Competitive Programming Library

Too bad to be Accepted 2023/2024

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8	Tec	hniques	21	Input/Output
O	8.1	Coordinate Compression	21	<pre>#include <bits stdc++.h=""></bits></pre>
	8.2	Binary to decimal		<pre>freopen("input.txt", "r", stdin);</pre>
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9	Nur	mber Theory	22	#define fastIO \
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	~			1.1.2 GCC Compiler Optimization (Vectorization)
10		ometry	24	
	10.1	Linearity	24	GCC Opt
	10.0	10.1.1 co-linear points	24	<pre>// Ref: USACO guide // will make GCC auto-vectorize for loops and optimizes floating points</pre>
	10.2	1 3 3 3		hattar (assumes associativity and turns off denormals)
		10.2.1 Polygon formation		#pragma GCC optimize ("Ofast")
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11	Mis	cellaneous	25	<pre>#pragma GCC target ("avx,avx2,fma")</pre>
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		11.1.1 hashes	25	<pre>// slows down run time but throws a Runtime Error if an overflow occured #pragma GCC optimize("trapv")</pre>
		11.1.2 Binary Search the value	25	#pragma GCC optimize("trapy")
				1.2 MOD Template

constexpr int MOD = 1e9+7; // must be a prime number

if(res >= MOD) return res -= MOD;

int add(int a, int b) {
 int res = a+b;

```
int sub(int a, int b) {
   int res = a-b;
   if(res < 0) return res += MOD;
}

int power(int a, int e) {
   int res = 1;
   while(e) {if(e & 1) res = res * a % MOD; a = a * a % MOD;
   e >>= 1;}
   return res;
}

int inverse(int a) {
   return power(a, MOD-2);
}

int div(int a, int b) {
   return a * inverse(b) % MOD;
}
```

MOD Template

1.3 Macros

Macros

```
#define getBit(n, k) (n >> k)
#define ON(n, idx) (n | (111 << idx))
#define OFF(n, idx) (n & ~(111 << idx))
#define toggle(n, idx) ((n) ^ (111 << (idx)))
#define gray(n) (n ^ (n >> 1))
#define bitCount(x) (__builtin_popcountll(x))
#define uniq(x) x.resize(unique(x.begin(), x.end())-x.begin());

#define angle(a) (atan2((a).imag(), (a).real()))
//#define vec(a, b) ((b)-(a))
#define same(v1, v2) (dp(vec(v1,v2),vec(v1,v2)) < EPS)
#define dotProduct(a, b) ((conj(a)*(b)).real()) // a*b cos(T), if zero -> prep
#define crossProduct(a, b) ((conj(a)*(b)).imag()) // a*b sin(T), if zero -> parallel
//#define length(a) (hypot((a).imag(), (a).real()))
```

```
#define normalize(a) ((a)/length(a))
#define rotateO(v, ang) ((v)*exp(point(0,ang)))
#define rotateA(p, ang, about) (rotateO(vec(about,p),ang)+about)
#define reflectO(v, m) (conj((v)/(m))*(m))
#define ceil_i(a, b) (((ll)(a)+(ll)(b-1))/(ll)(b))
#define floor_i(a, b) (a/b)
#define round_i(a, b) ((a+(b/2))/b) // if a>0
#define round_m(a, b) ((a-(b/2))/b) // if a<0
#define round_multiple(n, m) round_i(n,m)*m // round to multiple if specified element</pre>
const double PI = acos(-1.0);
```

1.4 Grid Navigation

Grid Nav

```
// knight moves on a chess board
int dx[] = { -2, -1, 1, 2, -2, -1, 1, 2 };
int dy[] = { -1, -2, -2, -1, 1, 2, 2, 1 };

// Grid up, down, right, left (Moves for Chess Rook)
int dx[4] = {1, -1, 0, 0};
int dy[4] = {0, 0, 1, -1};

// Grid cell all neighbours
const int dx[8] = {1, 0, -1, 0, 1, 1, -1, -1}
const int dy[8] = {0, 1, 0, -1, -1, 1, -1, 1};

// Grid Diagonal (Moves for Chess Bishop)
int dx[] = {1, 1, -1, -1};
int dy[] = {1, -1, 1, -1};
```

2 Dynamic Programming

2.1 Some dp patterns

Maximumu/Minimum path cost

```
const int MAX = 21;
int grid[MAX][MAX];
int mem[MAX][MAX];
int n = 20;
bool valid(int r, int c){
 return r >= 0 \&\& r < n \&\& c >= 0 \&\& c < n;
int maxPathSum(int r, int c){
   if(!valid(r,c)){
       return 0;
   }
   if(r == n-1 \&\& c == n-1){
       return mem[r][c] = grid[r][c];
   // available moves
   int path1 = maxPathSum(r+1,c);
   int path2 = maxPathSum(r,c+1);
   return grid[r][c] + max(path1,path2);
}
```

add operators between numbers to get max prod/sum

```
// put +, -, between sequence of numbers such that the sum is divisible by
    k, and maximum as possible
const int MAX = 21;
long long mem[MAX][MAX];
const int n = 20;
int k = 4; // example
int v[20];
int fix(int a){
    return (a % k + k) % k;
}
long long tryAll(int pos, int mod){
    long long &ret = mem[pos][mod];
    if(ret != -1){
        return ret;
    }
    if(pos == n){
```

```
return ret = mod == 0;
}
if(tryAll(pos+1,fix(mod + v[pos])) || tryAll(pos+1,fix(mod-v[pos]))){
    return ret = 1;
}
return ret = 0;
}
```

