
   for (int i = M - 1; i >= 0; i--) {
       if (ancestors[u][i] == ancestors[v][i]) continue;
       u = ancestors[u][i];
       v = ancestors[v][i];
   return ancestors[u][0];
}
int getDistance(int u, int v) {
   int lca = getLCA(u, v);
   return (depth[u] + depth[v]) - (2 * depth[lca]);
}
int dfs_accumulate(const int &node, const int &par) {
```

```
for (const int& ch: adj[node]) {
       if (ch == par) continue;
       val[node] += dfs_accumulate(ch, node);
   }
   return val[node];
void applyOpOnPath(const int a, const int b, const int w) {
   // adding w to each node on the path a to b
   val[a] += w;
   val[b] += w;
   int lca = getLCA(a, b);
   val[lca] -= w;
   val[parent[lca]] -= w;
int main(void) {
   int n, q;
   cin >> n >> q;
   adj.resize(n + 1);
   int u, v;
   for (int i = 2; i <= n; ++i) {
       cin >> u >> v;
       adj[u].push_back(v);
       adj[v].push_back(u);
   }
   dfs_LCA(1, 1);
   parent[1] = -1;
   int w;
   for (int i = 0; i < q; ++i) {</pre>
       cin >> u >> v;
       cout << getDistance(u, v) << el;</pre>
   }
     dfs_accumulate(1, 0);
     for (int i = 1; i <= n; i++) {
         cout << val[i] << " ";
     }
     cout << el:</pre>
```

}

7.3.4 Topological Sort

Topological Sort Using DFS

```
//REF: USACO Guide
vector<int> top_sort;
vector<vector<int>> graph;
vector<bool> visited;
void dfs(int node) {
for (int next : graph[node]) {
 if (!visited[next]) {
  visited[next] = true;
  dfs(next);
top_sort.push_back(node);
int main() {
int n, m; // The number of nodes and edges respectively
std::cin >> n >> m;
 graph = vector<vector<int>>(n);
for (int i = 0; i < m; i++) {</pre>
 int a, b;
 std::cin >> a >> b;
 graph[a - 1].push_back(b - 1);
}
visited = vector<bool>(n);
for (int i = 0; i < n; i++) {</pre>
 if (!visited[i]) {
  visited[i] = true;
  dfs(i);
 std::reverse(top_sort.begin(), top_sort.end());
vector<int> ind(n);
for (int i = 0; i < n; i++) { ind[top_sort[i]] = i; }</pre>
```

```
// Check if the topological sort is valid
bool valid = true;
for (int i = 0; i < n; i++) {
  for (int j : graph[i]) {
    if (ind[j] <= ind[i]) {
     valid = false;
     goto answer;
    }
  }
}
answer:;

if (valid) {
  for (int i = 0; i < n - 1; i++) { cout << top_sort[i] + 1 << ' '; }
  cout << top_sort.back() + 1 << endl;
} else {
  cout << "IMPOSSIBLE" << endl;
}
</pre>
```

8 Techniques

8.1 Coordinate Compression

```
void coordinate_compress(vector<int> &x, int start=0, int
    step=1) {
    set unique(x.begin(), x.end());
    map<int, int> valPos;

    int idx=0;
    for (auto i: unique) {
       valPos[i] = start + idx * step;
       ++idx;
    }
    for(auto &i: x) i = valPos[i];
}
```

$Coordinate\ Compression$

8.2 Binary to decimal

Binary to decimal

```
// Function to convert binary to decimal
// 0(32)
int binaryToDecimal(string str)
{
   int dec_num = 0;
   int power = 0;
   int n = str.length();

   for(int i = n-1; i>=0; i--){
    if(str[i] == '1'){
      dec_num += (1<<power);
   }
   power++;
   }

   return dec_num;
}</pre>
```

8.3 Decimal to binary

Decimal to bianry

```
// Function that convert Decimal to binary
// 0(32)
void decToBinary(int n)
{
    // Size of an integer is assumed to be 32 bits
    for (int i = 31; i >= 0; i--) {
        int k = n >> i;
        if (k & 1)
            cout << "1";
        else
            cout << "0";
    }
}</pre>
```

```
// O(logn)
string DecimalToBinary(int num)
{
    string str;
    while(num){
    if(num & 1) // 1
        str+='1';
    else // 0
        str+='0';
    num>>=1; // Right Shift by 1
    }
    return str;
}
```

9 Number Theory

9.1 Divisors

9.1.1 formulas

number of divisors

```
int d(int n){
    unordered_map<int, int> factors = pf(n);
    int c = 1;
    for(const auto& factor: factors){
        c *= (factor.second+1);
    }
    return c;
}

// range Count Divisors backward thinking MAXN = 2e6
    for(int i=1; i <= n; ++i) {
        for(int j = i; j <= n; j += i) {
            numFactors[j]++;
        }
    int countDivisors(int n) {
        int count = 0;
    }
}</pre>
```

```
for (int i = 1; i * i <= n; ++i) {
   if (n % i == 0) {
      if (i == n / i) {
           count++; // Perfect square
      } else {
           count += 2; // Pair of divisors
      }
   }
}
return count;</pre>
```

sum of divisors

```
int s(int n){
   unordered_map<int,int> factors = pf(n);
   int sum = 1;
   for(const auto& factor: factors){
      int p = factor.first;
      int exp = factor.second;
      sum *= (pow(p,exp+1)-1)/p-1;
   }
   return sum;
}
```

9.2 Primes

$prime\ factorization$

number of co-primes with n

```
int eulerTotient(int n){
   int result = n;
   for(int i = 2; SQ(i) \le n; i++){
       if(n\%i == 0){
           while (n\%i == 0) {
              n/=i;
          result -= result/i;
   }
   if(n > 1) result -= result/n;
   return result;
//Phi(n) = n * (1 - 1/P1) * (1 - 1/P2) * ...
//NOTE: summation of Euler function over divisors of n is equal to n
// using seive
void phi_generator() {
   const int MAX = 1000000;
   char primes[MAX];
   int phi[MAX];
   memset(primes, 1, sizeof(primes));
   for (int k = 0; k < MAX; ++k)
       phi[k] = 1;
   for (int i = 2; i <= MAX; ++i) {</pre>
       if (primes[i]) {
           phi[i] = i - 1; // phi(prime) = p-1
          for (int j = i * 2; j <= MAX; j += i) {
              primes[j] = 0;
              int n = j, pow = 1;
              while (n % i == 0) {
```

Prime Check

```
vector<bool> isPrime(MAXN, true);
void sieve() {
 isPrime[0] = isPrime[1] = false;
 for (int i=2; i * i <= isPrime.size(); ++i) {</pre>
   if(isPrime[i]) {
     for (int j = 2 * i; i <= isPrime.size(); j += i)</pre>
       prime[j] = false;
   }
 }
}
bool Prime(int n) {
 if(n == 2) return true;
 if(n < 2 || n % 2 == 0) return false;</pre>
 for(int i=3; i * i <= n; i += 2) {
   if(n % i == 0) return false;
 }
 return true;
// Generate Primes
```