pick choices with no two similar consecutive choices

```
// pick minimum of choinces costs with no two similar consecutive choices
const int choices = 4;
const int n = 20:
int MAX = n:
int mem[MAX][choices];
const int 00 = 1e6+1;
int minCost(int pos, int lastChoice){
   if(pos == n){
       return 0: // invalid move
   int &ret = mem[pos][lastChoice];
   if(ret != -1){
       return ret;
   ret = 00; // want to minimze
   // let choices are 0, 1, 2
   if(lastChoice != 0){
       ret = min(ret, minCost(pos+1,0));
   if(lastChoice != 1){
       ret = min(ret, minCost(pos+1,1));
   if(lastChoice != 2){
       ret = min(ret, minCost(pos+1,2));
   return ret:
```

sum S and max/min Product

```
int maxK:
ll mem[21][101]; // k, and s
// You are given an integer s and an integer k. Find k positive integers
   a1, a2, ..., ak
// such that their sum is equal to s and their product is the maximal
   possible. Return their product.
11 maxProd(int k, int rem)
if(k == maxK){
 // base case
 if(rem == 0)
 return 1;
 return 0;
if(rem == 0) // invalid case
 return 0;
11 &ret = mem[k][rem];
if(ret != -1)
 return ret;
ret = 0;
 for (int i = 1; i <= rem; ++i) {</pre>
 ll sol = maxProd(k+1, rem - i) * i;
 ret = max(ret, sol);
}
return ret;
```

2.2 DP solutions

2.2.1 Max Subarray sum (Kadane's Algorithm)

Max Subarray sum

```
int maxSubarraySum(vector<int>& arr, int len) {
   int ans = INT_MIN, cur = 0;

   for (int i = 0; i < len; i++) {
      cur = cur + arr[i];
      if (ans < cur)
            ans = cur;

      if (cur < 0)
            cur = 0;
   }

   return ans;
}</pre>
```

2.2.2 Maximum Subarray Alternating Sum

Maximum Subarray Alternating Sum

```
/* REF: GeeksForGeeks
Input: arr[] = \{-4, -10, 3, 5\}
Output: 9
Explanation: Subarray {arr[0], arr[2]} = {-4, -10, 3}. Therefore, the sum
     of this subarray is 9.
*/
int maxSubarraySumALT(vector<int>& a, int len) {
   int ans = INT_MIN, cur = 0;
   for (int i = 0; i < len; i++) {
       if (i % 2 == 0)
           cur = max(cur + a[i], a[i]);
           cur = max(cur - a[i], -a[i]);
       ans = max(ans, cur);
   }
   cur = 0;
   for (int i = 0; i < len; i++) {</pre>
       if (i % 2 == 1)
           cur = max(cur + a[i], a[i]);
```

```
else
           cur = max(cur - a[i], -a[i]);
       ans = max(ans, cur);
   }
   return ans;
}
```

2.2.3sums to x

Count distinct

```
/*
For example, if the coins are \{2,3,5\} and the desired sum is 9, there
    are 3 ways:
2+2+5
3+3+3
2+2+2+3
*/
int n, x;
cin >> n >> x;
vector<int> coins(n);
read(coins);
vector dp(x + 1, 0);
dp[0] = 1;
for (int i = 0; i < n; ++i) {</pre>
for (int j = coins[i]; j <= x; ++j) {</pre>
 dp[j] = add(dp[j], dp[j - coins[i]]);
}
}
cout << dp[x] << el;
```

2.2.4 Min absolute difference between 2 elements from (L, R) (DP Ranges)

Min absolute difference

```
const int N = 1e4 + 1;
                                                                    int dp[N][N];
                                                                    int n;
                                                                    cin >> n;
                                                                    vector<int> a(n);
                                                                    read(a);
Count number of DISTINCT ordered ways to produce coins for (int i = 0; i < n; ++i) dp[i][i] = 1e6; // INF, you can't take the
                                                                        element with it self
                                                                    for (int i = 1; i < n; ++i) dp[i - 1][i] = abs(a[i] - a[i - 1]);
                                                                    for (int len = 3; len <= n; ++len) {
                                                                     for (int l = 0, r = len - 1; r < n; ++1, ++r) {
                                                                      dp[l][r] = min(dp[l][r - 1], dp[l + 1][r]);
                                                                      dp[l][r] = min(dp[l][r], abs(a[l] - a[r]));
                                                                    int q;
                                                                    cin >> q;
                                                                    while (q--) {
                                                                     int 1, r;
                                                                     cin >> 1 >> r;
                                                                     --1, --r;
                                                                     cout << dp[l][r] << el;
```

Bit Manipulation 3

3.1 **Subset Operations**

count subsets with give sum

```
int countDistinctSubsetsWithSum(vector<int>& arr, int n, int k) {
```

```
// Count distinct subsets of array arr that sum up to k
vector<int> dp(k + 1, 0);
dp[0] = 1;
for (int i = 0; i < n; ++i) {
    for (int j = k; j >= arr[i]; --j) {
        dp[j] += dp[j - arr[i]];
    }
}
return dp[k]; // Number of distinct subsets with sum k
```

max xor of any subset of elements in the array

```
int maximalSubsetXOR(vector<int>& arr, int n) {
    // Find the maximum XOR of any subset of elements in array arr
    int maxXor = 0;
    for (int mask = 0; mask < (1 << n); ++mask) {
        int xorSum = 0;
        for (int i = 0; i < n; ++i) {
            if (mask & (1 << i)) {
                  xorSum ^= arr[i];
            }
        }
        maxXor = max(maxXor, xorSum);
    }
    return maxXor;
}</pre>
```

min xor of any subset

```
int minimumSubsetXOR(vector<int>& arr, int n) {
    // Find the minimum XOR of any pair of elements in array arr
    int minSubsetXor = INT_MAX;
    for (int mask = 0; mask < (1 << n); ++mask) {
        int xorSum = 0;
        for (int i = 0; i < n; ++i) {
            if (mask & (1 << i)) {
                  xorSum ^= arr[i];
            }
        }
        minSubsetXor = min(minSubsetXor, xorSum);
}</pre>
```

```
return minSubsetXor;
}
```