```
const int sz = sqrt(MAXN);
vector<int> prime;
vector<bool> vis(sz);
void pre() {
   prime.push_back(2);
   for (int j = 4; j < sz; j += 2) vis[j] = true;
   for (int i = 3; i < sz; i += 2) {
       if (vis[i]) continue;
       prime.push_back(i);
       for (int j = i * i; j < sz; j += i) vis[j] = true;
   }
// Preprocessing Prime Factorization of range numbers
constexpr int N = 5e6+1;
int a[N];
for(int i=2; i < N; ++i) {</pre>
   if(!a[i]) {
       for(int j=1; i*j < N; ++j) {</pre>
           for(int k=i*j; k%i==0; k/=i) a[i*j]++;
   }
   a[i] += a[i-1];
```

9.3 Math

9.3.1 Vieta's Formulas for a Polynomial of Degree n

Problem: Given a polynomial of degree n:

$$P(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

with roots r_1, r_2, \ldots, r_n , express the sums and products of its roots using Vieta's formulas.

Solution: Using Vieta's formulas, we can relate the coefficients of the polynomial to sums and products of its roots:

• Sum of the roots taken one at a time:

$$r_1 + r_2 + \dots + r_n = -\frac{a_{n-1}}{a_n}$$

• Sum of the products of the roots taken two at a time:

$$r_1r_2 + r_1r_3 + \dots + r_{n-1}r_n = \frac{a_{n-2}}{a_n}$$

• Sum of the products of the roots taken three at a time:

$$r_1 r_2 r_3 + r_1 r_2 r_4 + \dots + r_{n-2} r_{n-1} r_n = -\frac{a_{n-3}}{a_n}$$

- Continue this pattern until:
- Product of the roots (for even n):

$$r_1 r_2 \cdots r_n = (-1)^n \frac{a_0}{a_n}$$

Example Problem Using Vieta's Formulas

Problem: Given a quadratic equation $x^2 + bx + c = 0$ with roots r_1 and r_2 , find $r_1 + r_2$ and r_1r_2 .

Solution: Using Vieta's formulas for a quadratic equation $ax^2 + bx + c = 0$:

• Sum of the roots:

$$r_1 + r_2 = -\frac{b}{a}$$

• Product of the roots:

$$r_1 r_2 = \frac{c}{a}$$

For the given quadratic $x^2 + bx + c = 0$ (where a = 1):

- $r_1 + r_2 = -b$
- $r_1 r_2 = c$

Example Vieta's Formula for Cubic Equation

When considering a cubic equation in the form of $f(x) = ax^3 + bx^2 + cx + d$, Vieta's formula states that if the equation f(x) = 0 has roots r_1, r_2 , and r_3 , then:

- $r_1 + r_2 + r_3 = -\frac{b}{a}$
- $r_1 r_2 + r_2 r_3 + r_3 r_1 = \frac{c}{a}$
- $r_1 r_2 r_3 = -\frac{d}{a}$

9.4 Phi Function

- Count integers i < n such that gcd(i, n) = 1
- $gcd(a, b) = 1 \Rightarrow$ then coprimes: gcd(5, 7), gcd(4, 9)
- gcd(prime, i) = 1 for i < prime
- $\varphi(10) = 4 \Rightarrow 1, 3, 7, 9$
- $\varphi(5) = 4 \Rightarrow 1, 2, 3, 4 \dots \varphi(\text{prime}) = \text{prime} 1$
- If a, b, c are pairwise coprimes, then

$$\varphi(a \cdot b \cdot c) = \varphi(a) \cdot \varphi(b) \cdot \varphi(c)$$

• If $k \geq 1$

$$\varphi(p^k) = p^k - p^{k-1} = p^{k-1}(p-1) = p^k \left(1 - \frac{1}{p}\right)$$

Euler's Totient Numbers

Online Sequence

•
$$\varphi(1) = \varphi(2) = 1, \ \varphi(5) = 4$$

Too bad to be Accepted (Alexandria University)

- $\varphi(n)$ is even for n > 2
- $\sqrt{n} \le \varphi(n) \le n \sqrt{n}$: Except 2, 6
- $\varphi(n^k) = n^{k-1} \cdot \varphi(n)$
- $n = \sum \varphi(d_i)$ where d are the divisors of n

9.5 Möbius Function

Möbius Function

```
int mobius(int n) {
   int p = 0;
   // Handling 2 separately
   if (n\%2 == 0){
       n = n/2;
       p++;
       // If 2^2 also divides N
       if (n \% 2 == 0)
          return 0;
   }
   // Check for all other prime factors
   for (int i = 3; i <= sqrt(n); i = i+2) {</pre>
       if (n\%i == 0){
           n = n/i;
           p++;
           if (n % i == 0) return 0;
   }
   return (p % 2 == 0)? -1 : 1;
}
void mobius_generator() const {
 const int MAX = 1000000;
 int moebius[MAX + 1];
 char prime[MAX + 1];
 for (ll i = 2; i <= MAX; i++)</pre>
```