subset generation

```
void subsetGeneration(int x, int n) {
    // Generate all non-empty subsets of a set represented by an integer x
    for (int subset = x; subset > 0; subset = (subset - 1) & x) {
        // Process subset
        cout << subset << endl;
    }
}</pre>
```

check if subset of elements in the array sum up to k

```
void subsetSumCheck(vector<int>& arr, int n, int k) {
    // Check if a subset of elements in array arr sums up to k
    for (int subset = 0; subset < (1 << n); ++subset) {
        int sum = 0;
        for (int i = 0; i < n; ++i) {
            if (subset & (1 << i)) {
                sum += arr[i];
            }
        }
        if (sum == k) {
                // Found subset with sum k
                cout << "Subset with sum " << k << ": " << subset << endl;
        }
    }
}</pre>
```

max subset sum mod m

```
int subsetWithMaxSumModuloM(vector<int>& arr, int n, int m) {
    // Find the maximum subset sum modulo m
    vector<int> dp(m, -1);
    dp[0] = 0;
    int currentMod = 0;
    for (int i = 0; i < n; ++i) {
        currentMod = (currentMod + arr[i]) % m;
}</pre>
```

iterate over all supersets represented by x

```
void iterateOverSupersets(int x, int n) {
    // Iterate over all supersets of a set represented by x
    int subset = x;
    do {
        // Process subset
        cout << subset << endl;
        subset = (subset + 1) | x;
    } while (subset <= (1 << n) - 1);
}</pre>
```

4 Algorithms

4.1 MO

MO Algorithm

```
idx = _idx;
       r = _r - 1;
       1 = _1 - 1;
       block_idx = _l / sqrt(n);
   }
    bool operator <(const query & y) const {</pre>
       if(y.block_idx == block_idx) return r < y.r;</pre>
       return block_idx < y.block_idx;</pre>
   }
int freq[N], ans;
void add(int idx) {
   freq[nums[idx]]++;
    if (freq[nums[idx]] == 2) ans++;
void remove(int idx) {
   freq[nums[idx]]--;
   if (freq[nums[idx]] == 1) ans--;
cin >> n >> m:
for (int i = 0; i < n; ++i) cin >> nums[i];
vector<query> Query(m);
for (int i = 0; i < m; ++i) {</pre>
   int 1, r; cin >> 1 >> r;
   Query[i] = query(1, r, i);
sort(Query.begin(), Query.end());
int 10 = 1, r0 = 0;
for (int i = 0; i < m; ++i) {</pre>
    while (10 < Query[i].1) remove(10++);</pre>
    while (10 > Query[i].1) add(--10);
   while (r0 < Query[i].r) add(++r0);</pre>
   while (r0 > Query[i].r) remove(r0--);
    q_ans[Query[i].idx] = ans;
for (int i = 0; i < m; ++i) {
    cout << q_ans[i] << '\n';</pre>
```

}

4.2 Intervals

4.2.1 Prefix Sum (L, R) intervals

Prefix Sum (L, R) intervals

```
// NOTE: works fine with small n or with large memory
int main() {
   int n, k;
   cin >> n >> k;
   vector < int > a(n + 1);
   vector<vector<int>> rangesPrefix(n + 1, vector<int>(n + 1, 0));
   for (int i = 1; i <= n; ++i)
       cin >> a[i];
   int 1 = 1, r = 1, sum = 0;
   // validate your intervals
   // here the intervals are the ones that have a sum of k
   while (r \le n) {
       sum += a[r];
       while (sum > k) {
           sum -= a[1];
           ++1;
       }
       while (1 <= r && a[1] == 0) {</pre>
           if (sum != k)
              break;
           rangesPrefix[r][l]++;
           ++1;
       if (sum == k) {
           rangesPrefix[r][1]++;
```

```
}
    ++r;
}
// prefix sum the columns
for (int i = 1; i <= n; ++i) {
   for (int j = n - 1; j \ge 0; --j) {
       rangesPrefix[i][j] += rangesPrefix[i][j + 1];
}
// prefix sum the rows
for (int i = 0; i <= n; ++i) {</pre>
   for (int j = 1; j <= n; ++j) {
       rangesPrefix[j][i] += rangesPrefix[j - 1][i];
   }
}
int q; cin >> q;
while (q--) {
   cin >> 1 >> r;
   // answer the number of intervals (X, Y) X <= Y that are included
        between L, R
   cout << rangesPrefix[r][l] - rangesPrefix[l - 1][l] << el;</pre>
}
```

4.2.2 Find subarrays intervals that sum to K Using Map

Find subarray intervals that sum to K Using Map

```
int n, k;
cin >> n >> k;

vector<int> a(n + 1);
vector<pair<int, int>> rng;
for (int i = 1; i <= n; ++i)
        cin >> a[i];

map<int, set<int>> prev;
```

```
int currSum = 0;

for (int i = 1; i <= n; ++i) {
    currSum += a[i];
    if (currSum == k) {
        rng.push_back({1, i});
    }
    if (prev.find(currSum - k) != prev.end()) {
        for (auto &j : prev[currSum - k]) {
            rng.push_back({j + 1, i});
        }
    }
    prev[currSum].insert(i);
}</pre>
```

4.3 Ad-hoc

4.3.1 Find duplicates

Find duplicates using XOR

```
int findDuplicate(int arr[] , int n)
{
   int answer=0;
    //XOR all the elements with 0
   for(int i=0; i<n; i++){
      answer=answer^arr[i];
   }
   //XOR all the elements with no from 1 to n
   // i.e answer^0 = answer
   for(int i=1; i<n; i++){
      answer=answer^i;
   }
   return answer;
}</pre>
```

5 Data Structures

5.1 Strings

5.1.1 Trie (Prefix Tree)

$Basic\ Implementation$

```
#define MAX_CHAR 26
struct TrieNode {
   TrieNode *pTrieNode[MAX_CHAR]{};
   bool isWord;
   TrieNode() {
       isWord = false;
       fill(pTrieNode, pTrieNode + 26, (TrieNode *) NULL);
   virtual ~TrieNode() = default;
};
class Trie {
private:
   TrieNode *root;
public:
   Trie() {
       root = new TrieNode();
   }
   virtual ~Trie() = default;
   TrieNode *getTrieNode() {
       return this->root;
   }
   void insert(const string &word) {
       TrieNode *current = root;
       for (char c: word) {
           int i = c - 'a';
          if (current->pTrieNode[i] == nullptr)
              current->pTrieNode[i] = new TrieNode();
           current = current->pTrieNode[i];
```

```
current->isWord = true:
   }
   bool search(const string &word) {
       TrieNode *current = root:
       int ch = 0:
       for (char c: word) {
          ch = c - 'a':
          if (current->pTrieNode[ch] == nullptr)
              return false:
           current = current->pTrieNode[ch];
       }
       return current->isWord;
   }
   bool startsWith(const string &prefix) {
       TrieNode *current = root;
       int ch = 0;
       for (char c: prefix) {
          ch = c - 'a';
          if (current->pTrieNode[ch] == nullptr)
              return false;
          current = current->pTrieNode[ch];
       }
       return true;
   }
};
```

5.2 Range Queries

5.2.1 Segment Tree

$Basic\ Implementation$

```
struct Node {
    long long val;
};

struct SegTree {
private:
    const Node NEUTRAL = {INT_MIN};
```

```
static Node merge(const Node& x1, const Node& x2) {
   return {x1.val + x2.val};
}
void set(const int& idx, const int& val, int x, int lx, int rx) {
   if (rx - lx == 1) return void(values[x].val = val);
   int mid = (rx + lx) / 2;
   if (idx < mid)</pre>
       set(idx, val, 2 * x + 1, lx, mid);
       set(idx, val, 2 * x + 2, mid, rx);
   values[x] = merge(values[2 * x + 1], values[2 * x + 2]);
}
Node query(const int& 1, const int& r, int x, int lx, int rx) {
   if (lx >= r || l >= rx) return NEUTRAL;
   if (lx >= 1 && rx <= r) return values[x];</pre>
   int mid = (rx + lx) / 2;
   return merge(query(1, r, 2 * x + 1, lx, mid), query(1, r, 2 * x +
        2, mid, rx));
}
void build(vector<int> &a, int x, int lx, int rx) {
   if (rx - 1x == 1) {
       if (lx < a.size()) {</pre>
           values[x].val = a[lx];
       return;
   int m = (1x + rx) / 2;
   build(a, 2 * x + 1, lx, m);
   build(a, 2 * x + 2, m, rx);
   values[x] = merge(values[2 * x + 1], values[2 * x + 2]);
}
 void assign_range(int 1, int r, int node, int lx, int rx, int time,
     int val) {
   if (lx > r || l > rx) return;
   if (lx >= 1 && rx <= r) {
       lazy[node] = {time, val};
```

```
return;
       int mid = (1x+rx) / 2;
       assign_range(1, r, 2*node+1, lx, mid, time, val);
       assign_range(1, r, 2*node+2, mid+1, rx, time, val);
   }
   pair<int, int> point_query(int lx, int rx, int node, int idx) {
       if(rx == lx) return lazy[node];
       int mid = (1x+rx) / 2;
       if(idx <= mid) {</pre>
           auto x = point_query(lx, mid, 2*node+1, idx);
           if(x.first > lazy[node].first) return x;
           return lazy[node];
       auto x = point_query(mid+1, rx, 2*node+2, idx);
       if(x.first > lazy[node].first) return x;
       return lazy[node];
   }
public:
   int size{};
   vector<Node> values;
   void build(vector<int> &a) {
       build(a, 0, 0, size);
   }
   void init(int _size) {
       size = 1;
       while (size < _size) size *= 2;</pre>
       values.assign(2 * size, NEUTRAL);
   }
   void set(int idx, int val) {
       set(idx, val, 0, 0, size);
   }
   Node query(const int& 1, const int& r) {
       return query(1, r, 0, 0, size);
   }
};
```

5.2.2 Lazy Propegation

Lazy Propegation

```
struct SegTree {
private:
   void propegate(int lx, int rx, int node) {
       if(!lazy[node]) return;
       if(lx != rx) {
           lazy[2*node+1] = lazy[node];
           lazy[2*node+2] = lazy[node];
       values[node] = lazy[node] * (rx - lx + 1);
       lazv[node] = 0;
   }
   // assign val in range [l, r]
   void update_range(int 1, int r, int node, int lx, int rx, int val,
       bool f) {
       propegate(lx, rx, node);
       if (lx > r \mid | l > rx) return;
       if (lx >= 1 && rx <= r) {
           lazy[node] = val;
          propegate(lx, rx, node);
           return;
       int mid = (lx+rx) / 2;
       update_range(l, r, 2*node+1, lx, mid, val, f);
       update_range(l, r, 2*node+2, mid+1, rx, val, f);
       values[node] = values[2*node+1] + values[2*node+2];
   }
   // get sum in range [1, r]
   int range_query(int 1, int r, int lx, int rx, int node) {
       propegate(lx, rx, node);
       if (lx > r || l > rx) return 0;
       if (lx >= 1 && rx <= r) return values[node];</pre>
       int mid = (lx+rx) / 2;
```

```
return range_query(1, r, lx, mid, 2*node+1) + range_query(1, r, mid
           +1, rx, 2*node+2);
   }
public:
   int size{};
   vector<int> values, lazy;
   void init(int _size) {
       size = 1;
       while (size < _size) size *= 2;</pre>
       values.assign(2 * size, 0);
       lazy.assign(2 * size, 0);
   }
   void update_range(int 1, int r, int v, bool f) {
       update_range(1, r, 0, 0, size-1, v, f);
   }
   int range_query(int 1, int r) {
       return range_query(1, r, 0, size-1, 0);
   }
};
```