```
moebius[i] = -1, prime[i] = 1;

for (ll i = 2; i <= MAX; ++i)
    if (prime[i]) {
        moebius[i] = 1;

        for (ll j = 2 * i; j <= MAX; j += i)
            prime[j] = 0, moebius[j] = j % (i * i) == 0 ? -moebius[j] : 1;
    }
}

// Mobius Inclusion Exclusion
// Count triples gcd(a, b, c) = 1
int n = 4;
ll sum = n * n * n;
for (ll i = 2; i <= n; ++i)
        sum -= moebius[i] * (n / i) * (n / i) * (n / i);</pre>
```

Möbius and Inclusion Exclusion

Count the triples (a, b, c) such that $a, b, c \le n$, and gcd(a, b, c) = 1

- Reverse thinking, total (# triples gcd > 1)
- How many triples with gcd multiple of 2: $(n/2)^3$
- How many triples with gcd multiple of 3: $(n/3)^3$
- and 4? Ignore any numbers of internal duplicate primes
- and 6? already computed in 2, 3. Remove it: $-(n/6)^3$

Totient and Möbius Connection

Sum over divisors d of n

$$\sum_{d} d\mu \left(\frac{n}{d}\right) = \varphi(n)$$

10 Geometry

10.1 Linearity

10.1.1 co-linear points

check if two points are co-linear

```
bool co_linear(int x1, int y1, int x2, int y2, int x3, int y3){
  int area = x1*(y2-y3) + x2*(y3-y1) + x3*(y1-y2);
  return area == 0;
}
```

10.2 polygons

10.2.1 Polygon formation

check if can form polygon with given angle

```
bool possible(double angle) {
  if(angle <= 0 || angle >= 180) return false;

double sides = 360.0/(180.0-angle);

return (sides == static_cast<int>(sides) && sides >= 3);
}
```

10.2.2 Rectangle Intersection

intersection area between 2 rectangles

```
struct Rectangle {
   int x1, y1; // Bottom-left corner
   int x2, y2; // Top-right corner
};

int intersectionArea(const Rectangle& rect1, const Rectangle& rect2){
   int x_left = max(rect1.x1, rect2.x1);
   int y_bottom = max(rect1.y1, rect2.y1);
```

```
int x_right = min(rect1.x2, rect2.x2);
int y_top = min(rect1.y2, rect2.y2);

int intersection_width = x_right - x_left;
int intersection_height = y_top - y_bottom;

if (intersection_width > 0 && intersection_height > 0) {
    return intersection_width * intersection_height;
}

return 0;
}
```

11 Miscellaneous

11.1 Faster implementations

11.1.1 hashes

custom hash

```
#define safe hash unordered_map<type, type, custom_hash> // same for
   gp_hash_table
struct custom_hash {
   static uint64_t splitmix64(uint64_t x) {
       // http://xorshift.di.unimi.it/splitmix64.c
       x += 0x9e3779b97f4a7c15;
       x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
       x = (x ^(x >> 27)) * 0x94d049bb133111eb;
       return x ^ (x >> 31);
   }
   size_t operator()(uint64_t x) const {
       static const uint64_t FIXED_RANDOM = chrono::steady_clock::now().
           time_since_epoch().count();
       return splitmix64(x + FIXED_RANDOM);
   }
};
```

gb hash table

```
//policy based ds (faster hash table)
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
gp_hash_table<int, int> table;
```

11.1.2 Binary Search the value

$nearest\ sqrt$

```
long long my_sqrt(long long a)
{
    long long l=0,r=5000000001;
    while(r-l>1)
    {
        long long mid=(l+r)/2;
        if(1ll*mid*mid<=a)l=mid;
        else r=mid;
    }
    return l;
}</pre>
```