5.2.3 Fenwick Tree

Fenwick Tree

```
struct Fenwick {
    // One Based
    vector<int> tree;

explicit Fenwick(int n) {tree.assign(n + 5, {});}

// Computes the prefix sum from [1, i], O(log(n))
int query(int i) {
    int res = 0;
    while (i > 0) {
        res += tree[i];
        i &= ~(i & -i);
    }
    return res;
}
```

```
int query(int 1, int r) {
       return query(r) - query(1-1);
   }
   // Get the value at index i
   int get(int i) {
       return query(i, i);
   }
   // Add 'v' to index 'i', O(log(n))
   void update(int i, int v) {
       while (i < tree.size()) {</pre>
           tree[i] += v;
           i += (i & -i);
   }
   // Update range, Point query
   // To get(k) do prefix sum [1, k] and in insert update_range(i, i, a[i
   void update_range(int 1, int r, int v) {
       update(1, v);
       update(r+1, -v);
   }
};
```

5.2.4 Fenwick UpdateRange

BIT UpdateRange

```
struct BITUpdateRange {
private:
   int n;
   vector<int> B1, B2;

  void add(vector<int> &b, int idx, int x) {
     while (idx <= n) {
        b[idx] += x;
        idx += idx & -idx;
     }
}</pre>
```

```
int sum(vector<int> &b, int idx) {
       int total = 0;
       while (idx > 0) {
          total += b[idx];
          idx &= ~(idx & -idx);
       }
       return total;
   }
   int prefix(int idx) {
       return sum(B1, idx) * idx - sum(B2, idx);
   }
public:
   explicit BITUpdateRange(int n) : n(n) {
       B1.assign(n + 1, {});
       B2.assign(n + 1, {});
   }
   void update(int 1, int r, int x) {
       add(B1, 1, x);
       add(B1, r + 1, -x);
       add(B2, 1, x * (1 - 1));
       add(B2, r + 1, -x * r);
   }
   int query(int i) {
       return prefix(i) - prefix(i - 1);
   }
   int query(int 1, int r) {
       return prefix(r) - prefix(l - 1);
   }
};
```

5.2.5 2D BIT

2D BIT

```
struct BIT2D {
   int n, m;
   vector<vector<int>> bit;
```

```
BIT2D(int n, int m) : n(n), m(m) {
   bit.assign(n + 2, vector<int>(m + 2));
}
void update(int x, int y, int val) {
   for (; x \le n; x += x & -x) {
       for (int i = y; i <= m; i += i & -i) {
           bit[x][i] += val;
   }
}
int prefix(int x, int y) {
   int res = 0;
   for (; x > 0; x &= (x & -x)) {
       for (int i = y; i > 0; i &= ~(i & -i)) {
           res += bit[x][i];
       }
   }
   return res;
}
int query(int sx, int sy, int ex, int ey) {
   int ans = 0;
   ans += prefix(ex, ey);
   ans -= prefix(ex, sy - 1);
   ans -= prefix(sx - 1, ey);
   ans += prefix(sx - 1, sy - 1);
   return ans;
}
```

5.2.6 Sparse Table

Impl with the index

```
// storing the index also
struct SNode {
   int val;
   int index;
};
class SparseTable {
```

```
private:
   vector<vector<SNode>> table;
   function<SNode(const SNode&, const SNode&)> merge;
   static SNode StaticMerge(const SNode& a, const SNode& b) {
       return a.val < b.val ? a : b;</pre>
   }
public:
    explicit SparseTable(const vector<int>& arr, const function<SNode(</pre>
       const SNode&, const SNode&)>& mergeFunc = StaticMerge) {
       int n = static_cast<int>(arr.size());
       int log_n = static_cast<int>(log2(n)) + 1;
       this->merge = mergeFunc;
       table.resize(n, vector<SNode>(log_n));
       for (int i = 0; i < n; i++) {</pre>
           table[i][0] = {arr[i], i};
       for (int j = 1; (1 << j) <= n; j++) {
           for (int i = 0; i + (1 << j) <= n; i++) {
               table[i][j] = mergeFunc(table[i][j - 1], table[i + (1 << (j
                   - 1))][j - 1]);
           }
   SNode query(int left, int right) {
       int j = static_cast<int>(log2(right - left + 1));
       return merge(table[left][j], table[right - (1 << j) + 1][j]);</pre>
   }
};
int main(void) {
   int n:
   cin >> n;
   vector<int> arr(n);
   for (auto& element : arr) cin >> element;
   SparseTable minSt(arr, [](const SNode& a, const SNode& b) -> SNode {
```

```
return a.val < b.val ? a : b;
});

SparseTable maxSt(arr, [](const SNode& a, const SNode& b) -> SNode {
    return a.val > b.val ? a : b;
});
```

5.3 Ordered Set

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;

template < typename T>
using ordered_set = tree < T, null_type, less < T>, rb_tree_tag,
    tree_order_statistics_node_update>;

void erase_set(ordered_set &os, int v) {
    // Number of elements less than v
    int rank = os.order_of_key(v);

    auto it = os.find_by_order(rank);
    os.erase(it);
}
```

Ordered Set

6 Counting Principles

6.1 nCr

$$C(n,k) = \frac{n!}{(n-k)!k!} = \frac{n*(n-1)*(n-2)*...*(n-k+1)}{k!}$$

6.1.1 Fast nCr

Fast nCr

```
int nCr(const int& n, const int& r) {
   double res = 1;
   for (int i = 1; i <= r; ++i)
       res = res * (n - r + i) / i;
   return (int)(res + 0.01);
}
```

6.1.2 Method 1: Pascal's Triangle (Dynamic Programming) - $\mathcal{O}(n^2)$

nCk using dp

```
// REF: USACO guide
/** Oreturn nCk mod p using dynamic programming */
int binomial(int n, int k, int p) {
// dp[i][j] stores iCj
vector<vector<int>> dp(n + 1, vector<int>(k + 1, 0));
// base cases described above
for (int i = 0; i <= n; i++) {</pre>
  * i choose 0 is always 1 since there is exactly one way
  * to choose O elements from a set of i elements
  * (don't choose anything)
 dp[i][0] = 1;
  * i choose i is always 1 since there is exactly one way
  * to choose i elements from a set of i elements
  * (choose every element in the set)
  */
 if (i <= k) { dp[i][i] = 1; }</pre>
```

```
C(n,k) = \frac{n*(n-1)*(n-2)*...*(n-k+1)}{1*2*3*...*k} = \prod_{i=0}^{k-1} \frac{n-i}{i+1} = \prod_{i=0}^{k-1} (n-i)(i+1)^{n-i} = \prod_{i=0}^{k-1} (n
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return dp[n][k]; // returns nCk modulo p
```

6.1.3 Method 2: Factorial Definition (Modular Inverses) - $\mathcal{O}(n +$ $\log MOD$

nCk using Modular Inverses

```
// REF: USACO guide
const int MAXN = 1e6;
long long fac[MAXN + 1];
long long inv[MAXN + 1];
/** @return x^n modulo m in O(log p) time. */
long long exp(long long x, long long n, long long m) {
x \% = m; // note: m * m must be less than 2^63 to avoid 11 overflow
long long res = 1;
while (n > 0) {
 if (n % 2 == 1) { res = res * x % m; }
 x = x * x % m;
 n /= 2;
return res;
/** Precomputes n! from 0 to MAXN. */
void factorial(long long p) {
fac[0] = 1;
for (int i = 1; i <= MAXN; i++) { fac[i] = fac[i - 1] * i % p; }
```

```
/**
 * Precomputes all modular inverse factorials
 * from 0 to MAXN in O(n + log p) time
void inverses(long long p) {
inv[MAXN] = exp(fac[MAXN], p - 2, p);
for (int i = MAXN; i >= 1; i--) { inv[i - 1] = inv[i] * i % p; }
/** @return nCr mod p */
long long choose(long long n, long long r, long long p) {
return fac[n] * inv[r] % p * inv[n - r] % p;
int main() {
factorial();
inverses();
int n;
 cin >> n;
for (int i = 0; i < n; i++) {</pre>
 int a, b;
 cin >> a >> b;
 cout << choose(a, b) << '\n';
}
}
```

7 Graph Theory

7.1 Shortest Path algorithms

7.1.1 Dijkstra Algorithm

Dijkstra Implementation

```
#define INF (1e18) // for int defined as ll
int n, m;
vector<vector<pair<int, int>>> adj;
vector<int> cost;
vector<int> parent;
```

```
void dijkstra(int startNode = 1) {
   priority_queue<pair<ll, int>, vector<pair<ll, int>>, greater<>> pq;
   cost[startNode] = 0;
   pq.emplace(0, startNode);
   while (!pq.empty()) {
       int u = pq.top().second;
       11 d = pq.top().first;
       pq.pop();
       if (d > cost[u]) continue;
       for (auto &p: adj[u]) {
           int v = p.first;
           int w = p.second;
           if (cost[v] > cost[u] + w) {
              cost[v] = cost[u] + w;
              parent[v] = u;
              pq.emplace(cost[v], v);
       }
   }
void run_test_case(int testNum) {
   cin >> n >> m;
   adj.assign(n + 1, {});
   cost.assign(n + 1, INF);
   parent.assign(n + 1, -1);
   while (m--) {
       // Read Edges
   }
   dijkstra();
   if (cost[n] == INF) {
       cout << -1 << el; // not connected {Depends on you use case}</pre>
       return;
   }
   stack<int> ans:
```

```
for (int v = n; v != -1; v = parent[v]) ans.push(v);
while (!ans.empty()) { // printing the path
    cout << ans.top() << ' ';
    ans.pop();
}
cout << el;</pre>
```

7.1.2 Floyd Warshal Algorithm

FloydWarshal Implementation

```
int main() {
    int n, m; cin >> n >> m;
    vector \langle \text{vector} \langle \text{int} \rangle \rangle adj(n + 1, vector \langle \text{int} \rangle \rangle (n + 1, 2e9));
    for (int i = 0; i < n; i++) adj[i][i] = 0;
    while(m--) {
        int u, v, w;
  cin >> u >> v >> w;
        adj[u][v] = min(adj[u][v], w);
        adj[v][u] = min(adj[v][u], w);
    }
    for (int mid = 1; mid <= n; mid++) {</pre>
        for (int start = 1; start <= n; start++) {</pre>
             for (int end = 1; end <= n; end++) {</pre>
                 adj[start][end] = min(adj[start][end], adj[start][mid] +
                      adj[mid][end]);
             }
    }
return 0;
```

7.1.3 Bellman Ford Algorithm

BellmanFord Implementation

```
vector <vector <pair<int, int>>> &adj
vector <long long> BellmanFord(int src) {
   int n = (int)adj.size();
   vector <long long> dist(n, 2e18);
   dist[src] = 0;
   for (int it = 0; it < n-1; it++) {</pre>
       bool in = false;
       for (int i = 0; i < n; i++) { // iterate on the edges
           for (auto &[j, w] : adj[i]) {
              if (dist[j] > dist[i] + w) {
                  in = true;
                  dist[j] = dist[i] + w;
              }
       if (!in) return dist;
   }
   for (int i = 0; i < n; i++) {</pre>
       for (auto &[j, w] : adj[i]) {
          if (dist[j] > dist[i] + w) { //negative cycle
              return vector <long long> (n, -1); // or any flag
       }
   }
   return dist:
```

7.2 Cycle Detection

7.2.1 DFS Implementation

DFS Implementation

```
// return true with number of nodes in the cycle, either odd cycle or even
bool cycle_detection(unordered_map<int, vector<int>> &graph, int source,
   int par, unordered_map<int,bool> vis, int c){
```

```
if(vis[source]) return true;

vis[source] = true;

for(int v: graph[source]){
   if(v != par){
      c++;
      if(dfs(graph,v, source, vis, c)) return true;
   }
}
return false;
```

7.2.2 Another way for undirected graphs

Another way for undirected graphs

```
// this is true only for undirected graphs
bool dfs1(int cur, int par) {
   bool ret = false;
   vis[cur] = true;
   for (auto &i : adj[cur]) {
      if (!vis[i]) ret|=dfs1(i, cur);
      else if (par != i) ret = true;
   }
   return ret;
}
```

7.2.3 General Way

General Way

```
// general algorithm
vector <bool> cyc;
bool dfs(int cur, int par) {
   bool ret = false;
   vis[cur] = cyc[cur] = true;
   for (auto &i : adj[cur]) {
      if (par == i) continue;
      if (!vis[i]) ret|=dfs(i, cur);
      else if (cyc[i]) ret = true;
```

```
}
cyc[cur] = false;
return ret;
}
```

7.2.4 DSU Implementation

$DSU\ Implementation$

```
#include <iostream>
#include <vector>
class UnionFind {
public:
   UnionFind(int n) {
       parent.resize(n);
       rank.resize(n, 0);
       for (int i = 0; i < n; ++i) {</pre>
           parent[i] = i;
       }
   }
   int find(int u) {
       if (parent[u] != u) {
           parent[u] = find(parent[u]);
       return parent[u];
   }
   void unionSets(int u, int v) {
       int rootU = find(u);
       int rootV = find(v);
       if (rootU != rootV) {
           if (rank[rootU] > rank[rootV]) {
               parent[rootV] = rootU;
           } else if (rank[rootU] < rank[rootV]) {</pre>
               parent[rootU] = rootV;
           } else {
               parent[rootV] = rootU;
               ++rank[rootU];
       }
```

```
}
private:
   std::vector<int> parent;
   std::vector<int> rank:
};
bool detectCycle(const std::vector<std::pair<int, int>>& edges, int n) {
   UnionFind uf(n);
   for (const auto& edge : edges) {
       int u = edge.first;
       int v = edge.second;
       if (uf.find(u) == uf.find(v)) {
           return true;
       uf.unionSets(u, v);
   return false;
}
int main() {
   std::vector<std::pair<int, int>> edges = { {0, 1}, {1, 2}, {2, 3}, {3,
        0} };
   int n = 4; // Number of vertices
   if (detectCycle(edges, n)) {
       std::cout << "Cycle detected" << std::endl;</pre>
   } else {
       std::cout << "No cycle detected" << std::endl;</pre>
   }
   return 0;
```

7.3 Algorithms

7.3.1 Heavy Light Decomposition

Basic HLD Impl

```
struct Node {
   int val;
};
const Node nullNode = {0};
const int N = 2e5 + 5, S = 1 << 19;
int n, q;
int val[N];
int sz[N], par[N], dep[N], id[N], top[N];
vector<int> adj[N];
Node st[S];
Node merge(const Node& a, const Node& b) {
   return {a.val + b.val};
void update(int idx, Node val) {
   st[idx += n] = val;
   for (idx /= 2; idx; idx /= 2) st[idx] = merge(st[idx * 2], st[idx * 2]
Node query(int lo, int hi) {
   Node ra = nullNode, rb = nullNode;
   for (lo += n, hi += n + 1; lo < hi; lo /= 2, hi /= 2) {
       if (lo & 1) ra = merge(ra, st[lo++]);
       if (hi & 1) rb = merge(st[--hi], rb);
   }
   return merge(ra, rb);
int dfs_size(const int& node, const int& parent) {
   sz[node] = 1;
   par[node] = parent;
   for (const int& ch : adj[node]) {
       if (ch == parent) continue;
       dep[ch] = dep[node] + 1;
       par[ch] = node;
       sz[node] += dfs_size(ch, node);
```

```
}
   return sz[node];
}
int curId = 0;
void dfs_hld(const int& cur, const int& parent, const int& curTop) {
   id[cur] = curId++;
   top[cur] = curTop;
   update(id[cur], {val[cur]});
   int heavyChild = -1, heavyMax = -1;
   for (const int& ch : adj[cur]) {
       if (ch == parent) continue;
       if (sz[ch] > heavyMax) {
          heavyMax = sz[ch];
          heavyChild = ch;
   }
   if (heavyChild == -1) return;
   dfs_hld(heavyChild, cur, curTop);
   for (int ch : adj[cur]) {
       if (ch == parent || ch == heavyChild) continue;
       dfs_hld(ch, cur, ch);
   }
}
Node path(int u, int v) {
   Node ans = nullNode;
   while (top[u] != top[v]) {
       if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
       ans = merge(ans, query(id[top[u]], id[u]));
       u = par[top[u]];
   }
   if (dep[u] > dep[v]) swap(u, v);
   ans = merge(ans, query(id[u], id[v]));
   return ans;
}
void init() {
   for (int i = 0; i < S; i++) st[i] = nullNode;</pre>
```

```
dfs_size(1, 1);
   dfs_hld(1, 1, 1);
int main() {
   cin >> n >> q;
   for (int i = 1; i <= n; i++) cin >> val[i];
   int a, b;
   for (int i = 2; i <= n; i++) {
       cin >> a >> b;
       adj[a].pb(b);
       adj[b].pb(a);
   }
   init(); // <----- DON'T FORGET TO CALL THIS FUNCTION
   int type;
   while (q--) {
       cin >> type;
       if (type == 1) {
           cin >> a >> b;
          val[a] = b;
          update(id[a], {val[a]});
       else {
           cin >> a;
           cout << path(1, a).val << el;</pre>
   }
```

8 Techniques

8.1 Coordinate Compression

```
void coordinate_compress(vector<int> &x, int start=0, int
    step=1) {
    set unique(x.begin(), x.end());
    map<int, int> valPos;
```

```
int idx=0;
for (auto i: unique) {
  valPos[i] = start + idx * step;
  ++idx;
}
for(auto &i: x) i = valPos[i];
}
```

Coordinate Compression

8.2 Binary to decimal

Binary to decimal

```
// Function to convert binary to decimal
// 0(32)
int binaryToDecimal(string str)
{
   int dec_num = 0;
   int power = 0;
   int n = str.length();

   for(int i = n-1; i>=0; i--){
    if(str[i] == '1'){
      dec_num += (1<<power);
   }
   power++;
   }

   return dec_num;
}</pre>
```

8.3 Decimal to binary

Decimal to bianry

```
// Function that convert Decimal to binary
// 0(32)
void decToBinary(int n)
```

```
// Size of an integer is assumed to be 32 bits
   for (int i = 31; i >= 0; i--) {
       int k = n >> i;
       if (k & 1)
          cout << "1";
       else
          cout << "0";
   }
// O(logn)
string DecimalToBinary(int num)
   string str;
     while(num){
     if(num & 1) // 1
       str+='1';
     else // 0
       str+='0';
     num>>=1; // Right Shift by 1
     return str;
```

9 Number Theory

9.1 Divisors

9.1.1 formulas

number of divisors

```
int d(int n){
   unordered_map<int, int> factors = pf(n);
   int c = 1;
   for(const auto& factor: factors){
      c *= (factor.second+1);
   }
   return c;
}
```

```
// range Count Divisors backward thinking MAXN = 2e6
for(int i=1; i <= n; ++i) {
  for(int j = i; j <= n; j += i) {
    numFactors[j]++;
  }
}
int countDivisors(int n) {
  int count = 0;
  for (int i = 1; i * i <= n; ++i) {
    if (n % i == 0) {
       if (i == n / i) {
          count++; // Perfect square
       } else {
          count += 2; // Pair of divisors
       }
  }
  return count;
}</pre>
```

sum of divisors

```
int s(int n){
   unordered_map<int,int> factors = pf(n);
   int sum = 1;
   for(const auto& factor: factors){
      int p = factor.first;
      int exp = factor.second;
      sum *= (pow(p,exp+1)-1)/p-1;
   }
   return sum;
}
```

9.2 Primes

prime factorization

```
void factorize(int x, unordered_map<int, int>& factors) {
```

```
while (x % 2 == 0) {
    factors[2]++;
    x /= 2;
}
for (int i = 3; i * i <= x; i += 2) {
    while (x % i == 0) {
        factors[i]++;
        x /= i;
    }
}
if (x > 2) factors[x]++;
```

number of co-primes with n

Prime Check

```
vector<bool> isPrime(MAXN, true);
void sieve() {
  isPrime[0] = isPrime[1] = false;
```

```
for (int i=2; i * i <= isPrime.size(); ++i) {</pre>
   if(isPrime[i]) {
     for (int j = 2 * i; i <= isPrime.size(); j += i)</pre>
       prime[j] = false;
   }
 }
bool Prime(int n) {
 if(n == 2) return true;
 if(n < 2 || n % 2 == 0) return false;</pre>
 for(int i=3; i * i <= n; i += 2) {</pre>
   if(n % i == 0) return false;
  return true;
}
// Generate Primes
const int sz = sqrt(MAXN);
vector<int> prime;
vector<bool> vis(sz);
void pre() {
   prime.push_back(2);
   for (int j = 4; j < sz; j += 2) vis[j] = true;
   for (int i = 3; i < sz; i += 2) {
       if (vis[i]) continue;
       prime.push_back(i);
       for (int j = i * i; j < sz; j += i) vis[j] = true;</pre>
}
// Preprocessing Prime Factorization of range numbers
constexpr int N = 5e6+1;
int a[N]:
for(int i=2; i < N; ++i) {</pre>
   if(!a[i]) {
       for(int j=1; i*j < N; ++j) {</pre>
           for(int k=i*j; k%i==0; k/=i) a[i*j]++;
       }
```

```
}
a[i] += a[i-1];
}
```

10 Geometry

10.1 Linearity

10.1.1 co-linear points

check if two points are co-linear

```
bool co_linear(int x1, int y1, int x2, int y2, int x3, int y3){
  int area = x1*(y2-y3) + x2*(y3-y1) + x3*(y1-y2);
  return area == 0;
}
```

10.2 polygons

10.2.1 Polygon formation

check if can form polygon with given angle

```
bool possible(double angle){
  if(angle <= 0 || angle >= 180) return false;

double sides = 360.0/(180.0-angle);

return (sides == static_cast<int>(sides) && sides >= 3);
}
```

10.2.2 Rectangle Intersection

intersection area between 2 rectangles

```
struct Rectangle {
   int x1, y1; // Bottom-left corner
   int x2, y2; // Top-right corner
```

```
int intersectionArea(const Rectangle& rect1, const Rectangle& rect2){
   int x_left = max(rect1.x1, rect2.x1);
   int y_bottom = max(rect1.y1, rect2.y1);
   int x_right = min(rect1.x2, rect2.x2);
   int y_top = min(rect1.y2, rect2.y2);

   int intersection_width = x_right - x_left;
   int intersection_height = y_top - y_bottom;

   if (intersection_width > 0 && intersection_height > 0) {
      return intersection_width * intersection_height;
   }

   return 0;
}
```

11 Miscellaneous

11.1 Faster implementations

11.1.1 hashes

custom hash

```
return splitmix64(x + FIXED_RANDOM);
}
```

gb hash table

```
//policy based ds (faster hash table)
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
gp_hash_table<int, int> table;
```

11.1.2 Binary Search the value

$nearest \ sqrt$

```
long long my_sqrt(long long a)
{
    long long l=0,r=5000000001;
    while(r-l>1)
    {
        long long mid=(l+r)/2;
        if(1ll*mid*mid<=a)l=mid;
        else r=mid;
    }
    return l;
}</pre>
```